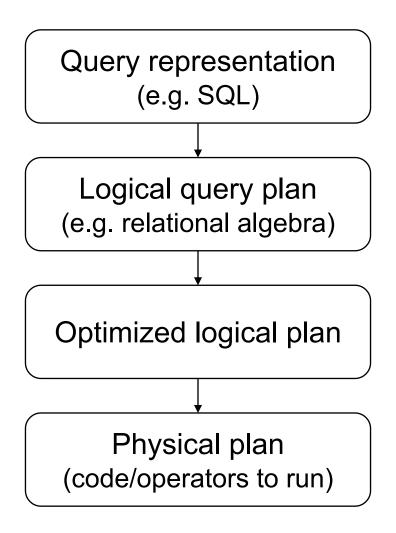
Query Optimization

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Query Execution Overview



Outline

What can we optimize?

Rule-based optimization

Data statistics

Cost models

Cost-based plan selection

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What Can We Optimize?

Operator graph: what operators do we run, and in what order?

Operator implementation: for operators with several impls (e.g. join), which one to use?

Access paths: how to read each table?

» Index scan, table scan, C-store projections, ...

Typical Challenge

There is an exponentially large set of possible query plans

Result: we'll need techniques to prune the search space and complexity involved

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What is a Rule?

Procedure to replace part of the query plan based on a pattern seen in the plan

Example: When I see expr OR TRUE for an expression expr, replace this with TRUE

Implementing Rules

Each rule is typically a function that walks through query plan to search for its pattern

```
void replaceOrTrue(Plan plan) {
  for (node in plan.nodes) {
    if (node instanceof Or) {
       if (node.right == Literal(true)) {
            plan.replace(node, Literal(true));
            break;
       }
       // Similar code if node.left == Literal(true)
    }
}
```

Implementing Rules

Rules are often grouped into phases

» E.g. simplify Boolean expressions, pushdown selects, choose join algorithms, etc

Each phase runs rules till they no longer apply

```
plan = originalPlan;
while (true) {
  for (rule in rules) {
    rule.apply(plan);
  }
  if (plan was not changed by any rule) break;
}
```

Result

Simple rules can work together to optimize complex query plans (if designed well):

```
SELECT * FROM users WHERE

(age>=16 && loc==CA) || (age>=16 && loc==NY) || age>=18

(age>=16) && (loc==CA || loc==NY) || age>=18

(age>16 && (loc IN (CA, NY)) || age>=18

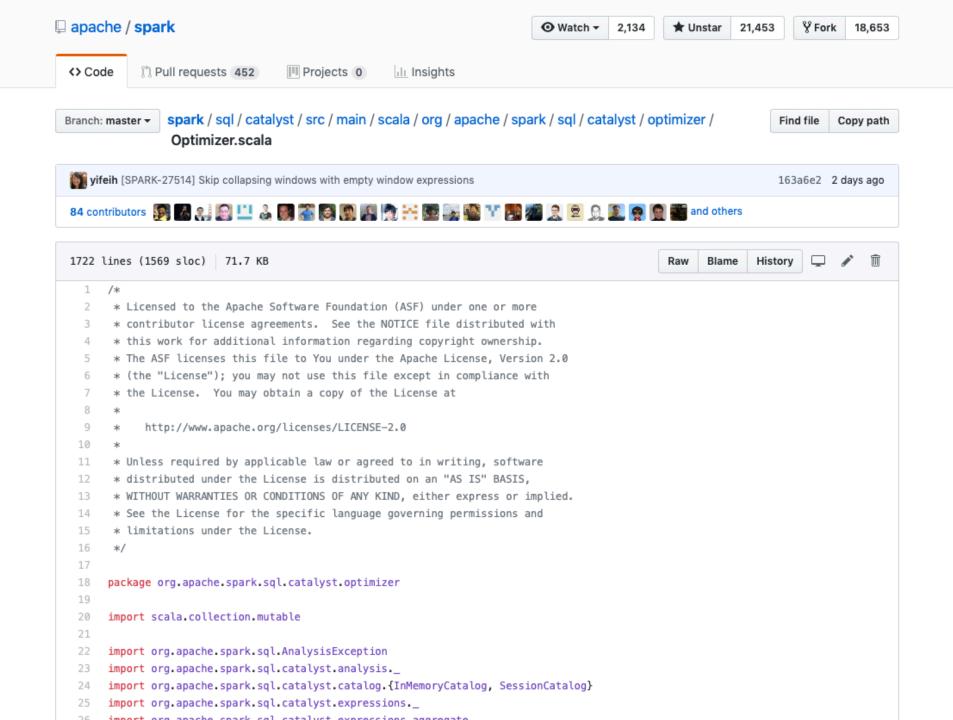
age>=18 || (age>16 && (loc IN (CA, NY))
```

