CS 106B Lecture 12: Memoization and Structs

Friday, April 28, 2017

Programming Abstractions Spring 2017 Stanford University Computer Science Department

Lecturer: Chris Gregg

reading: Programming Abstractions in C++, Chapter 10





# Today's Topics

- •Logistics
- Practice Midterm: went pretty well from our end!
- •You can still take the on-computer test and submit for a bonus point on your midterm
- •We have put together a midterm information page on the website, with old midterms, study tips, and information about the exam: <u>http://web.stanford.edu/</u> <u>class/cs106b/handouts/midterm.html</u>
- Assignment four: Boggle! (now has suggested milestones)
- Memoization
- More on Structs



# The Triangle Game

#### https://www.youtube.com/watch?v=kbKtFN71Lfs&feature=youtu.be



# Assignment 4: Boggle



A classic board game with letter cubes (dice) that is not dog friendly: <u>https://www.youtube.com/watch?v=2shOz1ZLw4c</u>



# Assignment 4b: Boggle

Human		5						puter				17
oil forr room	n roomy		F	Y	С	L	coif giro limy roil	coil glim miri roof	coir hoof moil	corm iglu moor	firm limo rimy	
				0	Μ	G						
			Ο	R		L						
			H	J	H	U						

In Boggle, you can make words starting with any letter and going to any adjacent letter (diagonals, too), but you cannot repeat a letter-cube.



# Memoization

# Tell me and I forget. Teach me and I rememoize.\*

- Xun Kuang, 300 BCE

\* Some poetic license used when translating quote

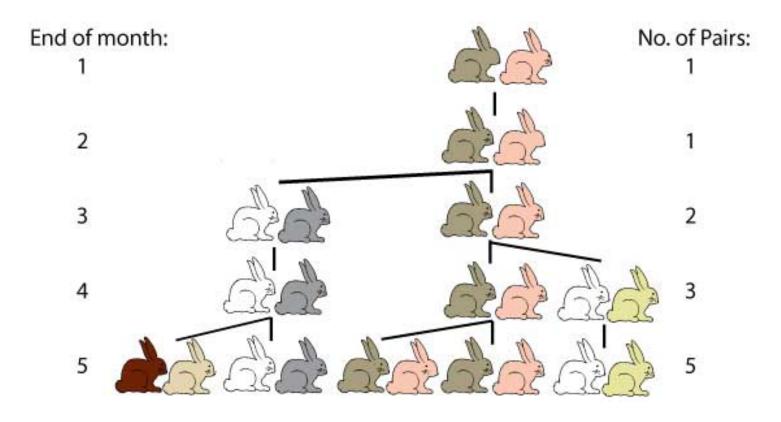


• Let's look at one of the most beautiful recursive definitions:

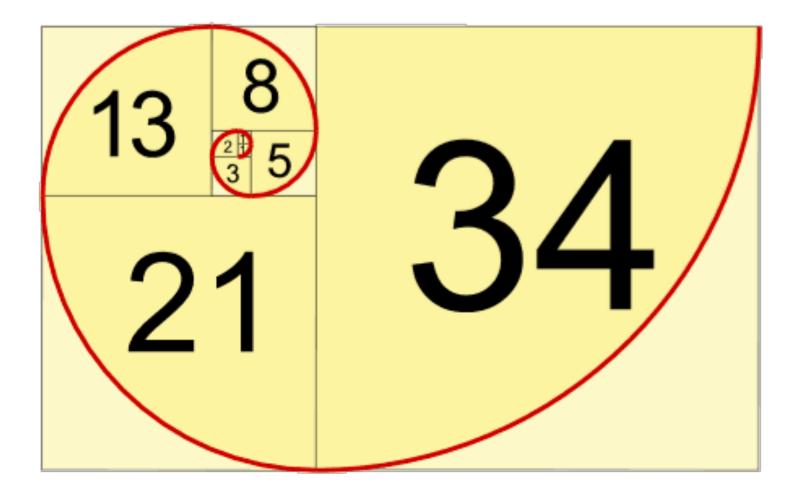
$$F_n = F_{n-1} + F_{n-2}$$
  
where  $F_0=0, F_1=1$ 



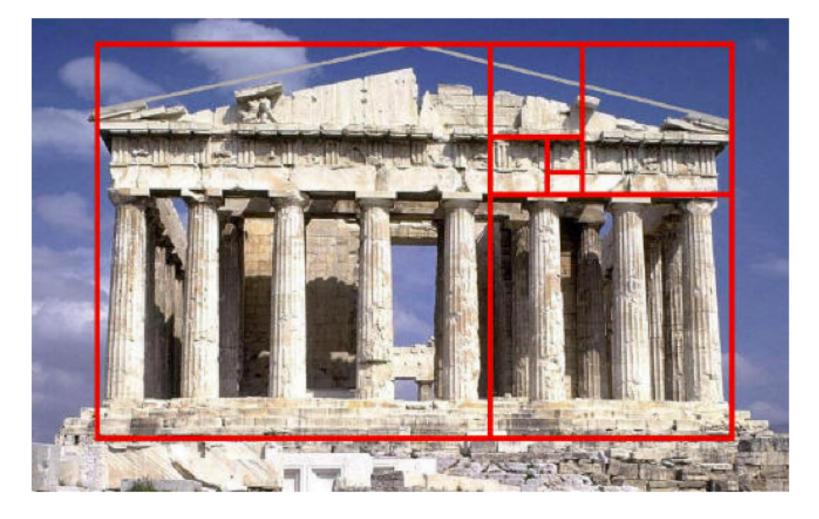
This definition leads to this:



