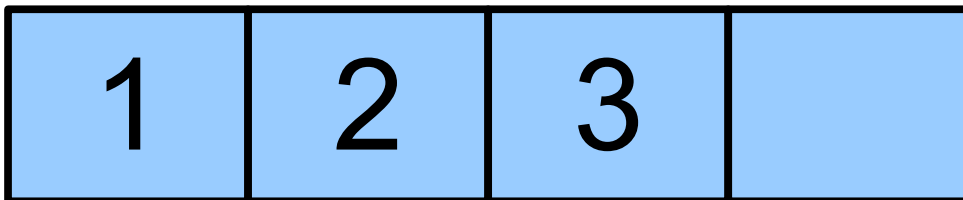


# Linked Lists

## Part One

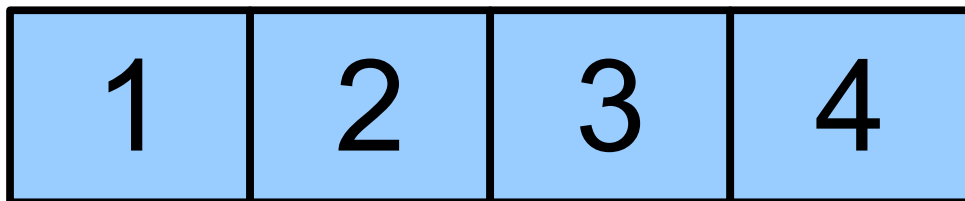
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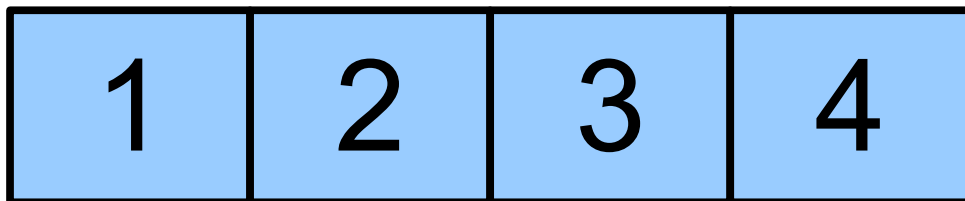
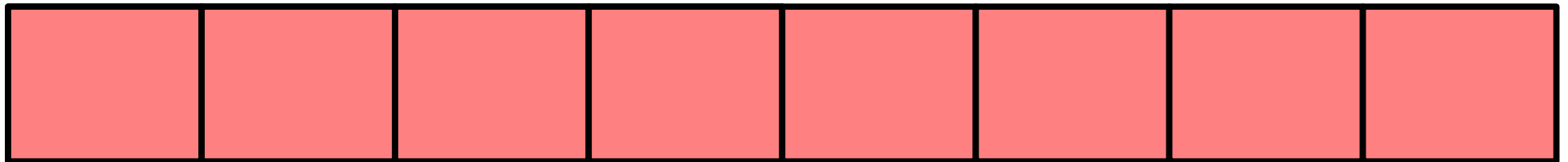
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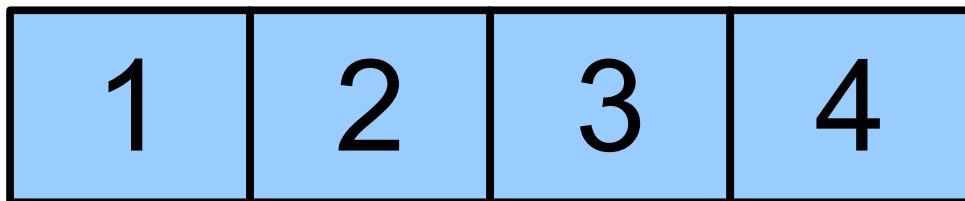
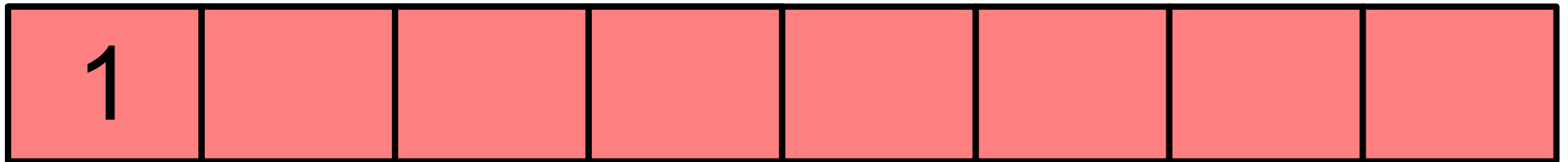
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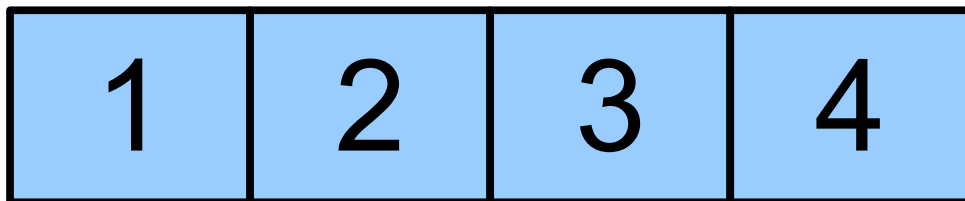
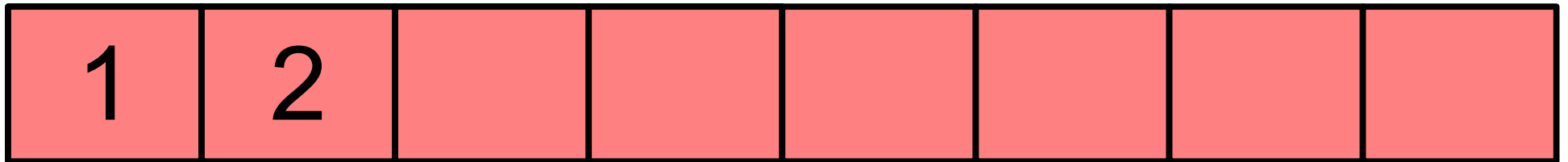
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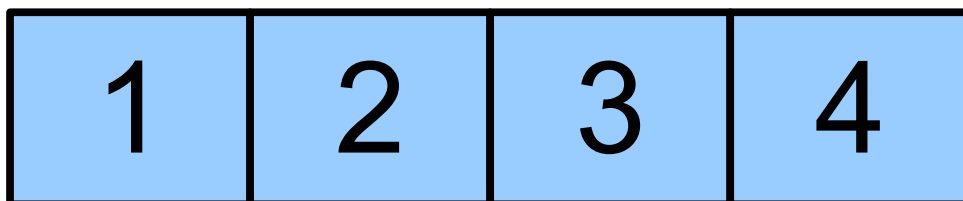
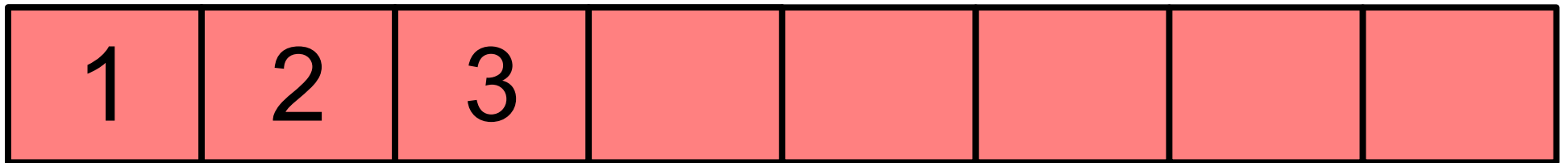