Example Extensible Optimizer

For Monday, you'll read about Spark SQL's Catalyst optimizer

- » Written in Scala using its pattern matching features to simplify writing rules
- » >500 contributors worldwide, >1000 types of expressions, and hundreds of rules

We'll also use Spark SQL in assignment 2



```
abstract class Optimizer(sessionCatalog: SessionCatalog)
       extends RuleExecutor[LogicalPlan] {
39
40
      def defaultBatches: Seq[Batch] = {
59
60
         val operatorOptimizationRuleSet =
           Seq(
61
62
             // Operator push down
63
             PushProjectionThroughUnion,
64
             ReorderJoin,
65
             EliminateOuterJoin,
             PushPredicateThroughJoin,
66
67
             PushDownPredicate,
68
             PushDownLeftSemiAntiJoin,
69
             PushLeftSemiLeftAntiThroughJoin,
70
             LimitPushDown,
             ColumnPruning,
71
72
             InferFiltersFromConstraints,
73
             // Operator combine
             CollapseRepartition,
74
             CollapseProject,
75
76
             CollapseWindow,
77
             CombineFilters,
             CombineLimits,
78
79
             CombineUnions,
80
             // Constant folding and strength reduction
81
             TransposeWindow,
             NullPropagation,
82
83
             ConstantPropagation,
84
             FoldablePropagation,
             OptimizeIn,
85
             ConstantFolding,
86
             ReorderAssociativeOperator,
87
88
             LikeSimplification,
             BooleanSimplification,
89
             SimplifyConditionals,
90
             RemoveDispensableExpressions,
91
             SimplifyBinaryComparison,
92
93
             ReplaceNullWithFalseInPredicate,
             PruneFilters.
```

Common Rule-Based Optimizations

Simplifying expressions in select, project, etc

- » Boolean algebra, numeric expressions, string expressions (e.g. regex -> contains), etc
- » SQL statements have redundancies because they're generated by humans who optimized for readability, or by code

Simplifying relational operator graphs

» Select, project, join, etc: we'll see some soon!

These relational optimizations have biggest impact

Common Rule-Based Optimizations

Selecting access paths and operator Also very implementations in simple cases high impact

- » Index column predicate ⇒ use index
- » Small table ⇒ use hash join against it
- » Aggregation on field with few values ⇒ use in-memory hash table

Rules also often used to do type checking and analysis (easy to write recursively)

Common Relational Rules

Push selects as far down the plan as possible Recall:

$$\sigma_p(R \bowtie S) = \sigma_p(R) \bowtie S$$
 if p only references R

$$\sigma_{a}(R \bowtie S) = R \bowtie \sigma_{a}(S)$$
 if q only references S

$$\sigma_{p \wedge q}(R \bowtie S) = \sigma_p(R) \bowtie \sigma_q(S)$$
 if p on R, q on S

Idea: reduce # of records early to minimize work in later ops; enable index access paths

Common Relational Rules

Push projects as far down as possible

Recall:

$$\Pi_x(\sigma_p(R)) = \Pi_x(\sigma_p(\Pi_{x \cup z}(R)))$$
 z = the fields in p

$$\Pi_{\mathsf{x}\cup\mathsf{y}}(\mathsf{R}\bowtie\mathsf{S})=\Pi_{\mathsf{x}\cup\mathsf{y}}\left(\left(\Pi_{\mathsf{x}\cup\mathsf{z}}\left(\mathsf{R}\right)\right)\bowtie\left(\Pi_{\mathsf{y}\cup\mathsf{z}}\left(\mathsf{S}\right)\right)\right)$$

x = fields in R, y = in S, z = in both

Idea: don't process fields you'll just throw away

Project Rules Can Backfire!