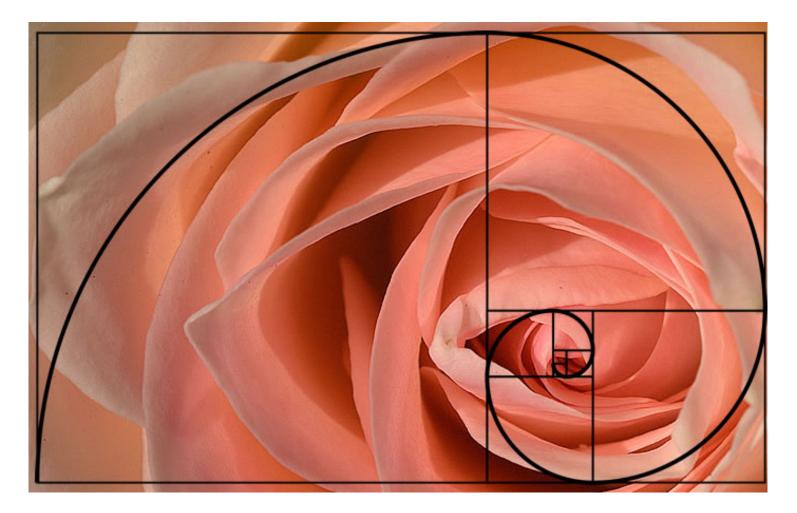




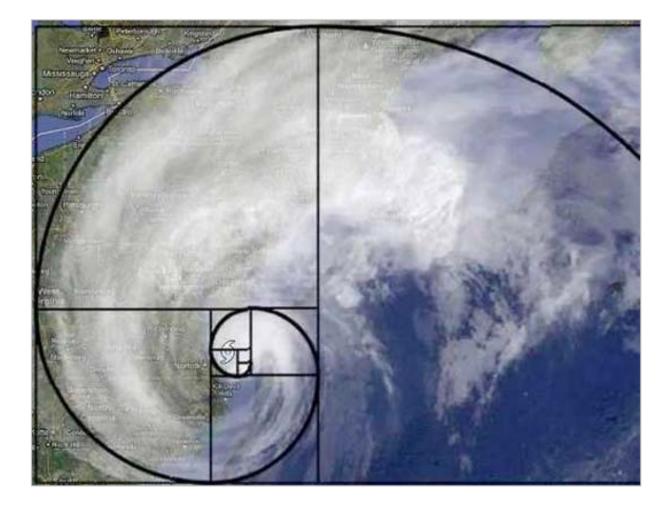




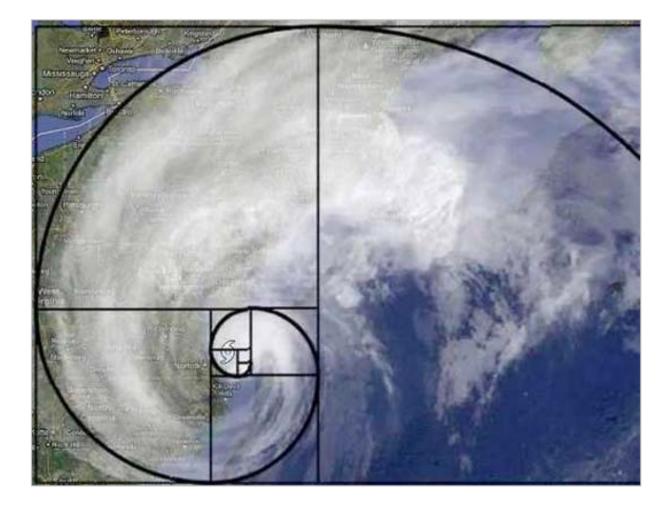










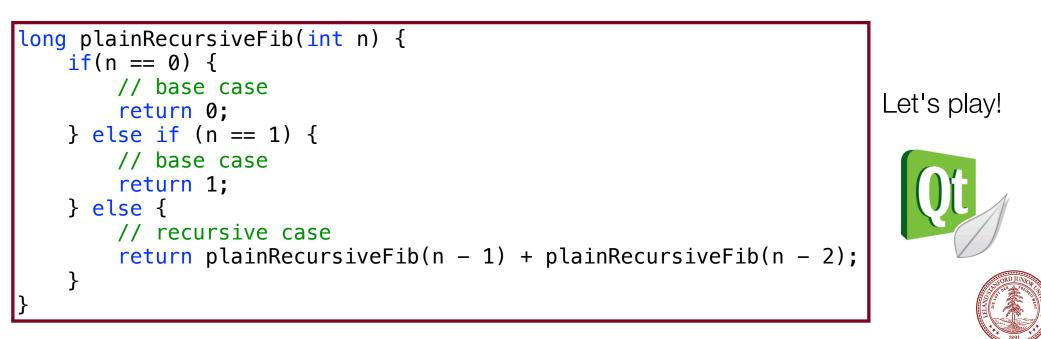


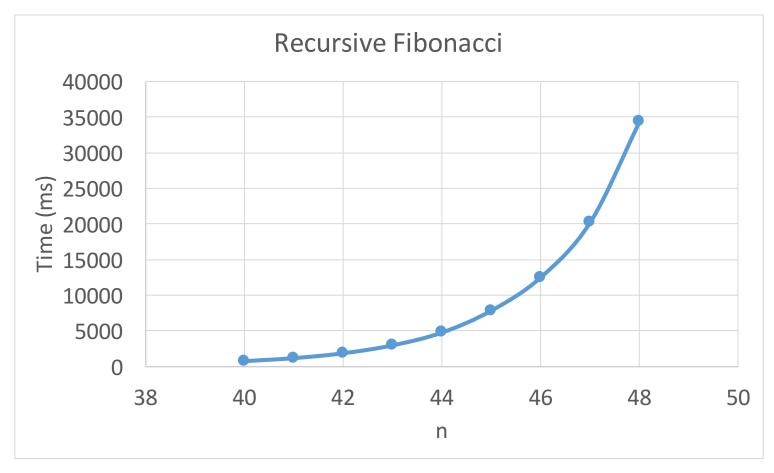


 $F_n = F_{n-1} + F_{n-2}$ where  $F_0=0, F_1=1$ 

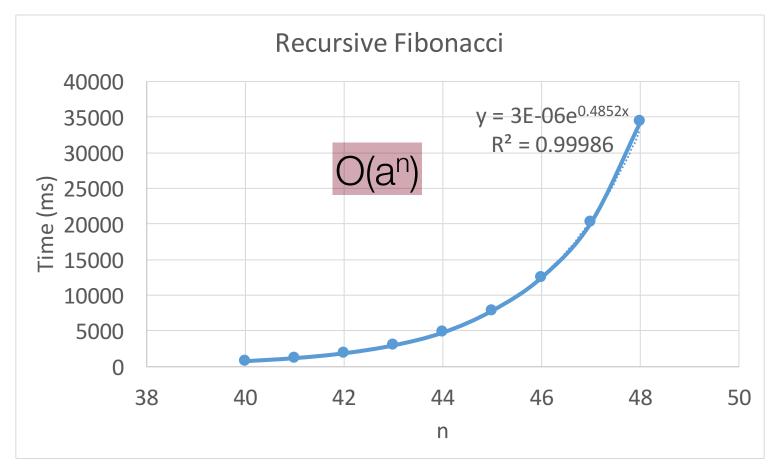
п	0	1	2	3	4	5	6	7	8	9	
$F_n$	0	1	1	2	3	5	8	13	21	34	

This is particularly easy to code recursively!

