

# Functions in C++

# Website is Up!!!

```
Vector<string> ListSubsets(string& str, int start) {
    /* Base case: The only subset of the empty set is
     * the empty set itself.
     */
    if (start == str.length()) {
        Vector<string> result;
        result.push_back("");
        return result;
    }
    /* Find all subsets excluding the current element. */
    Vector<string> exclude = ListSubsets(str, start + 1);
    /* For each of those subsets, consider it and the
     * subset formed by adding in the current character.
     */
    Vector<string> result;
    foreach (string s in exclude) {
        result.push_back(s);
        result.push_back(s + str[start]);
    }
    return result;
}
```

# CS106B

## Programming Abstractions in C++

### Welcome to CS106B!

June 24, 2013

Welcome to CS106B! We've got an exciting quarter ahead of us and you're in for a real programming treat. Over the next ten weeks, we'll be exploring the fundamental techniques necessary to reason about, model, and solve big, important problems. It's going to be a lot of fun, and I hope that you're able to join us!

In the meantime, feel free to check out the [course information handout](#) and [syllabus](#) to learn more about what this class is all about, the prerequisites, and the course policies. If you have any questions in the meantime, feel free to email me at [adgress@cs.stanford.edu](mailto:adgress@cs.stanford.edu) with questions.

See you soon!

### Handouts

- [00: Course Information](#)
- [01: Syllabus](#)
- [02: Course Placement](#)
- [03L: Running C++ On Linux](#)
- [03M: Running C++ On Mac](#)
- [03W: Running C++ On Windows](#)
- [04: Honor Code](#)
- [06M: Debugging with Xcode](#)
- [06W: Debugging with Visual Studio](#)
- [07: Submitting Assignments](#)

### Section Handouts

### Assignments

### Resources

- [Course Reader PDF](#)
- [Tresidder LaIR Office Hours](#)
- [C and C++ Standard Library Docs](#)
- [Stanford C++ Library Docs](#)
- [Good Programming Style 1](#)
- [Good Programming Style 2](#)
- [Submitter](#)
- [Lecture Videos](#)
- [QuestionHut](#)
- [Blank Windows Project](#)
- [Blank Mac Project](#)

### Lectures

# Website is Up!!!

```
Vector<string> ListSubsets(string& str, int start) {  
    /* Base case: The only subset of the empty set is  
     * the empty set itself.  
     */  
    if (start == str.length()) {  
        Vector<string> result;  
        result.push_back("");  
        return result;  
    }  
    /* Find all subsets excluding the current element. */  
    Vector<string> exclude = ListSubsets(str, start + 1);  
    /* For each of those subsets, consider it and the  
     * subset formed by adding in the current character.  
     */  
    Vector<string> result;  
    foreach (string s in exclude) {  
        result.push_back(s);  
        result.push_back(s + str[start]);  
    }  
    return result;  
}
```

# CS106B

## Programming Abstractions in C++

### Welcome to CS106B!

June 24, 2013

Welcome to CS106B! We've got an exciting quarter ahead of us and you're in for a real programming treat. Over the next ten weeks, we'll be exploring the fundamental techniques necessary to reason about, model, and solve big, important problems. It's going to be a lot of fun, and I hope that you're able to join us!

In the meantime, feel free to check out the [course information handout](#) and [syllabus](#) to learn more about what this class is all about, the prerequisites, and the course policies. If you have any questions in the meantime, feel free to email me at [adgresh@cs.stanford.edu](mailto:adgresh@cs.stanford.edu) with questions.

See you soon!

### Handouts

- [00: Course Information](#)
- [01: Syllabus](#)
- [02: Course Placement](#)
- [03L: Running C++ On Linux](#)
- [03M: Running C++ On Mac](#)
- [03W: Running C++ On Windows](#)
- [04: Honor Code](#)
- [06M: Debugging with Xcode](#)
- [06W: Debugging with Visual Studio](#)
- [07: Submitting Assignments](#)

### Section Handouts

### Assignments

### Resources

- [Course Reader PDF](#)
- [Tresidder LaIR Office Hours](#)
- [C and C++ Standard Library Docs](#)
- [Stanford C++ Library Docs](#)
- [Good Programming Style 1](#)
- [Good Programming Style 2](#)
- [Submitter](#)
- [Lecture Videos](#)
- [QuestionHut](#)
- [Blank Windows Project](#)
- [Blank Mac Project](#)

### Lectures

# Today

- Getting Started in C++
- Thinking Recursively
- Style Gameshow
- Parameter Passing and Common Mistakes

# Today

- **Getting Started in C++**
- Thinking Recursively
- Style Gameshow
- Parameter Passing and Common Mistakes

# The main Function

- A C++ program begins execution in a function called `main` with the following signature:

```
int main() {  
    /* ... code to execute ... */  
}
```

- By convention, `main` should return 0 unless the program encounters an error.

# Getting Input from the User

- In C++, we use `cout` to display text.
- We can also use `cin` to receive input.
- For technical reasons, we've written some functions for you that do input.
  - Take CS106L to see why!
- The library "`simpio.h`" contains methods for reading input:

```
int getInteger(string prompt = "");  
double getReal(string prompt = "");  
string getLine(string prompt = "");
```

# Getting Input from the User

- In C++, we use `cout` to display text.
- We can also use `cin` to receive input.
- For technical reasons, we've written some functions for you that do input.
  - Take CS106L to see why!
- The library "`simpio.h`" contains methods for reading input:

```
int getInteger(string prompt = "");  
double getReal(string prompt = "");  
string getLine(string prompt = "");
```

These functions have **default arguments**. If you don't specify a prompt, it will use the empty string.

hello-world.cpp  
(On Board)

# C++ Functions

- Functions in C++ are similar to methods in Java:
  - Piece of code that performs some task.
  - Can accept parameters.
  - Can return a value.
- Syntax similar to Java:

```
return-type function-name (parameters) {  
    /* ... function body ... */
```

Note: no  
**public** or  
**private**.

abs.cpp  
(On Computer)

# What Went Wrong?

# One-Pass Compilation

- Unlike some languages like Java or C#, C++ has a **one-pass compiler**.
  - Think of it like a person reading a book from start to finish.
  - If a function has not yet been declared when you try to use it, you will get a compiler error.