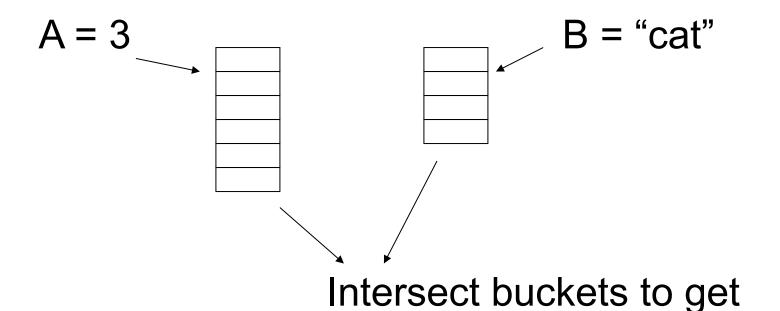
Example: R has fields A, B, C, D, E

p: A=3 ∧ B="cat"

x: {E}

 $\Pi_{x}(\sigma_{p}(R))$ vs $\Pi_{x}(\sigma_{p}(\Pi_{A,B,E}(R)))$

What if R has Indexes?



In this case, should do $\sigma_p(R)$ first!

pointers to matching tuples

Bottom Line

Many possible transformations aren't always good for performance

Need more info to make good decisions

- » Data statistics: properties about our input or intermediate data to be used in planning
- » Cost models: how much time will an operator take given certain input data statistics?

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What can we optimize?

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What Are Data Statistics?

Information about the tuples in a relation that can be used to estimate size & cost

» Example: # of tuples, average size of tuples, # distinct values for each attribute, % of null values for each attribute

Typically maintained by the storage engine as tuples are added & removed in a relation

» File formats like Parquet can also have them

Some Statistics We'll Use

For a relation R,

T(R) = # of tuples in R

S(R) = average size of R's tuples in bytes

B(R) = # of blocks to hold all of R's tuples

V(R, A) = # distinct values of attribute A in R

R:

Α	В	С	D
cat	1	10	а
cat	1	20	b
dog	1	30	а
dog	1	40	С
bat	1	50	d

A: 20 byte string

B: 4 byte integer

C: 8 byte date

D: 5 byte string

R:

Α	В	C	D
cat	1	10	а
cat	1	20	b
dog	1	30	а
dog	1	40	С
bat	1	50	d

A: 20 byte string

B: 4 byte integer

C: 8 byte date

D: 5 byte string

$$T(R) = 5$$

$$V(R, A) = 3$$

$$V(R, B) = 1$$

$$S(R) = 37$$

$$V(R, C) = 5$$

$$V(R, D) = 4$$

Challenge: Intermediate Tables

Keeping stats for tables on disk is relatively easy, but what about intermediate tables that appear during a query plan?

Examples:

```
\sigma_p(R) \leftarrow \begin{array}{l} \text{We already have T(R), S(R), V(R, a), etc,} \\ \text{but how to get these for tuples that pass p?} \end{array}
```

R ⋈ S ← How many and what types of tuple pass the join condition?

Should we do $(R \bowtie S) \bowtie T$ or $R \bowtie (S \bowtie T)$ or $(R \bowtie T) \bowtie S$?

Stat Estimation Methods

Algorithms to estimate subplan stats

An ideal algorithm would have:

- 1) Accurate estimates of stats
- 2) Low cost
- 3) Consistent estimates (e.g. different plans for a subtree give same stats)

Can't always get all this!

Size Estimates for $W = R_1 \times R_2$

$$S(W) =$$

$$T(W) =$$

Size Estimates for $W = R_1 \times R_2$

$$S(W) = S(R_1) + S(R_2)$$

$$T(W) = T(R_1) \times T(R_2)$$

Size Estimate for W = $\sigma_{A=a}(R)$

$$S(W) =$$

$$T(W) =$$

Size Estimate for W = $\sigma_{A=a}(R)$

$$S(W) = S(R)$$
 \leftarrow Not true if some variable-length fields are correlated with value of A

$$T(W) =$$

R

Α	В	O	D
cat	~	10	а
cat	1	20	b
dog	1	30	а
dog	1	40	С
bat	1	50	d

$$V(R,A)=3$$

$$V(R,B)=1$$

$$V(R,C)=5$$

$$V(R,D)=4$$

$$W = \sigma_{Z=val}(R)$$
 $T(W) =$

R

Α	В	C	D
cat	1	10	а
cat	1	20	b
dog	1	30	а
dog	1	40	С
bat	1	50	d

$$V(R,A)=3$$

$$V(R,B)=1$$

$$V(R,C)=5$$

$$V(R,D)=4$$

what is probability this tuple will be in answer?