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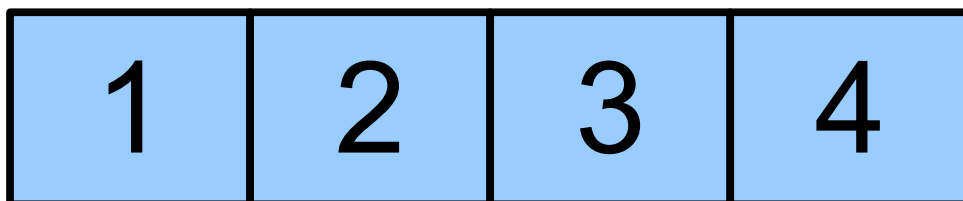
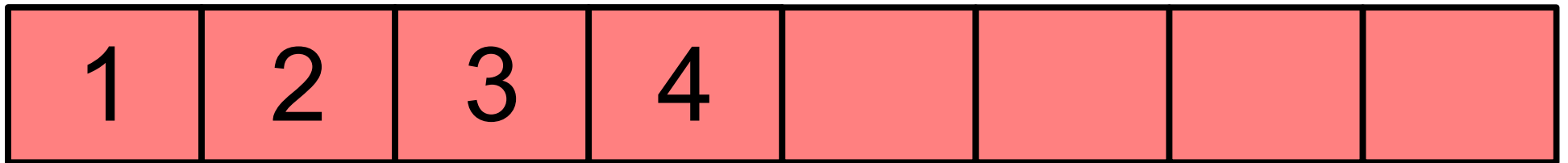
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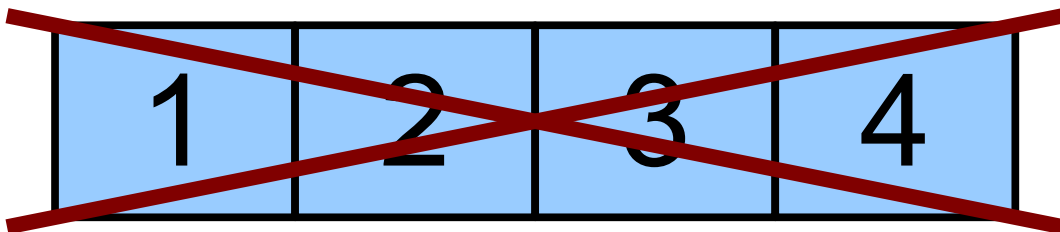
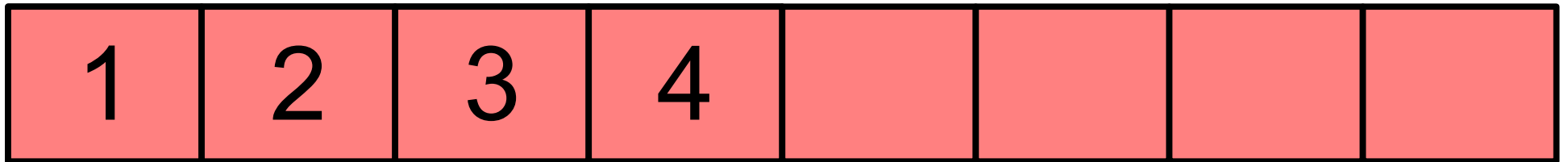
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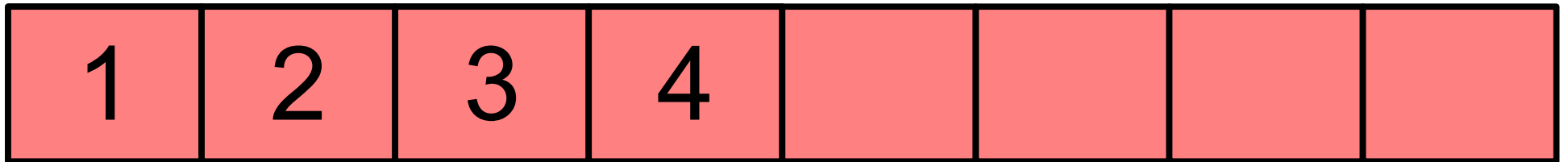
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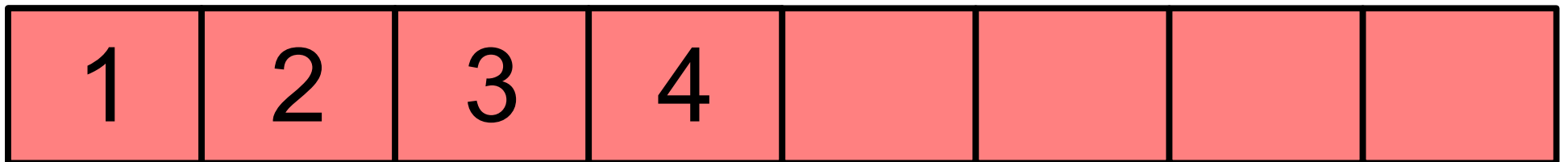
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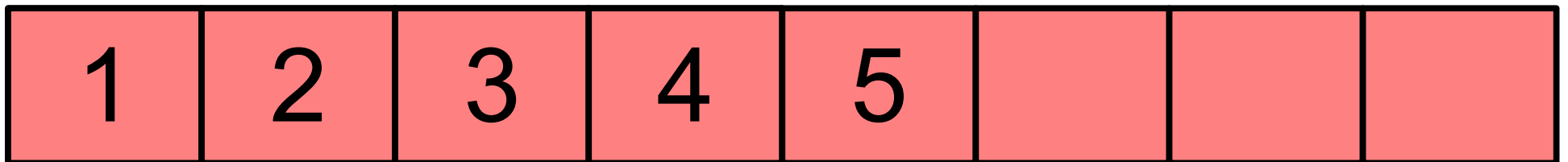
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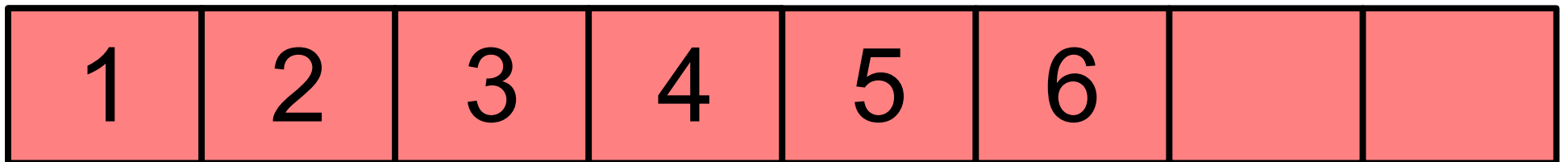
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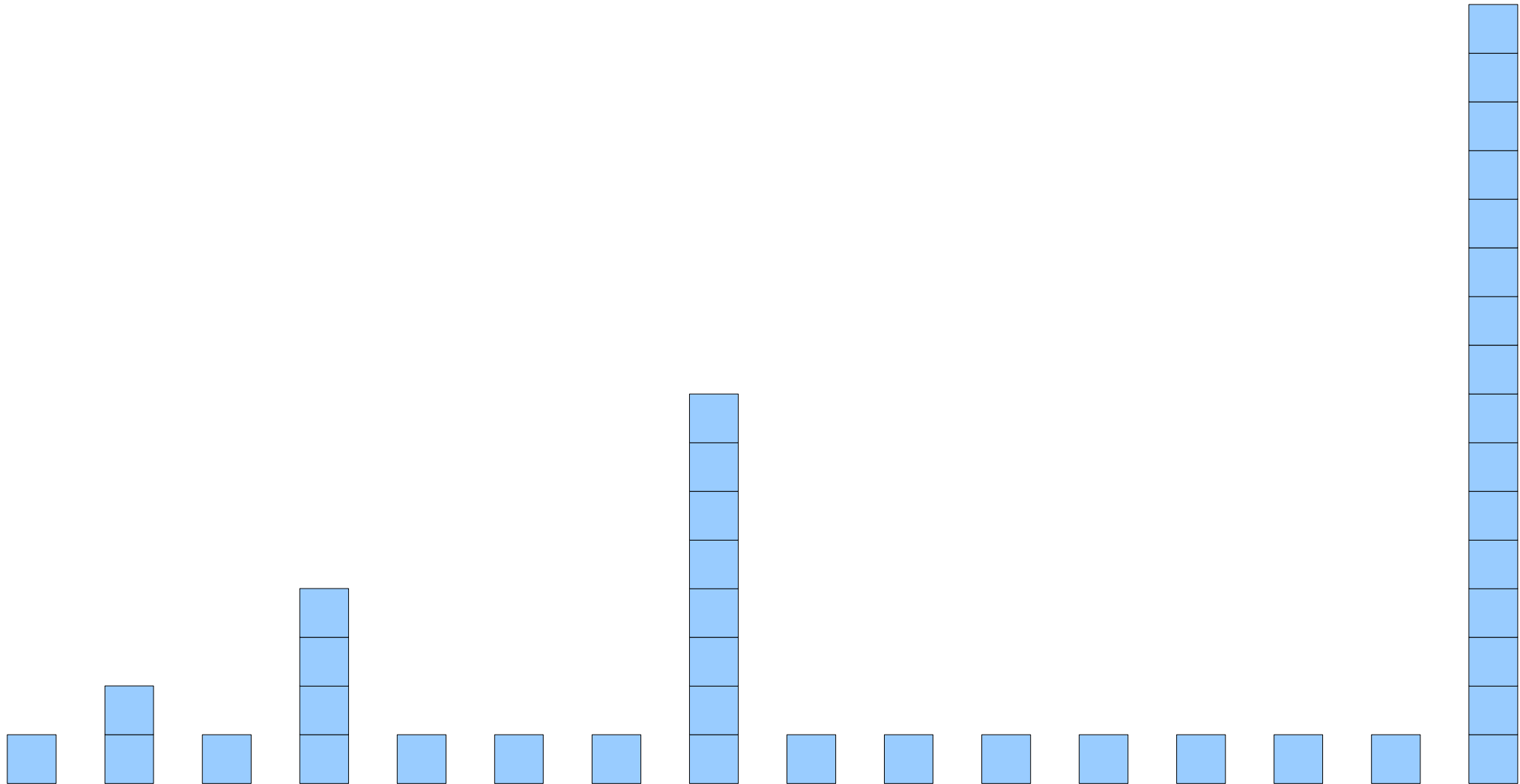


