CS 106X Lecture 18: Trees

Wednesday, February 22, 2017

Programming Abstractions (Accelerated) Winter 2017 Stanford University Computer Science Department

Lecturer: Chris Gregg

reading: Programming Abstractions in C++, Section 16.1





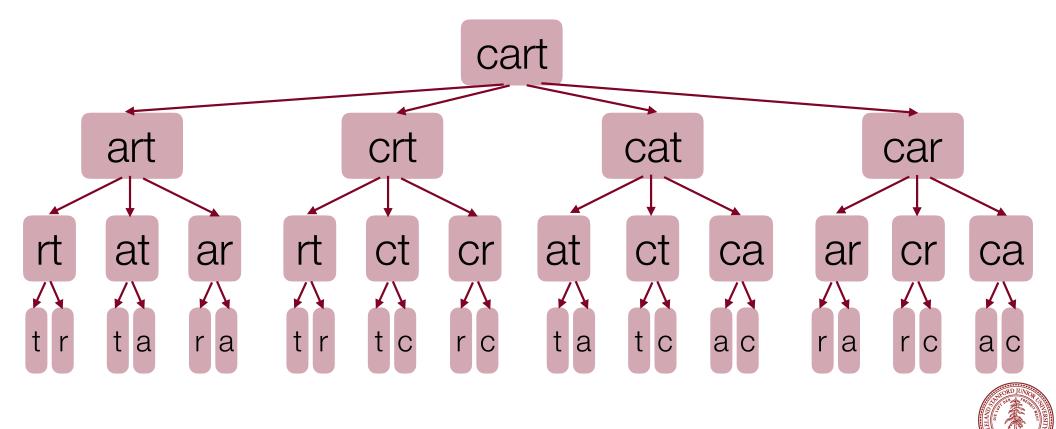
Today's Topics

- •Logistics
- Midterm Tomorrow!
- Midterm will cover up to and including Linked Lists
- Introduction to Trees



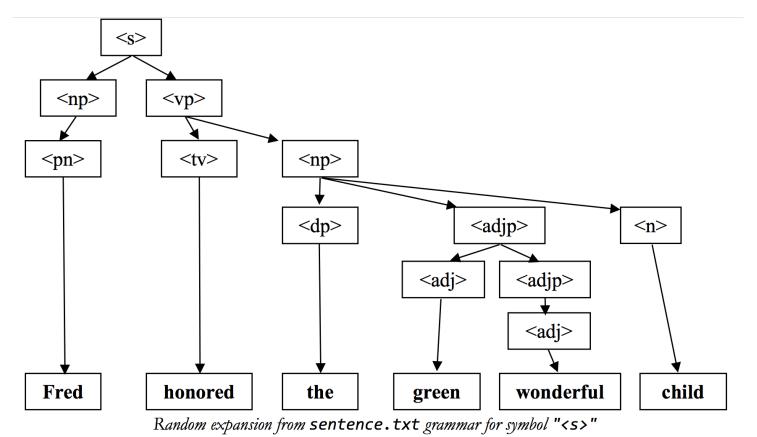
Trees

We have already seen trees in the class in the form of decision trees!



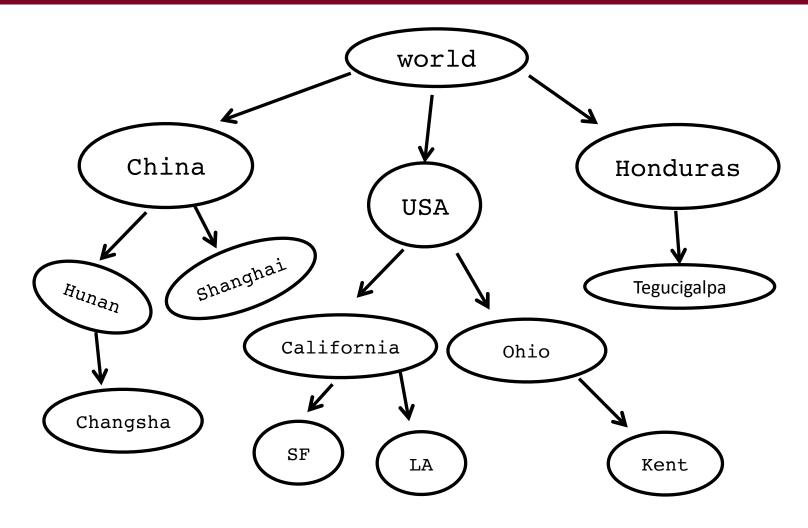
Trees

You've coded trees for recursive assignments!