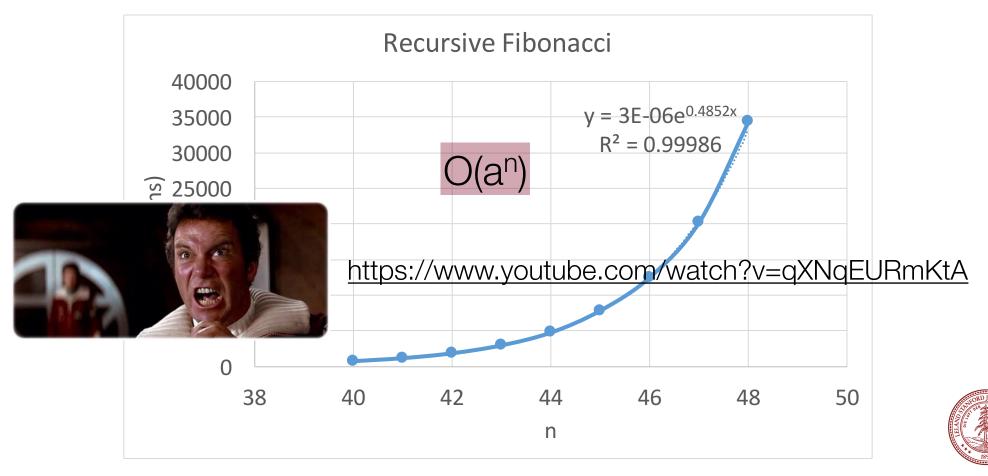


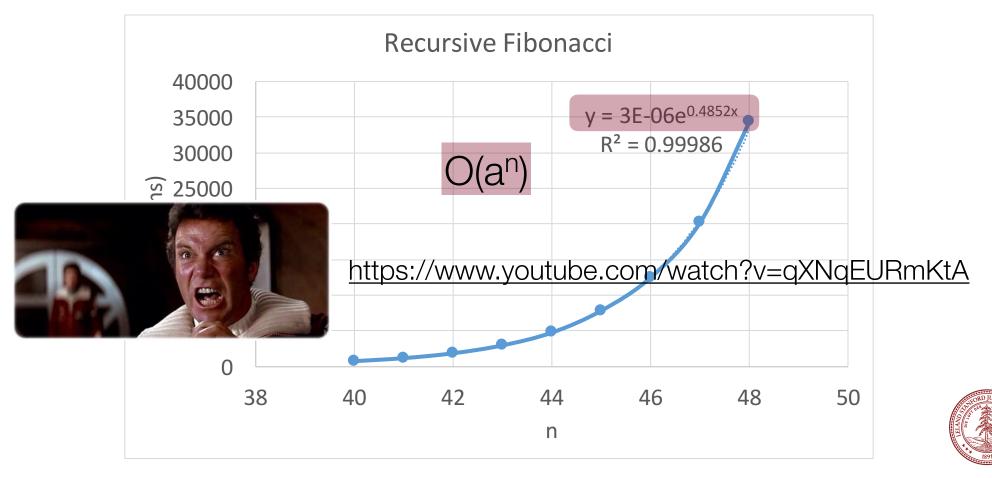


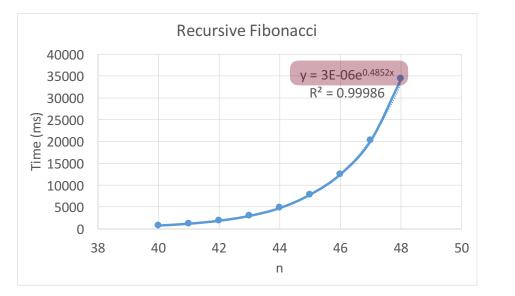












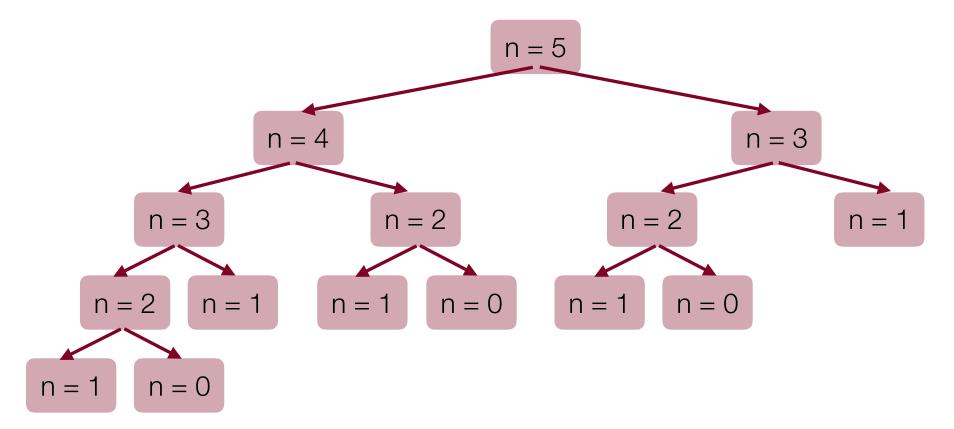
By the way:

 $3x10^{-6}e^{0.4852n} \approx O(1.62^{n})$ O(1.62<sup>n</sup>) is technically O(2<sup>n</sup>) because O(1.62<sup>n</sup>) < O(2<sup>n</sup>)

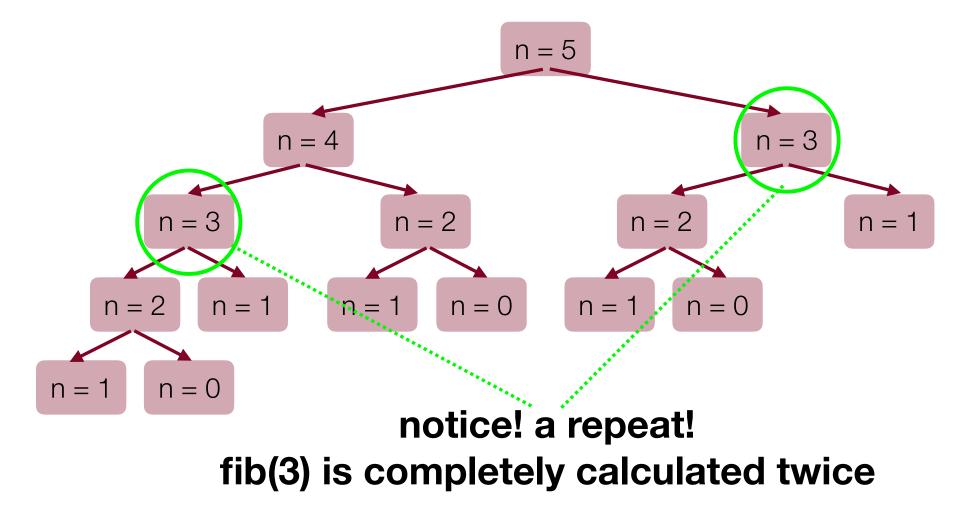
We call this a "tighter bound," and we like round numbers, especially ones that are powers of two. :)