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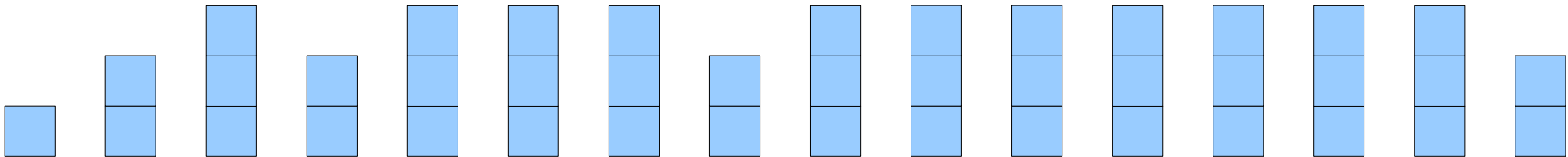
# Spreading the Work



# Spreading the Work

On average, we do just 3  
units of work!

This is  $O(1)$  work on  
average!



**Vector** is implemented in a similar manner.



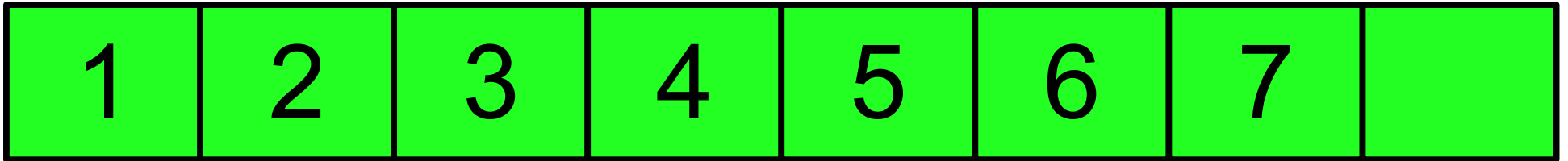
# Data Structures

- Last Lecture: **Stack, Vector**
- Today: **Queue**

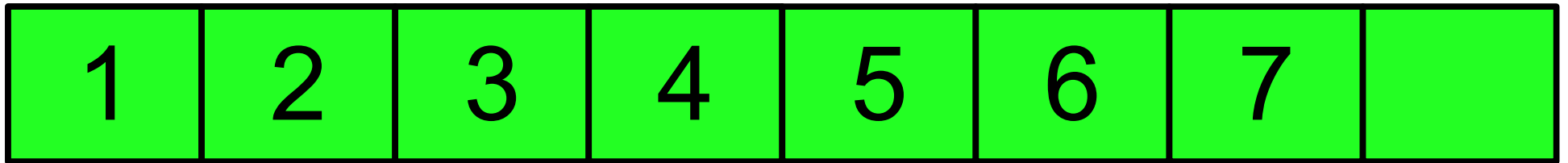
# Array Based Queue?

- Instead of reallocating a huge array to get the space we need, why not just get a tiny amount of extra space for the next element?
- Taking notes – when you run out of space on a page, you just get a new page. You don't copy your entire set of notes onto a longer sheet of paper!

Excuse Me, Coming Through...

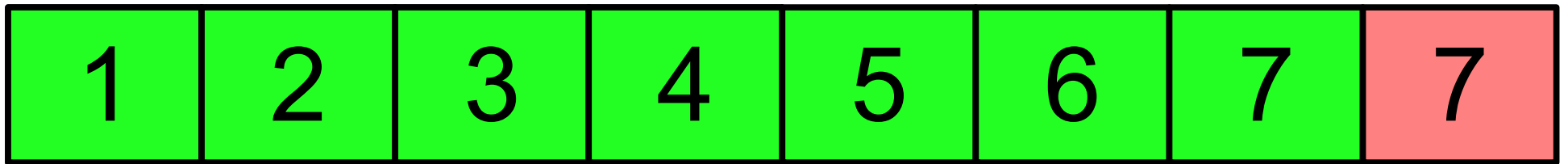


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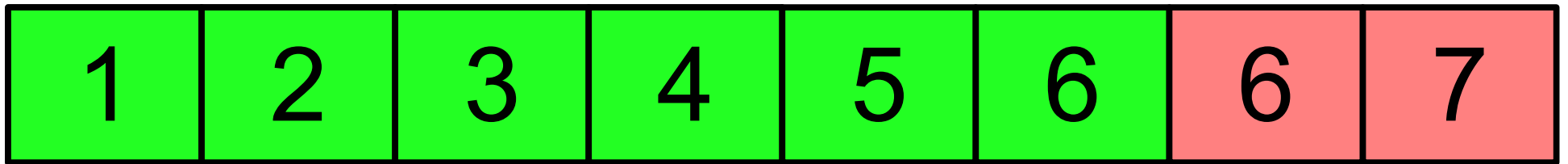
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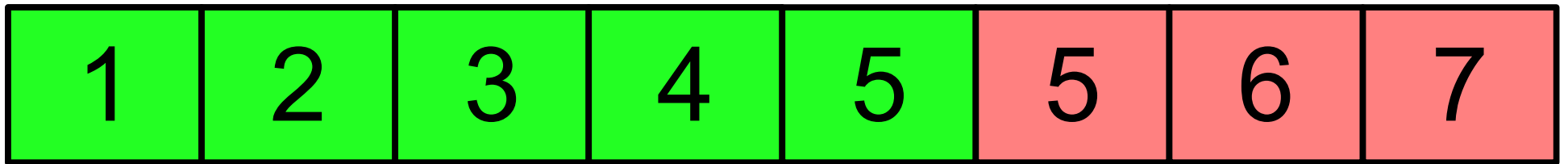
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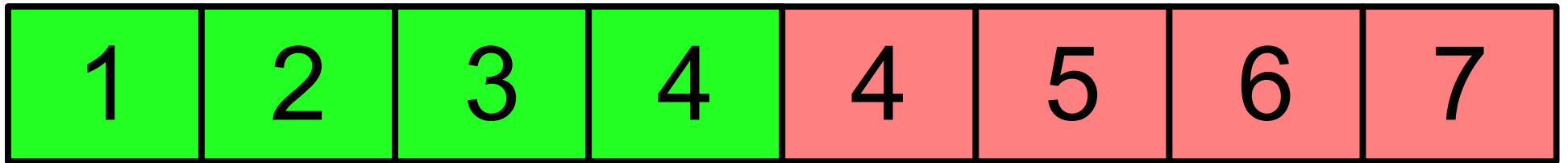
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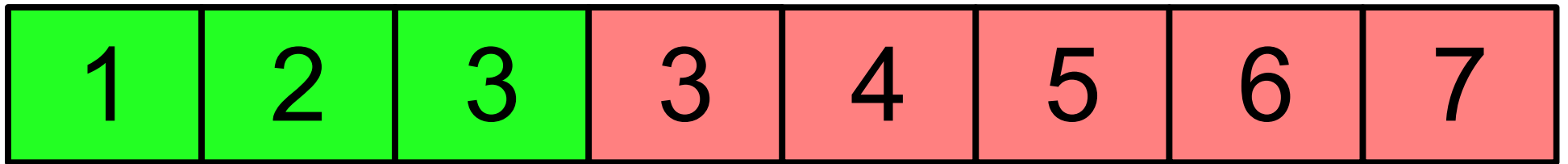
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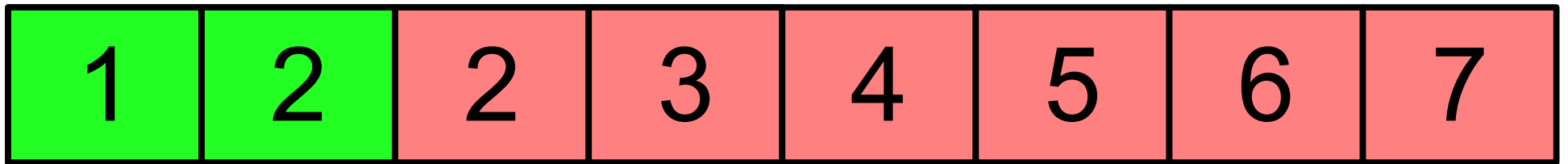


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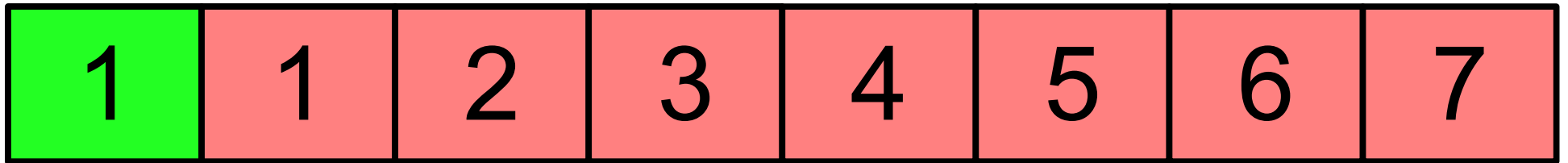
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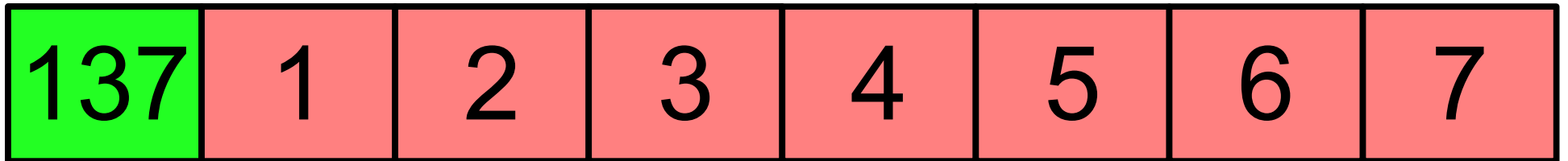
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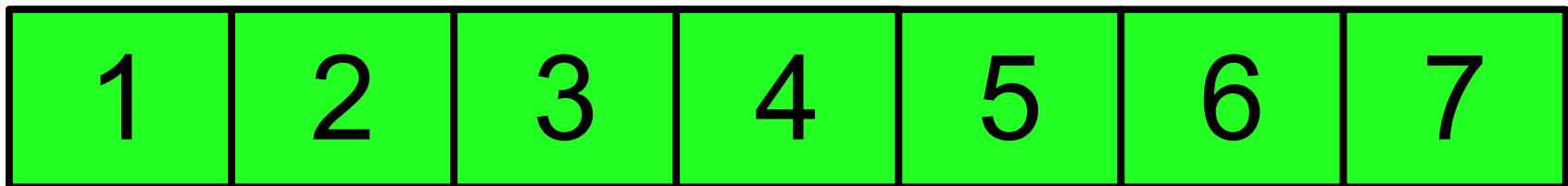
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# Shoving Things Over

- Right now, inserting an element into a middle of a **Vector** can be very costly.
- Couldn't we just do something like this?



