



# Precise Timing in Financial Markets

Time Distribution in Deutsche Börse's T7<sup>®</sup> Trading Network

CS 349F Technology for Financial Systems | October 2020 | Stanford



# About the speakers

## Andreas Lohr

- Degree in computer science from University of Applied Sciences in Darmstadt (1994)
- Working in technology for financial trading since
- Various roles in two investment banks (Frankfurt, London)
- Performance engineer in a technology-driven trading firm (Amsterdam)

## Joined Deutsche Börse in 2016

- Trading IT, monitoring, infrastructure, co-location, and part-time chief cable measurer
- Deutsche Börse operates Xetra, the reference market for exchange trading in German shares and ETFs, and Eurex, a leading global derivatives exchange

## Sebastian Neusüß

- Diploma in Theoretical Physics from Johannes Gutenberg University in Mainz (1999)

## Joined Deutsche Börse in 1999

- Co-authored the messaging system that drives the current trading system of Deutsche Börse (T7)
- Designed the latency monitoring for T7
- Heads the trading system analytics team
- Does real time application monitoring for the T7 platform, market microstructure analysis, data analysis and chasing nanoseconds

We will go deep and move from business logic to ASIC design.

# Agenda

**3** Overview

**7** Central Limit Order Book

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**22** Time Distribution in T7<sup>®</sup>

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Overview



## The New York Times

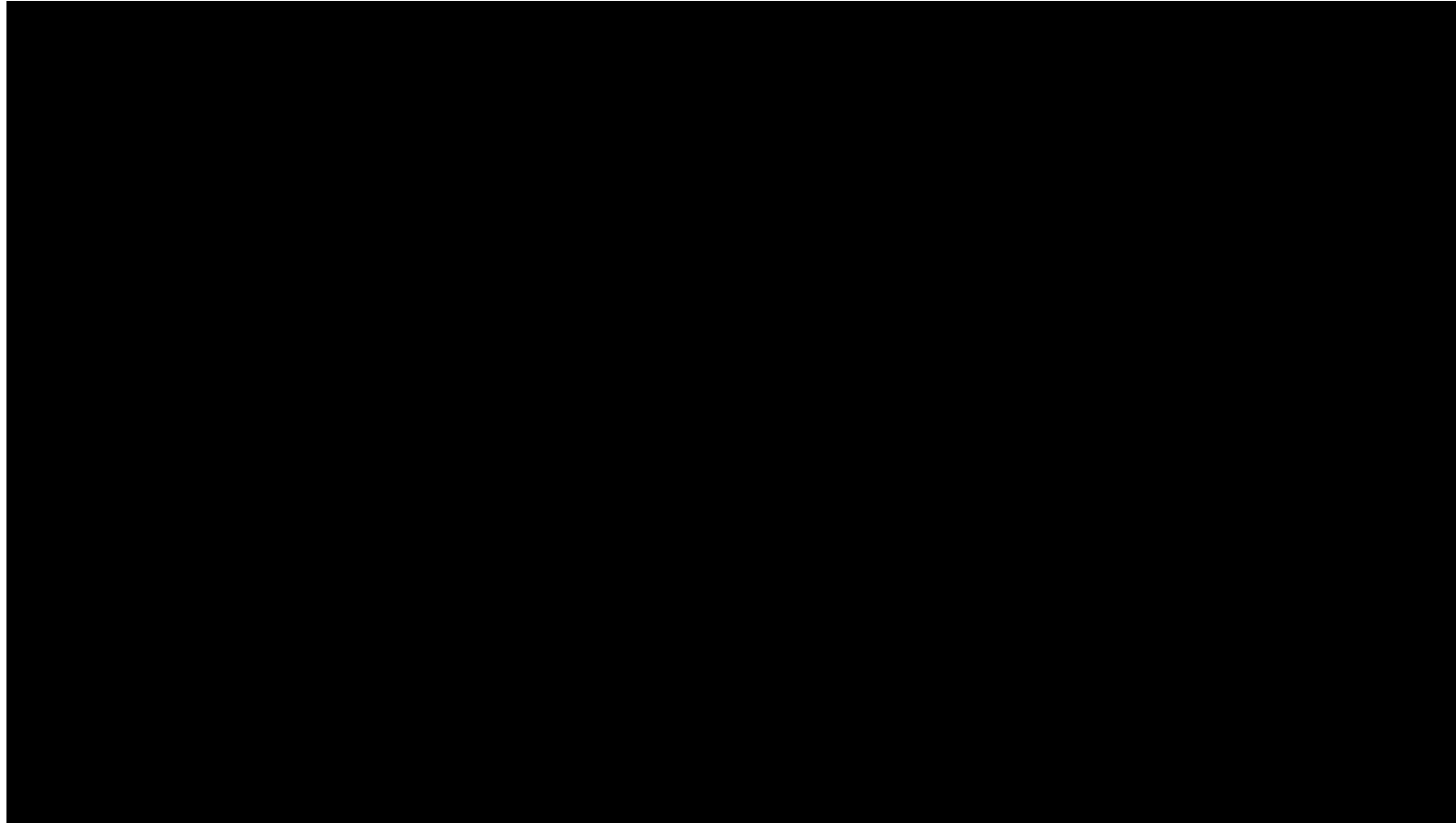
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*“Time Split to the Nanosecond Is Precisely  
What Wall Street Wants”*

“The financial industry has easily become the most obsessed with time”

-Balaji Prabhakar, Stanford University

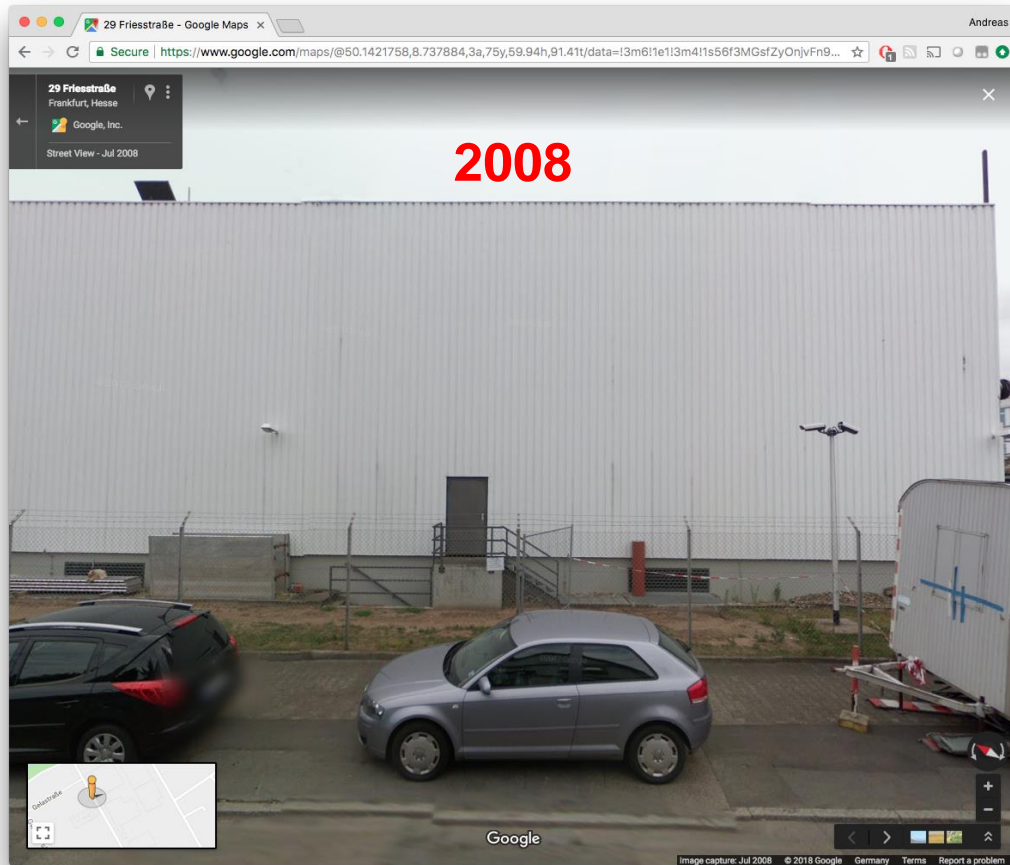
## The Hummingbird Project (2018), fiction based on a true story



<https://www.youtube.com/watch?v=YtAz6CT-1yA>

# Obsessed with Time?

## Data center in Frankfurt, Germany



GPS (and other similar systems) disseminate precise time

## History of financial trading in Frankfurt

1150 Medieval trade fair

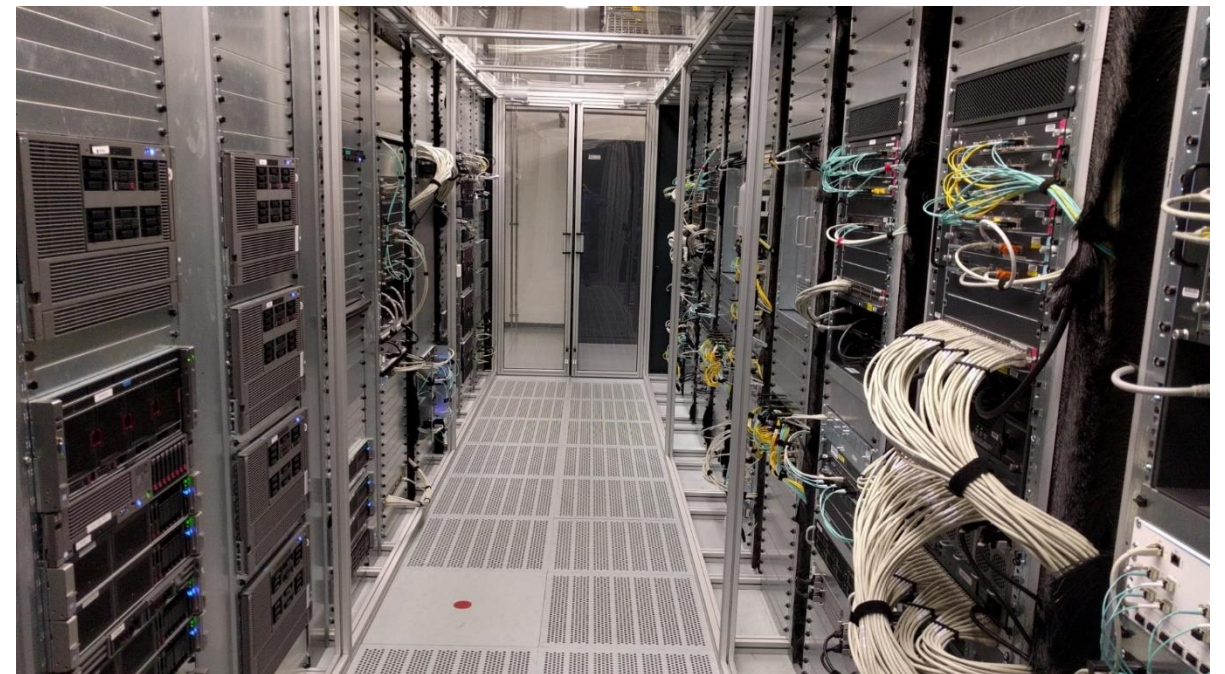
1585 Frankfurt merchants set uniform exchange rates for the first time

1820 The first share is listed in Frankfurt (shares of the Austrian National Bank)

1843 The first stock exchange building

1990 First electronic-only market for derivatives (DTB, Deutsche Terminbörse, now Eurex)

1997 Introduction of Xetra as the electronic stock market





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## Central Limit Order Book



# Central Limit Order Book (1)

LastTime	LastVolume	Last			
10:20:10.123	165	73.04			
BidCount	BidVolume	Bid	Ask	AskVolume	AskCount
3	624	73.04	73.05	3081	5
10	1474	73.03	73.06	2662	15
14	2505	73.02	73.07	5854	17
16	2843	73.01	73.08	4284	14
10	1925	73.00	73.09	6388	15
12	2328	72.99	73.10	1908	11
11	2814	72.98	73.11	1151	5
7	967	72.97	73.12	534	4
10	1803	72.96	73.13	4090	5
8	938	72.95	73.14	1104	4



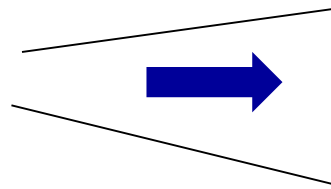
Ask	AskVolume	QueuePos
73.05	100	1
73.05	791	2
73.05	1368	3
73.05	685	4
73.05	137	5

- List of **buy** orders on the “Bid” side
- List of **sell** orders on the “Ask” side
- Sorted by price

- Priority on each price level by time
- Price-time priority is the most used electronic execution model

## Central Limit Order Book (2)

LastTime	LastVolume	Last			
10:20:10.123	165	73.04			
BidCount	BidVolume	Bid	Ask	AskVolume	AskCount
3	624	73.04	73.05	3081	5
10	1474	73.03	73.06	2662	15
14	2505	73.02	73.07	5854	17
16	2843	73.01	73.08	4284	14
New order: Buy 100 @ 73.05					
LastTime	LastVolume	Last			
10:20:10.352	100	73.05			
BidCount	BidVolume	Bid	Ask	AskVolume	AskCount
3	624	73.04	73.05	<b>2981</b>	<b>4</b>
10	1474	73.03	73.06	2662	15
14	2505	73.02	73.07	5854	17
16	2843	73.01	73.08	4284	14



Ask	AskVolume	QueuePos
73.05	100	1
73.05	791	2
73.05	1368	3
73.05	685	4
73.05	137	5

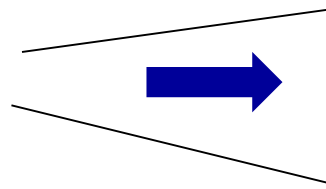
Example:

We want to buy 100 shares at a price of 73.05

Q: Which of the 5 sell orders is “matched” with our buy order?

## Central Limit Order Book (3)

LastTime	LastVolume	Last			
10:20:10.123	165	73.04			
BidCount	BidVolume	Bid	Ask	AskVolume	AskCount
3	624	73.04	73.05	3081	5
10	1474	73.03	73.06	2662	15
14	2505	73.02	73.07	5854	17
16	2843	73.01	73.08	4284	14
New order: Buy 100 @ 73.05					
LastTime	LastVolume	Last			
10:20:10.352	100	73.05			
BidCount	BidVolume	Bid	Ask	AskVolume	AskCount
3	624	73.04	73.05	<b>2981</b>	<b>4</b>
10	1474	73.03	73.06	2662	15
14	2505	73.02	73.07	5854	17
16	2843	73.01	73.08	4284	14



Ask	AskVolume	QueuePos
73.05	100	1
73.05	791	2
73.05	1368	3
73.05	685	4
73.05	137	5

Example:

We want to buy 100 shares at a price of 73.05

Q: Which of the 5 sell orders is “matched” with our buy order?

A: The sell order which entered the order book the **earliest**.