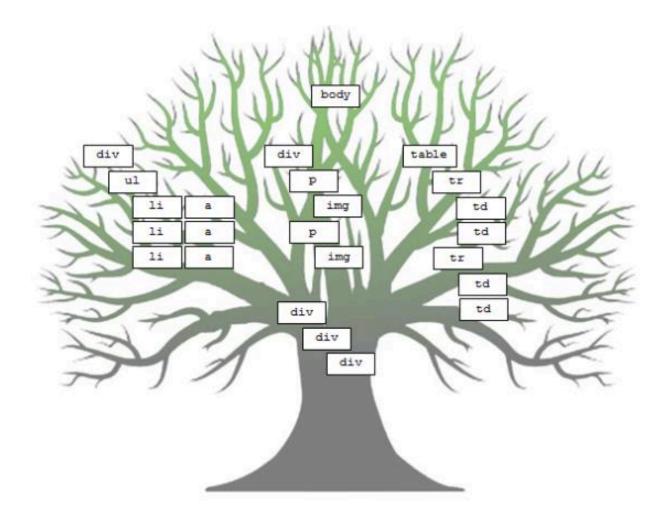


Trees Can Describe Hierarchies



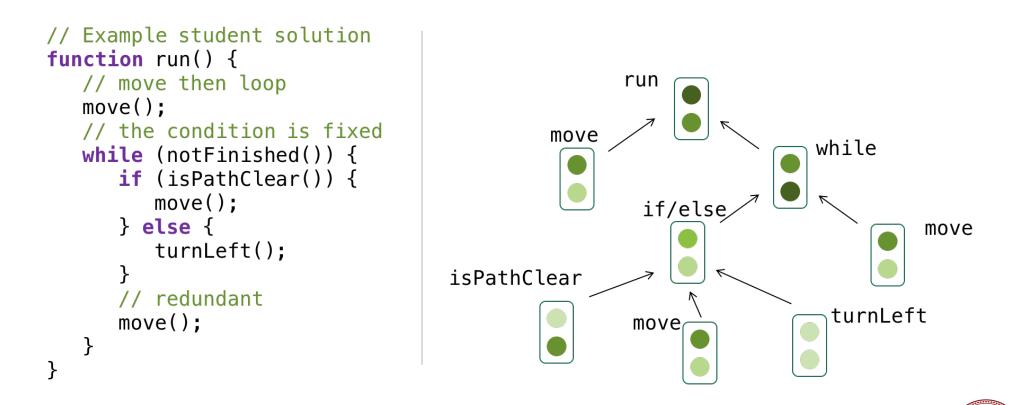


Trees Can Describe Websites (HTML)





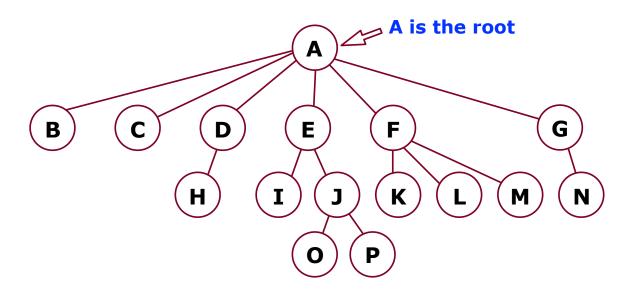
Trees Can Describe Programs



* This is a figure in an academic paper written by a recent CS106 student!