# Shoving Things Over

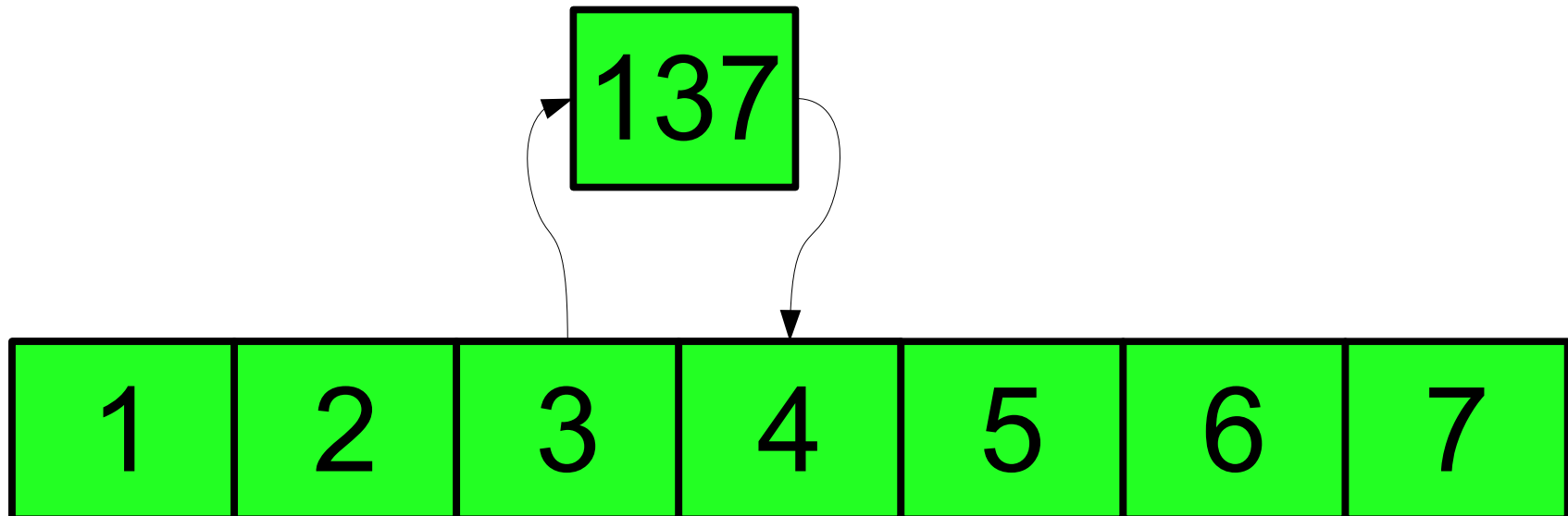
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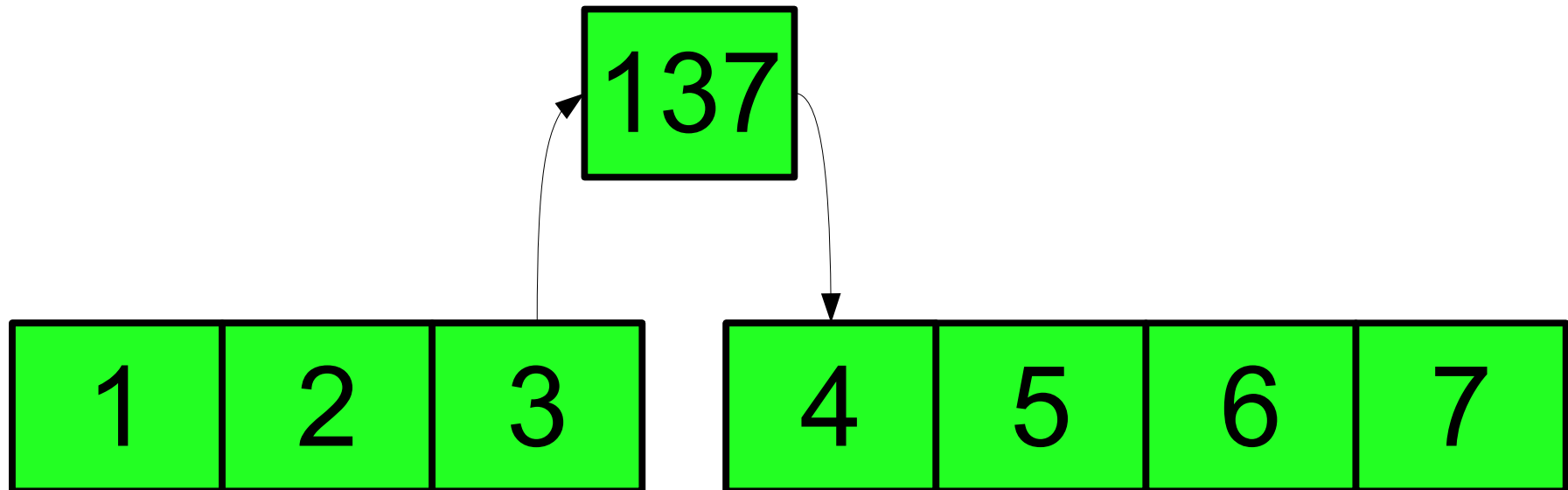
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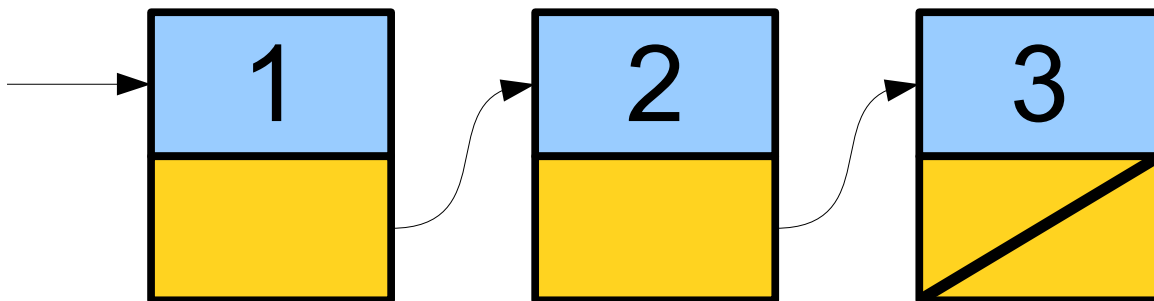
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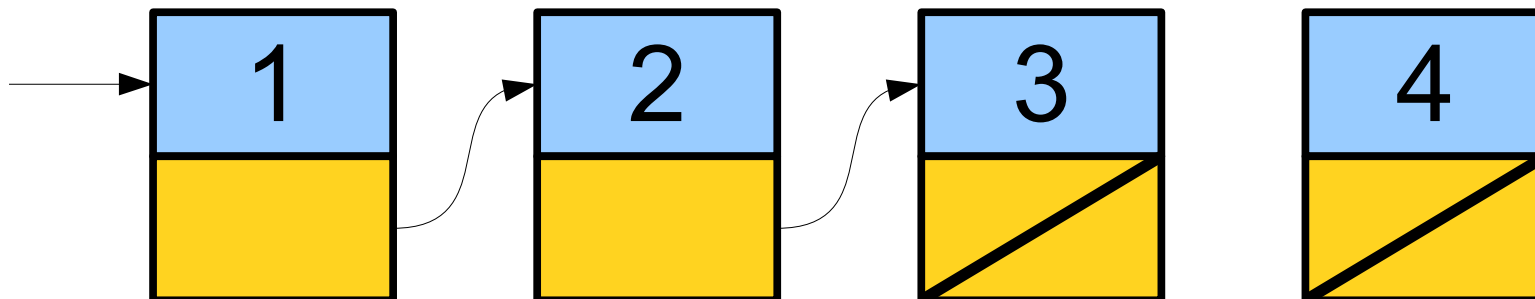
# Linked Lists at a Glance

- A **linked list** is a data structure for storing a sequence of elements.
- Each element is stored separately from the rest.
- The elements are then chained together into a sequence.



