Practice Midterm #1

This is an open-note, open-reader exam. You can refer to any course handouts, textbooks, handwritten lecture notes, and printouts of any code relevant to any CS106B assignment. You may not use any laptops, cell phones, or handheld devices of any sort. You will be graded on functionality—but good style helps graders understand what you were attempting. You do not need to include any libraries and you do not need to forward declare any functions. You have 2 hours. We hope this exam is an exciting journey 😊.

Last Name: _____________________  
First Name: ____________________  
Section Leader: _________________

I accept the letter and spirit of the honor code. I’ve neither given nor received aid on this exam. I pledge to write more neatly than I ever have in my entire life.

(signed) ________________________________

<table>
<thead>
<tr>
<th>Question</th>
<th>Score</th>
<th>Grader</th>
</tr>
</thead>
<tbody>
<tr>
<td>1. Mystery</td>
<td>[10]</td>
<td>____</td>
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<tr>
<td><strong>Total</strong></td>
<td>[55]</td>
<td>____</td>
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</tbody>
</table>
Problem 1: Tracing C++ programs and big-O (10 points)

Assume that the functions Mystery and Enigma have been defined as follows:

```cpp
int Mystery(int n) {
    if (n == 0) {
        return 0;
    } else {
        return Mystery(n - 1) + Enigma(n/2) + Enigma(n/2);
    }
}

int Enigma(int n) {
    int index = 0;
    int sum = 0;
    while (index < n * 2) {
        sum += index;
        index++;
    }
    return sum;
}
```

(a) [3 points] What is the value of Enigma(2)?

(b) [3 points] What is the value of Mystery(4)?

(c) [2 points] What is the worst case computational complexity of the Enigma function expressed in terms of big-O notation, where N is the value of the argument n? In this problem, you may assume that n is always a nonnegative integer.

(d) [2 points] What would be the effect on the worst case big-O of Enigma if the line:

```cpp
if(RandomChance(0.5)) break;
```

had been added to the beginning of the while loop in Enigma?
Problem 2: Grids, Vectors, Stacks, and Queues (15 points)

A common operation on 2D data (think images or scientific data) is to smooth out the values of each cell. In images it blurs the picture, on scientific data it reduces the effect of outliers.

Your job is to write a function `smooth` that takes in a `Grid<double>` by reference, and smooths out every cell in the grid. On a single cell from the data, the smoothed value is the average of its neighbors and its own value. Most cells have eight neighbors, except for cells at the edge of the grid. Consider the following cell in blue, and its eight neighbors:

```
  | 1.0 | 1.0 | 2.0 |
  | 6.0 | 5.0 | 3.0 |
  | 1.0 | 2.0 | 2.0 |
```

The average of the cell and its eight neighbors is \((1 + 1 + 2 + 6 + 5 + 3 + 1 + 2 + 2) / 9\) which equals 2.56. Thus the new value of the cell will be 2.56.

You should apply such an averaging to every cell in the grid (which could have any size). Importantly, when you compute the average of a cell, it should use the original value of the neighbors, not a smoothed value. In the example above, if you were calculated the smoothed value of one of the blue cell’s neighbor it should use the old value of the cell (5) instead of the smoothed value (2.56).
Answer to problem 2:

```cpp
void smooth (Grid<double> & values) {
```
Problem 3: Maps and Sets (15 points)

In any map, multiple keys can have the same value. The Most Common Value is the value in the map with the largest number of associated keys.

Your job is to write a function `KeysForMostCommonValue` that takes in a `Map<string, string>`, finds the Most Common Value and returns the set of keys that map to the Most Common Value.

```
Set<string> KeysForMostCommonValue (Map<string, string> & map)
```

Consider the following map which stores username password combinations:

<table>
<thead>
<tr>
<th>Key</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>“cpiech”</td>
<td>“password”</td>
</tr>
<tr>
<td>“mfaulk”</td>
<td>“pizza”</td>
</tr>
<tr>
<td>“zuckerberg”</td>
<td>“12345”</td>
</tr>
<tr>
<td>“haxor2000”</td>
<td>“password”</td>
</tr>
<tr>
<td>“sheen”</td>
<td>“12345”</td>
</tr>
<tr>
<td>“rebeccablack”</td>
<td>“friday”</td>
</tr>
<tr>
<td>“neo”</td>
<td>“password”</td>
</tr>
</tbody>
</table>

The Most Common Value in the map is “password” and the keys that map to the Most Common Value are “cpiech”, “haxor2000” and “neo”.

*Hint: This problem is much easier to solve if you populate internal set(s) and/or map(s) that will help you find the Most Common Value.*

(space for the answer to problem 3 appears on the next page)
Answer to problem 3:

```cpp
Set<string> KeysForMostCommonValue (Map<string, string> & map) {
```
Problem 4: Recursive Exploration (15 points)

It has been thought that Ancient Egyptians used systems of mirrors to bring light into the inner chambers of their temples! Light normally travels in a straight line (think of a laser) but you can turn the path of the light using reflective surfaces.

Your job is to write a predicate function `IsSolvable` that returns whether or not there is a system of mirrors for a given temple such that light traveling in a specific direction from a starting position can be directed to a goal position using a limited number of mirrors.

This problem is constrained so that light is always traveling north, south, east or west and mirrors turn light clockwise (to the right relative to the previous direction) or counterclockwise (to the left). The temple is stored as a `Grid<bool>` where `true` means that the location is blocked—light cannot travel through this location—and `false` means that the location is open—light can travel through this location.

As an example: in the temple depicted in the image below-on-the-left, light starts in the bottom left corner traveling to the east and the goal is to get the light to the upper right corner. In this example there is no solution with three or fewer mirrors. However using four mirrors the system in the image below-on-the-right will direct light to the goal:

![Temple Diagrams](image)

*Hint: You should think of this problem step by step from the perspective of the light. At each square you can: move straight, turn left or turn right. It costs nothing to move straight—in the direction you were already facing—but it costs a mirror to turn left or to turn right.*
The problem uses the Point class to represent a position in the grid and the Direction enum to represent light direction:

```java
// Directions that light can travel
enum Direction = {NORTH, EAST, SOUTH, WEST};

// Position in the temple
Point is a class in the cs106b library that stores an x and y position as ints. The two methods it supports are getX() and getY().

Point myPoint(2, 3);
int x = myPoint.getX();
int y = myPoint.getY();
```

To help you with the updating of positions and directions, we provide you with the following functions (you don't have to write them):

```java
Point move(Point curPos, Direction curDir);
Direction turnLeft(Direction curDir);
Direction turnRight(Direction curDir);
```

Move returns the new position obtained by taking one step from the passed-in-position oriented in the passed-in-direction. TurnLeft and TurnRight return the orientation obtained from rotating left and right respectively from the passed-in-direction.

Using these predefined functions write a recursive predicate IsSolvable that takes a grid, a number of mirrors, a start configuration and a goal position as arguments and returns true if there is a system of mirrors to direct light to the goal and false otherwise.

(space for the answer to problem 4 appears on the next page)
Answer to problem 4:

// predefined helper functions (you can use and don’t have to implement)
Point Move(Point curPos, Direction curDir);
Direction TurnLeft(Direction curDir);
Direction TurnRight(Direction curDir);

bool IsSolvable(Grid<bool> templeBlocks, int numMirrors, Position startPos, 
                Direction startDir, Position goalPos) {


Problem 5: Optional Fun Problem (0 points)

Make your own paneled style stick figure comic pontificating or commenting about CS, computers, life, etc. Here's one for reference:

This problem isn't required and there are no points associated with doing any work here, but any great gems will be very much appreciated by the course staff :).