# Function Prototypes

- A **function prototype** is a declaration that tells the C++ compiler about an upcoming function.
- Syntax:  
*return-type function-name (parameters) ;*
- A function can be used if the compiler has seen either the function itself or its prototype.

# Factorials

- The number  **$n$  factorial**, denoted  **$n!$** , is

$$n \times (n - 1) \times \dots \times 3 \times 2 \times 1$$

- For example:
  - $3! = 3 \times 2 \times 1 = 6.$
  - $5! = 5 \times 4 \times 3 \times 2 \times 1 = 120$
  - $0! = 1$  (by definition)
- Factorials show up everywhere:
  - Taylor series.
  - Counting ways to shuffle a deck of cards.
  - Determining how quickly computers can sort values (more on that later this quarter).

factorial.cpp  
(On Board)

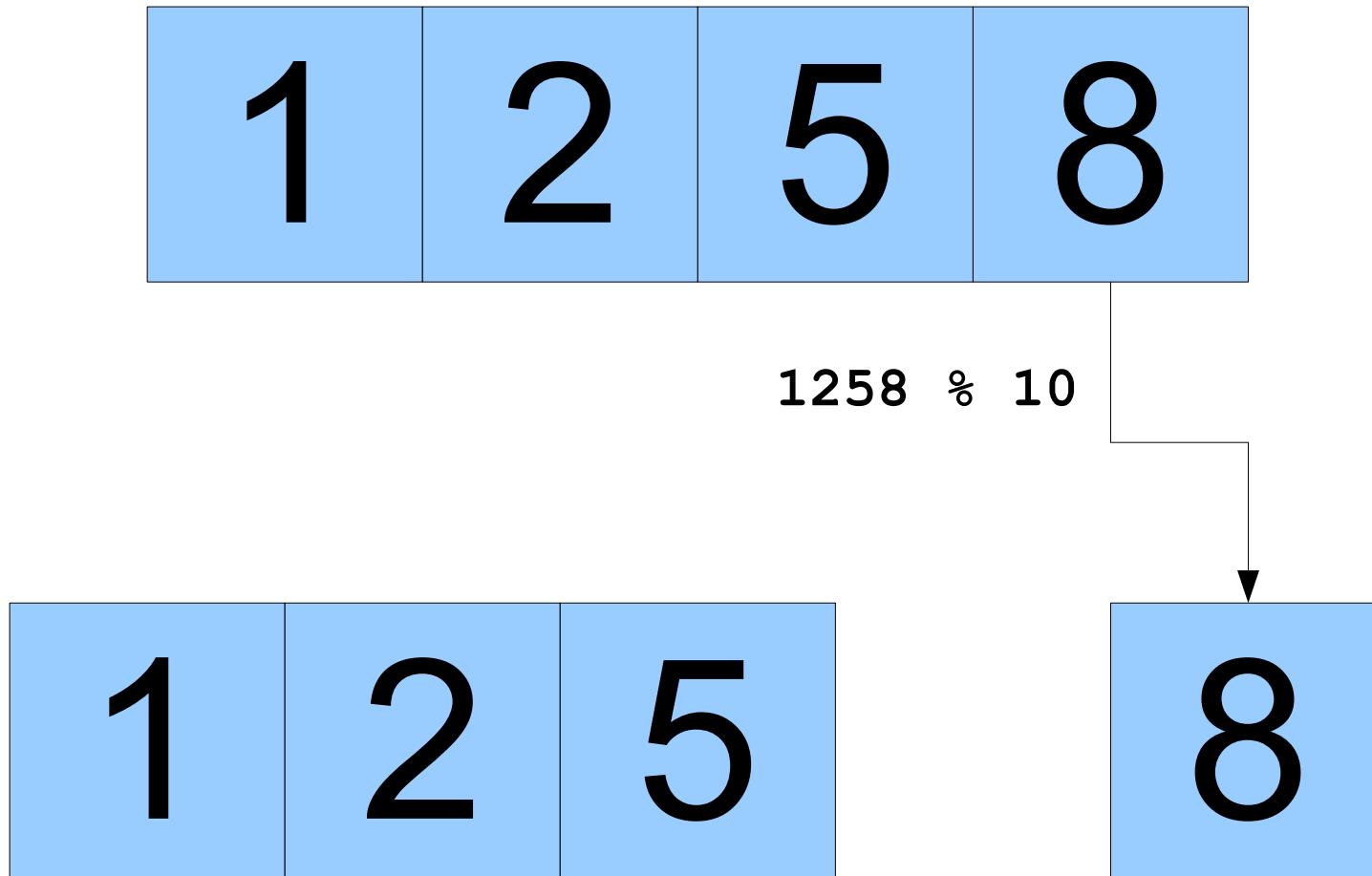
# Digital Roots

- The **digital root** of a number can be found as follows:
  - If the number is just one digit, then it's its own digital root.
  - If the number is multiple digits, add up all the digits and repeat.
- For example:
  - 5 has digital root 5.
  - $42 \rightarrow 4 + 2 = 6$ , so 42 has digital root 6.

