Today's larger example demonstrates the use of a grid—that is, a single declaration of a `Grid<bool>`. to maintain information about a chessboard and queen placement. All relevant code is presented here in the handout.

The following function `clearBoard` takes a `Grid<bool>` by reference and initializes every entry of the grid to be `false`. Note the use of a double-`for` loop to generate every pair of `row` and `col` that corresponds to a legal coordinate.
static void clearBoard(Grid<bool>& board) {
    for (int row = 0; row < board.numRows(); row++) {
        for (int col = 0; col < board.numCols(); col++) {
            board[row][col] = false;
            drawSquare(row, col, "Blue"); // assume a square is drawn at (row, col)
        }
    }
}

Next, we want a function `placeRandomQueens` that places some number of queens on the board at random locations. We enter the function with an idea of exactly how many queens need to be placed, and then repeatedly generate random coordinates on the board and place queens there. Note the care `placeRandomQueens` takes to assign at most one queen to each location—otherwise, the `if (!board[row][col])` wouldn't be necessary.
static void placeRandomQueens(Grid<bool>& board, int numQueensToPlace) {
    int numQueensPlaced = 0;
    while (numQueensPlaced < numQueensToPlace) {
        int row = randomInteger(0, board.numRows() - 1);
        int col = randomInteger(0, board.numCols() - 1);
        if (!board[row][col]) {
            board[row][col] = true;
            markLocation("Q", row, col, "Black"); // assume a Q is drawn
            numQueensPlaced++;
        }
    }
}

If we are dealing with an 8 x 8 board, then a call to **placeRandomQueens(board, 8)** might just produce the following:

![Queen Safety](image)

At this point, we want to determine which of the unoccupied squares can be attacked. Pretending for the moment that an **isSafe** predicate function already exists, we can easily label each of the empty locations as safe or not using the following code snippet:
static void identifySafeLocations(Grid<bool>& board) {
    for (int row = 0; row < board.numRows(); row++) {
        for (int col = 0; col < board.numCols(); col++) {
            if (!board[row][col]) {
                if (isSafe(board, row, col)) {
                    markLocation("S", row, col, "Green");
                } else {
                    markLocation("X", row, col, "Red");
                }
            }
        }
    }
}

To determine whether or not a particular location is safe from attack, we need to search in all eight directions to see whether or not a queen is visible. At first glance, we might be interested in writing functions like \texttt{isSouthWestSafe}, \texttt{isSouthSafe}, \texttt{isSouthEastSafe}, etc. and then implement a function \texttt{isSafe} to simply return the conjunction of all of them.

\begin{verbatim}
/**
 * Predicate Function: isSafe
 * --------------------------
 * isSafe returns true if and only if no queen
 * can be seen in any of the eight directions stemming radially
 * outward from the specified row and column.
 */
static bool isSafe(Grid<bool>& board, int row, int col) {
    return ( isSouthWestSafe(board, row, col) &&
             isSouthSafe(board, row, col) &&
             isSouthEastSafe(board, row, col) &&
             isWestSafe(board, row, col) &&
             isEastSafe(board, row, col) &&
             isNorthWestSafe(board, row, col) &&
             isNorthSafe(board, row, col) &&
             isNorthEastSafe(board, row, col) );
}
\end{verbatim}

However, doing so requires the implementation of eight distinct helper functions, all of which are basically the same code block with a few minor differences. Just compare two of them (I omit the other six, because once you understand two, you really understand all eight.)
/**
 * Function: isSouthWestSafe
 * -------------------------
 * isSouthWestSafe decides whether or not any danger can be seen
 * by looking from the specified (row, col) coordinate in the
 * southwestern direction. Assuming that the origin (0,0) coincides
 * with the upper left corner of the board, isSouthWestSafe must examine
 * the coordinates (row + 1, col - 1), (row + 2, col - 2), etc, in that
 * order, until either the edge of the board or a queen is encountered.
 */
static bool isSouthWestSafe(Grid<bool>& board, int row, int col) {
    row++;
    col--;
    while (board.inBounds(row, col) && !board[row][col]) {
        row++;
        col--;
    }
    return !board.inBounds(row, col);
}

