CS256/Winter 2009 Lecture #2

Zohar Manna

SPL (Simple Programming Language) Syntax

Basic Statements

- skip
- assignment $\underbrace{(u_1, \dots, u_k)}_{\text{variables}} := \underbrace{(e_1, \dots, e_k)}_{\text{expressions}}$
- await c

(where c is a boolean expression)

special case: halt \equiv await F

- Communication by message-passing
 - $\begin{array}{ll} \alpha \ \Leftarrow \ e & (\text{send}) \\ \alpha \ \Rightarrow \ u & (\text{receive}) \end{array}$

(where α is a channel)

• Semaphore operations request r $(r > 0 \rightarrow r := r - 1)$ release r (r := r + 1)(where r is an integer variable) 2-2

Schematic Statements

In Mutual-Exclusion programs:

• noncritical

may not terminate

• critical

terminates

In Producer-Consumer programs:

• produce x

terminates – assign nonzero value to x

• consume y

terminates

No program variables are modified by schematic statements. One exception: "x" in **produce** x

Compound Statements

- Conditional if c then S_1 else S_2 if c then S
- Concatenation $S_1; \dots; S_k$

Example: when $c \operatorname{do} S \equiv \operatorname{await} c; S$

- <u>Selection</u> S_1 or \cdots or S_k
- while while c do S

Example:

loop forever do $S \equiv$ while T **do** S

Compound Statements (Con't)

• Cooperation Statement

$$\ell: [\underbrace{\ell_1:S_1; \ \hat{\ell}_1:}_{\text{process}}] \parallel \cdots \parallel [\ell_k:S_k; \ \hat{\ell}_k:]; \ \hat{\ell}:$$

 S_1, \ldots, S_k are <u>parallel</u> to one another <u>interleaved</u> execution.

 $\underbrace{\text{entry step: from } \ell \text{ to } \ell_1, \ell_2, \dots, \ell_k,}_{\text{exit step: from } \widehat{\ell_1}, \widehat{\ell_2}, \dots, \widehat{\ell_k} \text{ to } \widehat{\ell}.}$

• <u>Block</u>

 $[\underline{local declaration}; S]$

local variable,..., variable: type where $\underbrace{\varphi_i}_{y_1 = e_1, \ldots, y_n = e_n}$

Basic types – boolean, integer, character, ...

<u>Structured types</u> – array, list, set, \ldots

Static variable initialization (variables get initialized at the start of the execution)

Programs

$$P :: \begin{bmatrix} declaration; P_1 :: [\ell_1:S_1; \hat{\ell}_1:] \parallel \cdots \parallel \\ P_k :: [\ell_k:S_k; \hat{\ell}_k:] \end{bmatrix}$$

 P_1, \ldots, P_k are top-level processes Variables in P called program variables

Declaration

mode variable, ..., variable: type where φ_i program variables in (not modified) local

out

constraints on initial values

 $\varphi_1 \wedge \ldots \wedge \varphi_n$ data-precondition of the program

2-7

Channel Declaration

• synchronous channels (no buffering capacity)

mode $\alpha_1, \alpha_2, \ldots, \alpha_n$: channel of type

asynchronous channels

 (unbounded buffering capacity)
 mode α₁, α₂, ..., α_n: channel [1..] of type
 where φ_i

 $-\varphi_i$ is optional

 $-\varphi_i = \Lambda$ (empty list) by default

Foundations for SPL Semantics

Labels

 $\ell : S$

- Label ℓ identifies statement S
- Equivalence Relation \sim_L between labels:
 - For ℓ : $[\ell_1: S_1; \ldots; \ell_k: S_k]$ $\ell \sim_L \ell_1$
 - For ℓ : $[\ell_1: S_1 \text{ or } \dots \text{ or } \ell_k: S_k]$ $\ell \sim_L \ell_1 \sim_L \dots \sim_L \ell_k$
 - For ℓ : [local declaration; $\ell_1: S_1$] $\ell \sim_L \ell_1$

Note: For ℓ : $[\ell_1 : S_1 || \dots || \ell_k : S_k]$ $\ell \not\sim_L \ell_1 \not\sim_L \ell_2 \not\sim_L \dots$ because of the entry step