Implication:

The faster you are, the higher the probability of an order being executed at the desired price. **True for both sides of the trade** (buyer and seller)

# Matching Algorithms

## Price Time

- Priority is determined by price then **time**
- FIFO queue per price level
- Higher queue priority increases probability of being matched
- The most common matching algorithm

## Other matching algorithms

- Pro-Rata (allocation based on volume)
- Auction models. Collect orders over a period of time, then match buys and sells at equilibrium price.

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## Asset Prices



# Asset Prices

The efficient-market hypothesis (EMH) says that asset prices fully reflect all available information.

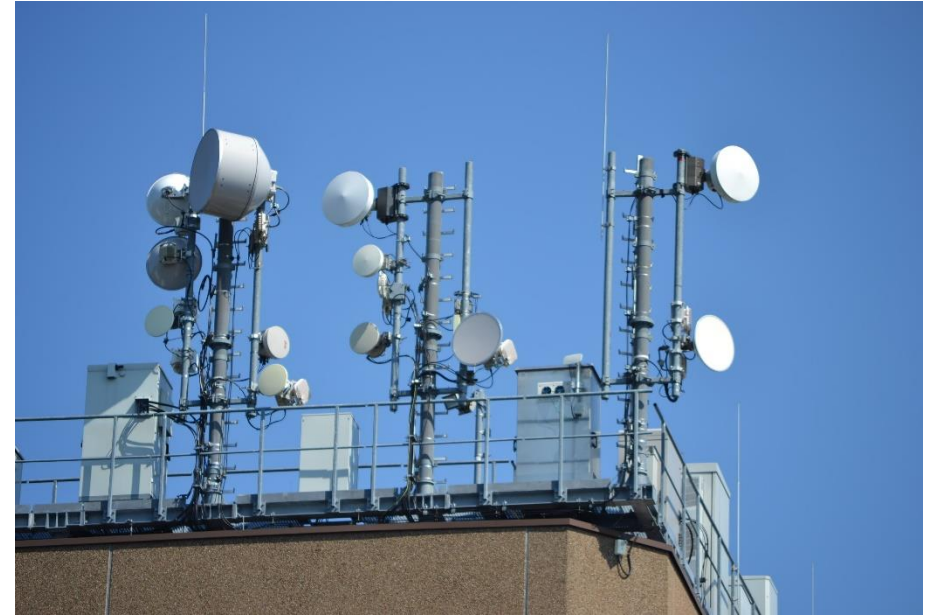
The EMH has critics, but we can agree on that new information (events) affect prices.

Examples:

- News
- Changes in interest rates
- Release of economic indicators (e.g. unemployment figures, non-farm payrolls)
- The central limit order book itself (e.g. more buyers than sellers)
- Prices of correlated instruments

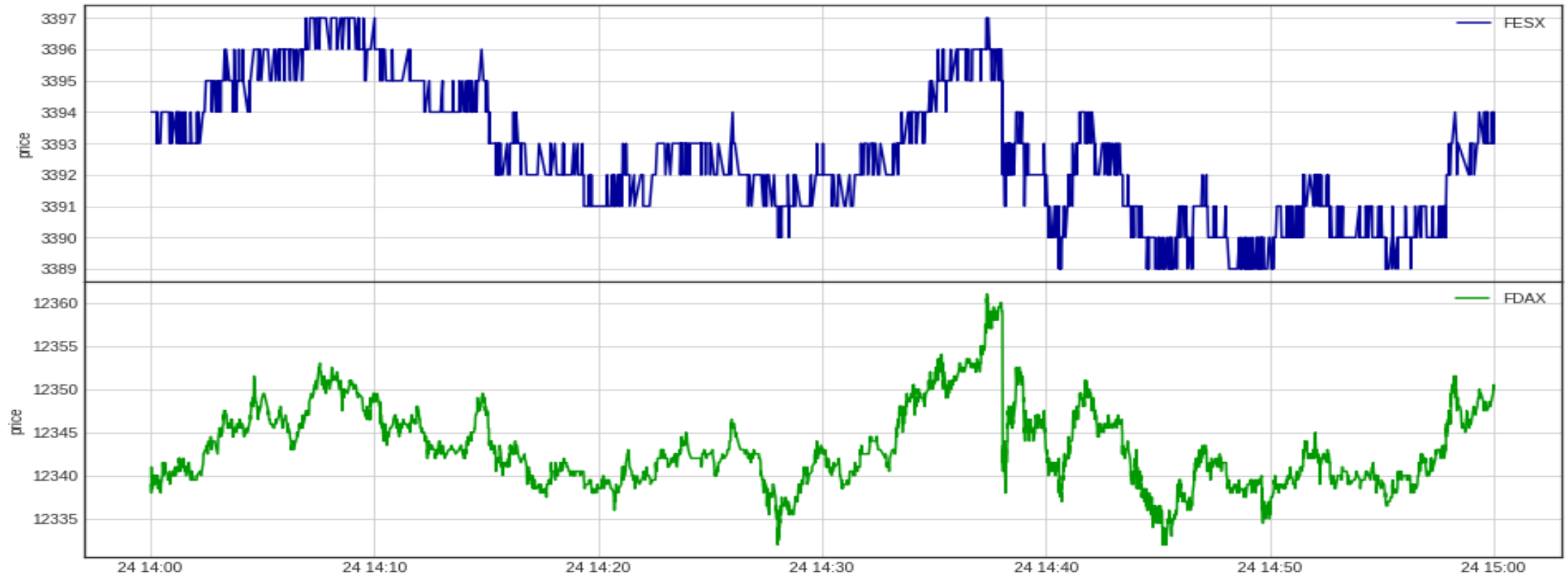
Event source can be:

- Remote (need to send information over WAN and/or radio links)
- Local (LAN, co-location)



## Correlated Asset Prices – Example

FDAX Future vs FESX Future - 2018-09-24 14:00-15:00 CET



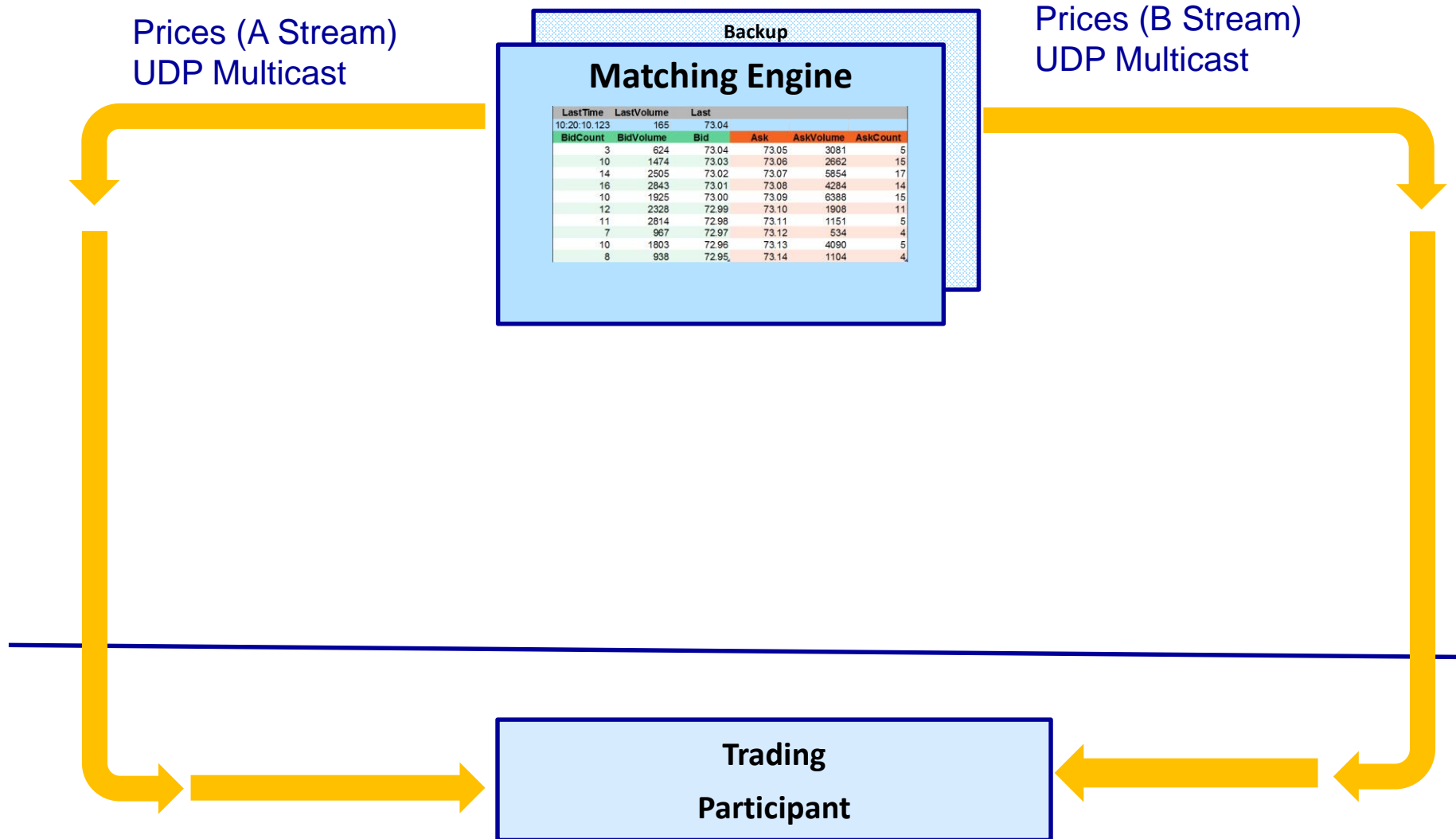


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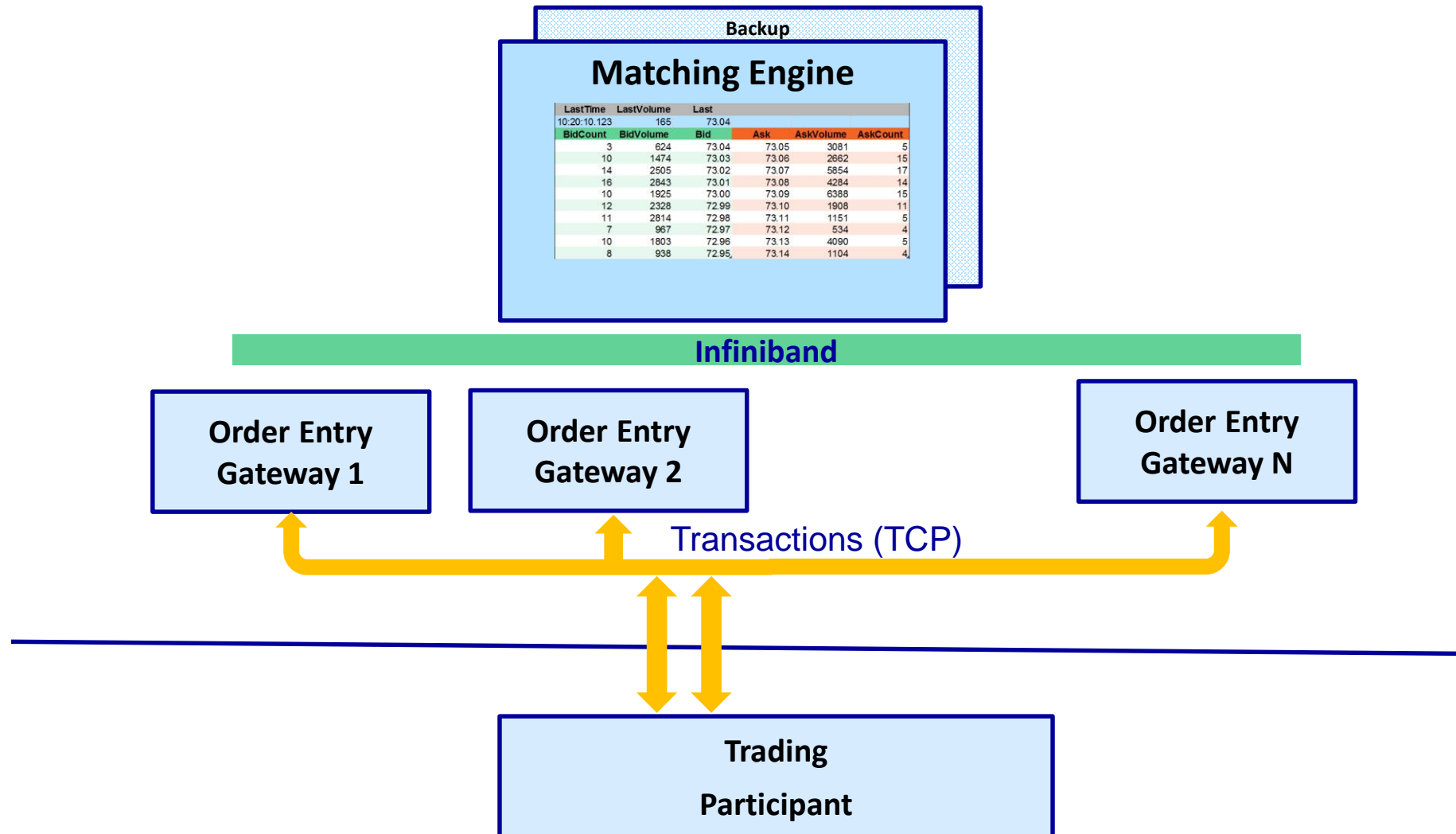
T7<sup>®</sup> Co-Location