$$W = \sigma_{z=val}(R)$$
 $T(W) =$

R

Α	В	C	D
cat	~	10	а
cat	1	20	b
dog	1	30	а
dog	1	40	С
bat	1	50	d

$$V(R,A)=3$$

$$V(R,B)=1$$

$$V(R,C)=5$$

$$V(R,D)=4$$

$$W = \sigma_{Z=val}(R)$$

$$T(W) = \frac{T(R)}{V(R,Z)}$$

Assumption:

Values in select expression Z=val are uniformly distributed over all V(R, Z) values

Alternate Assumption:

Values in select expression Z=val are **uniformly distributed** over a domain with DOM(R, Z) values

 R

Α	В	С	D
cat	1	10	а
cat	1	20	b
dog	1	30	а
dog	1	40	С
bat	1	50	d

Alternate assumption

$$V(R,A)=3$$
, $DOM(R,A)=10$

$$V(R,B)=1$$
, $DOM(R,B)=10$

$$V(R,C)=5$$
, $DOM(R,C)=10$

$$V(R,D)=4$$
, $DOM(R,D)=10$

$$W = \sigma_{Z=val}(R)$$
 $T(W) =$

 R

Α	В	С	D
cat	1	10	а
cat	1	20	b
dog	1	30	а
dog	1	40	С
bat	1	50	d

Alternate assumption

$$V(R,A)=3$$
, $DOM(R,A)=10$

$$V(R,B)=1$$
, $DOM(R,B)=10$

$$V(R,C)=5$$
, $DOM(R,C)=10$

$$V(R,D)=4$$
, $DOM(R,D)=10$

what is probability this tuple will be in answer?

$$W = \sigma_{z=val}(R)$$
 $T(W) =$

R

Α	В	C	D
cat	1	10	а
cat	1	20	b
dog	1	30	а
dog	1	40	С
bat	1	50	d

Alternate assumption

$$V(R,A)=3$$
, $DOM(R,A)=10$

$$V(R,B)=1$$
, $DOM(R,B)=10$

$$V(R,C)=5$$
, $DOM(R,C)=10$

$$V(R,D)=4$$
, $DOM(R,D)=10$

$$W = \sigma_{z=val}(R) \qquad T(W) = \frac{T(R)}{DOM(R,Z)}$$

Selection Cardinality

SC(R, A) = average # records that satisfy equality condition on R.A

$$SC(R,A) = \begin{cases} T(R) \\ \hline V(R,A) \end{cases}$$

$$T(R) \\ \hline T(R) \\ \hline DOM(R,A)$$

What About W = $\sigma_z \ge val(R)$?

$$T(W) = ?$$

What About W = $\sigma_{z \ge val}(R)$?

T(W) = ?

Solution 1: T(W) = T(R) / 2

What About W = $\sigma_{z \ge val}(R)$?

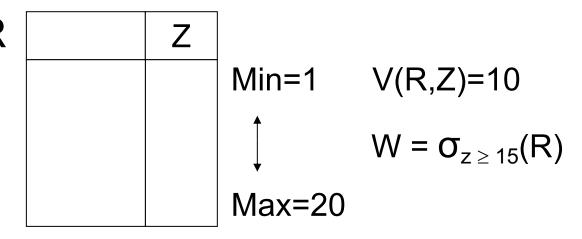
T(W) = ?

Solution 1: T(W) = T(R) / 2

Solution 2: T(W) = T(R) / 3

Solution 3: Estimate Fraction of Values in Range

Example: R



$$f = 20-15+1 = 6$$
 (fraction of range)
20-1+1 20

$$T(W) = f \times T(R)$$

Solution 3: Estimate Fraction of Values in Range

Equivalently, if we know values in column:

f = fraction of distinct values ≥ val

$$T(W) = f \times T(R)$$

What About More Complex Expressions?

E.g. estimate selectivity for

```
SELECT * FROM R
WHERE user defined func(a) > 10
```



Size Estimate for W = $R_1 \bowtie R_2$

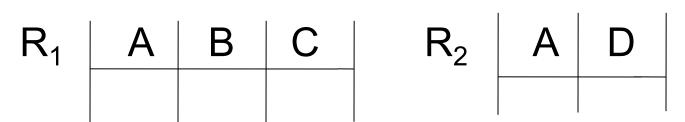
Let $X = attributes of R_1$

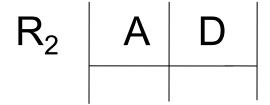
 $Y = attributes of R_2$

Case 1: $X \cap Y = \emptyset$:

