Please read all instructions (including these) carefully.

There are 6 questions on the exam, each with multiple parts. You have 180 minutes to work on the exam.

The exam is open note and open laptop, but no Internet connectivity or computation may be used—you can use your laptop to read electronic notes, but nothing more.

Please write your answers in the space provided on the exam, and clearly mark your solutions. Please do not use any additional scratch paper.

Solutions will be graded on correctness and clarity. Each problem has a relatively simple and straightforward solution. You may get as few as 0 points for a question if your solution is far more complicated than necessary. Partial solutions will be graded for partial credit.

NAME: ____________________________________________

In accordance with both the letter and spirit of the Honor Code, I have neither given nor received assistance on this examination.

SIGNATURE: _______________________________________

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<th>Problem</th>
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1. **Code Generation and Runtime Organization** (20 points)
   For each of the following modifications to Cool, explain how you can generate more efficient code than for the standard definition of Cool. Each part is a single change to the full Cool language (the changes are not cumulative). Give a short (2-3 sentence) explanation of how you would modify code generation and why the generated code would be faster.

   - Disallow method override—methods cannot be redefined in subclasses.

   - Disallow recursive method calls. No method can call itself, directly or indirectly (i.e., no recursive or mutually recursive methods).

   - Disallow inheritance. Classes do not inherit from other classes.
2. **Register Allocation** (20 points)

Give a program with the minimum number of statements that satisfies the following conditions:

- All statements are of the form \( a = b + c \) where \( a, b \) and \( c \) are program variables (and note, they need not be literally just the names \( a, b \) and \( c \), but any variable names).
- Assume that only the variable on the left-hand side of the last assignment is live on exit from the program.
- The register interference graph of the program has 4 nodes and all possible edges (i.e., it is the complete graph of 4 nodes).

Do not be concerned with the values of the variables (in particular, don’t worry about how or whether they are initialized). Explain why your solution is the shortest possible program.
3. **Garbage Collection** (20 points)

Consider a programming language with the following grammar:

\[
P \rightarrow S; P \\
| \epsilon \\
S \rightarrow \text{VAR} = \text{new} \\
| \text{VAR} = \text{VAR}.1 \\
| \text{VAR} = \text{VAR}.2 \\
| \text{VAR}.1 = \text{VAR} \\
| \text{VAR}.2 = \text{VAR}
\]

A program is a sequence of statements. A `new` statement allocates a pair, an object with two fields named “1” and “2”. The two fields are initialized to null pointers. The next two statements are field reads from “1” and “2” respectively, and the last two statements are field writes, again to “1” and “2” respectively. \text{VAR} is a variable name. Now consider the following program fragment.

\[
x = \text{new} \\
y = \text{new} \\
y.1 = x \\
z = \text{new} \\
z.2 = y \\
w = \text{new} \\
w.1 = y \\
v = z.2 \\
z.1 = z \\
x.2 = v
\]

For both of the following questions, assume that when a garbage collection is invoked, the root set is the set of live variables and that only the variable \text{w} is live on exit from this program fragment.

- Assume a Stop and Copy garbage collection takes place after the last statement. Show the state of the local variables and heap after the collection.
• At what point in the program would a Mark and Sweep collection result in the largest set of retained (uncollected) objects? If there are multiple points that result in the same size set of retained objects, choose the last one. Show the heap that results from running a collection at this point.
4. **Dataflow Analysis** (20 points)

Consider the following program:

```c
a = 1
b = 2
c = 3
e = b
d = b
f = a
while * {
    if * then
        if * then
            e = a
            f = c
d = e
        else
            e = d
            f = c
d = b
    else
        if * then
            f = e
            e = b
            f = d
        else
            /* nothing */
    }
    /* nothing */
}
```

You should assume the omitted predicates marked with * are sometimes true and sometimes false. Otherwise, they play no role in this problem.

- Recall that constant propagation as presented in lecture is done for a single variable at a time. Assuming constant propagation can be done as many times as desired (including repeating it for some variables if necessary), mark the variable-variable assignments that can be replaced by variable-constant assignments in the program above by crossing out the right-hand side and writing in the corresponding constant. Briefly (one or two sentences) justify your answer.
• Give a shortest sequence of constant propagation analysis passes that will result in all possible constants being propagated in this program. It is sufficient to give the order of the variables analyzed.

• Modify the right-hand side of just one assignment operation so that as many additional constants can be propagated as possible. On the copy of the original program below, mark which statement is modified and what the new right-hand side is. Then show all the additional statements (beyond the answer to the first part) where constants can be propagated and what those constants are by crossing out the right-hand side and writing in the corresponding constant.

```c
a = 1
b = 2
c = 3
e = b
d = b
f = a
while * {
    if * then
        if * then
            if * then
                e = a
                f = c
                d = e
            else
                e = d
                f = c
                d = b
        else
            if * then
                f = e
                e = b
                f = d
            else
                /* nothing */
```
5. **Types and Runtime Organization** (20 points)

Consider the following class declarations:

```plaintext
class X {
   foo() : Foo { ... };
   bar() : Int { ... };
   b : Bool;
   c : String;
};

class Y inherits X {
   bar() : Int { ... };
   baz() : Object { ... };
   d : Int;
};

class Z inherits Y {
   foo() : Foo { ... };
   qux() : Int { ... };
   a : Object;
};
```
• Give the object layouts and dispatch tables for each of the three classes. You may ignore the inherited methods of the Object class.

• Consider the definition of method foo() in class Z. Cool requires that the declared return type of an overridden method be exactly the same as the return type of the original method. If instead we allow foo’s return type foo() : Bazz to be some class such that Bazz ≤ Foo, can a program that typechecks crash due to trying to access a method or attribute that does not exist? If your answer is no, argue why not. If your answer is yes, sketch a (short) example program that has this behavior.

• Still considering the definition of foo in class Z, consider the case where we allow foo to have the declared return type foo() : Bazz where Foo ≤ Bazz. Can a program that typechecks under this rule crash due to trying to access a method or attribute that does not exist? If your answer is no, argue why not. If your answer is yes, sketch a (short) example program that has this behavior.
6. **Code Generation** (20 points)

Below is the (partial) output of a Cool compiler. Show Cool source code that could compile to this assembly. Just show the fragment corresponding to this code (you do not need to show a complete Cool program). Please write your answer on this page.

```
int_const0: .word 2 .word 4 .word Int_dispTab .word 0 .word -1
bool_const0: .word 3 .word 4 .word Bool_dispTab .word 0 .word -1
bool_const1: .word 3 .word 4 .word Bool_dispTab .word 1
Main.f: addiu $sp $sp -16 sw $fp 16($sp) sw $s0 12($sp) sw $ra 8($sp)
addiu $fp $sp 4
move $s0 $a0 sw $s1 0($fp) la $s1 int_const0 lw $a0 20($fp)
blt $t1 $t2 label2
la $a0 bool_const1
label2: lw $t1 12($s1)
lw $t2 12($a0)
la $a0 bool_const0
lw $t2 12($s0)
add $t1 $t1 $t2
sw $t1 12($a0)
sw $s1 12($s0)
b label1
label0: la $a0 int_const0
label1:
move $a0 $s0 lw $s1 0($fp)
lw $fp 16($sp)
lw $s0 12($sp)
lw $ra 8($sp)
addiu $sp $sp 24 jr $ra
```