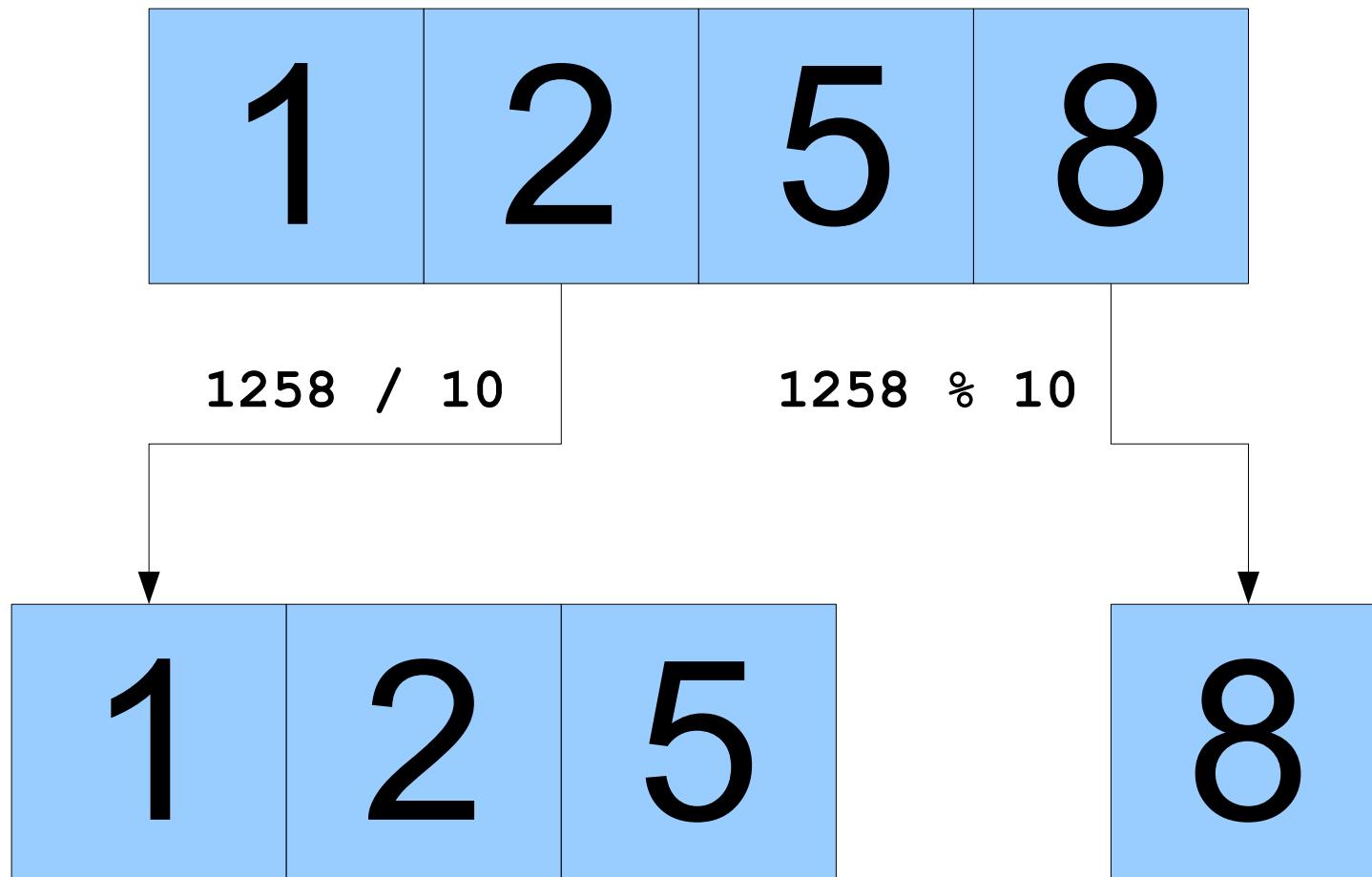
# Digital Roots

- The **digital root** of a number can be found as follows:
  - If the number is just one digit, then it's its own digital root.
  - If the number is multiple digits, add up all the digits and repeat.
- For example:
  - 5 has digital root 5.
  - $42 \rightarrow 4 + 2 = 6$ , so 42 has digital root 6.
  - $137 \rightarrow 1 + 3 + 7 = 11$   
 $11 \rightarrow 1 + 1 = 2$ ,  
so 137 has digital root 2.

# Working One Digit at a Time



# Working One Digit at a Time



digital-root.cpp  
(On Board)

# Announcements

- Lectures are recorded. Link on website.
- Lecture slides and code are posted on the website.
- Correction: LAIR hours are 7-11pm, Sunday-Wednesday (starting this Wednesday)
- No section this week
- More course readers in bookstore Wednesday ~Noon

# More Announcements...

- Five Handouts Today:
  - Downloading XCode/Visual Studio/g++
  - **Honor Code**
  - **Assignment 1: Welcome to C++!**
  - Submitting Assignments
  - Debugging with Visual Studio/Xcode
- Assignment 1 (Welcome to C++!) out later today, due Tuesday, July 2 at 11AM.
  - **Starter files are being updated, email will be sent when ready**

# The CS106B Grading Scale

++

+

✓+

✓

✓-

-

--

0

# Assignment Grading

- You will receive two scores: a functionality score and a style score.
- The **functionality score** is based on correctness.
  - Do your programs produce the correct output?
  - Do they work on all legal inputs?
- The **style score** is based on how well your program is written.
  - Are your programs well-structured?
  - Do you use variable naming conventions consistently?