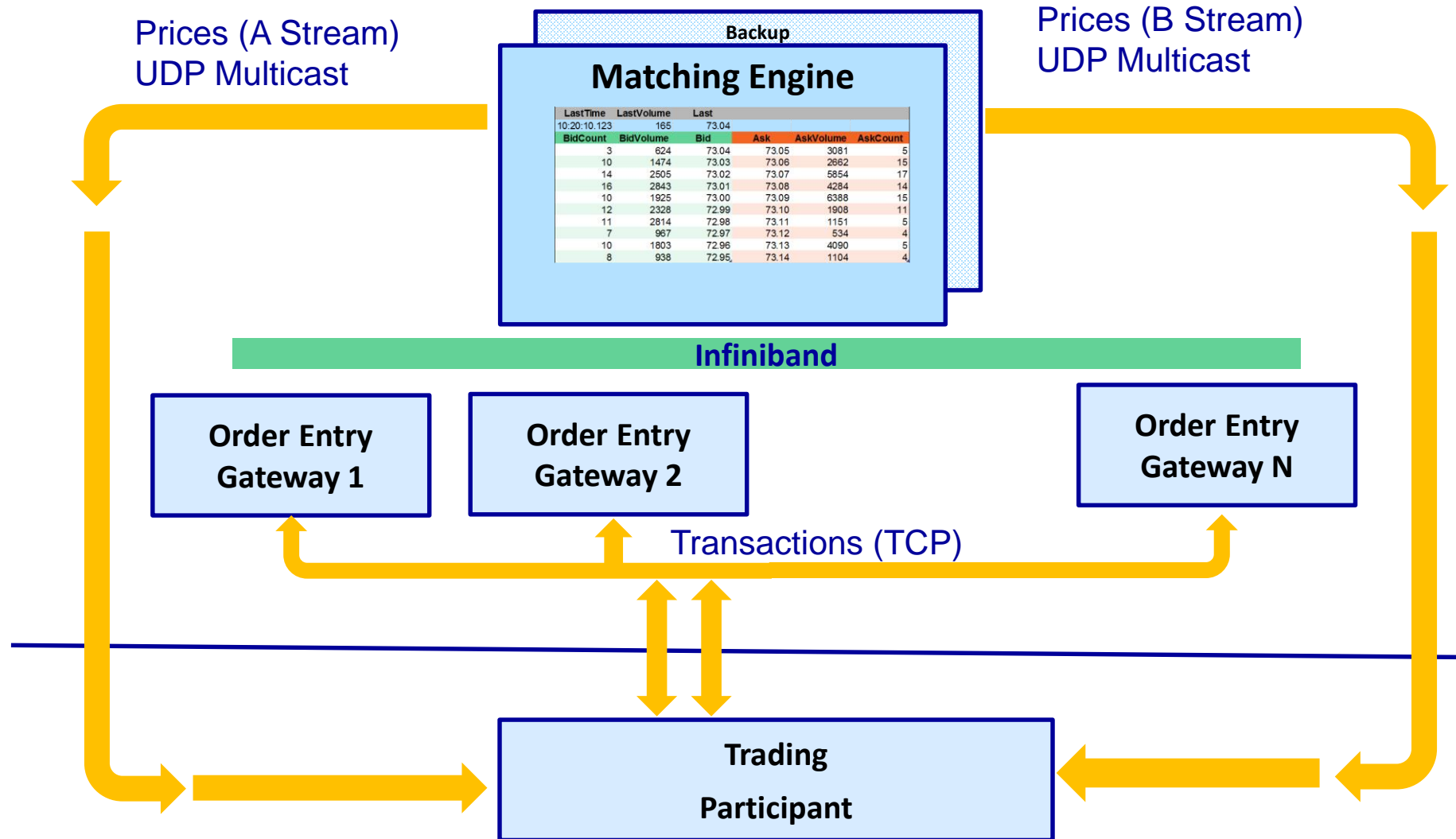
# T7<sup>®</sup> Architecture – Price Information



# T7<sup>®</sup> Architecture – Interaction (placing orders)

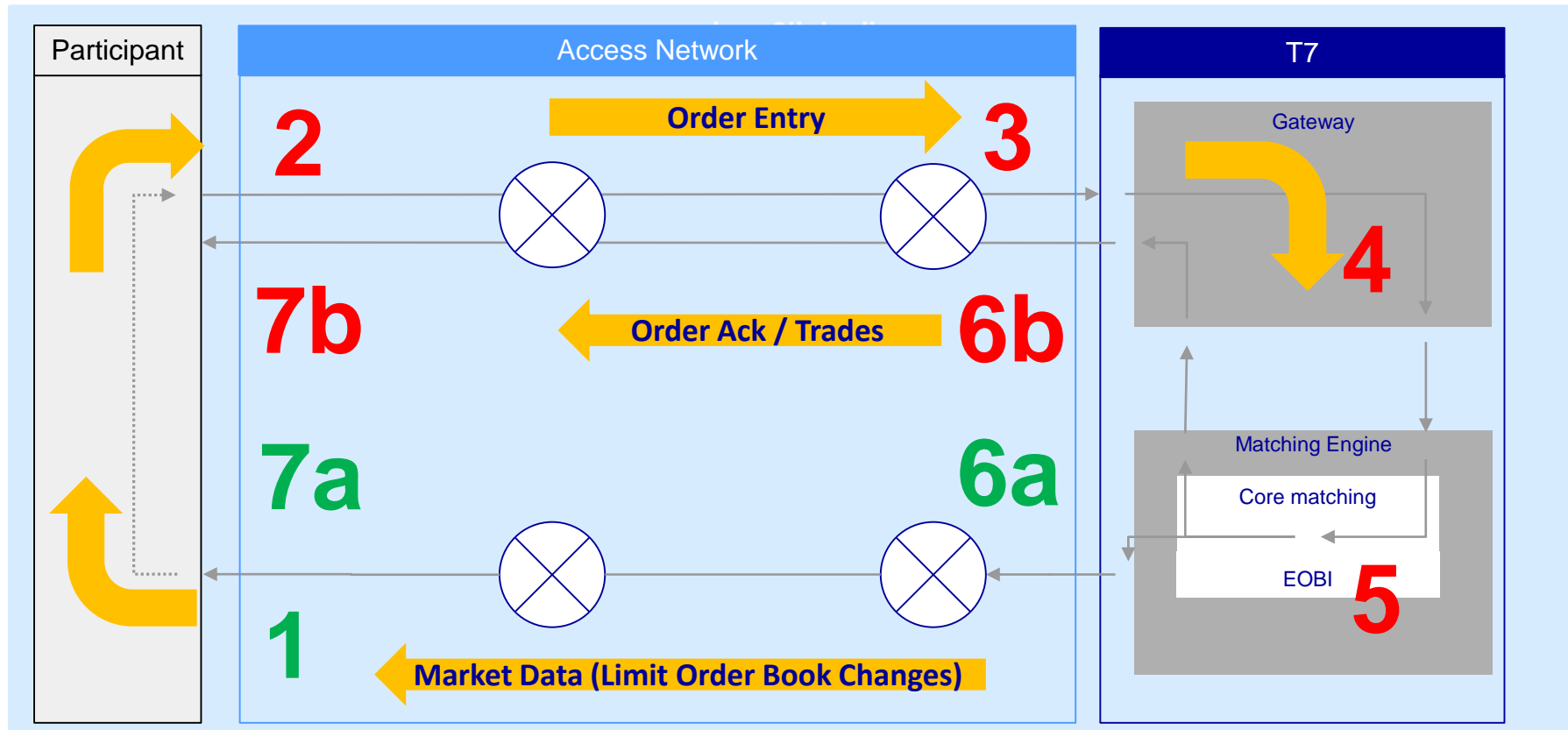


# T7<sup>®</sup> Architecture



# T7<sup>®</sup> Co-location

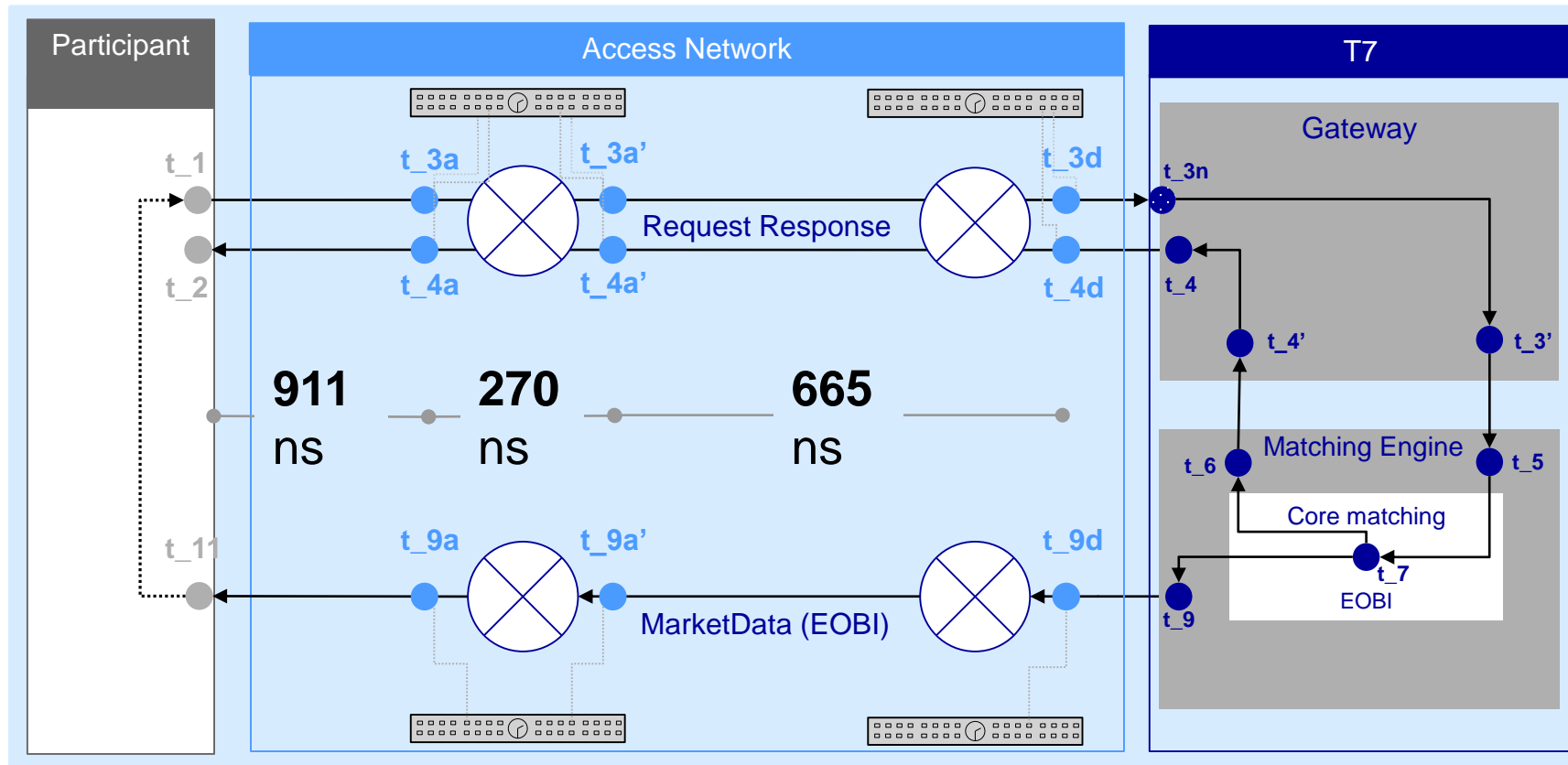
Zoom in to a single matching engine



Median round-trip from order entry to acknowledgement  $\approx 60\mu\text{s}$  (2)  $\rightarrow$  (7)

The fastest participants have **sub 100ns** response times (1)  $\rightarrow$  (2)

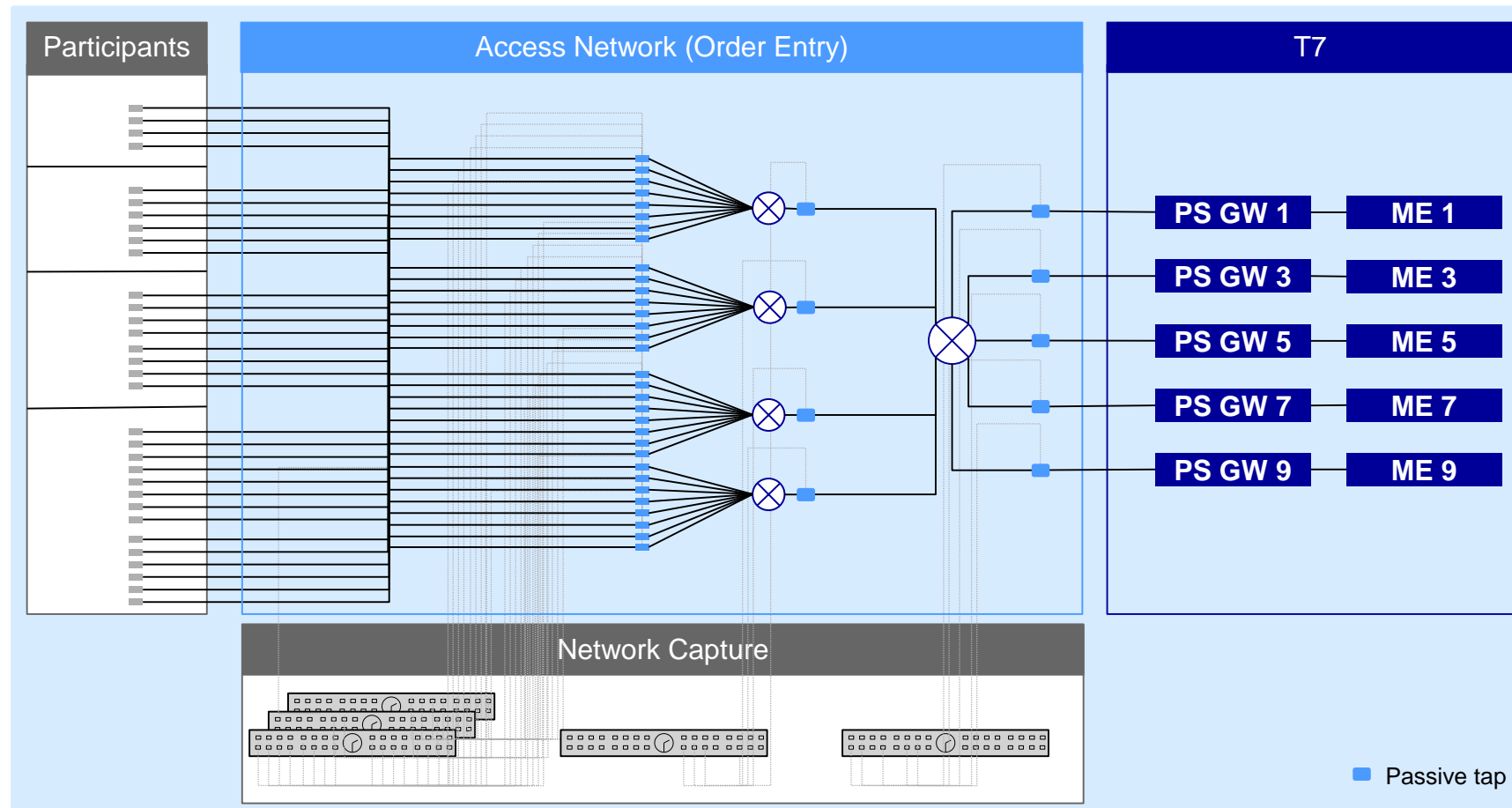
# T7<sup>®</sup> Co-location Timestamps



- Timestamps provided in T7 API (real-time) in dark blue ( $t_{3n}$ : taken by network card, other: application level)
- Network timestamps taken using taps & timestamping switches
- Timestamps possibly taken by participants are shown in grey

## T7<sup>®</sup> Co-location

Scale (> 500 capture ports, > 60 timestamping devices)



> 260 Order Entry lines captured (> 500 capture ports)

Identical setup regardless of participant room location and assigned access switch