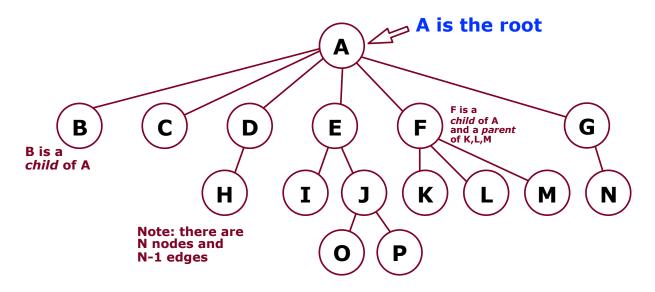
Trees are inherently recursive

What is a Tree (in Computer Science)?



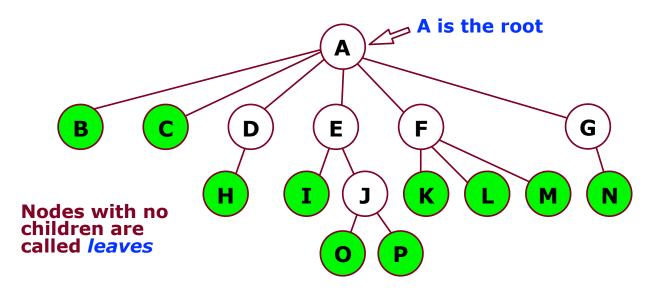


What is a Tree (in Computer Science)?



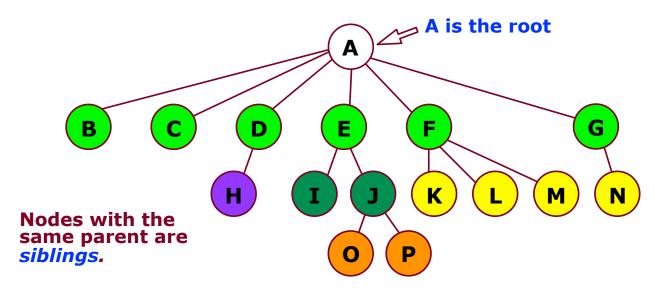


What is a Tree (in Computer Science)?

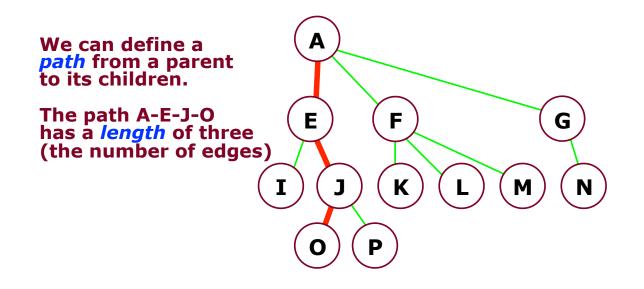




What is a Tree (in Computer Science)?



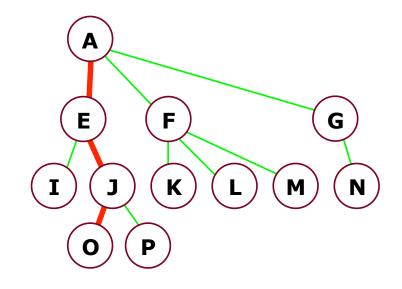




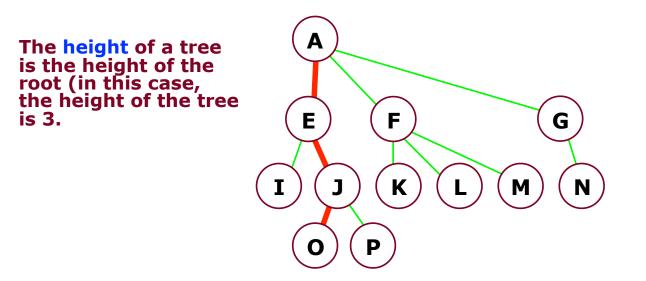


The *depth* of a node is the length from the root. The depth of node J is 2. The depth of the root is 0.

The *height* of a node is the longest path from the node to a leaf. The height of node F is 1. The height of all leaves is 0.