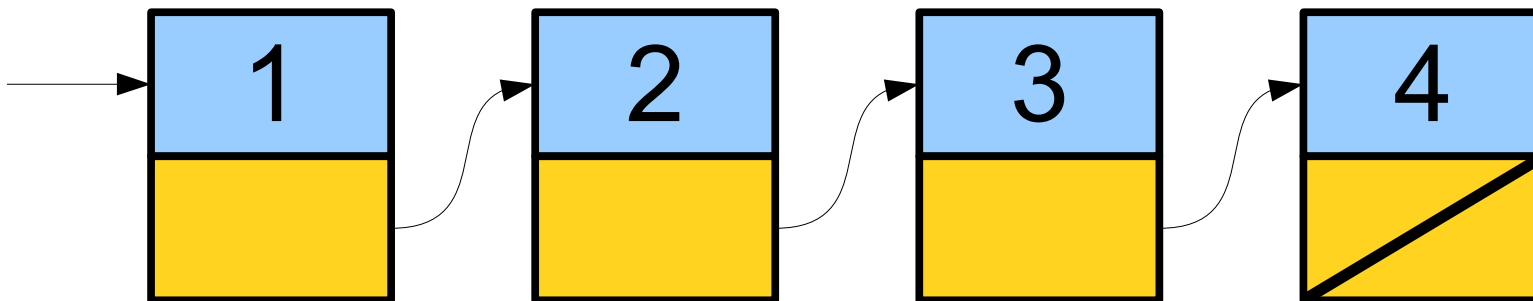
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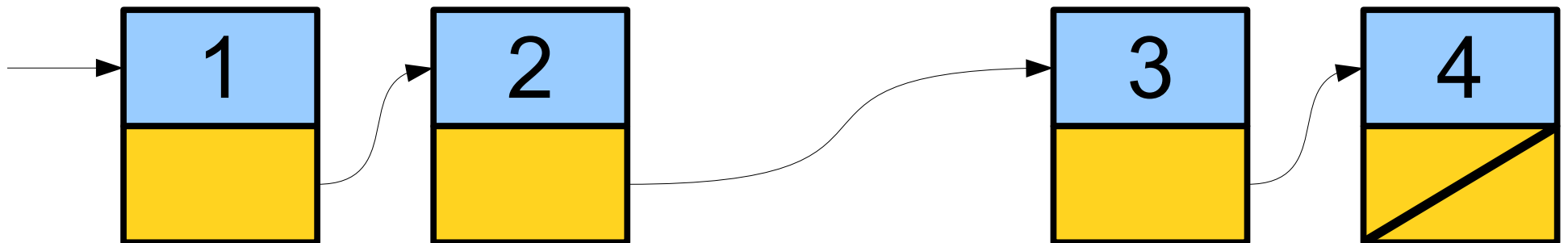
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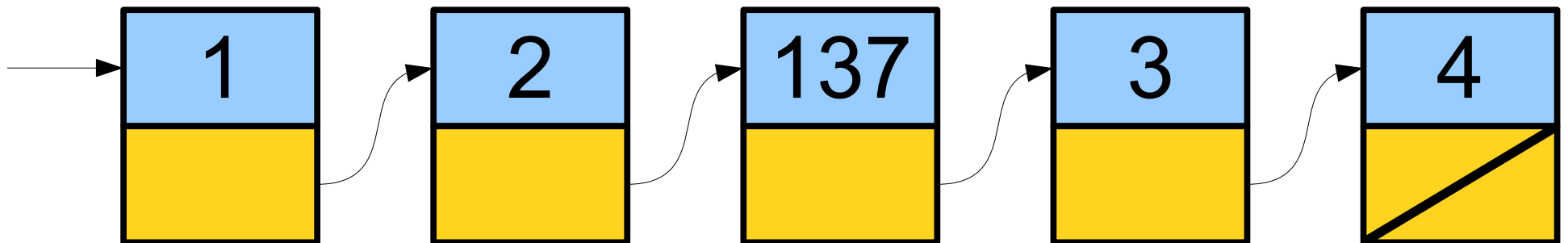
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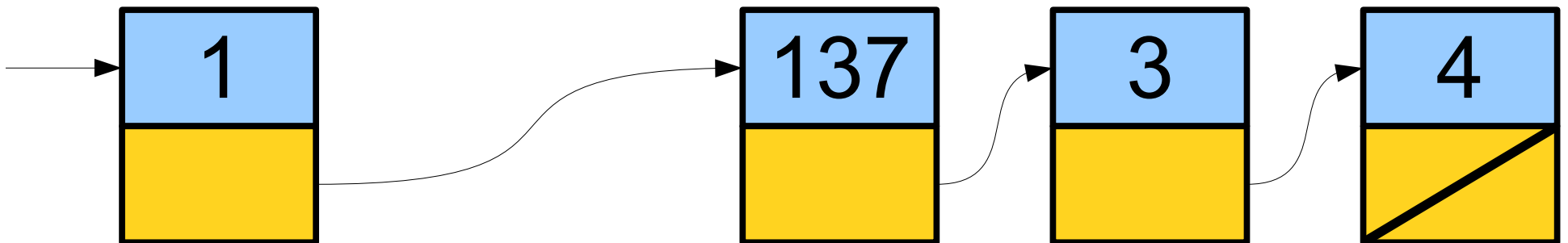
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# Linked Lists at a Glance

- Can efficiently splice new elements into the list or remove existing elements anywhere in the list.
- Never have to do a massive copy step; insertion is efficient in the worst-case.
- Has some tradeoffs; we'll see this later.

# Building our Vocabulary

- In order to use linked lists, we will need to introduce or revisit several new language features:
  - Structures
  - Dynamic allocation
  - Null pointers



# Building our Vocabulary

In order to use linked lists, we will need to introduce or revisit several new language features:

- **Structures**

Dynamic allocation

Null pointers

# Structures

- In C++, a **structure** is a type consisting of several individual variables all bundled together.
- To create a structure, we must
  - Define what fields are in the structure, then
  - Create a variable of the appropriate type.
- Similar to using classes – need to define and implement the class before we can use it.

# Defining Structures

- You can define a structure by using the **struct** keyword:

```
struct TypeName {  
    /* ... field declarations ... */  
};
```

- For those of you with a C background: in C++, “**typedef struct**” is not necessary.

# A Simple Structure

```
struct Tribute {  
    string name;  
    int districtNumber;  
};
```

# A Simple Structure

```
struct Tribute {  
    string name;  
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};
```

```
Tribute t;
```

# A Simple Structure

```
struct Tribute {  
    string name;  
    int districtNumber;  
};
```

```
Tribute t;  
t.name = "Katniss Everdeen";  
t.districtNumber = 1;
```

# A Simple Structure

```
struct Tribute {  
    string name;  
    int districtNumber;  
};
```

```
Tribute t;  
t.name = "Katniss Everdeen";  
t.districtNumber = 12;
```

# structs and classes

- In C++, a **class** is a pair of an interface and an implementation.
  - Interface controls how the class is to be used.
  - Implementation specifies how it works.
- A **struct** is *usually* a stripped-down version of a **class**:
  - Purely implementation, no interface.
  - Primarily used to bundle information together when no interface is needed.



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# Building our Vocabulary

In order to use linked lists, we will need to introduce or revisit several new language features:

Structures

- **Dynamic allocation**

Null pointers

# Dynamic Memory Allocation

- We have seen the **new** keyword used to allocate arrays, but it can also be used to allocate single objects.
- The syntax

**new** *T*(*args*)

creates a new object of type *T* passing the appropriate arguments to the constructor, then returns a pointer to it.