# Late Days

- Everyone has **four** free “late days” to use as needed.
- A “late day” is an automatic 24 hour extension.
- If you need an extension beyond late days, please talk to Aubrey.
  - We generally only give extra extensions for medical reasons.
- **Max days an assignment can be late is 3.** Past this we won't grade it.

# Honor Code

- Unfortunately the Computer Science department has a disproportionately high number of honor code violations.
- The most likely reason for this is that we are very good at detecting honor code violations (we have automated tools that do this for us).

# Honor Code

- Handout on the honor code is on the website. Please read it.
- The overwhelming majority of the honor code for CS106B is:
  - Don't look at over students' (past or present) code.
  - Don't show your code to any else in the class.
  - If your code is based off of something you found online or in the course reader, then cite the source.

# Today

- Getting Started in C++
- **Thinking Recursively**
- Style Gameshow
- Parameter Passing and Common Mistakes

A **recursive solution** is a solution that is defined in terms of itself.

# Recursion: Fibonacci Numbers

- Fibonacci Numbers
  - 0, 1, 1, 2, 3, 5, 8, 13, 21, ...
  - Defined *recursively*:

$$fib(n) = \begin{cases} n & \text{if } n = 0 \text{ or } 1 \\ fib(n-1) + fib(n-2) & \text{otherwise} \end{cases}$$

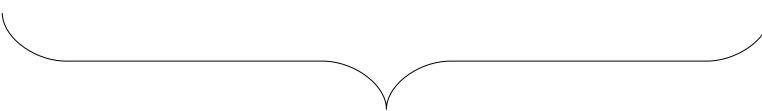
# Factorial Revisited

$$5! = 5 \times 4 \times 3 \times 2 \times 1$$

# Factorial Revisited

$$5! = 5 \times 4 \times 3 \times 2 \times 1$$

# Factorial Revisited

$$5! = 5 \times 4 \times 3 \times 2 \times 1$$

$$4!$$

# Factorial Revisited

$$5! = 5 \times 4!$$

# Factorial Revisited

$$5! = 5 \times 4!$$

# Factorial Revisited

$$5! = 5 \times 4!$$

$$4! = 4 \times 3 \times 2 \times 1$$

# Factorial Revisited

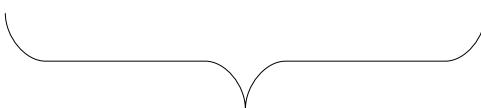
$$5! = 5 \times 4!$$

$$4! = 4 \times 3 \times 2 \times 1$$

# Factorial Revisited

$$5! = 5 \times 4!$$

$$4! = 4 \times 3 \times 2 \times 1$$

A curly brace is positioned above the numbers 4, 3, 2, and 1, indicating they are being grouped together.

$$3!$$

# Factorial Revisited

$$5! = 5 \times 4!$$

$$4! = 4 \times 3!$$

# Factorial Revisited

$$5! = 5 \times 4!$$

$$4! = 4 \times 3!$$

# Factorial Revisited

$$5! = 5 \times 4!$$

$$4! = 4 \times 3!$$

$$3! = 3 \times 2 \times 1$$

# Factorial Revisited

$$5! = 5 \times 4!$$

$$4! = 4 \times 3!$$

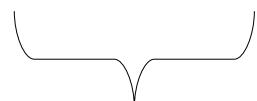
$$3! = 3 \times 2 \times 1$$

# Factorial Revisited

$$5! = 5 \times 4!$$

$$4! = 4 \times 3!$$

$$3! = 3 \times 2 \times 1$$



$$2!$$

# Factorial Revisited

$$5! = 5 \times 4!$$

$$4! = 4 \times 3!$$

$$3! = 3 \times 2!$$

# Factorial Revisited

$$5! = 5 \times 4!$$

$$4! = 4 \times 3!$$

$$3! = 3 \times 2!$$

# Factorial Revisited

$$5! = 5 \times 4!$$

$$4! = 4 \times 3!$$

$$3! = 3 \times 2!$$

$$2! = 2 \times 1!$$

# Factorial Revisited

$$5! = 5 \times 4!$$

$$4! = 4 \times 3!$$

$$3! = 3 \times 2!$$

$$2! = 2 \times 1!$$

$$1! = 1 \times 0!$$

# Factorial Revisited

$$5! = 5 \times 4!$$

$$4! = 4 \times 3!$$

$$3! = 3 \times 2!$$

$$2! = 2 \times 1!$$

$$1! = 1 \times 0!$$

$$0! = 1$$

factorial.cpp  
(On Computer)

# Another View of Factorials

$$n! = \begin{cases} 1 & \text{if } n = 0 \\ n \times (n - 1)! & \text{otherwise} \end{cases}$$

```
int factorial(int n)  {
    if (n == 0)  {
        return 1;
    } else  {
        return n * factorial(n - 1);
    }
}
```

# Another View of Factorials

$$n! = \begin{cases} 1 & \text{if } n = 0 \\ n \times (n - 1)! & \text{otherwise} \end{cases}$$

```
int factorial(int n) {
    if (n == 0) {
        return 1;
    } else {
        return n * factorial(n - 1);
    }
}
```

# Recursion in Action

```
int main() {  
    int n = factorial(5);  
    cout << "5! = " << n << endl;  
}
```

# Recursion in Action

```
int main() {  
    int n = factorial(5);  
    cout << "5! = " << n << endl;  
}
```

# Recursion in Action

```
int main() {  
    int factorial(int n) {  
        if (n == 0) {  
            return 1;  
        } else {  
            return n * factorial(n - 1);  
        }  
    }  
}  
  
int n 5
```