Example: In Figure 0.1 $\ell_0 \sim_L \ell_1$ $\ell_2 \sim_L \ell_3 \sim_L \ell_5$ in a, b: integer where a > 0, b > 0local y_1, y_2 : integer where $y_1 = a, y_2 = b$ out g: integer

$$\ell_{0}: \begin{bmatrix} \ell_{1}: \text{ while } y_{1} \neq y_{2} \text{ do} \\ & \ell_{3}: \text{ await } y_{1} > y_{2}; \ \ell_{4}: \ y_{1} := y_{1} - y_{2} \\ \text{ or } \\ & \ell_{5}: \text{ await } y_{2} > y_{1}; \ \ell_{6}: \ y_{2} := y_{2} - y_{1} \end{bmatrix} \\ \ell_{7}: \ g := y_{1} \end{bmatrix}$$

Figure 0.1

A Fully Labeled Program GCD-F

Locations

$[\ell]$

Identify site of control

- $[\ell]$ is the location corresponding to label ℓ .
- Multiple labels identifying different statements may identify the same location.

 $[\ell] = \{\ell' \mid \ell' \sim_L \ell\}$

Example: Fig 0.1: A fully labeled program $[\ell_0] = [\ell_1] = \{\ell_0, \ell_1\}$ $[\ell_6] = \{\ell_6\}$ $[\ell_2] = \{\ell_2, \ell_3, \ell_5\}$ $[\ell_7] = \{\ell_7\}$ $[\ell_4] = \{\ell_4\}$ $[\ell_8] = \{\ell_8\}$

Example: Fig 0.2: A partially labeled program ℓ_0' $\ell_3 \rightarrow \ell_2^a$ $\ell_5 \rightarrow \ell_2^b$

shortcut: label ℓ_2 "represents" $\{\ell_2, \ell_2^a, \ell_2^b\}$

in a, b: integer where a > 0, b > 0local y_1, y_2 : integer where $y_1 = a, y_2 = b$ out g: integer

$$\begin{array}{l} \ell_1: \ \textbf{while} \ y_1 \neq y_2 \ \textbf{do} \\ \\ \ell_2: \ \begin{bmatrix} \ell_2^a: \ \textbf{await} \ y_1 > y_2; \ \ell_4: \ y_1 := y_1 - y_2 \\ \textbf{or} \\ \\ \ell_2^b: \ \textbf{await} \ y_2 > y_1; \ \ell_6: \ y_2 := y_2 - y_1 \end{bmatrix} \\ \\ \ell_7: \ g := y_1 \\ \ell_8: \end{array}$$

Figure 0.2

A Partially Labeled Program GCD

Post Location

 $\ell: S; \ \hat{\ell}: \qquad post(S) = [\hat{\ell}]$

• For $[\ell_1: S_1; \hat{\ell}_1:] \parallel \cdots \parallel [\ell_k: S_k; \hat{\ell}_k:]$ $post(S_i) = [\hat{\ell}_i]$, for every $i = 1, \dots, k$

• For
$$S = [\ell_1 : S_1; \dots; \ell_k : S_k]$$

 $post(S_i) = [\ell_{i+1}], \text{ for } i = 1, \dots, k-1$
 $post(S_k) = post(S)$

- For $S = [\ell_1 : S_1$ or ... or $\ell_k : S_k]$ $post(S_1) = \cdots = post(S_k) = post(S)$
- For $S = [\text{if } c \text{ then } S_1 \text{ else } S_2]$ $post(S_1) = post(S_2) = post(S)$
- For $[\ell : \text{while } c \text{ do } S']$ $post(S') = [\ell]$

Example: Post Locations of Fig 0.2

$$post(\ell_1) = [\ell_7]$$

$$post(\ell_2) = post(\ell_4)$$

$$= post(\ell_6) = [\ell_1]$$

$$post(\ell_2^a) = [\ell_4]$$

$$post(\ell_2^b) = [\ell_6]$$

$$post(\ell_7) = [\ell_8]$$

Ancestor

S is an <u>ancestor</u> of S'if S' is a substatement of S

S is a <u>common ancestor</u> of S_1 and S_2 if it is an ancestor of both S_1 and S_2

S is a <u>least common ancestor</u> (LCA) of S_1 and S_2 if S is a common ancestor of S_1 and S_2 and any other common ancestor of S_1 and S_2 is an ancestor of S

LCA is unique for given statements S_1 and S_2

Example:
$$\begin{bmatrix} S_1; & [S_2 || S_3]; & S_4 \end{bmatrix} || S_5$$

LCA of $S_2, & S_3 & [S_2 || S_3]$
LCA of $S_2, & S_4 & [S_1; & [S_2 || S_3]; & S_4]$
LCA of $S_2, & S_5 & [S_1; & [S_2 || S_3]; & S_4] || S_5$