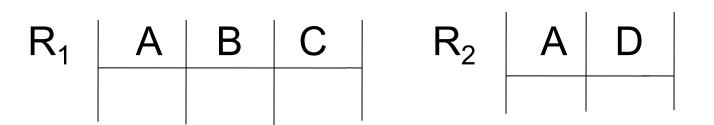
Same as R₁ x R₂

Case 2: W = $R_1 \bowtie R_2$, X \cap Y = A





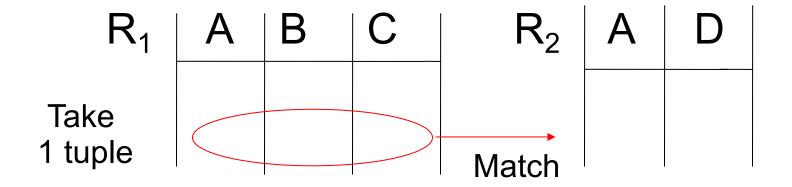
Case 2: W = $R_1 \bowtie R_2$, X \cap Y = A



Assumption ("containment of value sets"):

 $V(R_1, A) \le V(R_2, A) \Rightarrow \text{Every A value in } R_1 \text{ is in } R_2$ $V(R_2, A) \le V(R_1, A) \Rightarrow \text{Every A value in } R_2 \text{ is in } R_1$

Computing T(W) when $V(R_1, A) \leq V(R_2, A)$



1 tuple matches with
$$T(R_2)$$
 tuples... $V(R_2, A)$

so
$$T(W) = \frac{T(R_1) \times T(R_2)}{V(R_2, A)}$$

$$V(R_1, A) \le V(R_2, A) \Rightarrow T(W) = \frac{T(R_1) \times T(R_2)}{V(R_2, A)}$$

$$V(R_2, A) \le V(R_1, A) \Rightarrow T(W) = \frac{T(R_1) \times T(R_2)}{V(R_1, A)}$$

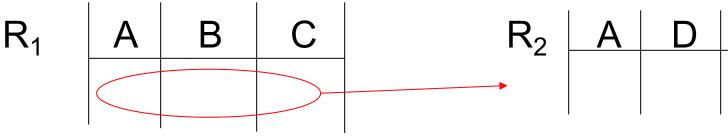
In General for W = $R_1 \bowtie R_2$

$$T(W) = \frac{T(R_1) \times T(R_2)}{\max(V(R_1, A), V(R_2, A))}$$

Where A is the common attribute set

Case 2 with Alternate Assumption

Values uniformly distributed over domain



This tuple matches $T(R_2)$ / $DOM(R_2, A)$, so

$$T(W) = \underline{T(R_1) T(R_2)} = \underline{T(R_1) T(R_2)}$$

$$DOM(R_2, A) DOM(R_1, A)$$

Tuple Size after Join

In all cases:

$$S(W) = S(R_1) + S(R_2) - S(A)$$

size of attribute A

Using Similar Ideas, Can Estimate Sizes of:

$$\Pi_{AB}(R)$$

$$\sigma_{A=a \wedge B=b}(R)$$

R M S with common attributes A, B, C

Set union, intersection, difference, ...

For Complex Expressions, Need Intermediate T, S, V Results

E.g.
$$W = \sigma_{A=a}(R_1) \bowtie R_2$$

Treat as relation U

$$T(U) = T(R_1) / V(R_1, A)$$
 $S(U) = S(R_1)$

Also need V(U, *)!!

To Estimate V

E.g.,
$$U = \sigma_{A=a}(R_1)$$

Say R₁ has attributes A, B, C, D

$$V(U, A) =$$

$$V(U, B) =$$

$$V(U, C) =$$

$$V(U, D) =$$

 R_1

Α	В	С	D
cat	1	10	10
cat	1	20	20
dog	1	30	10
dog	1	40	30
bat	1	50	10

$$V(R_1, A)=3$$

$$V(R_1, B)=1$$

$$V(R_1, C)=5$$

$$V(R_1, D)=3$$

$$U = \sigma_{A=a}(R_1)$$

 R_1

Α	В	O	D
cat	1	10	10
cat	1	20	20
dog	1	30	10
dog	1	40	30
bat	1	50	10

$$V(R_1, A)=3$$

$$V(R_1, B)=1$$

$$V(R_1, C)=5$$

$$V(R_1, D)=3$$

$$U = \sigma_{A=a}(R_1)$$

$$V(U, A) = 1$$
 $V(U, B) = 1$ $V(U, C) = T(R1)$ $V(R1,A)$

V(U, D) = somewhere in between...