# Recursion in Action

```
int main() {  
    int factorial(int n) {  
        if (n == 0) {  
            return 1;  
        } else {  
            return n * factorial(n - 1);  
        }  
    }  
}  
  
int n 5
```

# Recursion in Action

```
int main() {  
    int factorial(int n) {  
        if (n == 0) {  
            return 1;  
        } else {  
            return n * factorial(n - 1);  
        }  
    }  
}  
  
int n = 5
```

# Recursion in Action

```
int main() {  
    int factorial(int n) {  
        if (n == 0) {  
            return 1;  
        } else {  
            return n * factorial(n - 1);  
        }  
    }  
}  
  
int n 5
```

# Recursion in Action

```
int main() {  
    int factorial(int n) {  
        int factorial(int n) {  
            if (n == 0) {  
                return 1;  
            } else {  
                return n * factorial(n - 1);  
            }  
        }  
    }  
}
```

int n 4

# Recursion in Action

```
int main() {  
    int factorial(int n) {  
        int factorial(int n) {  
            if (n == 0) {  
                return 1;  
            } else {  
                return n * factorial(n - 1);  
            }  
        }  
    }  
}
```

int n 4

# Recursion in Action

```
int main() {  
    int factorial(int n) {  
        int factorial(int n) {  
            if (n == 0) {  
                return 1;  
            } else {  
                return n * factorial(n - 1);  
            }  
        }  
    }  
}
```

int n 4

# Recursion in Action

```
int main() {  
    int factorial(int n) {  
        if (n == 0) {  
            return 1;  
        } else {  
            return n * factorial(n - 1);  
        }  
    }  
}
```

int n 4

# Recursion in Action

```
int main() {  
    int factorial(int n) {  
        }  
        int factorial(int n) {  
            int factorial(int n) {  
                if (n == 0) {  
                    return 1;  
                } else {  
                    return n * factorial(n - 1);  
                }  
            }  
        }  
    }  
}
```

int n 3

# Recursion in Action

```
int main() {  
    int factorial(int n) {  
        }  
        int factorial(int n) {  
            int factorial(int n) {  
                if (n == 0) {  
                    return 1;  
                } else {  
                    return n * factorial(n - 1);  
                }  
            }  
        }  
    }  
}
```

int n 3

# Recursion in Action

```
int main() {  
    int factorial(int n) {  
        }  
        int factorial(int n) {  
            int factorial(int n) {  
                if (n == 0) {  
                    return 1;  
                } else {  
                    return n * factorial(n - 1);  
                }  
            }  
        }  
    }  
}  
  
int n 3
```

# Recursion in Action

```
int main() {  
    int factorial(int n) {  
        }  
        int factorial(int n) {  
            int factorial(int n) {  
                if (n == 0) {  
                    return 1;  
                } else {  
                    return n * factorial(n - 1);  
                }  
            }  
        }  
    }  
}
```

int n 3

# Recursion in Action

```
int main() {  
    int factorial(int n) {  
        }  
        int factorial(int n) {  
            int factorial(int n) {  
                int factorial(int n) {  
                    if (n == 0) {  
                        return 1;  
                    } else {  
                        return n * factorial(n - 1);  
                    }  
                }  
            }  
        }  
    }  
}
```

int n 2

# Recursion in Action

```
int main() {  
    int factorial(int n) {  
        }  
        int factorial(int n) {  
            int factorial(int n) {  
                int factorial(int n) {  
                    if (n == 0) {  
                        return 1;  
                    } else {  
                        return n * factorial(n - 1);  
                    }  
                }  
            }  
        }  
    }  
}
```

int n 2

# Recursion in Action

```
int main() {  
    int factorial(int n) {  
        }  
        int factorial(int n) {  
            int factorial(int n) {  
                int factorial(int n) {  
                    if (n == 0) {  
                        return 1;  
                    } else {  
                        return n * factorial(n - 1);  
                    }  
                }  
            }  
        }  
    }  
}
```

int n 2

# Recursion in Action

```
int main() {  
    int factorial(int n) {  
        }  
        int factorial(int n) {  
            int factorial(int n) {  
                int factorial(int n) {  
                    if (n == 0) {  
                        return 1;  
                    } else {  
                        return n * factorial(n - 1);  
                    }  
                }  
            }  
        }  
    }  
}
```

int n 2

# Recursion in Action

```
int main() {  
    int factorial(int n) {  
        }  
    }  
    int factorial(int n) {  
        }  
        int factorial(int n) {  
            }  
            int factorial(int n) {  
                }  
                int factorial(int n) {  
                    }  
                    if (n == 0) {  
                        return 1;  
                    } else {  
                        return n * factorial(n - 1);  
                    }  
    }  
}  
int n 1
```