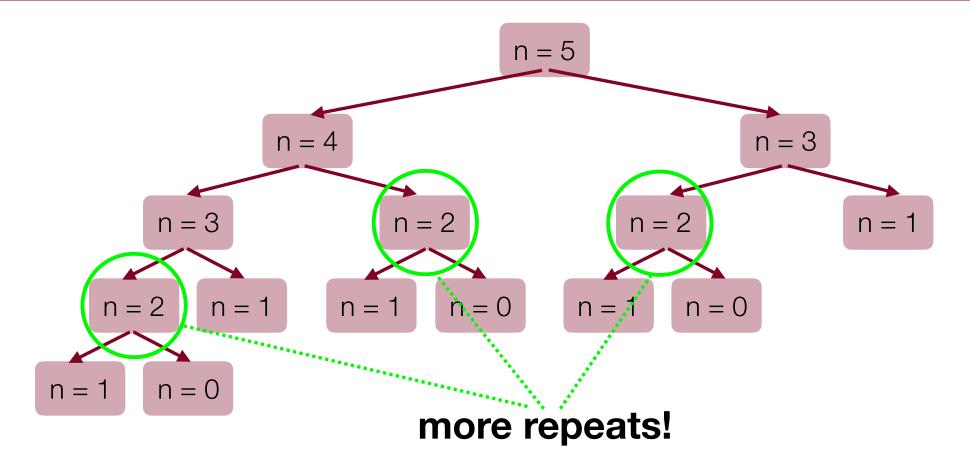


# Fibonacci: Recursive Call Tree

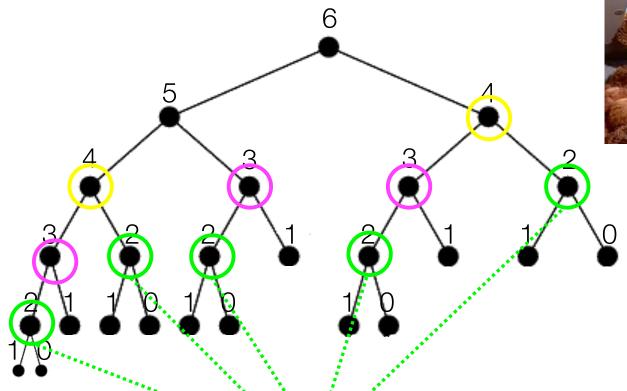


This is basically the reverse of binary search: we are splitting into two marginally smaller cases, not splitting into half of the problem size!





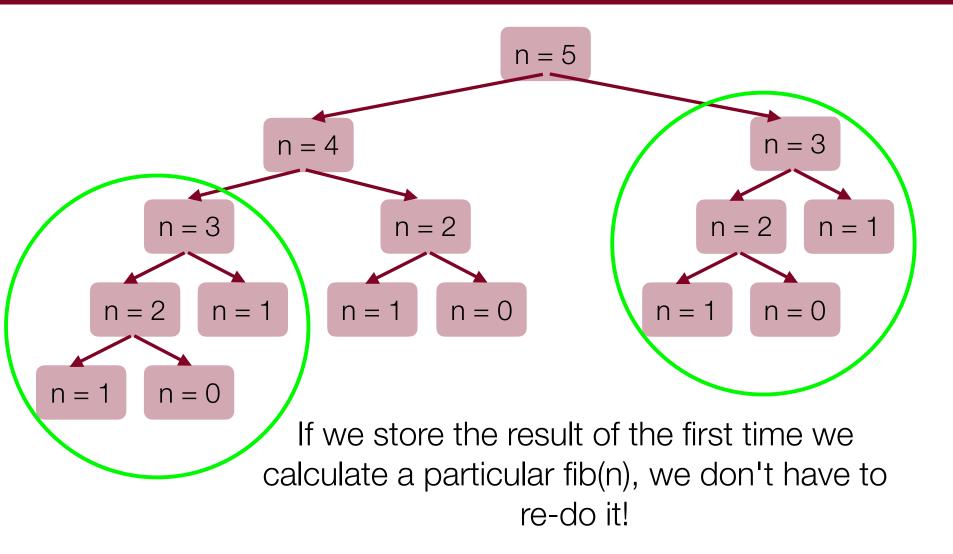






# let's leverage all the repeats!





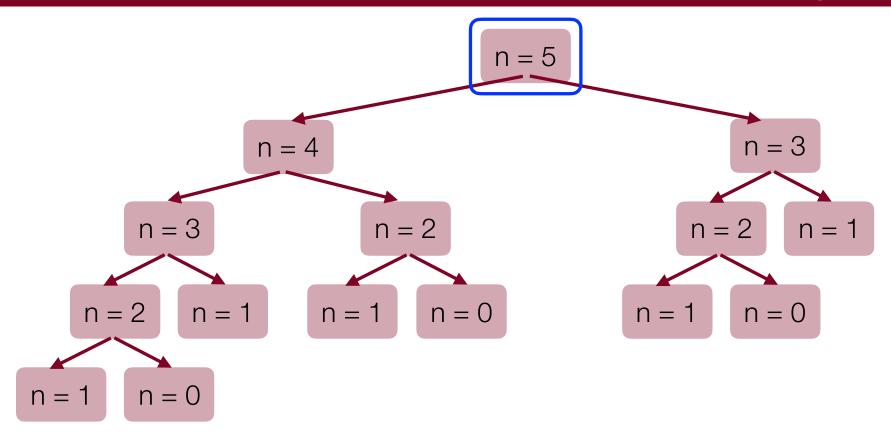
**Memoization**: Store previous results so that in future executions, you don't have to recalculate them.

aka

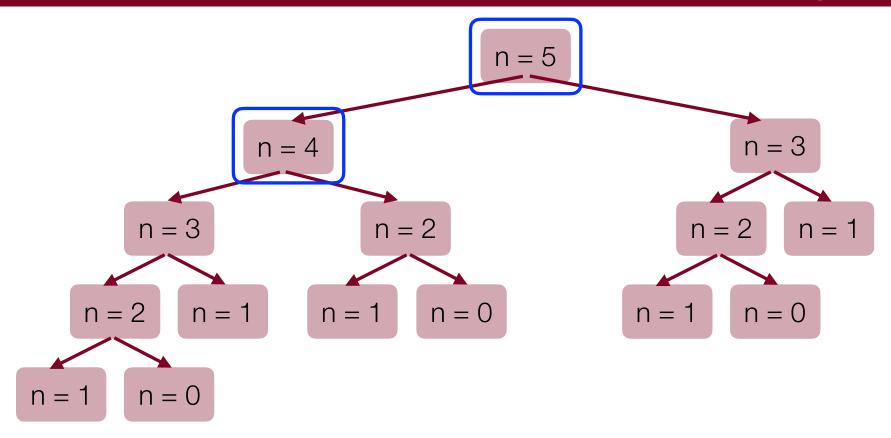
Remember what you have already done!



