



## 2 Beta Prior Update

Now suppose your prior is  $X \sim \text{Beta}(a_0, b_0)$ . Then you flip your coin and observe  $h$  heads and  $t$  tails. Derive the posterior distribution of  $X$  and give its parameters in terms of  $a_0, b_0, h, t$ .

## 3 Beta(1, 1)

What is the pdf of  $X$  where  $X \sim \text{Beta}(a = 1, b = 1)$ ?

## 4 A Beta Example

A medicine is believed to work about 80% of the time before testing. Then you try the medicine on 20 patients. It “works” for 14 and “doesn’t work” for 6. What is your updated belief that the drug works?

(a) To start, first write down how you would represent your prior belief that the medicine works 80% of the time?

(b) Now, write an expression for the posterior belief.



## 5. Decision-Making with Beta Beliefs

You are choosing between Drug A and Drug B. Let  $X_A, X_B$  be success probabilities.

- Prior for each drug: Beta(1, 1)
- You tested Drug B five times and observed 2 successes and 3 failures.

a) Write the posterior for  $X_B$ .

b) Compute  $E[X_B]$ .

c) Describe the Thompson Sampling algorithm.