# Recursion in Action

```
int main() {  
    int factorial(int n) {  
        int factorial(int n) {  
            int factorial(int n) {  
                int factorial(int n) {  
                    int factorial(int n) {  
                        if (n == 0) {  
                            return 1;  
                        } else {  
                            return n * factorial(n - 1);  
                        }  
                    }  
                }  
            }  
        }  
    }  
}
```

int n 1

# Recursion in Action

```
int main() {  
    int factorial(int n) {  
        }  
    }  
    int factorial(int n) {  
        int factorial(int n) {  
            int factorial(int n) {  
                int factorial(int n) {  
                    if (n == 0) {  
                        return 1;  
                    } else {  
                        return n * factorial(n - 1);  
                    }  
                }  
            }  
        }  
    }  
}
```

int n 1

# Recursion in Action

```
int main() {  
    int factorial(int n) {  
        }  
        int factorial(int n) {  
            int factorial(int n) {  
                int factorial(int n) {  
                    int factorial(int n) {  
                        if (n == 0) {  
                            return 1;  
                        } else {  
                            return n * factorial(n - 1);  
                        }  
                    }  
                }  
            }  
        }  
    }  
}
```

int n 1

# Recursion in Action

```
int main() {  
    int factorial(int n) {  
        }  
        int factorial(int n) {  
            int factorial(int n) {  
                int factorial(int n) {  
                    int factorial(int n) {  
                        int factorial(int n) {  
                            if (n == 0) {  
                                return 1;  
                            } else {  
                                return n * factorial(n - 1);  
                            }  
                        }  
                    }  
                }  
            }  
        }  
    }  
}
```

int n 0

# Recursion in Action

```
int main() {  
    int factorial(int n) {  
        int factorial(int n) {  
            int factorial(int n) {  
                int factorial(int n) {  
                    int factorial(int n) {  
                        if (n == 0) {  
                            return 1;  
                        } else {  
                            return n * factorial(n - 1);  
                        }  
                    }  
                }  
            }  
        }  
    }  
}
```

int n 0

# Recursion in Action

```
int main() {  
    int factorial(int n) {  
        int factorial(int n) {  
            int factorial(int n) {  
                int factorial(int n) {  
                    int factorial(int n) {  
                        if (n == 0) {  
                            return 1;  
                        } else {  
                            return n * factorial(n - 1);  
                        }  
                    }  
                }  
            }  
        }  
    }  
}
```

int n 0

# Recursion in Action

```
int main() {  
    int factorial(int n) {  
        }  
        int factorial(int n) {  
            int factorial(int n) {  
                int factorial(int n) {  
                    int factorial(int n) {  
                        if (n == 0) {  
                            return 1;  
                        } else {  
                            return n * factorial(n - 1);  
                        }  
                    }  
                }  
            }  
        }  
    }  
}
```

int n 1

# Recursion in Action

```
int main() {  
    int factorial(int n) {  
        int factorial(int n) {  
            int factorial(int n) {  
                int factorial(int n) {  
                    if (n == 0) {  
                        return 1;  
                    } else {  
                        return n * factorial(n - 1);  
                    }  
                }  
            }  
        }  
    }  
}
```

The diagram illustrates the execution of a recursive factorial function. It shows four nested levels of the factorial function. The innermost level is highlighted with a red border around the recursive call line: `return n * factorial(n - 1);`. To the right of this line, there is a yellow box containing the value `1`, indicating the result of the base case. Below the red box, there is a blue box containing the parameter `int n 1`, indicating the current value of `n` for this recursive call.

# Recursion in Action

```
int main() {  
    int factorial(int n) {  
        }  
        int factorial(int n) {  
            int factorial(int n) {  
                int factorial(int n) {  
                    if (n == 0) {  
                        return 1;  
                    } else {  
                        return n * factorial(n - 1);  
                    }  
                }  
            }  
        }  
    }  
}
```