# Dynamic Memory Allocation

```
struct Tribute {  
    string name;  
    int districtNumber;  
};
```

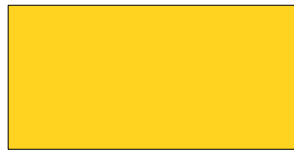
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Tribute* t = new Tribute;
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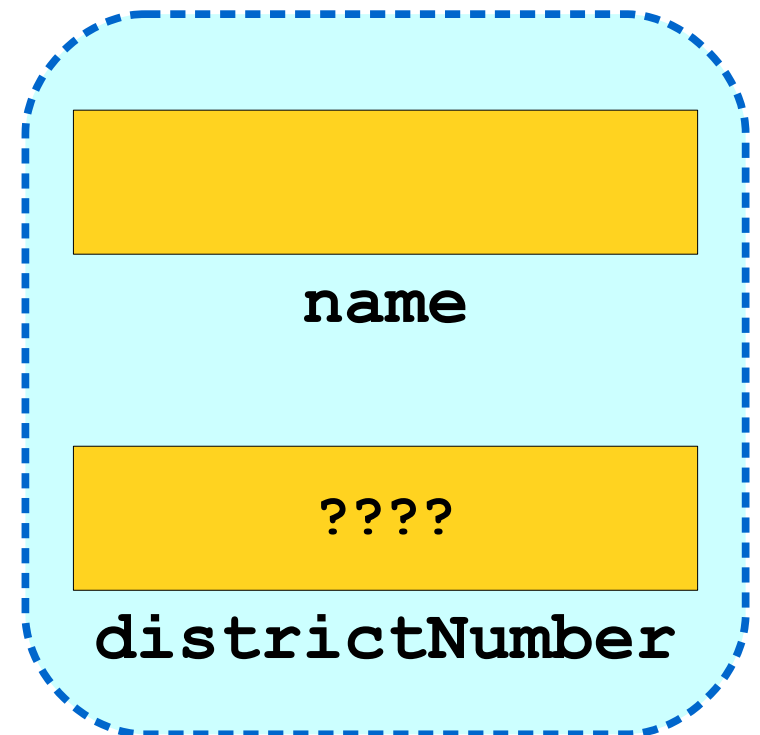
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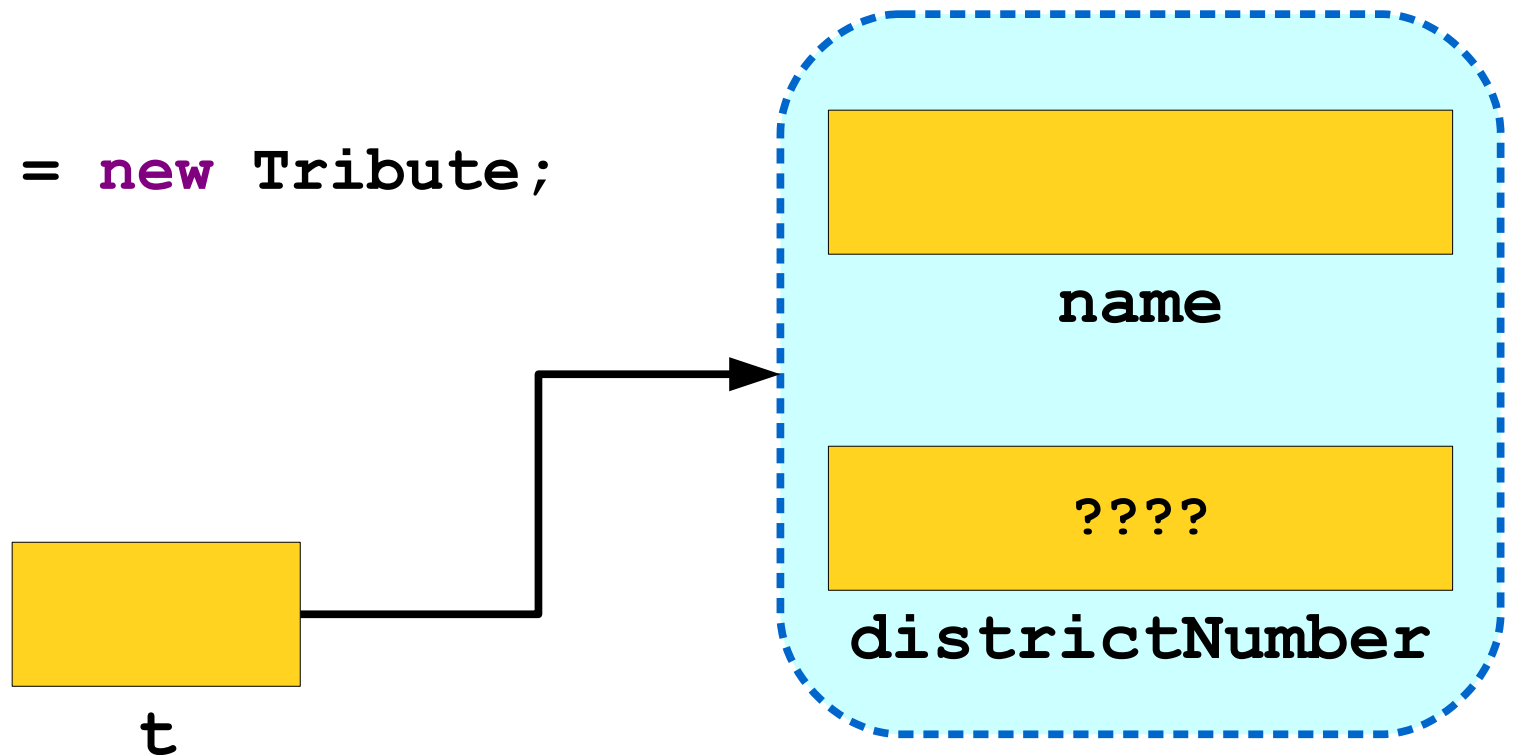
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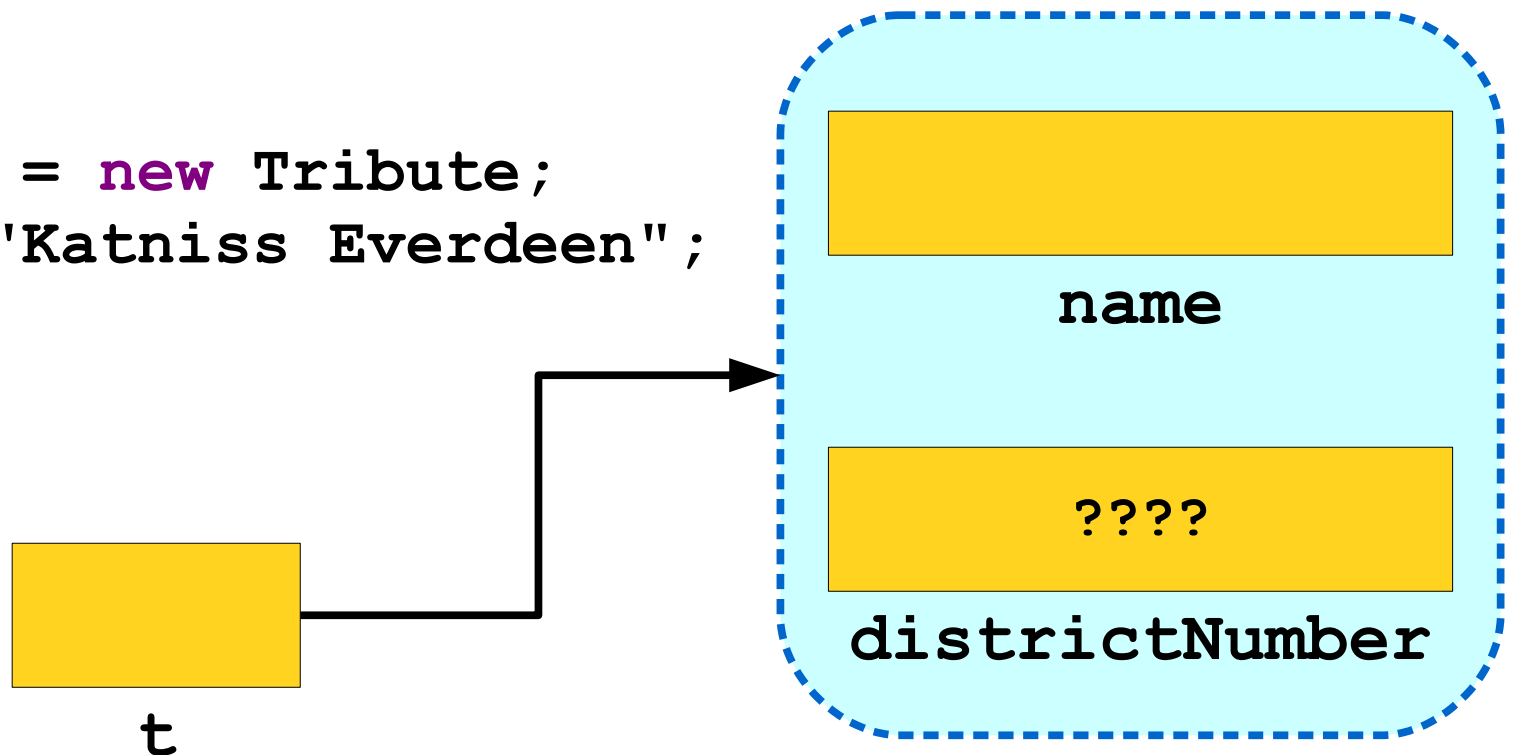




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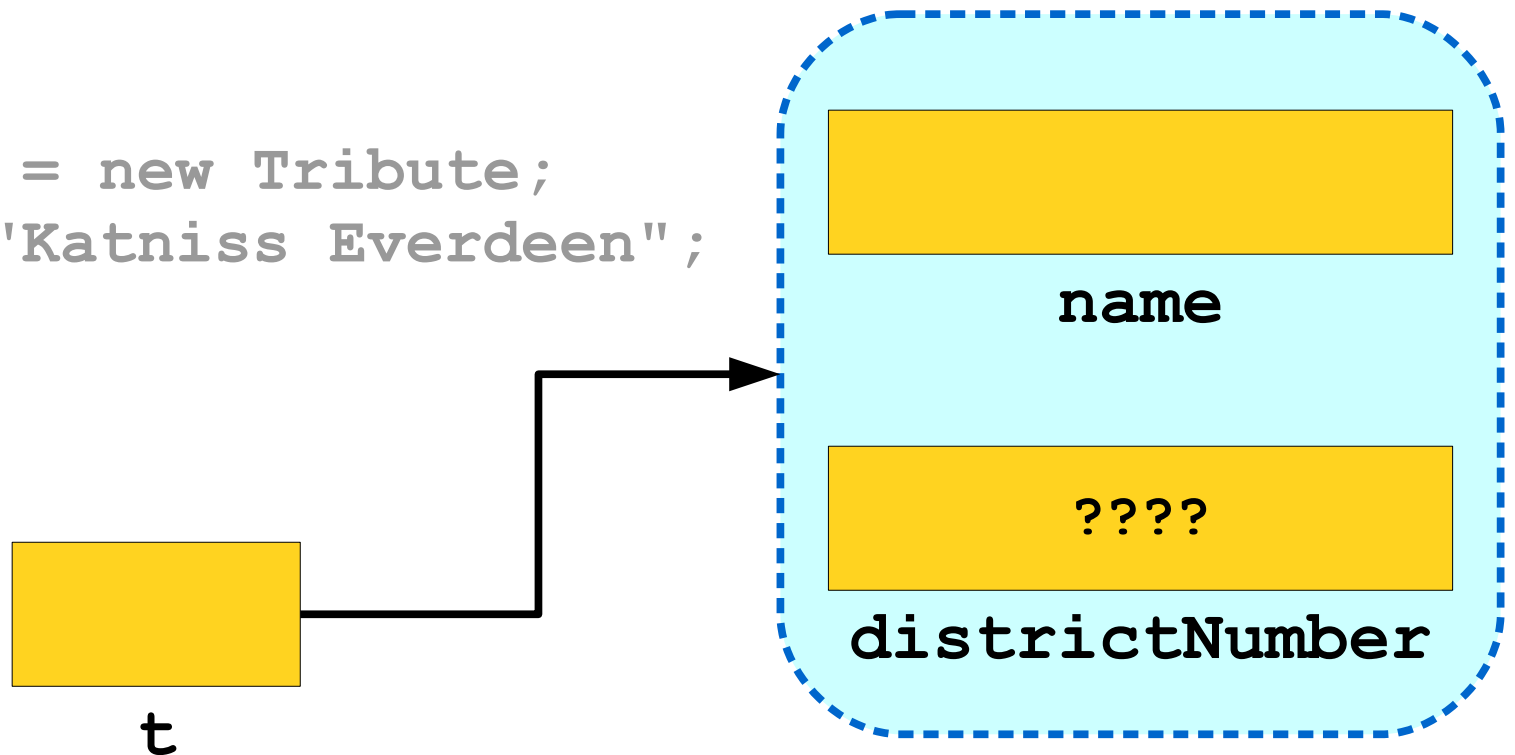
```
Tribute* t = new Tribute;  
t->name = "Katniss Everdeen";
```