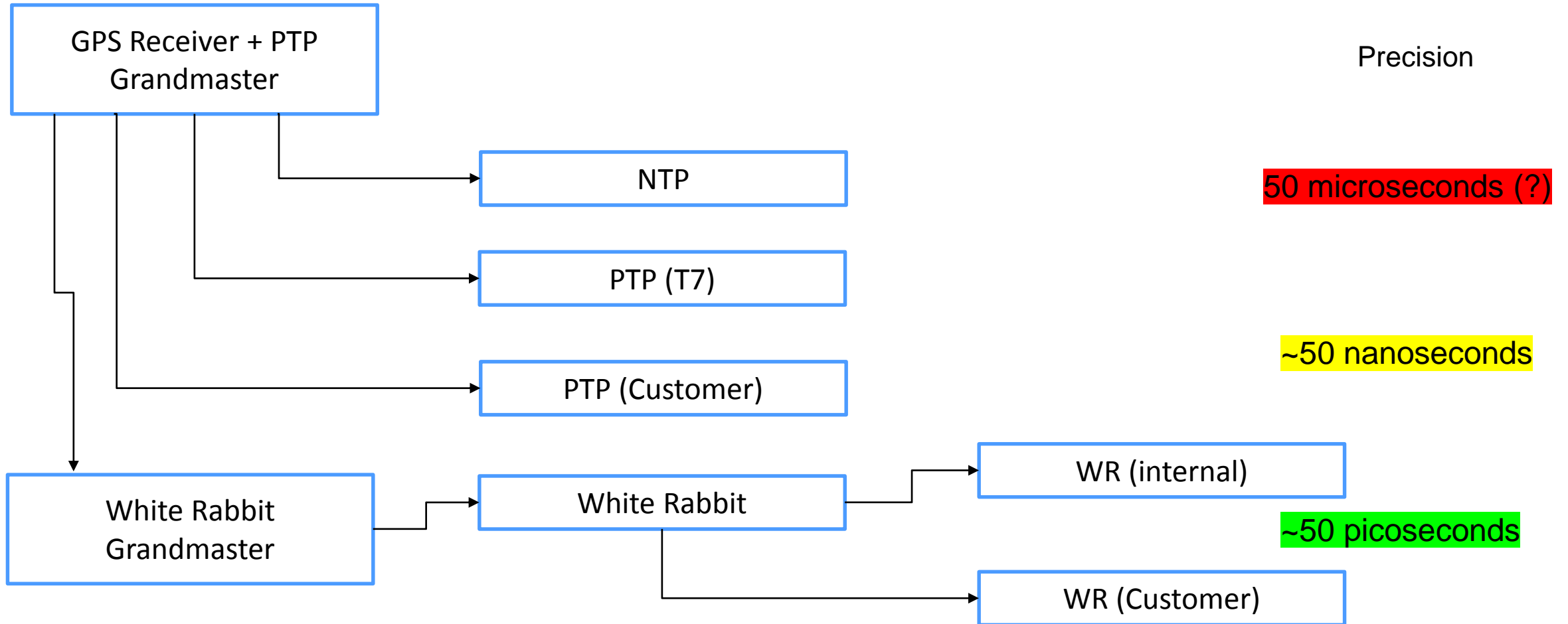
# 23

## Time Distribution in T7

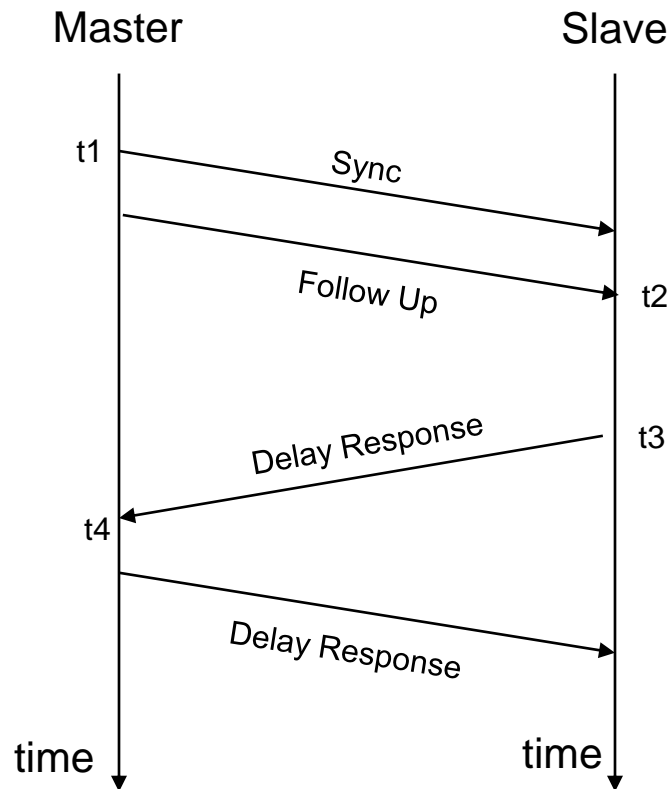




# Time Distribution in T7



# PTP v2 aka IEEE 1588-2008



- Slave has to know its offset from master (one-way delay)
- Calculates this with 4 timestamps

$$\text{Path Delay} = ((t4 - t1) - (t3 - t2)) / 2$$

$$\text{Offset from Master} = (t2 - t1) - \text{Path Delay}$$

- Works best on dedicated network
- Requires network path symmetry
- BMCA Best Master Clock Algorithm to select grandmaster

# PTP v2 aka IEEE 1588-2008

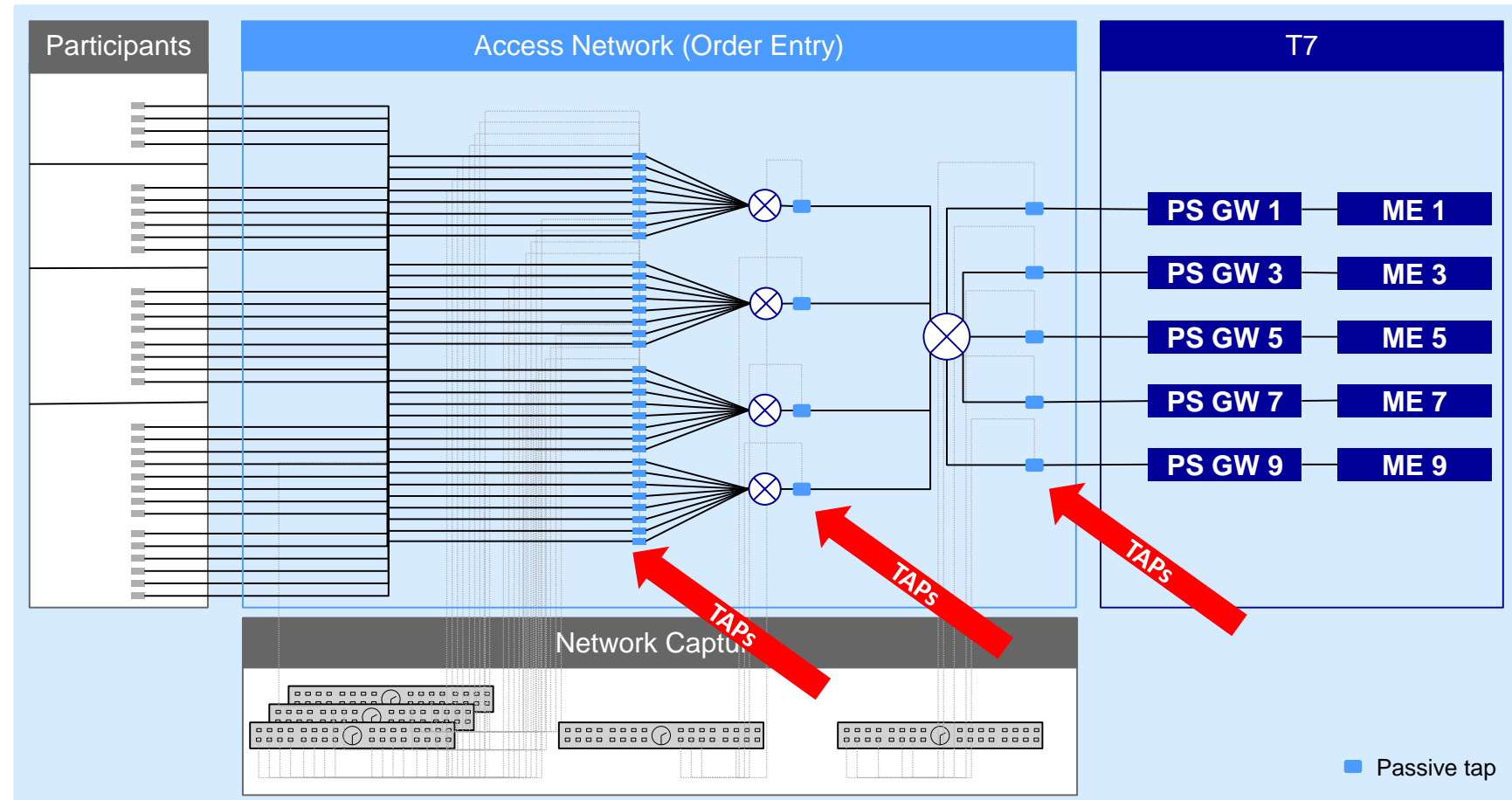
## PTP Precision in Practice



## Problem Statement – Why PTP is not good enough

How to capture and timestamp all customer cross-connects in co-location?

- 500+ capture ports
- 60+ capture devices
- 4 datacentre modules
- PTP +/- 50ns jitter in our infrastructure at best
- Serialization time of order entry message = 120ns
- Goal of sub-10ns precision
- Distances too long for PPS over coax cables



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White Rabbit at  
Deutsche Börse



## White Rabbit



## The White Rabbit Project



White Rabbit is a fully deterministic Ethernet-based network for general purpose data transfer and synchronization. It can synchronise over 1000 nodes with sub-ns accuracy over fibre lengths of up to 10 km.

White Rabbit provides **sub-nanosecond accuracy** and **picoseconds precision** of synchronisation for large distributed systems. It also allows for deterministic and reliable data delivery. White Rabbit allows you to precision time-tag measured data and lets you trigger data taking in large installations while at the same time using the same network to transmit data.

<http://white-rabbit.web.cern.ch>

<http://www.ohwr.org/projects/white-rabbit/wiki>

Used by CERN (Switzerland), GSI (Germany), Nikhef (Netherlands), and many more ...

# White Rabbit

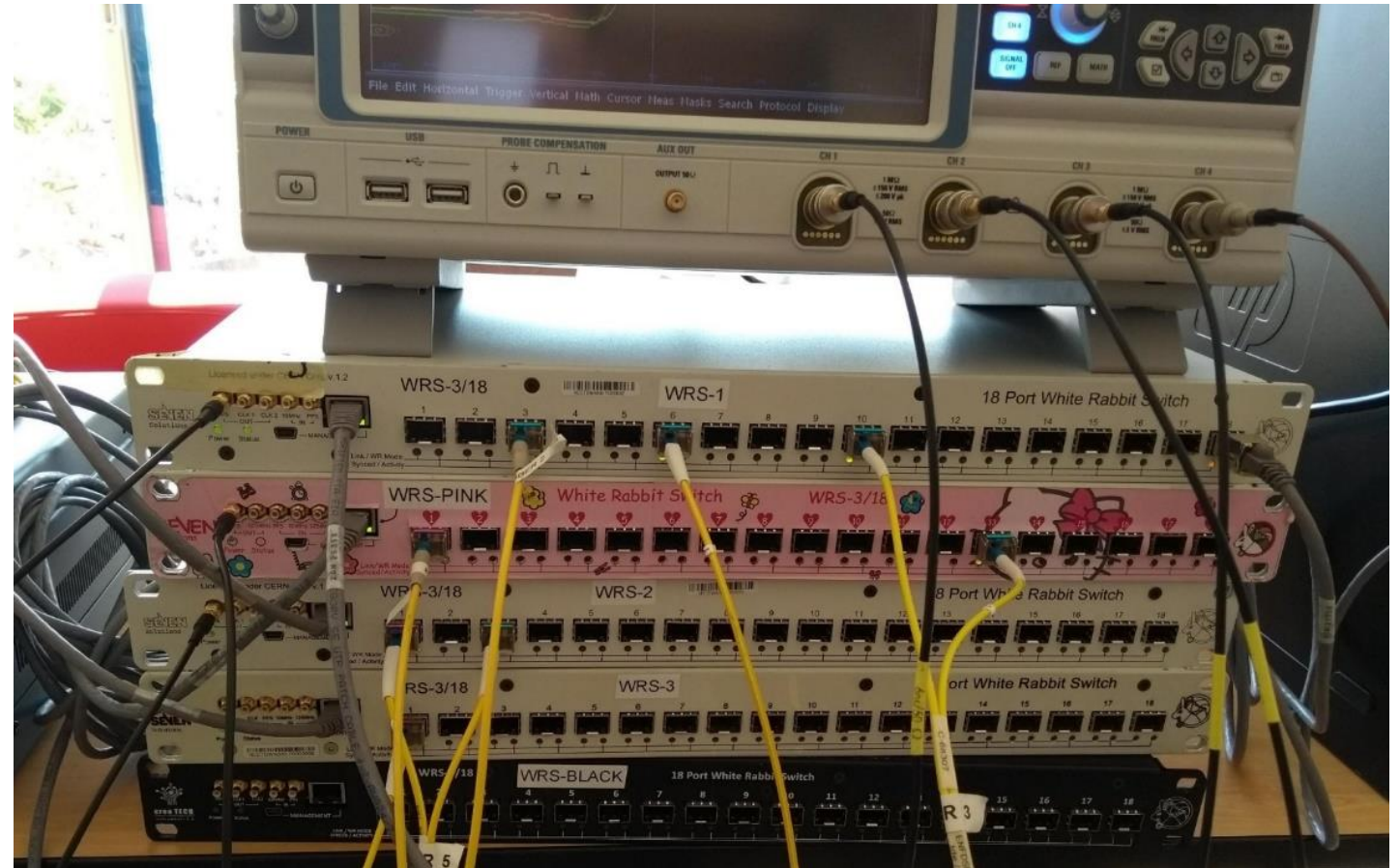
- Came out of the University of Warsaw
- Developed at CERN
- Provides sub-nanosecond accuracy and picoseconds precision of synchronization
- Tried and tested
- PTP over Synchronous Ethernet
- “High Accuracy” profile of the PTP standard IEEE1588-2019
- Commercially available (except the Hello Kitty model)

Issue for us:

No native White Rabbit support in NICs and switches

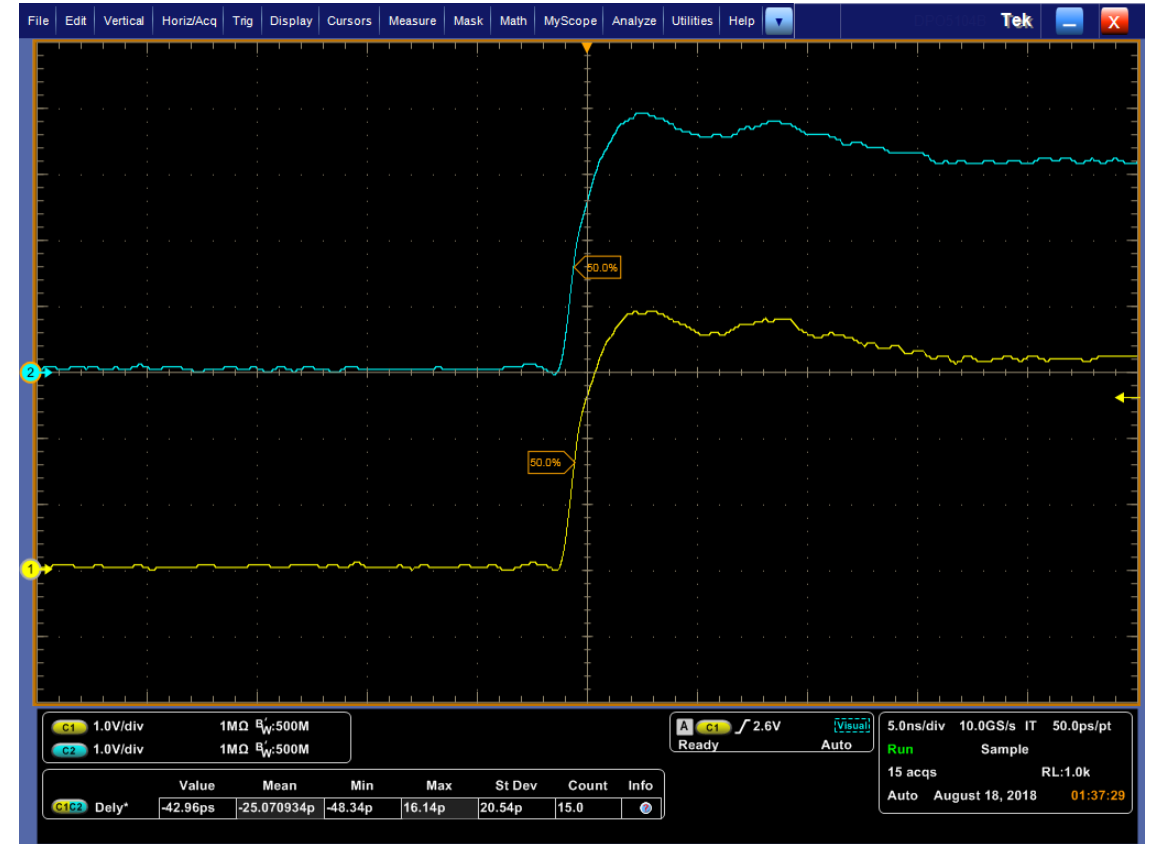
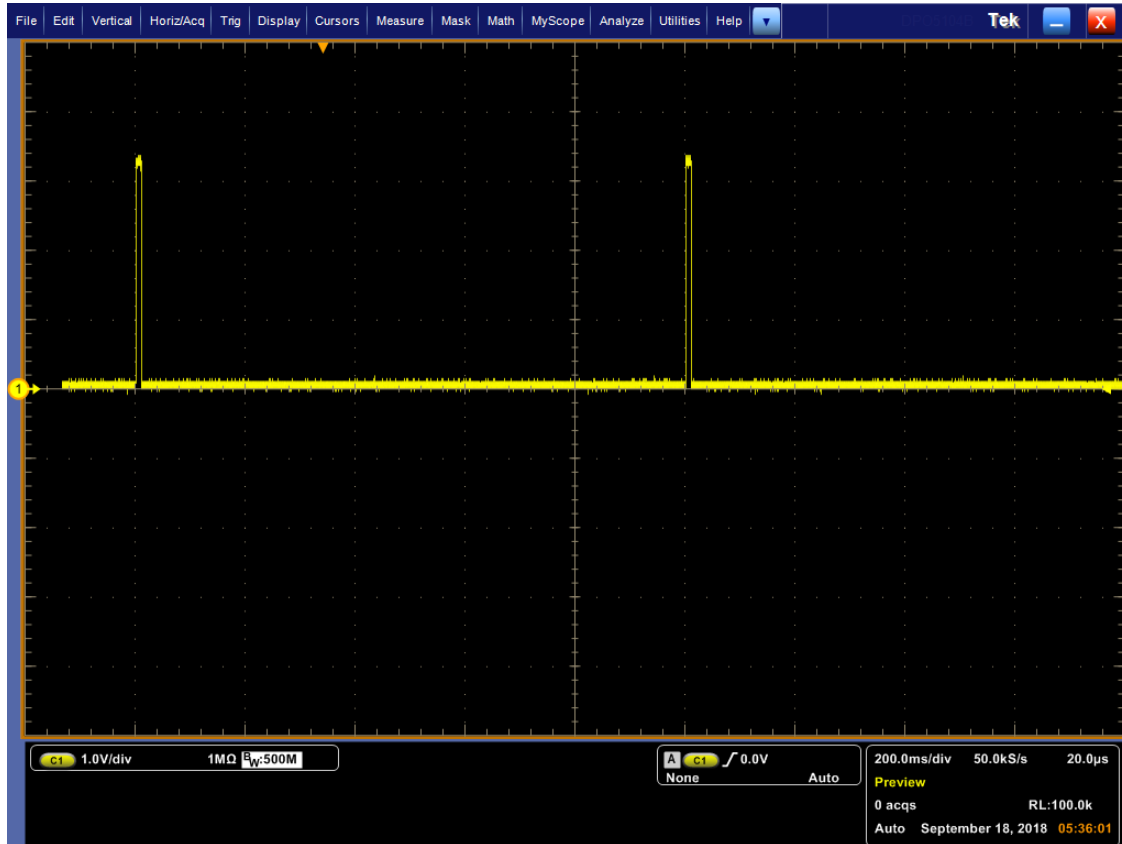
Solution:

We use White Rabbit to distribute 1PPS



# White Rabbit

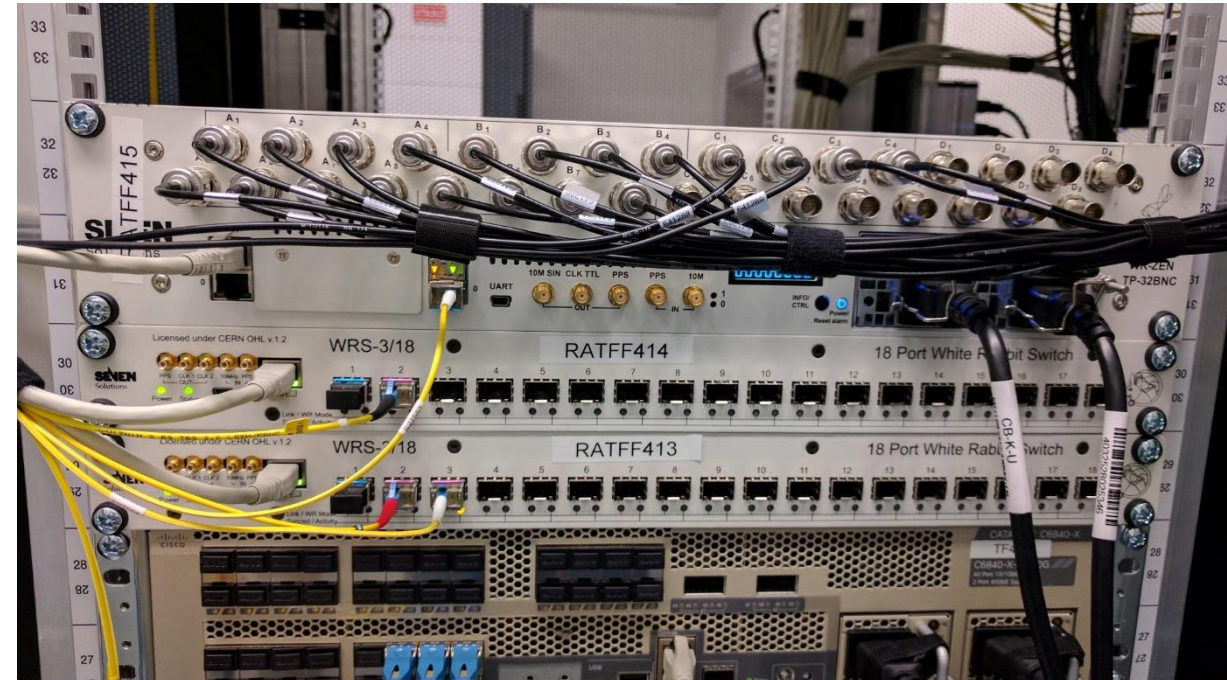
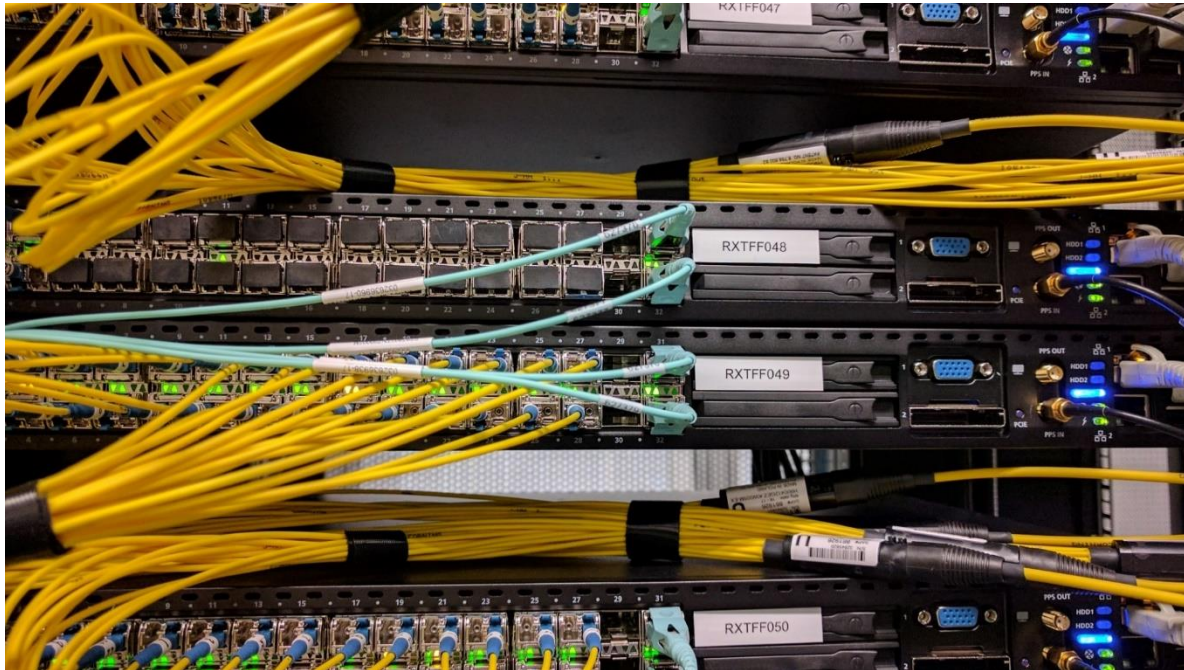
## What is PPS?





# White Rabbit deployed hardware

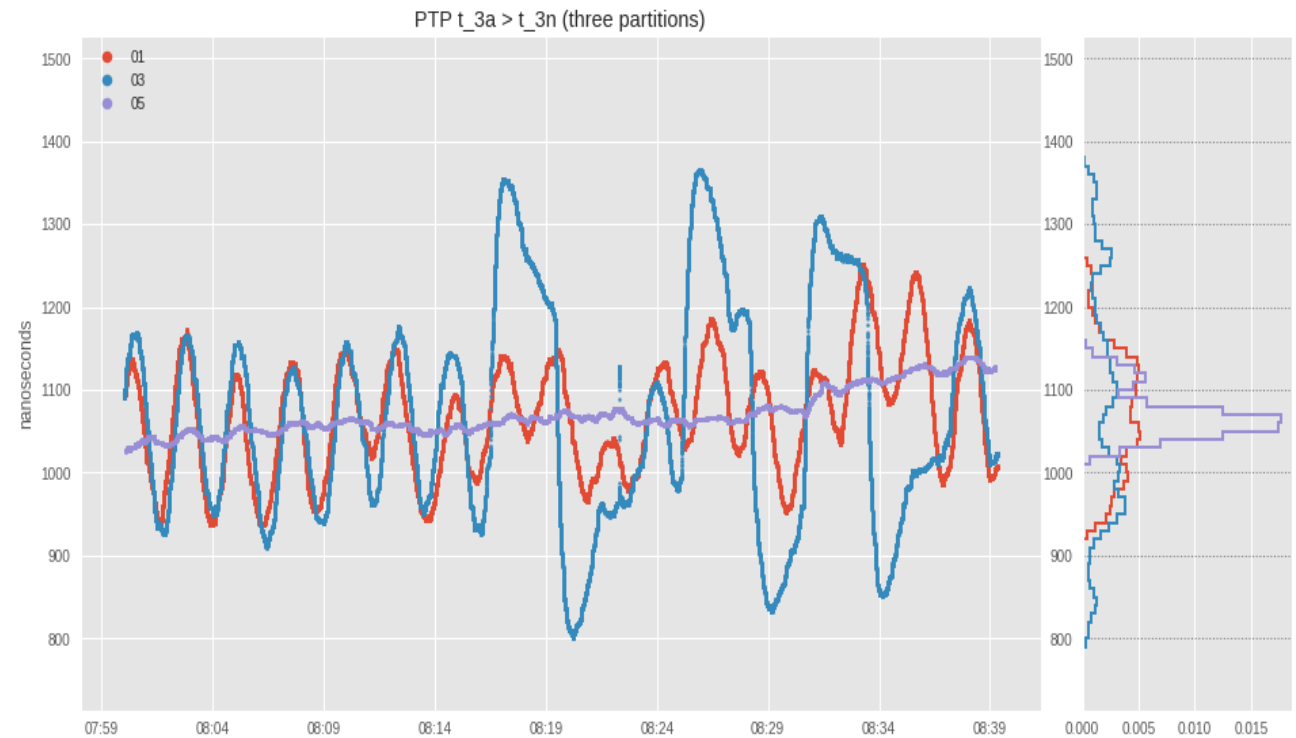
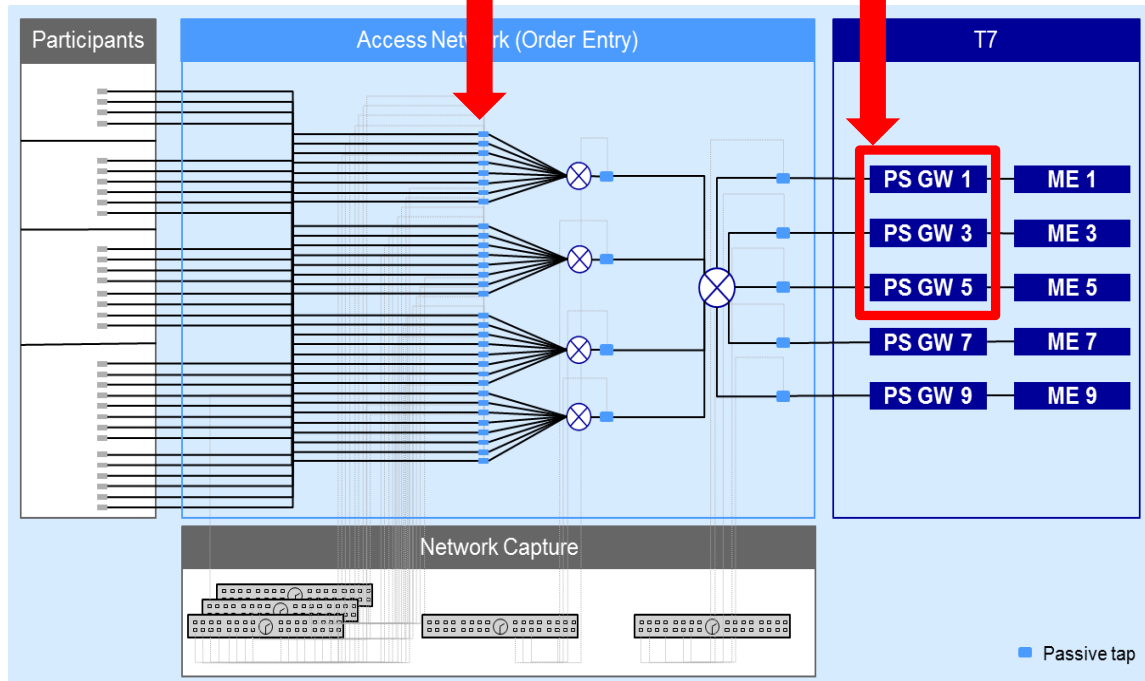
Timestamping devices synchronized by 1PPS over White Rabbit