Parallel Labels

• <u>Statements</u> S and \tilde{S} are <u>parallel</u> if their LCA is a cooperation statement that is different from statements S and \tilde{S}

Example: $S = [S_1; [S_2 S_3]; S_4] S_5$			
<u>Statements</u>	<u>LCA</u>		
S_2 parallel to S_3 S_2 parallel to S_5 S_2 not parallel to S_4 S_2 not parallel to $S_2 \parallel S_3$	$S_2 \parallel S_3$ S $[S_1; \dots; S_4]$ not coop. $S_2 \parallel S_3$ same		

• parallel labels – labels of parallel statements

Conflicting Labels

<u>conflicting labels</u> – not equivalent and not parallel

Example: $\left[\begin{array}{c} \ell_1: S_1; \\ \ell_2: \left([\ell_3: S_3; \ \hat{\ell}_3:] \parallel [\ell_4: S_4; \ \hat{\ell}_4:] \right); \\ \ell_5: S_5; \ \hat{\ell}_5: \end{array} \right] \parallel [\ell_6: S_6; \ \hat{\ell}_6:]$ ℓ_3 is parallel to each of $\{\ell_4, \hat{\ell}_4, \ell_6, \hat{\ell}_6\}$ and in conflict with each of $\{\ell_1, \ell_2, \hat{\ell}_3, \ell_5, \hat{\ell}_5\}$ ℓ_6 and $\hat{\ell}_6$ are in conflict with each other but are parallel to each of $\{\ell_1, \ell_2, \ell_3, \hat{\ell}_3, \ell_4, \hat{\ell}_4, \ell_5, \hat{\ell}_5\}$

Critical References

Writing References:

$x := \ldots$	$\alpha \Rightarrow u$	$\mathbf{produce}\;x$	request	r
↑	\uparrow	\uparrow		\uparrow
			release	r
				\uparrow

Reading References: all other references

 $\underline{\text{critical reference}}$ of a variable in S if:

- writing ref to a variable that has reading or writing refs in S' (parallel to S)
- reading reference to a variable that has writing references in S' (parallel to S)
- reference to a channel

Limited Critical References (LCR)

Statement obeys <u>LCR restriction</u> (<u>LCR-Statement</u>) if each test (for await, conditional, while) and entire statement (for assignment) contains at most one critical reference.

Example: Fig 0.3

 ℓ_2, m_1, m_3 are LCR-Statements

 ℓ_1, m_2 violate the LCR-requirement

LCR-Program: only LCR-statements

Interleaved vs. Concurrent Execution

Claim : If P is an LCR program, then the interleaving computations of P and the concurrent executions of P give the same results.

Discussion & explanation: *Blue Book*.

$$P_{1}:: \begin{bmatrix} \ell_{1}: b := b \cdot y_{1} \\ \ell_{2}: y_{1}:= y_{1} - 1 \\ \ell_{3}: \end{bmatrix} \mid P_{2}:: \begin{bmatrix} m_{1}: \text{ await } y_{1} + y_{2} \le n \end{bmatrix}$$
$$m_{2}: b := b / y_{2}$$
$$m_{3}: y_{2}:= y_{2} + 1$$
$$m_{4}:$$

Figure 0.3

Critical references

SPL Semantics

Transition Semantics:

$$\begin{array}{ccc} \text{SPL P} & \text{computation of P} \\ \downarrow & & \uparrow \\ \text{FTS } \varPhi & \rightarrow & \text{computation of } \varPhi \end{array}$$

Given an SPL-program P, we can construct the corresponding FTS $\Phi = \langle V, \Theta, \mathcal{T}, \mathcal{J}, \mathcal{C} \rangle$:

• system variables V

 $Y = \{y_1, \dots, y_n\} - \text{program variables of } P$ domains: as declared in P π - control variable domain: sets of locations in P $V = Y \cup \{\pi\}$

Comments:

- For label
$$\ell$$
, at_{ℓ} : $[\ell] \in \pi$
 at'_{ℓ} : $[\ell] \in \pi'$

Note: When going from an SPL program to an FTS we lose the sequential nature of the program. We need to model control explicitly in the FTS: π can be viewed as a program counter.