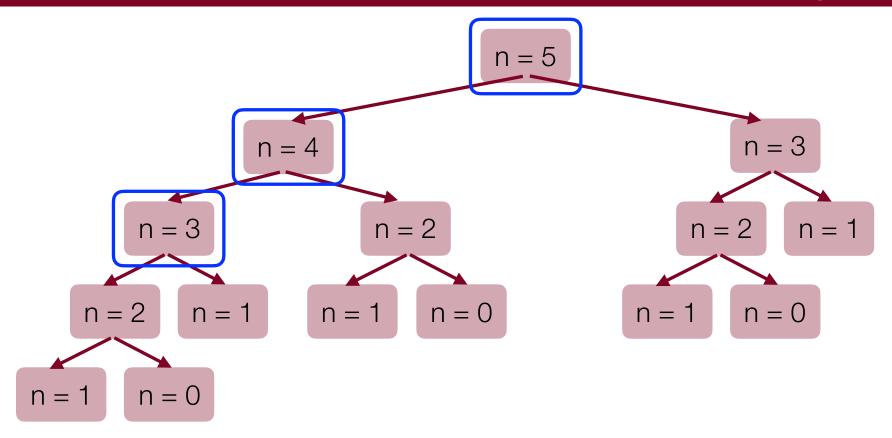




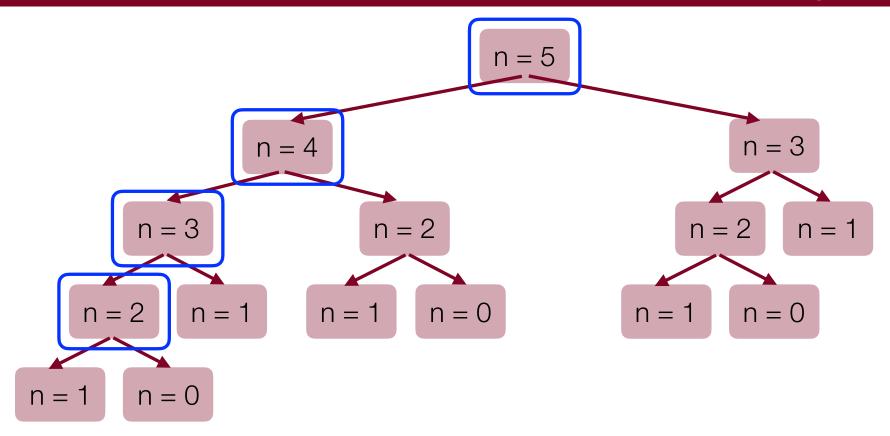




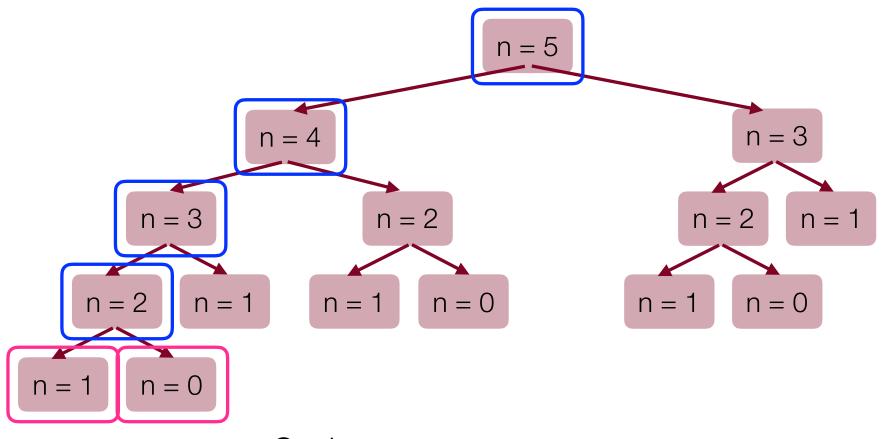




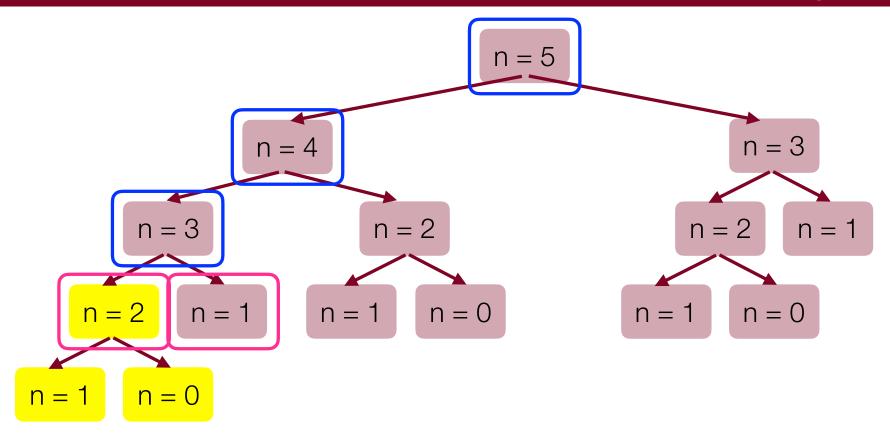






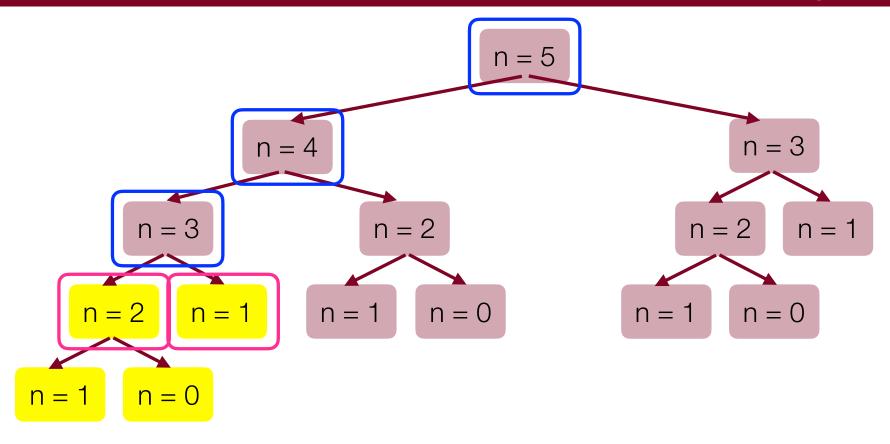






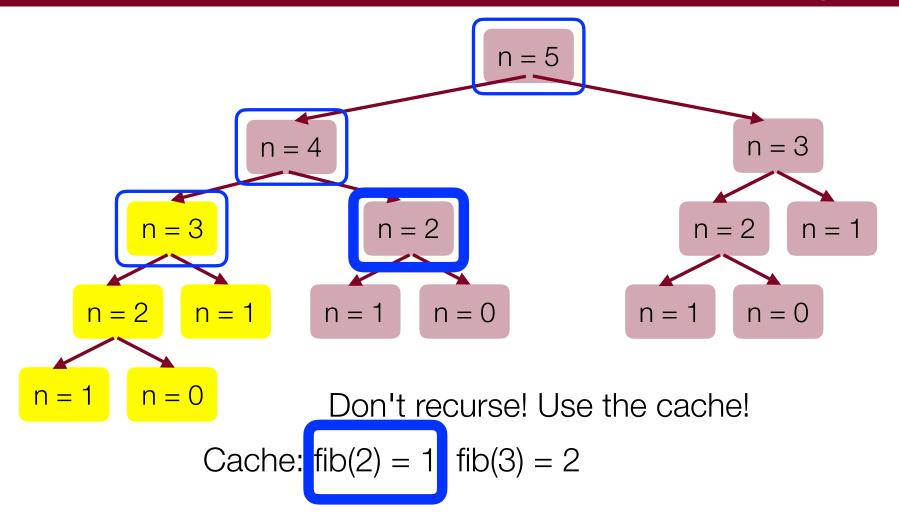
Cache: fib(2) = 1

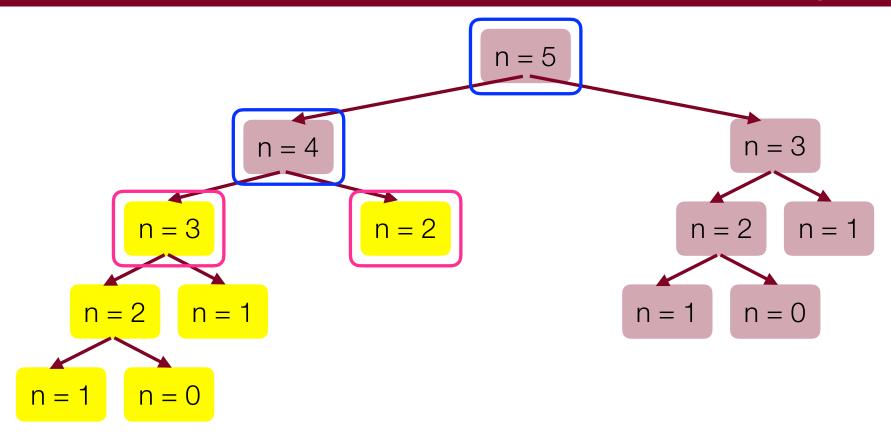




Cache: fib(2) = 1, fib(3) = 2

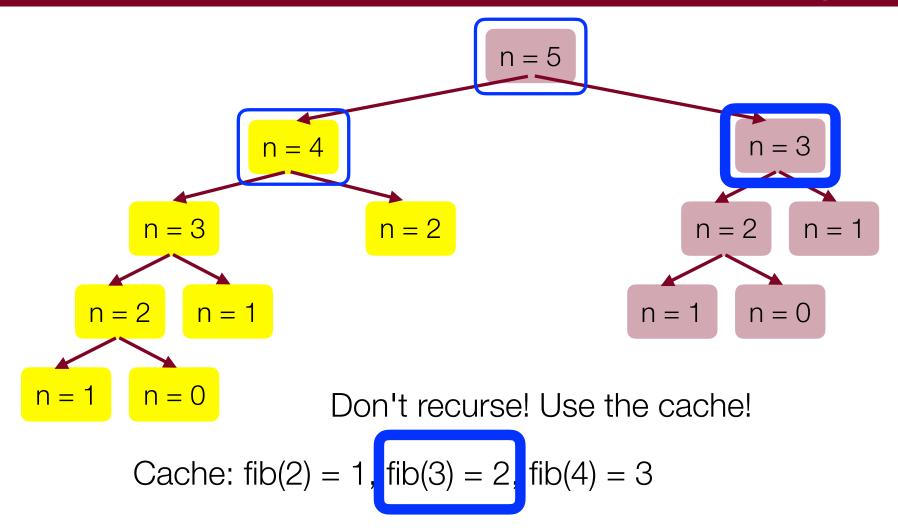


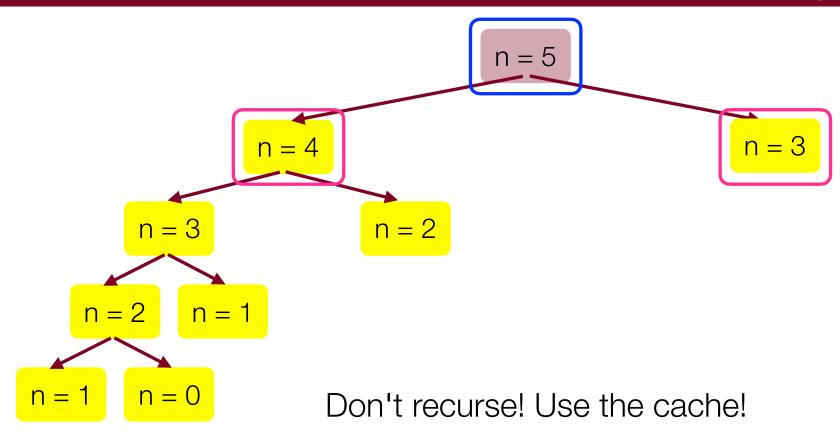




Cache: fib(2) = 1, fib(3) = 2

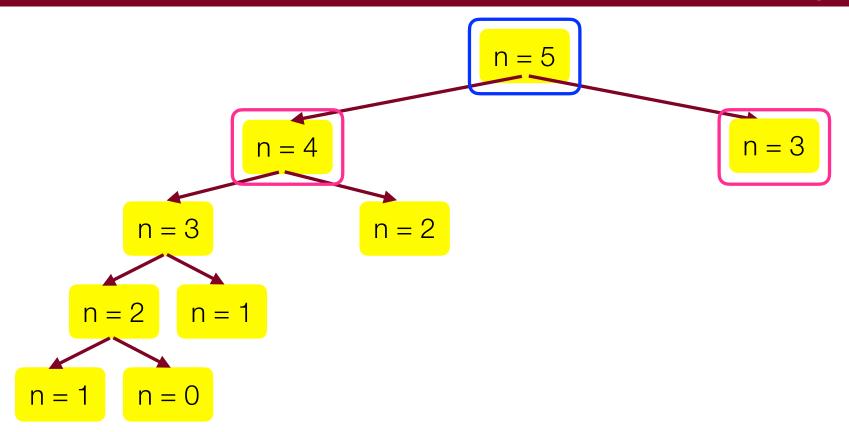






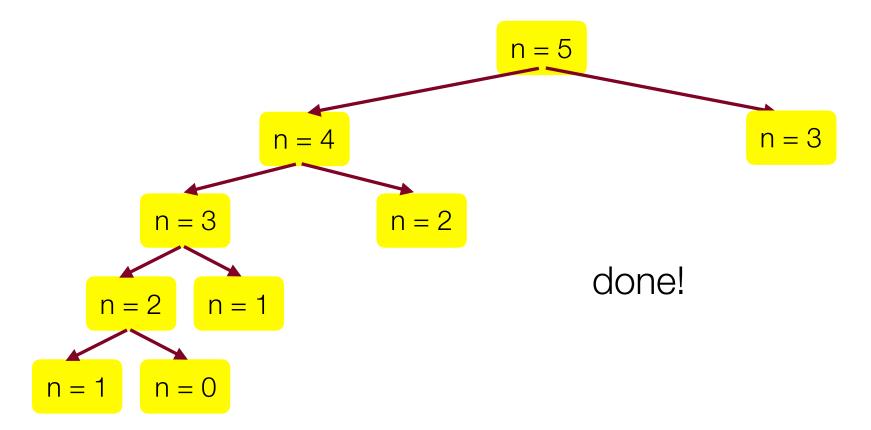
Cache: fib(2) = 1, fib(3) = 2, fib(4) = 3





Cache: fib(2) = 1, fib(3) = 2, fib(4) = 3, fib(5) = 5





Cache: fib(2) = 1, fib(3) = 2, fib(4) = 3, fib(5) = 5



long memoizationFib(int n) {
 Map<int, long> cache;
 return memoizationFib(cache, n);
}

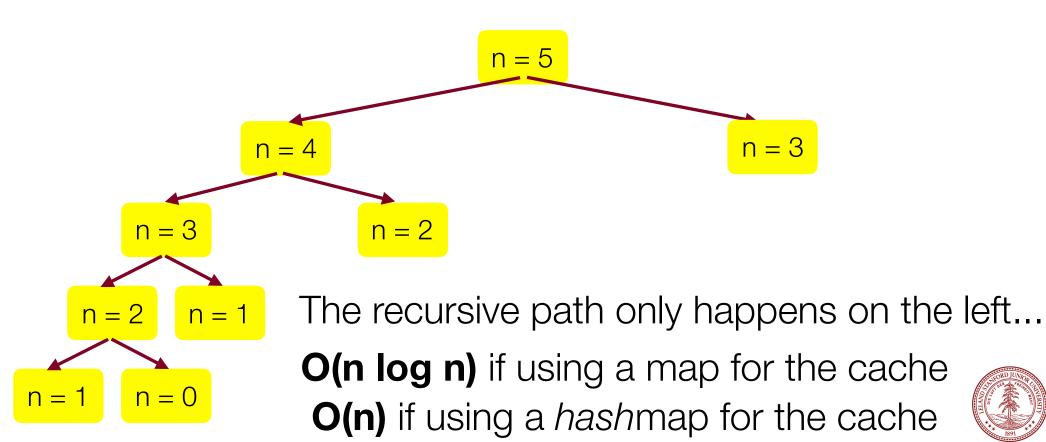
setup for helper function



```
long memoizationFib(int n) {
    Map<int, long> cache;
    return memoizationFib(cache, n);