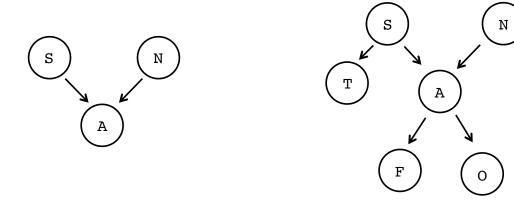




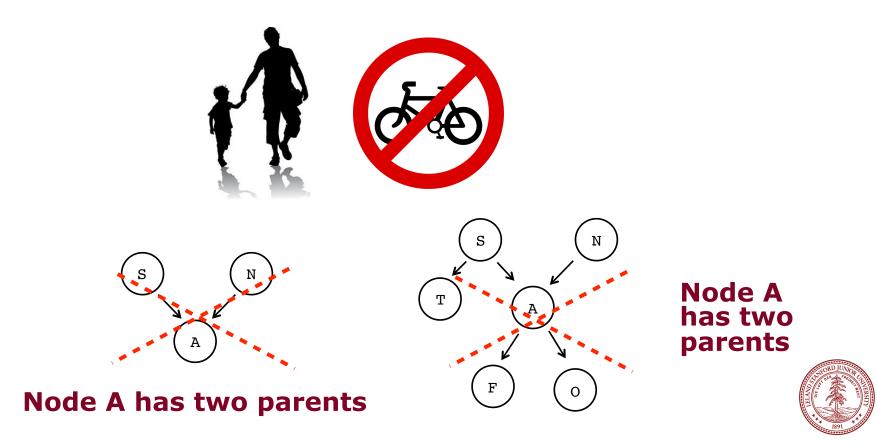


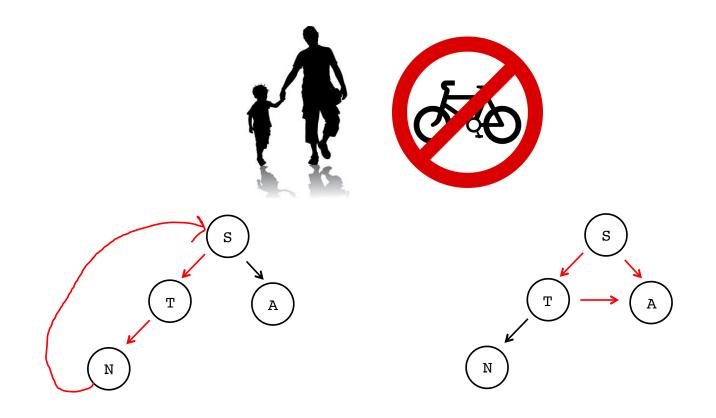




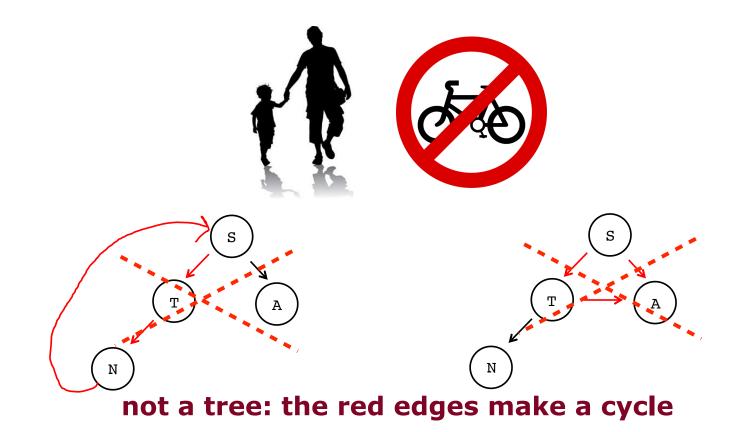




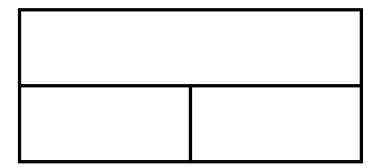














Binary Tree:

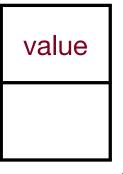
value



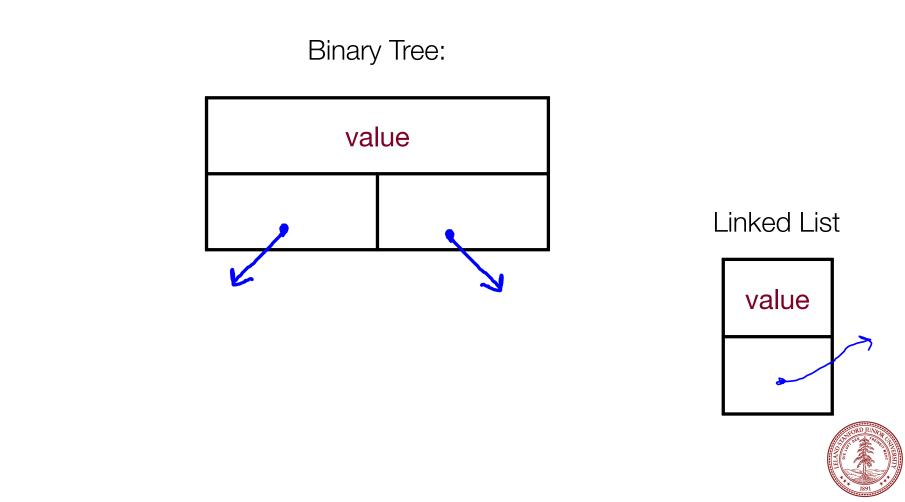
Binary Tree:

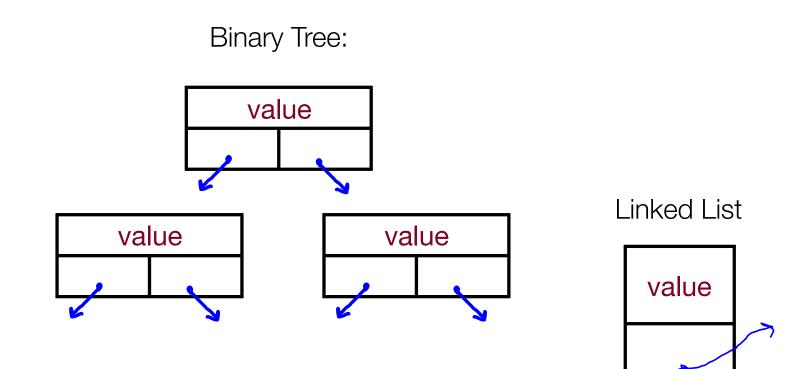
value

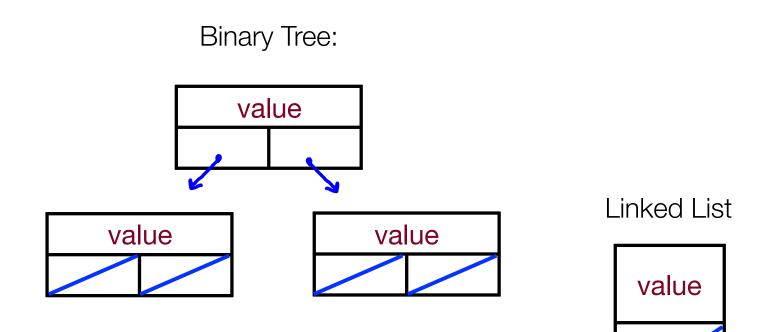
Linked List







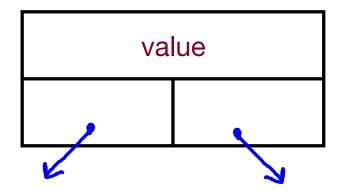




The Most Important Slide

Binary Tree:

```
struct Tree {
    string value;
    Tree *left;
    Tree *right;
};
```

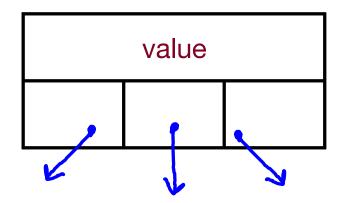




We Can Have Ternary Trees (or any number, *n*)

Ternary Tree:

```
struct Tree {
    string value;
    Tree *left;
    Tree *middle;
    Tree *right;
};
```