Example: Fig 0.1

$$V = \{\pi, a, b, y_1, y_2, g\}$$

 π - ranges over subsets of
 $\{[\ell_1], [\ell_2], [\ell_4], [\ell_6], [\ell_7], [\ell_8]\}$
 a, b, \dots, g - range over integers

• Initial Condition
$$\Theta$$

For $P :: \left[\text{dec}; \left[P_1 :: \left[\ell_1 : S_1; \ \hat{\ell}_1 : \ \right] \parallel \cdots \parallel \right] \right]$
 $P_k :: \left[\ell_k : S_k; \ \hat{\ell}_k : \ \right] \right]$
with data-precondition φ ,
 Θ : $\pi = \{ [\ell_1], \ldots, \ [\ell_k] \} \land \varphi$

Example: Fig 0.1

$$\Theta: \pi = \{ [\ell_1] \} \land$$

$$\underbrace{a > 0 \land b > 0 \land y_1 = a \land y_2 = b}_{\text{data-precondition}}$$

2-24

in a, b: integer where a > 0, b > 0local y_1, y_2 : integer where $y_1 = a, y_2 = b$ out g: integer

$$\begin{array}{l} \ell_1: \ \textbf{while} \ y_1 \neq y_2 \ \textbf{do} \\ \\ \ell_2: \ \begin{bmatrix} \ell_2^a: \ \textbf{await} \ y_1 > y_2; \ \ell_4: \ y_1 := y_1 - y_2 \\ \textbf{or} \\ \\ \ell_2^b: \ \textbf{await} \ y_2 > y_1; \ \ell_6: \ y_2 := y_2 - y_1 \end{bmatrix} \\ \\ \ell_7: \ g := y_1 \\ \ell_8: \end{array}$$

Figure 0.2

A Partially Labeled Program GCD

• <u>Transitions</u> \mathcal{T}

 $\mathcal{T} = \{\tau_I\} \cup \left\{ \begin{array}{l} \text{transitions associated with} \\ \text{the statements of } P \end{array} \right\}$

where τ_I is the "idling transition" $\rho_I: V' = V$

abbreviation

- pres(U): $\bigwedge_{u \in U} (u' = u)$ (where $U \subseteq V$) the value of $u \in U$ are preserved
- move(L, \widehat{L}): $L \subseteq \pi \land \pi' = (\pi L) \cup \widehat{L}$ where L, \widehat{L} are sets of locations

 $- move(\ell, \hat{\ell}): move(\{[\ell]\}, \{[\hat{\ell}]\})$

We list the transitions (transition relations) associated with the statements of P

$\underline{\ell}:S$		$\underline{ ho_\ell}$
Basic Statem	ents	
ℓ : skip; $\widehat{\ell}$:	\rightarrow	$move(\ell, \widehat{\ell}) \land pres(Y)$
ℓ : $\overline{u} := \overline{e}$; $\hat{\ell}$:	\rightarrow	$move(\ell, \hat{\ell}) \land \overline{u}' = \overline{e} \ \land pres(Y - \{\overline{u}\})$

Basic Statements (Con't)

$$\begin{split} \ell: \text{ await } c; \ \widehat{\ell}: & \to & move(\ell, \widehat{\ell}) \land c \land pres(Y) \\ \ell: \text{ request } r; \ \widehat{\ell}: & \to & move(\ell, \widehat{\ell}) \land r > 0 \\ & \land r' = r - 1 \\ & \land pres(Y - \{r\}) \end{split}$$

$$\ell: \text{ release } r; \ \widehat{\ell}: \longrightarrow move(\ell, \widehat{\ell}) \land r' = r + 1 \\ \land pres(Y - \{r\})$$

Basic Statements (Con't)

$$\underline{\operatorname{asynchronous send}} \\ \widehat{\ell}: \ \alpha \Leftarrow e; \ \widehat{\ell}: \qquad \rightarrow \qquad \operatorname{move}(\ell, \widehat{\ell}) \ \land \ \alpha' = \alpha \bullet e \\ \land \ \operatorname{pres}(Y - \{\alpha\}) \\ \underline{\operatorname{asynchronous receive}} \\ \widehat{\ell}: \ \alpha \Rightarrow u; \ \widehat{\ell}: \qquad \rightarrow \qquad \operatorname{move}(\ell, \widehat{\ell}) \ \land \ |\alpha| > 0 \\ \land \ \alpha = u' \bullet \alpha' \\ \land \ \operatorname{pres}(Y - \{u, \alpha\}) \\ \end{array}$$

