

Section #3

Problems by Chris

Reminder: Sign up for a PEP session. Sessions take place next week Mon Feb 2 - Wed Feb 4.

1 Better Evaluation of Eye Disease

When a patient has eye inflammation, eye doctors “grade” the inflammation. When “grading” inflammation they randomly look at a single 1 millimeter by 1 millimeter square in the patient’s eye and count how many “cells” they see.

There is uncertainty in these counts. If the true average number of cells for a given patient’s eye is 6, the doctor could get a different count (say 4, or 5, or 7) just by chance. As of 2021, modern eye medicine did not have a sense of uncertainty for their inflammation grades! In this problem we are going to change that. At the same time we are going to learn about poisson distributions over space.

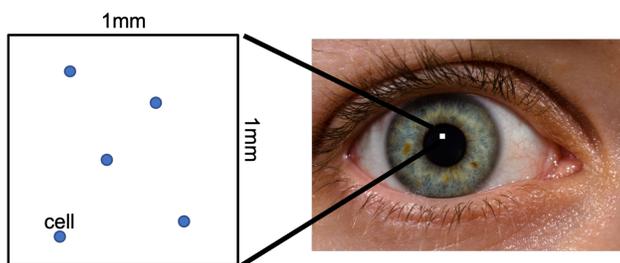


Figure 1: A $1 \times 1 \text{mm}$ sample used for inflammation grading. Inflammation is graded by counting cells in a randomly chosen 1mm by 1mm square. This sample has 5 cells.

- a. Explain, as if teaching, why the number of cells observed in a 1×1 square is governed by a poisson process. Make sure to explain how a binomial distribution could approximate the count of cells. Explain what λ means in this context. Note: for a given person’s eye, the presence of a cell in a location is independent of the presence of a cell in another location.

- b. For a given patient the true average rate of cells is 5 cells per 1×1 sample. What is the probability that in a single 1×1 sample the doctor counts 4 cells?