# Time Synchronisation

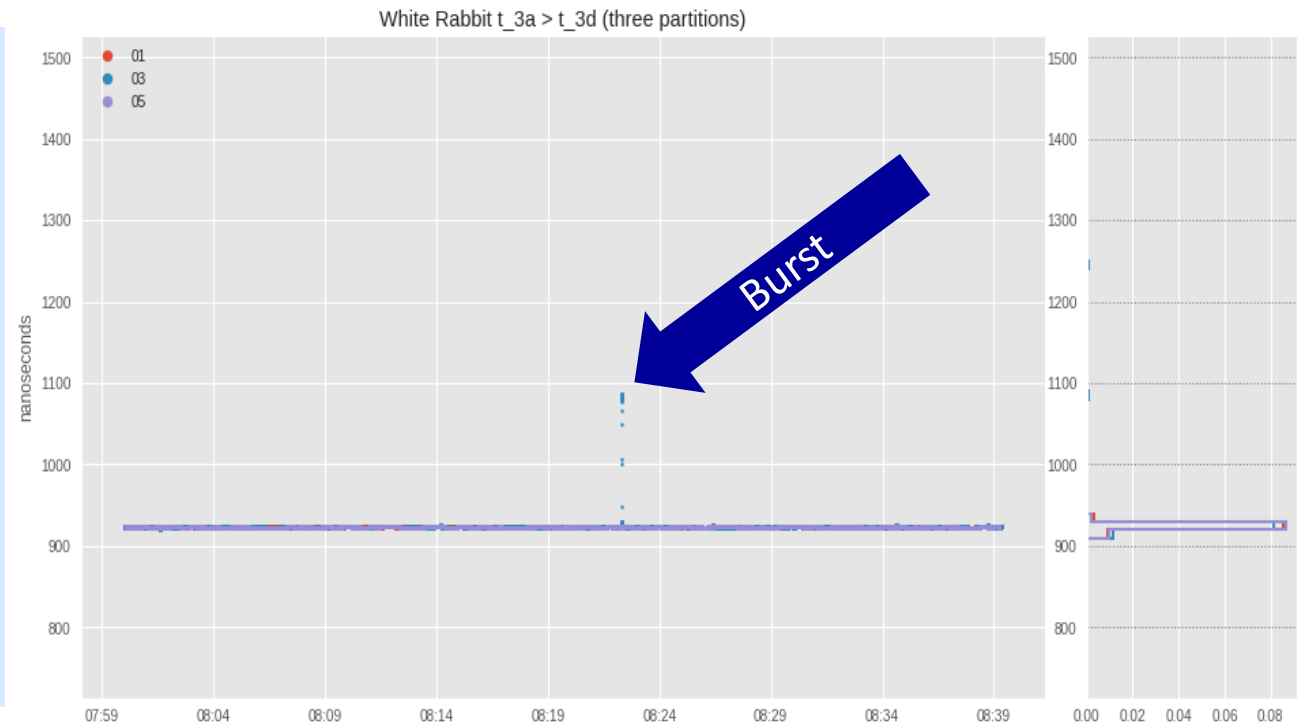
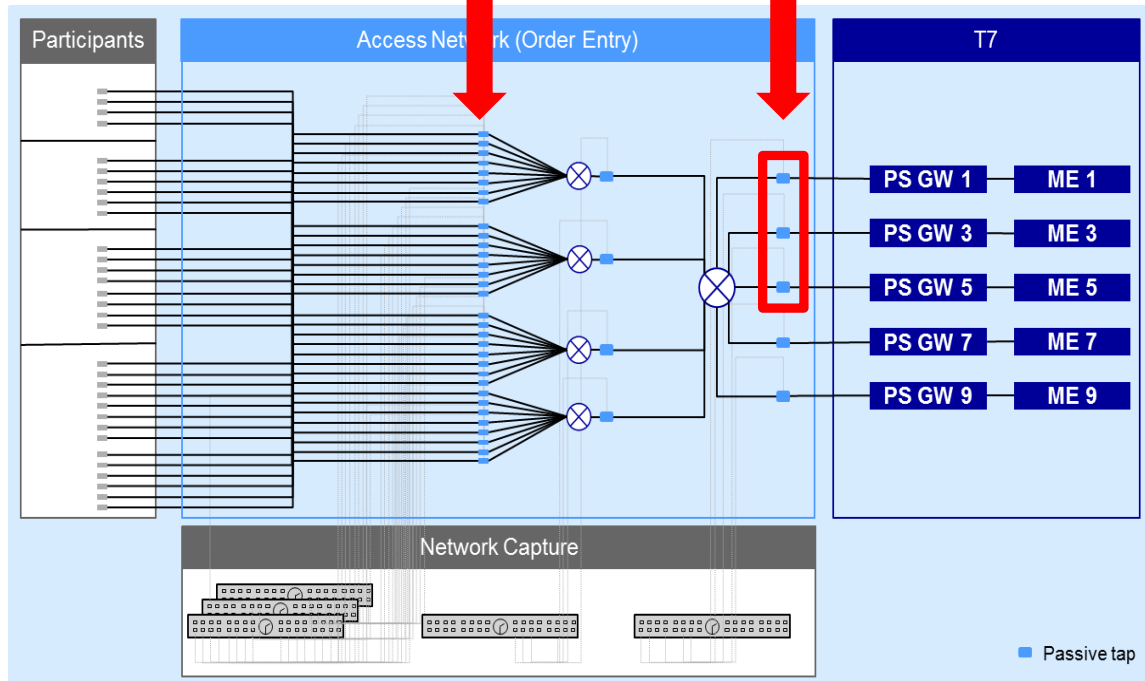
## PTP

t<sub>3a</sub> (WR)      t<sub>3n</sub> (PTP)



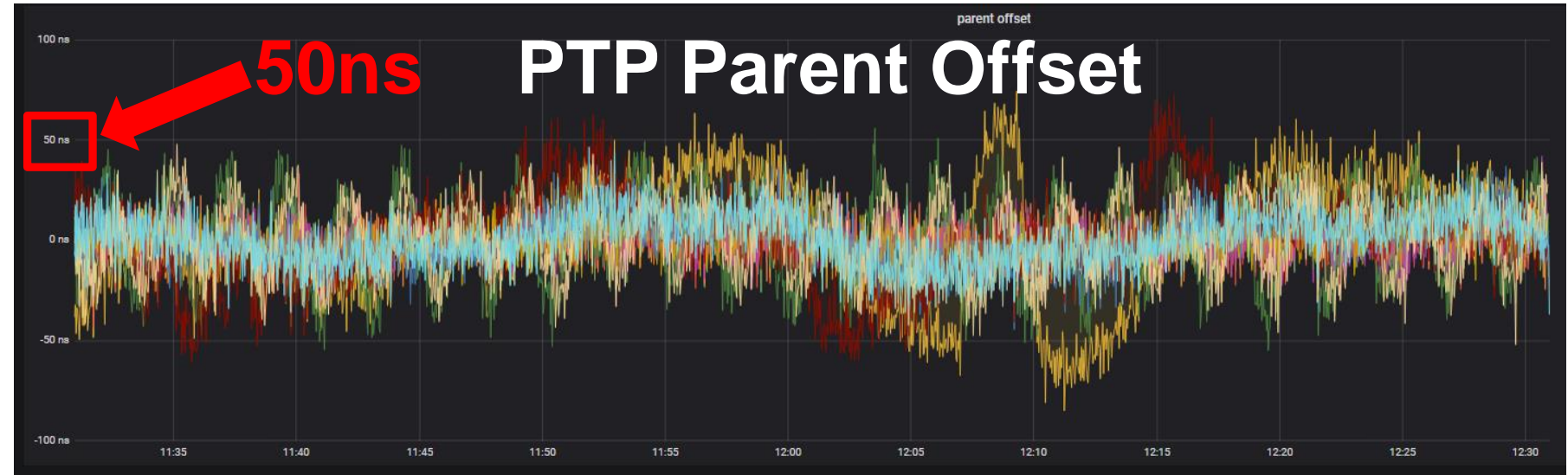
# Time Synchronisation White Rabbit

t\_3a (WR)      t\_3d (WR)

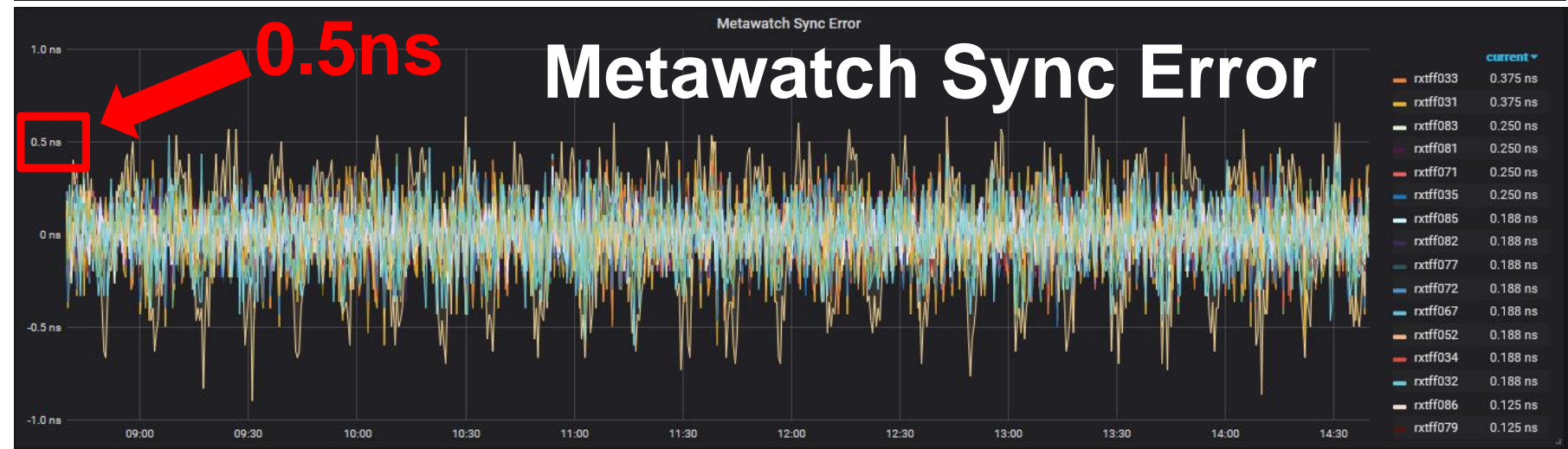


# PTP vs White Rabbit

PTP



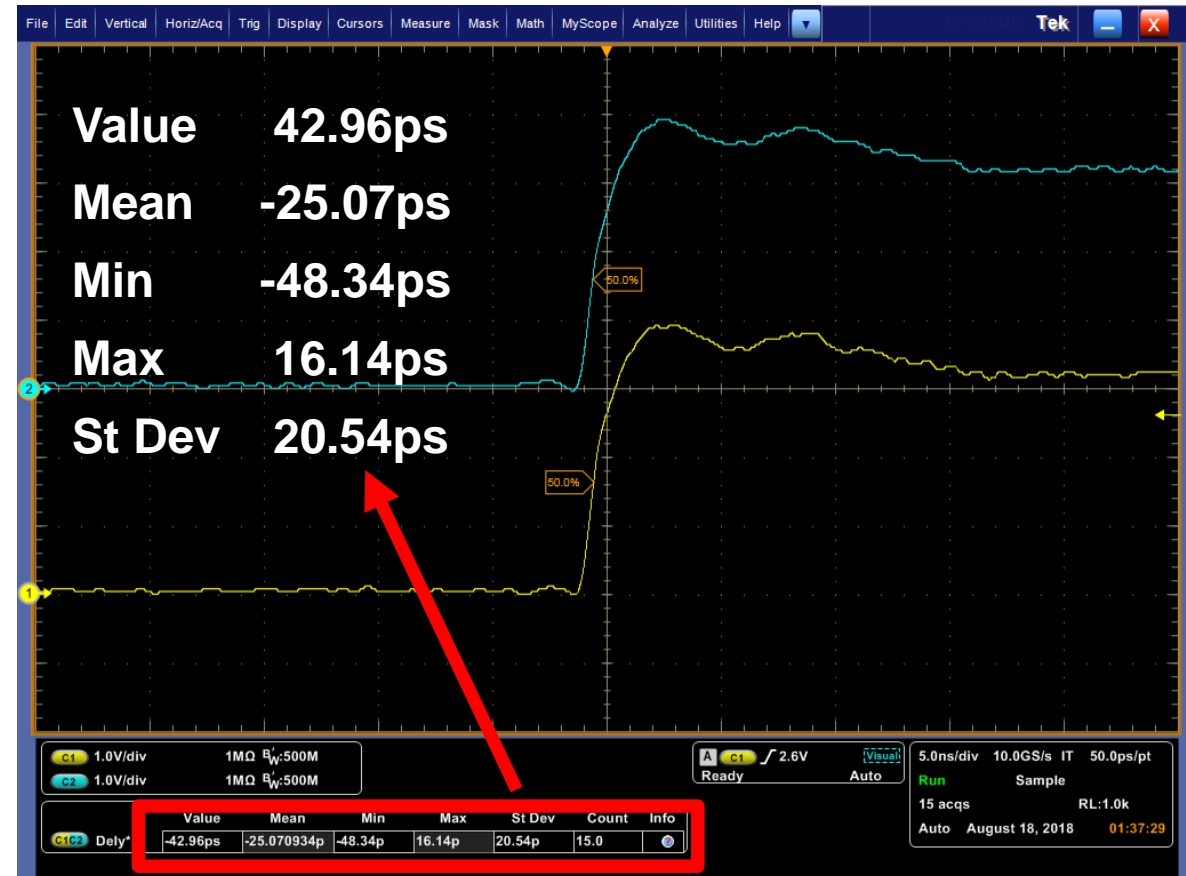
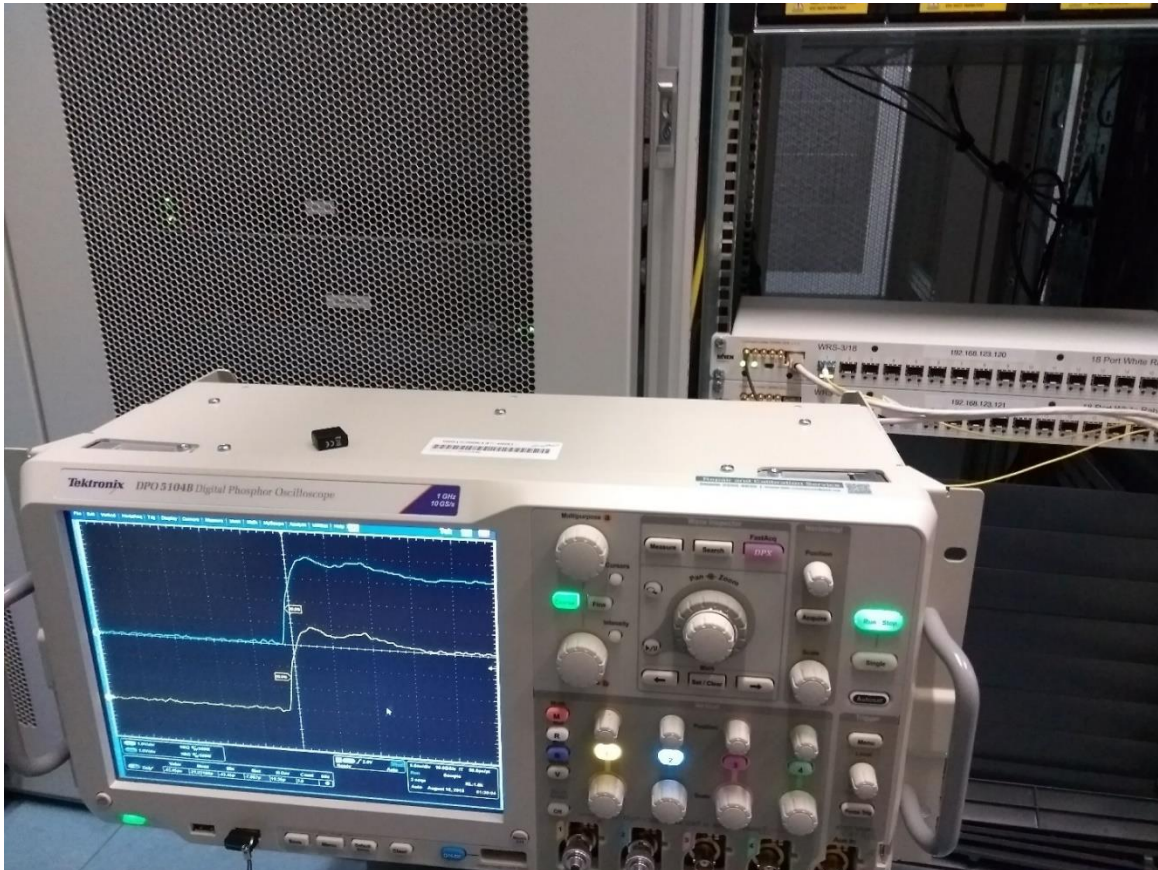
White Rabbit