}
long memoizationFib(Map<int, long>&cache, int n) {
    if(n == 0) \{
        // base case #1
        return 0;
    else if (n == 1) {
        // base case #2
        return 1;
    } else if(cache.containsKey(n)) {
        // base case #3
        return cache[n];
    }
    // recursive case
    long result = memoizationFib(cache, n-1) + memoizationFib(cache, n-2);
    cache[n] = result;
    return result;
}
```



#### Complexity?



## Fibonacci: the bigger picture

There are actually many ways to write a fibonacci function.

This is a case where the plain old iterative function works fine:

```
long iterativeFib(int n) {
    if(n == 0) {
        return 0;
    }
    long prev0 = 0;
    long prev1 = 1;
    for (int i=n; i >= 2; i--) {
        long temp = prev0 + prev1;
        prev0 = prev1;
        prev1 = temp;
    }
    return prev1;
}
```

Recursion is used often, but not *always*.



### Fibonacci: Okay, one more...

Another way to keep track of previously-computed values in fibonacci is through the use of a different helper function that simply passes along the previous values:

```
long passValuesRecursiveFib(int n) {
    if (n == 0) {
        return 0;
    }
    return passValuesRecursiveFib(n, 0, 1);
}
long passValuesRecursiveFib(int n, long p0, long p1) {
    if (n == 1) {
        // base case
        return p1;
    }
    return passValuesRecursiveFib(n-1, p1, p0 + p1);
}
```



## More on Structs

We have mentioned structs already -- they are useful for keeping track of related data as one type, which can get used like any other type. You can think of a struct as the *Lunchable* of the C++ world.



```
struct Lunchable {
    string meat;
    string dessert;
    int numCrackers;
    bool hasCheese;
}
```

};

// Vector of Lunchables
Vector<Lunchable> lunchableOrder;



## A Real Problem



Your cool picture from that trip to Europe doesn't fit on Instagram!



## Bad Option #1: Crop



You got cropped out!