 $\frac{\text{synchronous send-receive}}{\ell: \ \alpha \Leftarrow e; \ \hat{\ell}: \ m: \ \alpha \Rightarrow u; \ \widehat{m}:$ $move(\{\ell, m\}, \{\hat{\ell}, \widehat{m}\}) \land u' = e \land pres(Y - \{u\})$

2-29

 ℓ : critical; $\hat{\ell}$: \rightarrow move $(\ell, \hat{\ell}) \land pres(Y)$

Compound Statements

$$\ell: \left[\text{if } c \text{ then } \ell_1 : S_1 \text{ else } \ell_2 : S_2 \right]; \ \widehat{\ell}: \rightarrow$$
$$\rho_{\ell}: \rho_{\ell}^{\mathrm{T}} \lor \rho_{\ell}^{\mathrm{F}} \text{ where}$$
$$\rho_{\ell}^{\mathrm{T}}: move(\ell, \ell_1) \land c \land pres(Y)$$
$$\rho_{\ell}^{\mathrm{F}}: move(\ell, \ell_2) \land \neg c \land pres(Y)$$

$$\begin{split} \ell: \left[\mathbf{while} \ c \ \mathbf{do} \ [\tilde{\ell}: \tilde{S} \] \right]; \ \hat{\ell}: \to \\ \rho_{\ell}: \rho_{\ell}^{\mathrm{T}} \lor \rho_{\ell}^{\mathrm{F}} \ \text{where} \\ \rho_{\ell}^{\mathrm{T}}: \ move(\ell, \tilde{\ell}) \ \land \ c \ \land \ pres(Y) \\ \rho_{\ell}^{\mathrm{F}}: \ move(\ell, \hat{\ell}) \ \land \ \neg c \ \land \ pres(Y) \end{split}$$

$$\ell: \left[[\ell_1: S_1; \ \hat{\ell}_1:] \parallel \cdots \parallel [\ell_k: S_k; \ \hat{\ell}_k:] \right]; \ \hat{\ell}: \rightarrow \\ \rho_{\ell}^{\mathrm{E}}: \ move(\{\ell\}, \ \{\ell_1, \dots, \ell_k\}) \land \ pres(Y) \ (\text{entry}) \\ \rho_{\ell}^{\mathrm{X}}: \ move(\{\hat{\ell}_1, \dots, \hat{\ell}_k\}, \ \{\hat{\ell}\}) \land \ pres(Y) \ (\text{exit}) \\ \\ 2-31 \end{cases}$$

Grouped Statements

$$\langle S \rangle$$

executed in a single atomic step

Example:

$$\langle x := y + 1; z := 2x + 1 \rangle$$

 $x' = y + 1 \land z' = 2y + 3$
the same as $(x, z) := (y + 1, 2y + 3)$

Example:

$$\underbrace{\langle a := 3; a := 5 \rangle}_{a' = 5}$$

$$a = 3 \text{ is never visible to the outside world, nor to other processes}$$

• Justice Set \mathcal{J}

All transitions except

 τ_{I} and all transitions associated with **noncritical** statements

• Compassion Set \mathcal{C}

All transitions associated with <u>send</u>, <u>receive</u>, request statements

Computations of Programs

local x: integer where
$$x = 1$$

 $P_1 :: \begin{bmatrix} \ell_0^a: \text{ await } x = 1 \\ \text{or} \\ \ell_0^b: \text{ skip} \end{bmatrix} \| P_2 :: \begin{bmatrix} m_0: \text{ while } T \text{ do} \\ [m_1: x := -x] \end{bmatrix}$

Fig 0.4 Process P_1 terminates in all computations.

$$\sigma: \langle \pi: \{\ell_0, m_0\}, x: 1 \rangle \xrightarrow{m_0} \langle \pi: \{\ell_0, m_1\}, x: 1 \rangle \xrightarrow{m_1} \rangle$$
$$\langle \pi: \{\ell_0, m_0\}, x: -1 \rangle \xrightarrow{m_0} \langle \pi: \{\ell_0, m_1\}, x: -1 \rangle \xrightarrow{m_1} \rangle$$
$$\langle \pi: \{\ell_0, m_0\}, x: 1 \rangle \xrightarrow{m_0} \cdots$$