/**
 * Function: isSouthSafe
 * ---------------------
 * isSouthSafe decides whether or not any danger can be seen
 * by looking from the specified (row, col) coordinate in the
 * southern direction. Assuming that the origin (0,0) coincides
 * with the upper left corner of the board, isSouthSafe must examine
 * the coordinates (row + 1, col), (row + 2, col), etc, in that
 * order, until either the edge of the board or a queen is encountered.
 */
static bool isSouthSafe(Grid<bool>& board, int row, int col) {
    row++;
    while (board.inBounds(row, col) && !board[row][col]) {
        row++;
    }
    return !board.inBounds(row, col);
}

To illustrate, consider the call isSouthWestSafe(board, 0, 5), where the distribution of
true and false in the board array corresponds to the placement of queens in the graphic
presented below. Notice that the specified location is circled, and that each of the locations
positioned southwest of it are labeled by the order isSouthWestSafe would visit them. The
isSouthWestSafe function would examine all squares along that direction until it hits the
edge of the board, or until it references one with a queen. For this call, we expect the algorithm
to return true.
However, a call to `isSouthWestSafe(board, 1, 6)` would return `false`, because the `(4, 3)` location of the board is occupied by a queen. Check out the following graphic to see:
My major problem with this implementation is that all eight directional checks currently have their own function, but all are really doing the same thing. The only difference between each is the manner in which we update the row and col variables to move in a particular direction:

- **SouthWest:** row is incremented and col is decremented with each move
- **South:** row is incremented with each move, and col remains the same
- **SouthEast:** row and col are incremented with each move
- **West:** row remains the same, but col is decremented with each move
- **East:** row remains the same, but col is incremented with each move
- **NorthWest:** row and col are decremented with each move
- **North:** row is decremented with each move, and col remains the same
- **NorthEast:** row is decremented and col gets incremented with each move

We should work to unify the implementations of the eight predicate functions into a single function. That way we refine and debug all logic in a single place instead of many. Check this out:
/**
 * Function: isDirectionSafe
 * -------------------------
 * isDirectionSafe decides whether or not any danger can be seen
 * by looking from the specified (row, col) coordinate in a particular
 * direction--specified by arguments four and five in the form of exactly
 * what values should be added to (row, col) to move in a specified
 * direction.
 *
 * Assuming that the origin (0,0) coincides with the upper left corner of
 * the board, isDirectionSafe must examine the coordinates
 * (row + drow, col + dcol), (row + 2 * drow, col + 2 * dcol), etc,
 * in that order, until either the edge of the board or a queen
 * is encountered.
 */

static bool isDirectionSafe(Grid<bool>& board, int row, int col, int drow, int dcol) {
    if (drow == 0 && dcol == 0) return true;
    row += drow;
    col += dcol;
    while (board.inBounds(row, col) && !board[row][col]) {
        row += drow;
        col += dcol;
    }
    return !board.inBounds(row, col);
}

Need to search northwest from index (6, 5)?
    Call isDirectionSafe(board, 6, 5, -1, -1).
Need to search south from index (6, 5)?
    Call isDirectionSafe(board, 6, 5, 1, 0).
Need to search east from the origin?
    Call isDirectionSafe(board, 0, 0, 0, 1).

This allows us to unify common functionality to a single helper function, not eight of them, and
it also makes the implementation of the isSafe function (the one that checks all eight
directions, not just one) more compact.

static bool isSafe(Grid<bool>& board, int row, int col) {
    for (int drow = -1; drow <= 1; drow++) {
        for (int dcol = -1; dcol <= 1; dcol++) {
            if (!isDirectionSafe(board, row, col, drow, dcol))
                return false;
        }
    }
    return true;
}