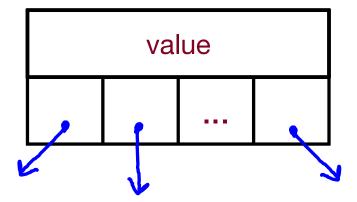




We Can Have Ternary Trees (or any number, n)

N-ary Tree:

```
struct Tree {
    string value;
    Vector<Tree *> children;
};
```





Trees can be defined as either structs or classes

```
struct Tree {
    string value;
    Tree * left;
    Tree * right;
};
```

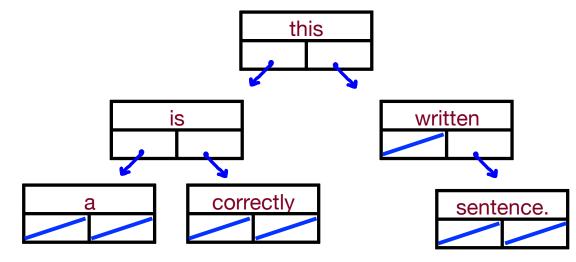
```
class Tree {
private:
   string value;
   Vector<Tree *> children;
};
```



```
struct Tree {
    string value;
    Tree * left;
    Tree * right;
};
```

There are multiple ways to traverse the nodes in a binary tree:

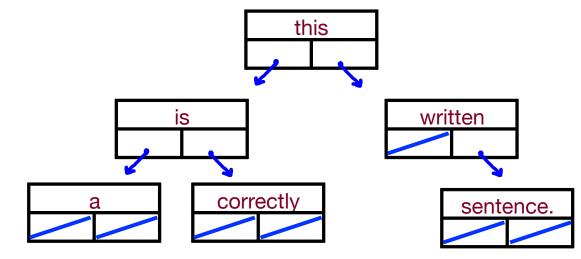
Pre-order
 In-order
 Post-order
 Level-order





```
struct Tree {
    string value;
    Tree * left;
    Tree * right;
};
```

There are multiple ways to traverse the nodes in a binary tree:



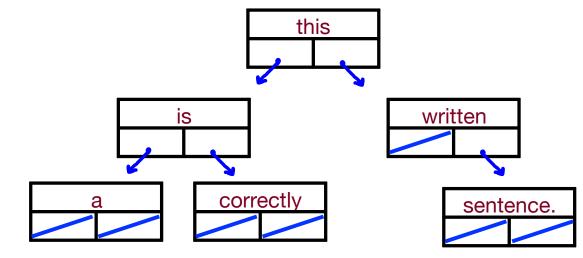
Pre-order
 In-order
 Post-order
 Level-order

1.Do something 2.Go left 3.Go right



```
struct Tree {
    string value;
    Tree * left;
    Tree * right;
};
```

There are multiple ways to traverse the nodes in a binary tree:



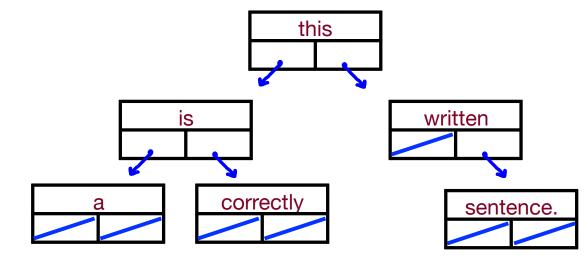
Pre-order
 In-order
 Post-order
 Level-order





```
struct Tree {
    string value;
    Tree * left;
    Tree * right;
};
```

There are multiple ways to traverse the nodes in a binary tree:



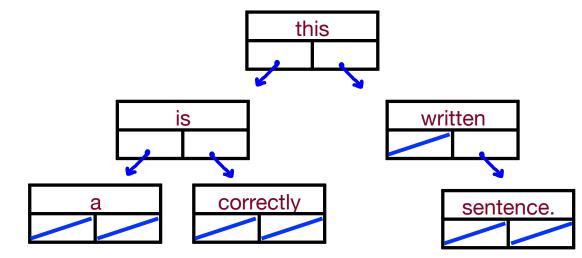
```
    Pre-order
    In-order
    Post-order
    Level-order
```





```
struct Tree {
    string value;
    Tree * left;
    Tree * right;
};
```