# White Rabbit Services for our Trading Customers

Launched two WR based services

1. High-Precision Timestamp (HPT) File (more in a moment)
2. High Precision Time Service (connect to our WR network)



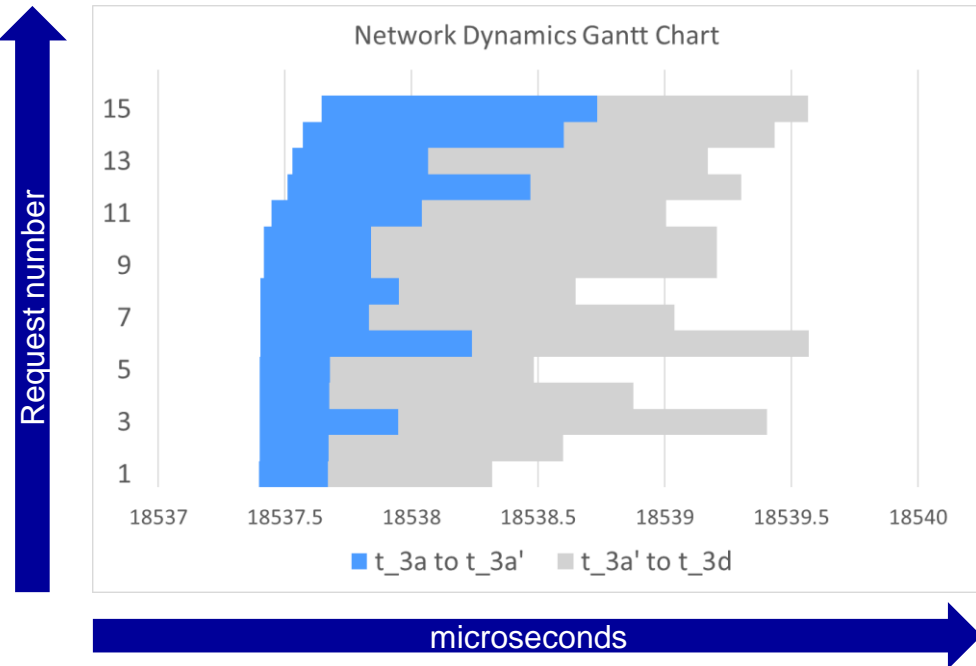
# Precise Timestamping

## Burst Analysis

Networking at our exchange is characterised by bursts

The most frequently asked question:

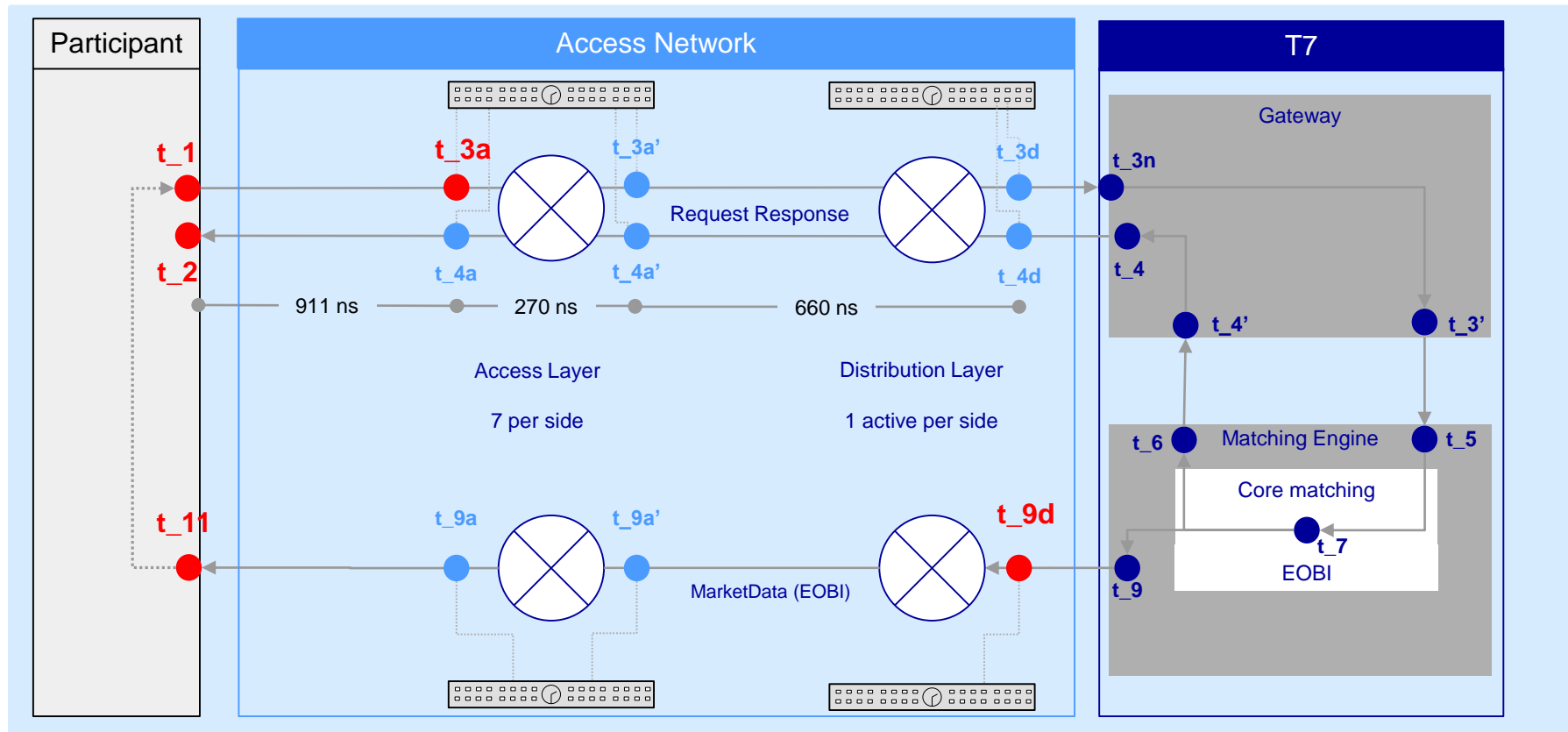
How far behind am I, really?



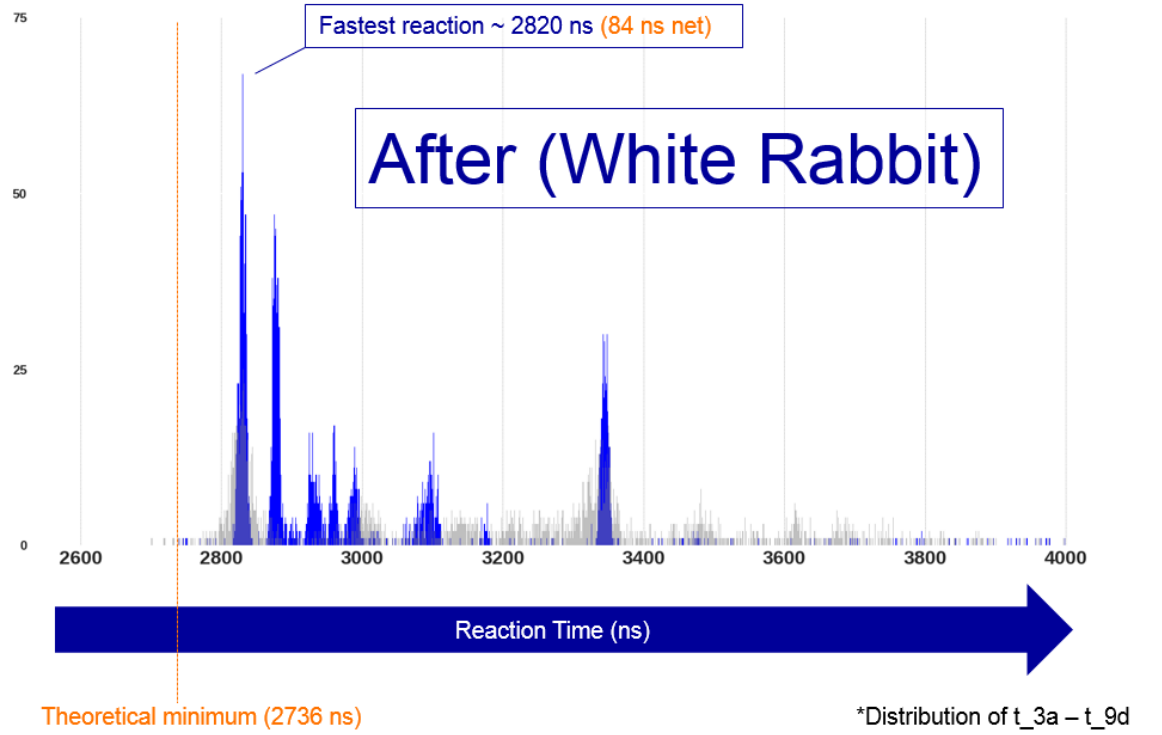
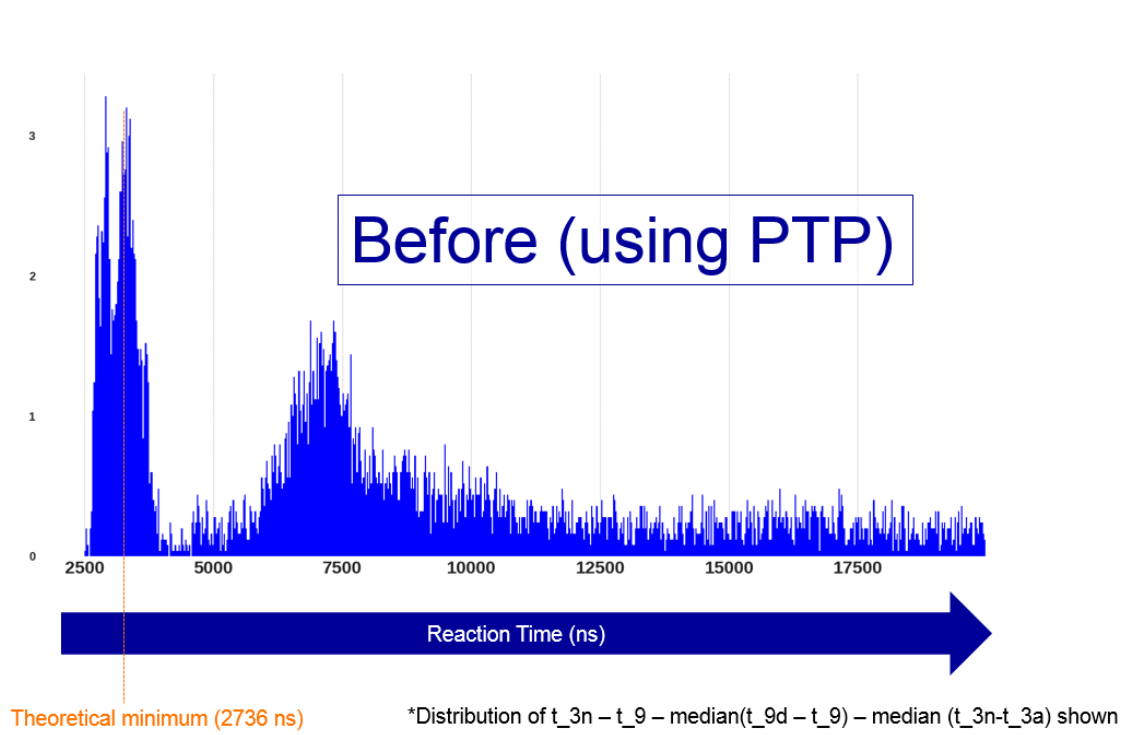
	t_3a (Access In)	t_3a' (Access Out)	t_3a to t_3a'	t_3a' to t_3d	delta.t3a	delta.t3a'	delta.t3d
1	11:05:00.018537384	11:05:00.018537659	275	650			
2	11:05:00.018537398	11:05:00.018537669	271	650	170	14	-4
3	11:05:00.018537399	11:05:00.018537672	273	925	206	1	2
4	11:05:00.018537399	11:05:00.018537947	548	1456	212	0	275
5	11:05:00.018537400	11:05:00.018537676	276	1199	204	1	-272
6	11:05:00.018537401	11:05:00.018537678	277	804	157	1	1
7	11:05:00.018537402	11:05:00.018538237	835	1332	224	1	558
8	11:05:00.018537403	11:05:00.018537832	429	1206	219	1	-406
9	11:05:00.018537404	11:05:00.018537950	546	698	169	1	117
10	11:05:00.018537416	11:05:00.018537839	423	1366	202	12	-123
11	11:05:00.018537416	11:05:00.018537839	423	1366	202	0	0
12	11:05:00.018537446	11:05:00.018538041	595	963	179	30	172
13	11:05:00.018537510	11:05:00.018538468	958	833	150	64	363
14	11:05:00.018537529	11:05:00.018538066	537	1104	161	19	-421
15	11:05:00.018537571	11:05:00.018538602	1031	833	166	42	494
16	11:05:00.018537644	11:05:00.018538734	1090	832	153	73	59
17	11:05:00.018581841	11:05:00.018582110	269	651	156	44197	-821