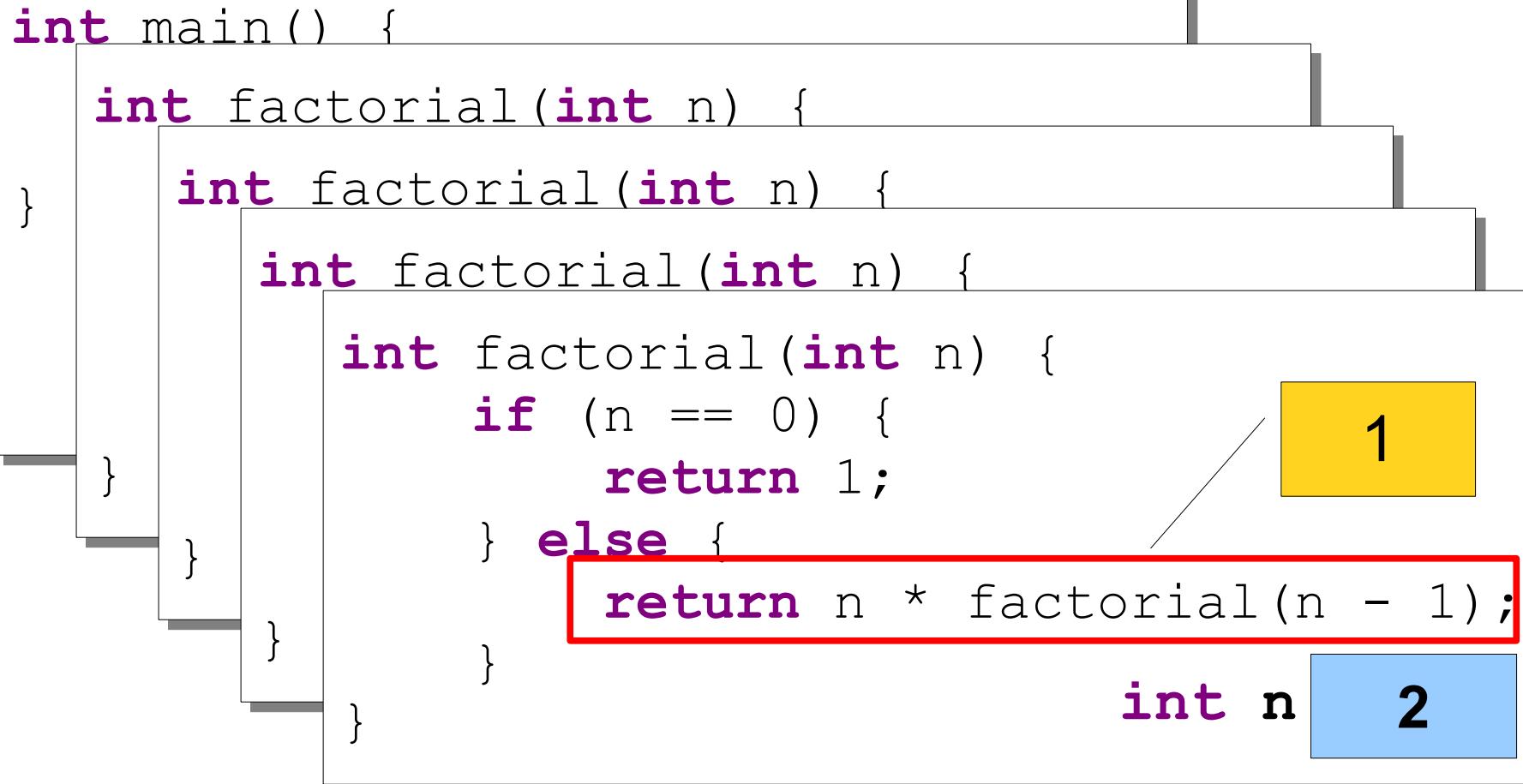
int n 2

# Recursion in Action

```
int main() {  
    int factorial(int n) {  
        int factorial(int n) {  
            int factorial(int n) {  
                int factorial(int n) {  
                    if (n == 0) {  
                        return 1;  
                    } else {  
                        return n * factorial(n - 1);  
                    }  
                }  
            }  
        }  
    }  
}
```

1

int n 2



# Recursion in Action

```
int main() {  
    int factorial(int n) {  
        }  
        int factorial(int n) {  
            int factorial(int n) {  
                if (n == 0) {  
                    return 1;  
                } else {  
                    return n * factorial(n - 1);  
                }  
            }  
        }  
    }  
}
```

int n 3

# Recursion in Action

```
int main() {  
    int factorial(int n) {  
        }  
        int factorial(int n) {  
            int factorial(int n) {  
                if (n == 0) {  
                    return 1;  
                } else {  
                    return n * factorial(n - 1);  
                }  
            }  
        }  
    }  
}
```

Diagram illustrating the execution stack for the recursive factorial function. The stack grows from bottom to top, with each frame representing a call to the factorial function.

- The outermost frame (main) contains the declaration `int factorial(int n)`.
- The second frame (factorial) contains the declaration `int factorial(int n)`.
- The innermost frame (factorial) contains the declaration `int factorial(int n)`, the base case `if (n == 0) { return 1; }`, and the recursive call `return n * factorial(n - 1);`.
- A yellow box labeled `2` is connected by a line to the recursive call line in the innermost frame.
- A blue box labeled `int n 3` is connected by a line to the parameter `n` in the innermost frame.

# Recursion in Action

```
int main() {  
    int factorial(int n) {  
        if (n == 0) {  
            return 1;  
        } else {  
            return n * factorial(n - 1);  
        }  
    }  
}
```

int n 4

# Recursion in Action

```
int main() {  
    int factorial(int n) {  
        if (n == 0) {  
            return 1;  
        } else {  
            return n * factorial(n - 1);  
        }  
    }  
}
```

6

int n 4

The diagram illustrates the execution stack for a recursive factorial call. The stack has three frames. The outermost frame contains the main() function. The middle frame contains the factorial() function with n=6. The innermost frame shows the recursive call factorial(n-1) with n=5. A red box highlights the recursive call line.

# Recursion in Action

```
int main() {  
    int factorial(int n) {  
        if (n == 0) {  
            return 1;  
        } else {  
            return n * factorial(n - 1);  
        }  
    }  
}  
  
int n 5
```

# Recursion in Action

```
int main() {  
    int factorial(int n) {  
        if (n == 0) {  
            return 1;  
        } else {  
            return n * factorial(n - 1);  
        }  
    }  
}
```

24

int n 5

The diagram illustrates a recursive call in a C program. The code defines a factorial function that returns the product of n and the factorial of n-1. For n=5, the recursive call n \* factorial(n-1) is highlighted with a red box. An arrow points from this red box to a yellow box containing the value 24, indicating the result of that specific recursive step.

# Recursion in Action

```
int main() {  
    int n = factorial(5);  
    cout << "5! = " << n << endl;  
}
```

# Recursion in Action

```
int main() {  
    int n = factorial(5);  
    cout << "5! = " << n << endl;  
}
```

int n 120

# Recursion in Action

```
int main() {  
    int n = factorial(5);  
    cout << "5! = " << n << endl;  
}
```

int n 120

# Thinking Recursively

- Solving a problem with recursion requires two steps.
- First, determine how to solve the problem for simple cases.
  - This is called the **base case**.
- Second, determine how to break down larger cases into smaller instances.
  - This is called the **recursive decomposition**.

# Another View of Factorials

$$n! = \begin{cases} 1 & \text{if } n = 0 \\ n \times (n - 1)! & \text{otherwise} \end{cases}$$

Base Case

Recursive Decomposition

# Thinking Recursively

**if** (*problem is sufficiently simple*) {

*Directly solve the problem.*

*Return the solution.*

} **else** {

*Split the problem up into one or more smaller problems with the same structure as the original.*

*Solve each of those smaller problems.*

*Combine the results to get the overall solution.*

*Return the overall solution.*

}

# Summing Up Digits

- One way to compute the sum of the digits of a number is shown here:

```
int sumOfDigits(int n) {  
    int result = 0;  
  
    while (n != 0) {  
        result += n % 10;  
        n /= 10;  
    }  
  
    return result;  
}
```

- How would we rewrite this function recursively?