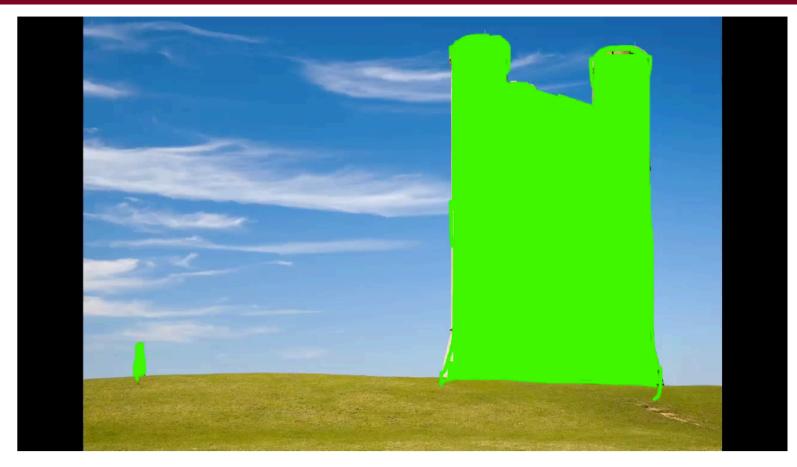


# Bad Option #2: Resize

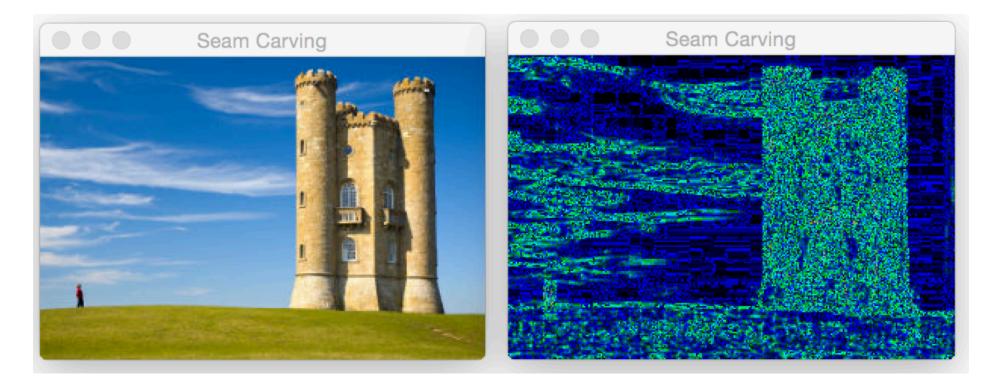


Stretchy castles look weird...



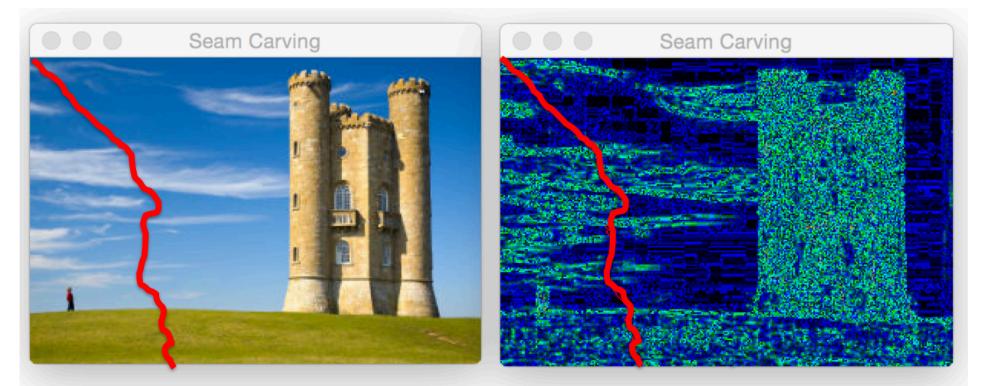






How can you change an image without changing its aspect ration, but while retaining the important information?





We could delete an entire column of pixels, but we could also weave our way through a path of 1-pixel wide image that removes the least amount of stuff.



## How to represent the path

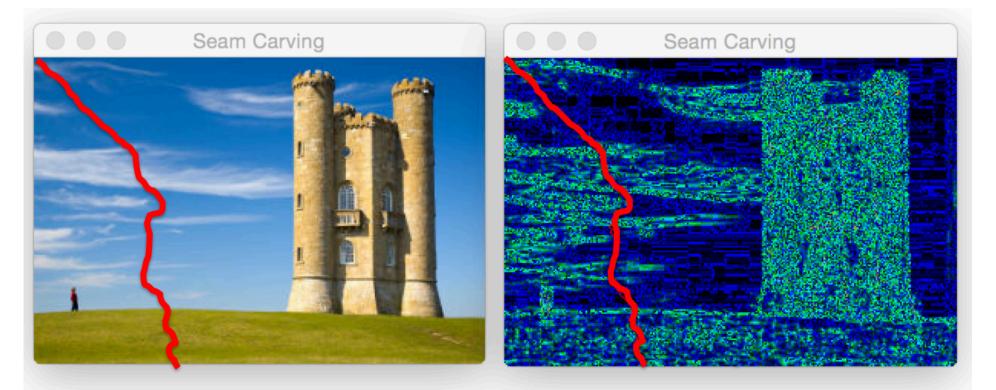
A struct!

```
struct Coord {
    int row;
    int col;
};
```

A path is just a Vector of coordinates:

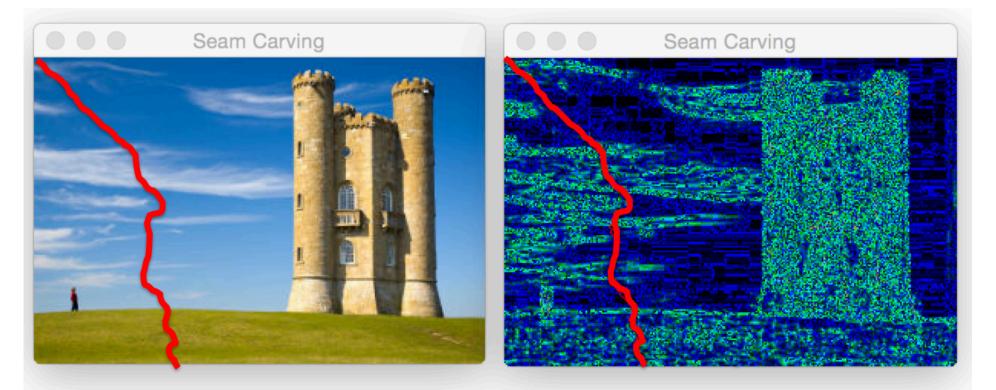
```
int main() {
    Coord myCord;
    myCoord.row = 5;
    myCoord.col = 7;
    cout << myCord.row << endl;
    Vector<Coord> path;
    return 0;
}
```





Important pixels are ones that are considerably different from their neighbors.





Let's write a recursive algorithm that can find the seam that minimizes the sum of all the importances of the pixels.



Vector<Coord> getSeam(Grid<double> &weight, Coord curr);



### References and Advanced Reading

References:

- <u>https://en.wikipedia.org/wiki/Fibonacci\_number</u>
- https://en.wikipedia.org/wiki/Seam\_carving



#### Extra Slides