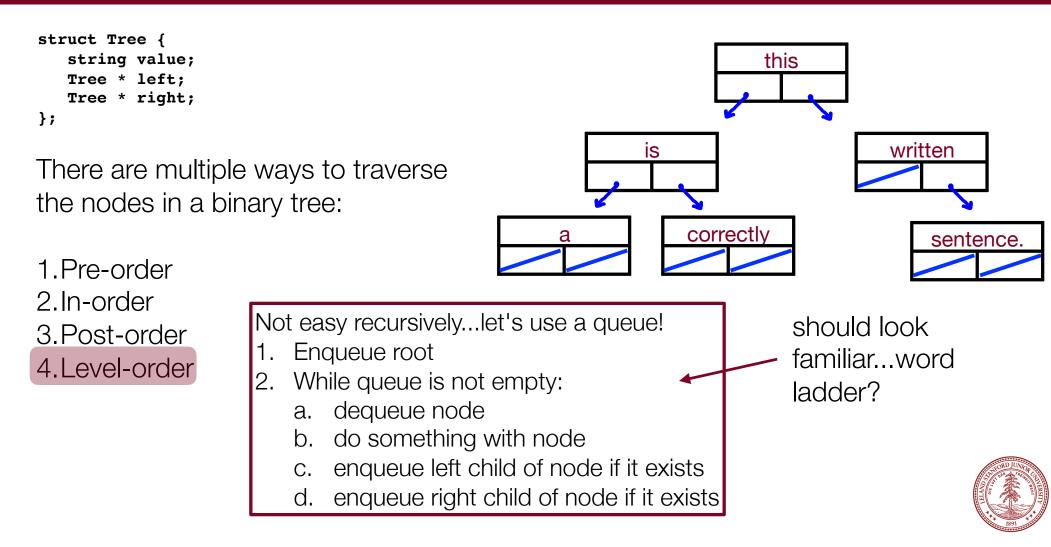
There are multiple ways to traverse the nodes in a binary tree:



1.Pre-order
 2.In-order
 3.Post-order
 4.Level-order

Hmm...can we do this recursively? We want to print the levels: 0, 1, 2 from left-to-right order





Let's write some code

```
struct Tree {
   string value;
                                                                                    this
   Tree * left;
   Tree * right;
};
                                                                                                  written
                                                                      is
void preOrder(Tree * tree) {
  if(tree == NULL) return;
  cout<< tree->value <<" ";</pre>
  preOrder(tree->left);
                                                                           correctly
  preOrder(tree->right);
                                                                                                       sentence.
}
void inOrder(Tree * tree) {
                                         void levelOrder(Tree *tree) {
  if(tree == NULL) return;
                                             Queue<Tree *>treeQueue;
                                             treeQueue.enqueue(tree);
  inOrder(tree->left);
                                             while (!treeQueue.isEmpty()) {
  cout<< tree->value <<" ";</pre>
                                                 Tree *node = treeQueue.dequeue();
  inOrder(tree->right);
                                                cout << node->value << " ";</pre>
}
                                                if (node->left != NULL) {
                                                    treeQueue.enqueue(node->left);
void postOrder(Tree * tree) {
                                                }
  if(tree == NULL) return;
                                                 if (node->right != NULL) {
  postOrder(tree->left);
                                                    treeQueue.enqueue(node->right);
  postOrder(tree->right);
                                                }
  cout<< tree->value << " ";</pre>
                                             }
}
                                         ł
```

References and Advanced Reading

References:

- •<u>https://en.wikipedia.org/wiki/Tree (data_structure)</u>
- •http://pages.cs.wisc.edu/~vernon/cs367/notes/8.TREES.html

Advanced Reading:

- •http://www.cs.cmu.edu/~adamchik/15-121/lectures/Trees/trees.html
- •Great set of tree-type questions:
- •http://cslibrary.stanford.edu/110/BinaryTrees.html