# Summing Up Digits

1 2 5 8

The sum of these digits of  
this number...

is equal to the sum of the  
digits of this number...

1 2 5

8

# Summing Up Digits

1 2 5 8

The sum of these digits of  
this number...

is equal to the sum of the  
digits of this number...

plus this number.

1 2 5

8

`digital-roots.cpp`  
(On Computer)

# Summing Up Digits

- A recursive implementation of sumOfDigits is shown here:

```
int sumOfDigits(int n) {  
    if (n < 10) {  
        return n;  
    } else {  
        return (n % 10) + sumOfDigits(n / 10);  
    }  
}
```

- Notice the structure:
  - If the problem is simple, solve it directly.
  - Otherwise, reduce it to a smaller instance and solve that one.

# Computing Digital Roots

- One way of computing a digital root is shown here:

```
int digitalRoot(int n) {  
    while (n >= 10) {  
        n = sumOfDigits(n);  
    }  
    return n;  
}
```

- How might we rewrite this function recursively?

# Digital Roots

# Digital Roots

The digital root of

9 2 5 8

# Digital Roots

The digital root of **9 2 5 8** is the same as

# Digital Roots

The digital root of **9 2 5 8** is the same as

The digital root of **9+2+5+8**

# Digital Roots

The digital root of **9 2 5 8** is the same as

The digital root of **2 4**

# Digital Roots

The digital root of **9 2 5 8** is the same as

The digital root of **2 4** which is the same as

# Digital Roots

The digital root of 9 2 5 8 is the same as

The digital root of 2 4 which is the same as

The digital root of 2 + 4

# Digital Roots

The digital root of 9 2 5 8 is the same as

The digital root of 2 4 which is the same as

The digital root of 6

# Computing Digital Roots

- Here is one recursive solution:

```
int digitalRoot(int n) {  
  
    if (n < 10) {  
  
        return n;  
  
    } else {  
  
        return digitalRoot(sumOfDigits(n));  
  
    }  
}
```

- Again, notice the structure:
  - If the problem is simple, solve it directly.
  - If not, solve a smaller version of the same problem.

# Recursion vs. Iteration

- Any problem solved using *iteration* (for/while loops) can be solved using *recursion*
- All the recursive solutions we've covered today can be solved equally well using iteration
  - This is to help us feel more comfortable with recursion
  - When the choice is available, iteration is preferred to recursion
- Soon we'll start covering problems that can only be solved using recursion

# Today

- Getting Started in C++
- Thinking Recursively
- **Style Gameshow**
- Parameter Passing and Common Mistakes

# Style Gameshow

- Style is a very important part of programming.
  - In the real world, other people need to be able to read your code!
- Guess what I don't like about the style of the code and get a prize!

# Bad Style #1

```
int spork(int x, int y) {  
    int p = Mumbo(y);  
  
    int pp = Jumbo(x);  
  
    if (p*pp > 0) {  
        return Jabba(p);  
    }  
  
    return Jabba(pp);  
}
```

# Bad Style #1

```
int spork(int x, int y) {  
    int p = Mumbo(y);  
    int pp = Jumbo(x);  
    if (p*pp > 0) {  
        return Jabba(p);  
    }  
    return Jabba(pp);  
}
```

I have no clue what is going  
on in this function!!!

# Good Style #1

```
int calculateAreaOfRectangle(int width, int height) {  
    return width*height  
}
```

# Bad Style #2

```
void printPrimeNumbers() {  
    for (int i = 0; i < 20; i++) {  
  
        if (isPrime(i)) {  
  
            cout << i << endl;  
  
        }  
  
    }  
}
```

# Bad Style #2

```
void printPrimeNumbers() {  
    for (int i = 0; i < 20; i++) {  
        if (isPrime(i)) {  
            cout << i << endl;  
        }  
    }  
}
```



# Better Style #2

```
const int kMaxPrime = 20;

int main() {
    printPrimeNumbers();
}

void printPrimeNumbers() {
    for (int i = 0; i < kMaxPrime; i++) {
        if (isPrime(i)) {
            cout << i << endl;
        }
    }
}
```

# Best Style #2

```
const int kMaxPrime = 20;

int main() {
    printPrimeNumbers(kMaxPrime);
}

void printPrimeNumbers(int maxPrime) {
    for (int i = 0; i < maxPrime; i++) {
        if (isPrime(i)) {
            cout << i << endl;
        }
    }
}
```

# Bad Style #3

```
if (isWord == true) {  
    return true;  
} else {  
    return false;  
}
```

# Bad Style #3

```
if (isWord == true) {  
    return true;  
} else {  
    return false;  
}
```

Redundant boolean check

# Better Style #3

```
if (isWord) {  
    return true;  
} else {  
    return false;  
}
```

# Best Style #3

```
if (isWord) {  
    return true;  
} else {  
    return false;  
}  
return isWord;
```

# Bad Style #4

```
const int kSumMax = 10;

int sum;

int main() {
    sum = 0;
    for (int i = 0; i < kSumMax; i++) {
        sum += i;
    }
    cout << "Sum:" << sum;
    return 0;
}
```

# Next Time

- **Strings and Streams**
  - Representing and manipulating text.
  - File I/O in C++.