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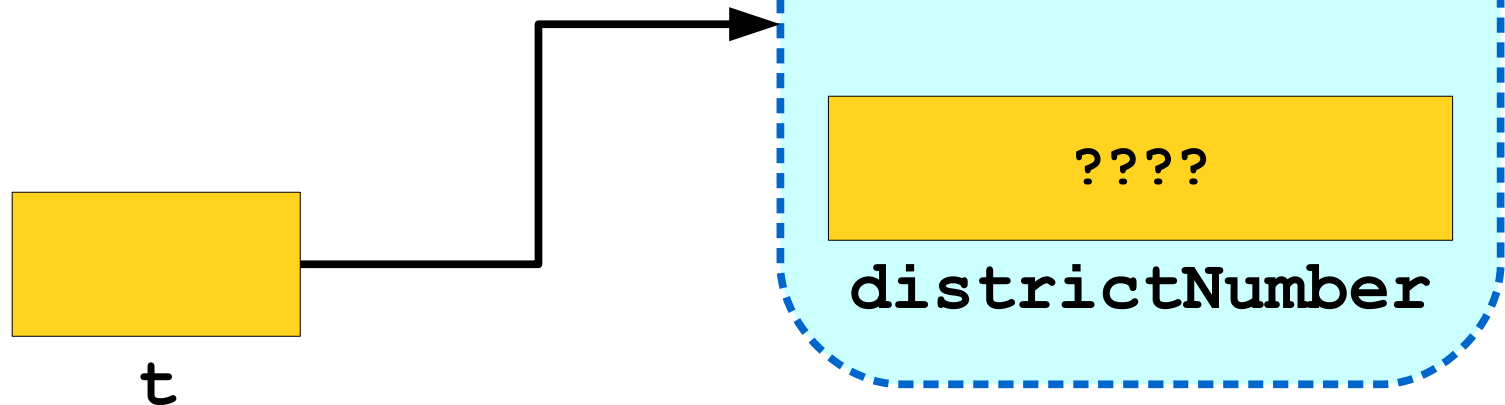


# Dynamic Memory Allocation

```
struct Tribute {  
    string name;  
    int districtNumber;  
};
```

Because `t` is a pointer to a `Tribute`, not an actual `Tribute`, we have to use the arrow operator to access the fields pointed at by `t`.