 $\sigma \text{ is not a computation. Unjust towards } \ell^b_0$ (enabled on all states but never taken)

local x: integer where
$$x = 1$$

 $P_1 :: \begin{bmatrix} \ell_0: & \begin{bmatrix} \ell_0^a: \text{ await } x = 1 \\ \text{or} & \\ \ell_0: & \end{bmatrix} \end{bmatrix} \parallel P_2 :: \begin{bmatrix} m_0: \text{ while } T \text{ do} \end{bmatrix} \\ \begin{bmatrix} m_1: & x := -x \end{bmatrix}$

Fig 0.5 skip
$$\rightarrow$$
 await $x \neq 1$

$$\sigma: \langle \pi: \{\ell_0, m_0\}, x: 1 \rangle \xrightarrow{m_0} \langle \pi: \{\ell_0, m_1\}, x: 1 \rangle \xrightarrow{m_1} \rangle$$
$$\langle \pi: \{\ell_0, m_0\}, x: -1 \rangle \xrightarrow{m_0} \langle \pi: \{\ell_0, m_1\}, x: -1 \rangle \xrightarrow{m_1} \rangle$$
$$\langle \pi: \{\ell_0, m_0\}, x: 1 \rangle \xrightarrow{m_0} \cdots$$

 σ is a computation – since none of the just transitions are continually enabled.

Computations of Programs (Con't)

local x: integer where
$$x = 1$$

 ℓ_0 : if $x = 1$ then
 ℓ_1 : skip
else
 ℓ_2 : skip
 ℓ_3 :
 $\begin{pmatrix} l_0 : if x = 1 \text{ then} \\ l_1 : skip \\ l_2 : if x = 1 \text{ then} \\ l_2 : l_2$

Fig 0.6 Process P_1 terminates in all computations.

$$\sigma: \langle \pi: \{\ell_0, m_0\}, x: 1 \rangle \xrightarrow{m_0} \langle \pi: \{\ell_0, m_1\}, x: 1 \rangle \xrightarrow{m_1} \langle \pi: \{\ell_0, m_0\}, x: -1 \rangle \xrightarrow{m_0} \langle \pi: \{\ell_0, m_1\}, x: -1 \rangle \xrightarrow{m_1} \langle \pi: \{\ell_0, m_0\}, x: 1 \rangle \xrightarrow{m_0} \cdots$$

 σ is not a computation – since ℓ_0 is continually enabled, but not taken.

Control Configurations

$$L = \left\{ [\ell_1], \dots, [\ell_k] \right\} \text{ of } P \text{ is called } \underline{\text{conflict-free}} \\ \text{if no } [\ell_i] \text{ conflicts with } [\ell_j], \text{ for } i \neq j.$$

L is called a (<u>control</u>) <u>configuration</u> of Pif it is a maximal conflict-free set.

Example:
local x: integer where
$$x = 0$$

 $P_1 :: \begin{bmatrix} \ell_0: x := 1 \\ \ell_1: \end{bmatrix} \parallel P_2 :: \begin{bmatrix} m_0: \text{ await } x = 1 \\ m_1: \end{bmatrix}$
Configurations
 $\{ [\ell_0], [m_0] \}, \{ [\ell_0], [m_1] \}, \{ [\ell_1], [m_1] \}$

accessible configuration – appears as value of π in some accessible state

Example:

 $\big\{ [\ell_0], [m_1] \big\}$ does not appear in any accessible state

Is a given configuration accessible?

Undecidable

The Mutual-Exclusion Problem



Requirements:

• <u>Exclusion</u>

While one of the processes is in its critical section, the other is not

• Accessibility

Whenever a process is at the noncritical section exit, it must eventually reach its critical section

Example: mutual exclusion by semaphores Fig. 0.7

local y: integer where y = 1



Fig. 0.7 Program MUX-SEM

Message-Passing Programs

Example: Producer-Consumer

Fig. 0.9

assumption:

channel <u>send</u> $\leq N$ values

local send, ack: channel [1..] of integer where send = Λ , ack = $\underbrace{[1, \dots, 1]}_{N}$

	$\begin{bmatrix} local x, t: integer \end{bmatrix}$		$\begin{bmatrix} local y: integer \end{bmatrix}$
	ℓ_0 : loop forever do		m_0 : loop forever do
Prod::	$\left\lceil \ell_1: \text{ produce } x \right\rceil$	Cons ::	$\left[m_1: send \Rightarrow y \right]$
	$\ell_2: ack \Rightarrow t$		$m_2: ack \notin 1$
	$\lfloor \ell_3: send \notin x \rfloor$		m_3 : consume y

Fig. 0.9 Program PROD-CONS