# High Precision Timestamp File

## For Modeling and Precision Latency Analysis



# High Precision Timestamp File





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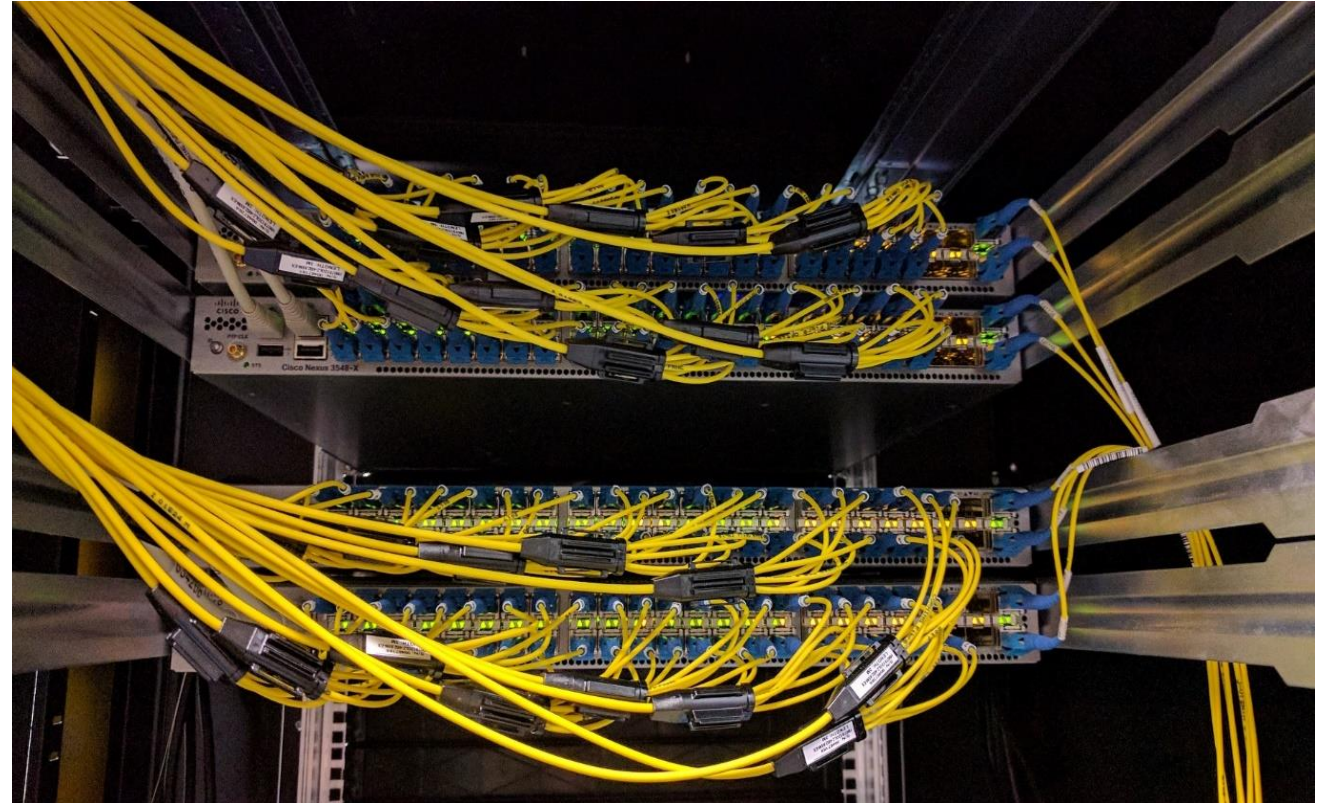
## Market Data Distribution



# Market Data Distribution

## UDP Multicast using a Cisco 3548-X

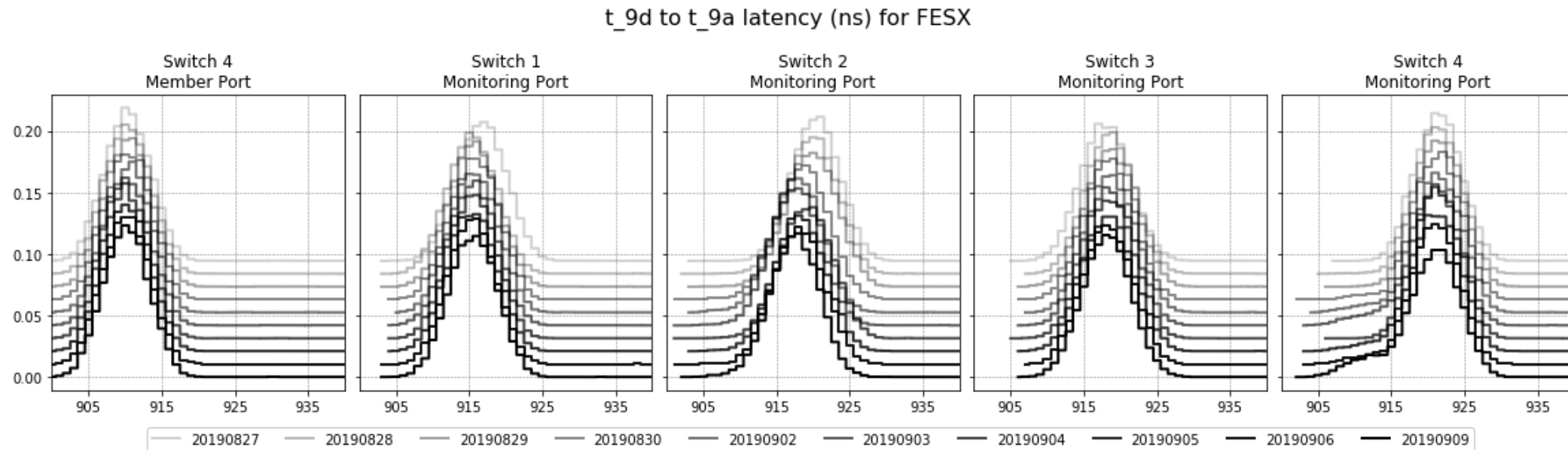
- ASIC designed in 2010
- Introduced in 2011
- Fully featured, low-latency switch which is popular in financial markets
- Cut-through
- ~200ns latency



# Market Data Distribution

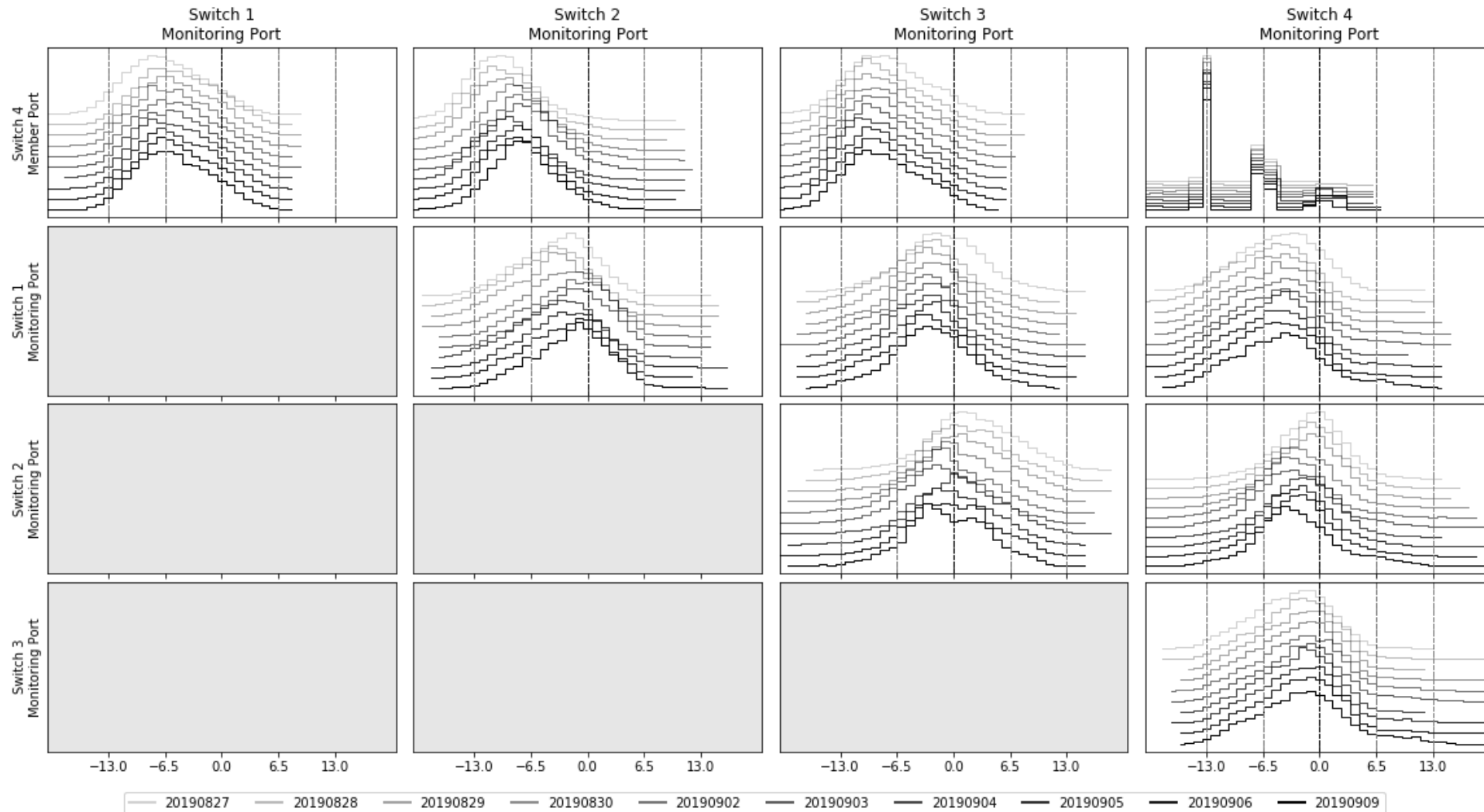
## Effects

- Jitter from one packet to the next  $\approx 15\text{-}20\text{ns}$
- Some ports show a static offset  $\approx 7\text{-}8\text{ns}$  (leftmost graph)
- The static offset is not caused by cable length differences
- The offset appears to depend on the multicast group subscription lists of a) the port under consideration and b) other ports on the same switch
- Analysis of this effect still ongoing



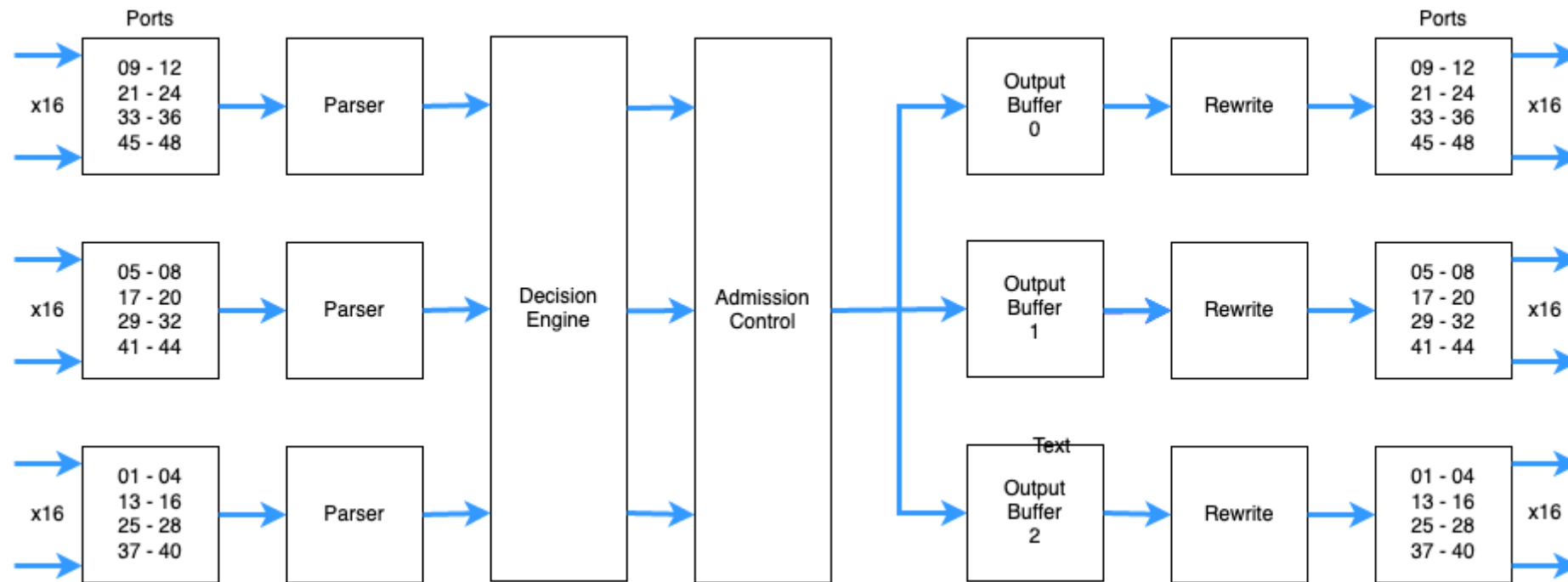
# Market Data Distribution Effects

Port to port latencies for FESX Market Data



# Market Data Distribution

## Monticello ASIC Block Diagram





Thank you for your attention

Contact

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**Sebastian Neusüß**

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Phone +49 69 2111 8686



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Appendix

# Matching Algorithms

## Measures to Reduce Need for Speed

### Actual

- Various “Speed Bumps”
  - Magic shoe box = long box of coiled up cable
  - “Latency floor”
  
- Passive Liquidity Protection on Eurex
  - New orders that could match with resting orders in the limit order book will be deferred
  - Pilot phase launched German (1ms delay) and French (3ms delay) equity options
  
- Last Look
  - Liquidity provider has additional time to decide whether to accept a trade or not
  - Used in foreign exchange markets (currencies)



# Matching Algorithms

## Measures to Reduce Need for Speed

### Proposals

- Frequent Batch Auctions
  - <https://faculty.chicagobooth.edu/eric.budish/research/HFT-FrequentBatchAuctions.pdf>

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