Possible Guess in $U = \sigma_{A \ge a}(R)$

$$V(U, A) = 1$$

$$V(U, B) = V(R, B)$$

For Joins: $U = R_1(A,B) \bowtie R_2(A,C)$

$$V(U, A) = min(V(R_1, A), V(R_2, A))$$

$$V(U, B) = V(R_1, B)$$

$$V(U, C) = V(R_2, C)$$

[called "preservation of value sets"]

$$Z = R_1(A,B) \bowtie R_2(B,C) \bowtie R_3(C,D)$$

 R_1 $T(R_1) = 1000 V(R_1,A)=50 V(R_1,B)=100$

 R_2 $T(R_2) = 2000 V(R_2,B)=200 V(R_2,C)=300$

 R_3 $T(R_3) = 3000 V(R_3,C)=90 V(R_3,D)=500$

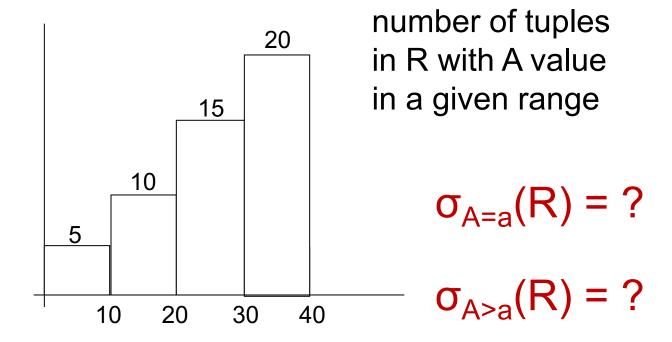
Partial Result: $U = R_1 \bowtie R_2$

$$T(U) = 1000 \times 2000$$
 $V(U,A) = 50$ $V(U,B) = 100$ $V(U,C) = 300$

End Result: $Z = U \bowtie R_3$

$$T(Z) = 1000 \times 2000 \times 3000$$
 $V(Z,A) = 50$ $V(Z,B) = 100$ $V(Z,C) = 90$ $V(Z,D) = 500$

Another Statistic: Histograms



Requires some care to set bucket boundaries

Outline

What can we optimize?

Rule-based optimization

Data statistics

Cost models

Cost-based plan selection

Cost Models

How do we measure a query plan's cost?

Many possible metrics:

» Number of disk I/Os

- ← We'll focus on this
- » Number of compute cycles
- » Combined time metric
- » Memory usage
- » Bytes sent on network
- **>>** ...

Example: Index vs Table Scan

Our query: $\sigma_p(R)$ for some predicate p

s = p's selectivity (fraction tuples passing)

Table scan:

block size

R has $B(R) = T(R) \times S(R)/b$ blocks on disk

Cost: B(R) I/Os

Index search:

Index lookup for p takes L I/Os

We then have to read part of R; Pr[read block i]

≈ 1 – Pr[no match]^{records in block}

$$= 1 - (1-s)^{b/S(R)}$$

Cost: L + $(1-(1-s)^{b/S(R)})$ B(R)

Example: Index vs Table Scan

Our query: $\sigma_p(R)$ for some predicate p s = p's selectivity (fraction tuples passing)

$$C_{scan} = B(R)$$

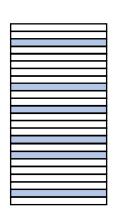
$$C_{index} = L + (1-(1-s)^{b/S(R)}) B(R)$$

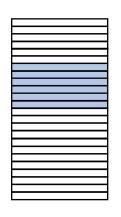
Index good when s is small, or S(R) is large

Index never "much worse" than table scan...

What If Results Were Clustered?

Unclustered: records that match p are spread out uniformly

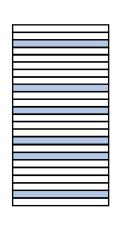


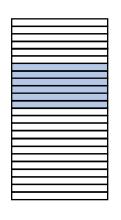


Clustered: records that match p are close together in R's file

What If Results Were Clustered?

Unclustered: records that match p are spread out uniformly





Clustered: records that match p are close together in R's file

We'd need to change our estimate of C_{index}:

$$C_{index} = L + s B(R)$$
Fraction of R's blocks read

Less than C_{scan} even for bigger s