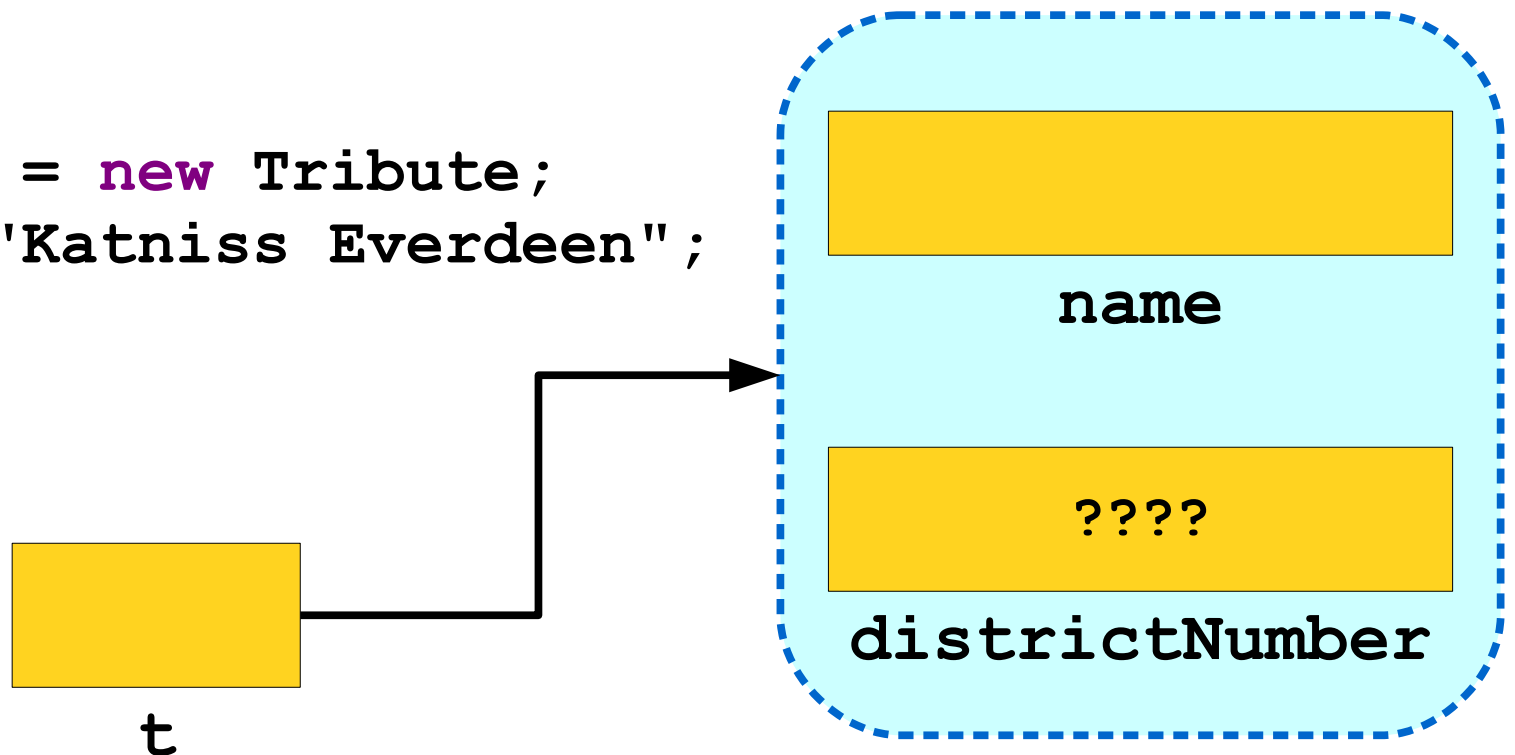
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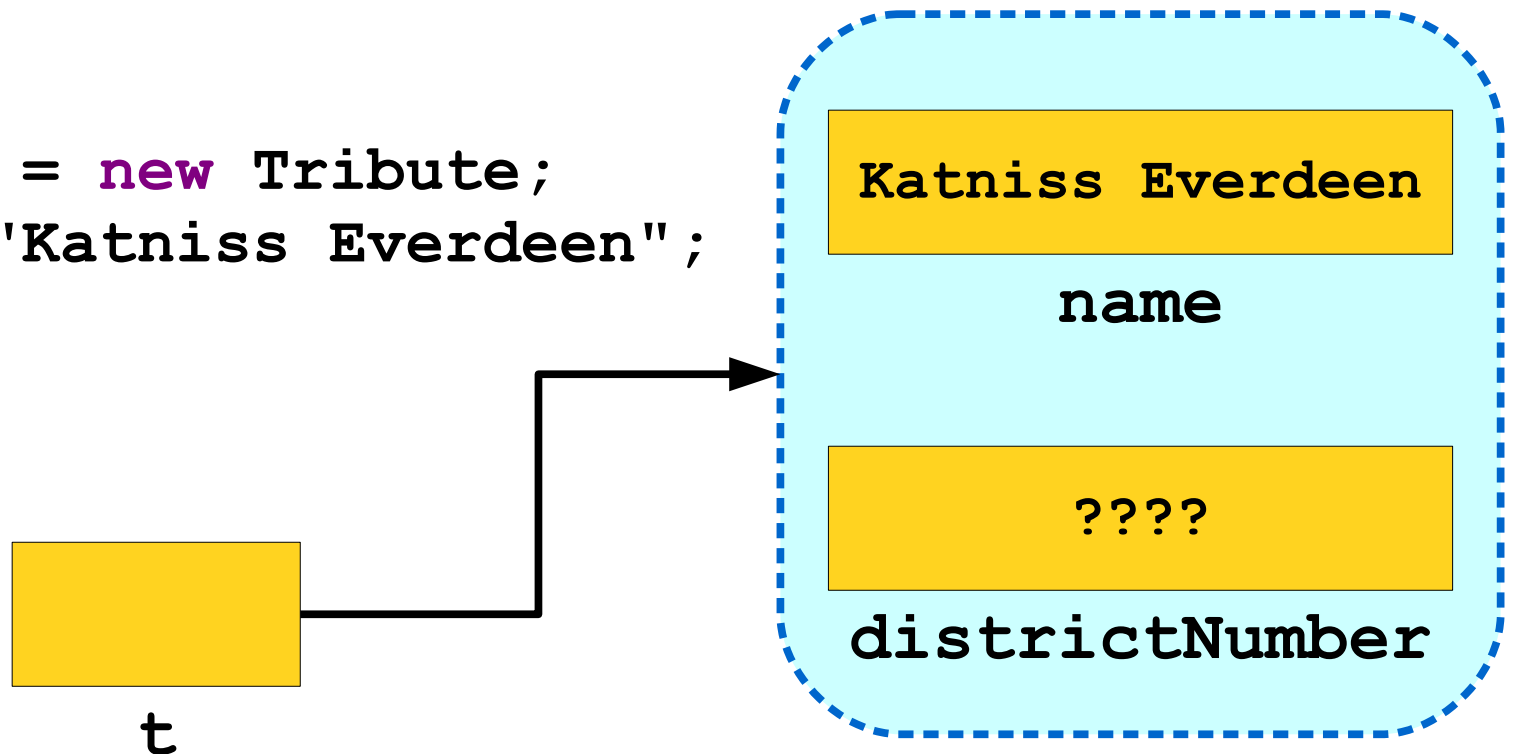
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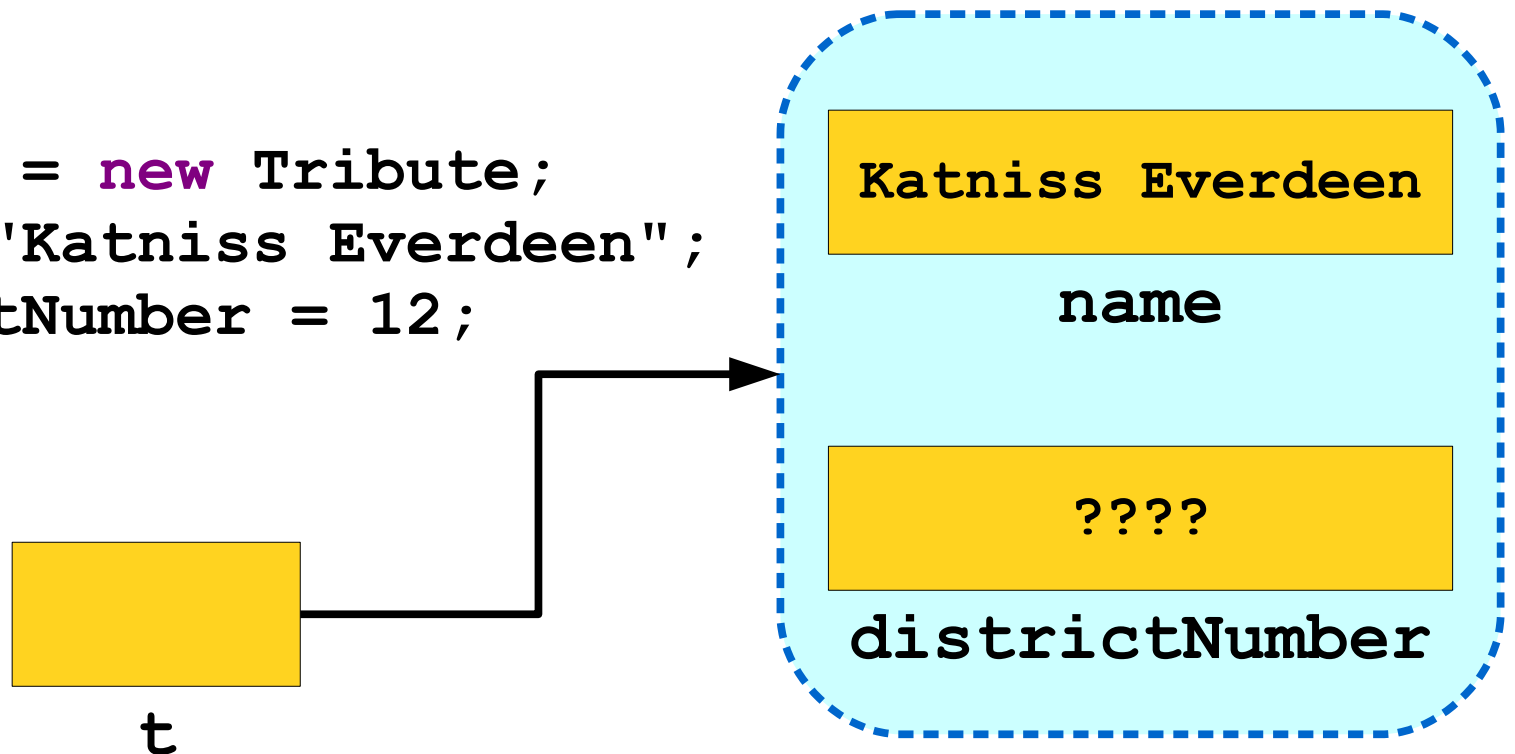
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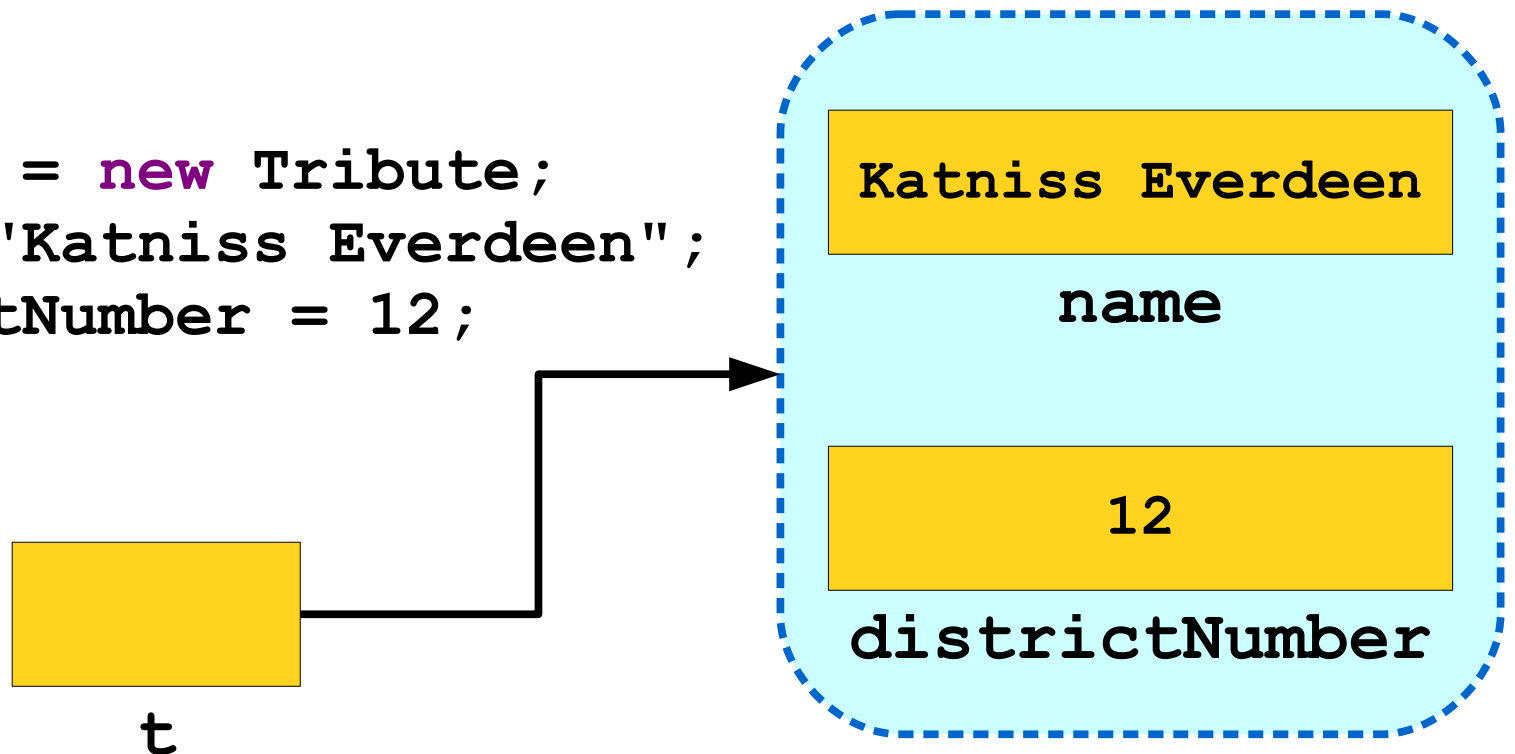
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Tribute* t = new Tribute;  
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# Cleaning Up

- As with dynamic arrays, you are responsible for cleaning up memory allocated with **new**.
- You can deallocate memory with the **delete** keyword:

**delete** *ptr*;

- This destroys the object pointed at by the given pointer, not the pointer itself.





# Cleaning Up

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**delete** *ptr*;

- This destroys the object pointed at by the given pointer, not the pointer itself.



# Unfortunately...

- In C++, all of the following result in undefined behavior:
  - Deleting an object with `delete[]` that was allocated with `new`.
  - Deleting an object with `delete` that was allocated with `new[]`.
- Although it is not always an error, it is usually a Very Bad Idea to treat an array like a single object or vice-versa.

# Building our Vocabulary

- In order to use linked lists, we will need to introduce or revisit several new language features:
  - Structures
  - Dynamic allocation
  - Null pointers

# Building our Vocabulary

In order to use linked lists, we will need to introduce or revisit several new language features:

Structures

Dynamic allocation

- **Null pointers**

# A Pointless Exercise

- When working with pointers, we sometimes wish to indicate that a pointer is not pointing to anything.
- In C++, you can set a pointer to **NULL** to indicate that it is not pointing to an object:

```
ptr = NULL;
```

- This is **not** the default value for pointers; by default, pointers default to a garbage value.

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- Dynamic allocation
- Null pointers



And now... linked lists!

# Linked List Cells

- A linked list is a chain of **cells**.
- Each cell contains two pieces of information:
  - Some piece of data that is stored in the sequence, and
  - A **link** to the next cell in the list.
- We can traverse the list by starting at the first cell and repeatedly following its link.

# Representing a Cell

- For simplicity, let's assume we're building a linked list of **strings**.
- We can represent a cell in the linked list as a structure:

```
struct Cell {  
    string value;  
    /* ? */ next;  
};
```

# Representing a Cell

- For simplicity, let's assume we're building a linked list of **strings**.
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```
struct Cell {  
    string value;  
    Cell* next;  
};
```

- **The structure is defined recursively!**

# Creating a Linked List (Pseudocode + Drawing)

# Building Linked Lists