

## Homework #4

Due: Fri, May-02-2025, 11:59pm – Gradescope entry code: R57ZN7

Please upload your answers timely to Gradescope. Start a new page for every problem. We strongly suggest LaTeX to type your answers. For the programming/simulation questions you can use any reasonable programming language (please no assembly, brainfuck, etc. ☺). Comment your source code and include the code and a brief overall explanation with your answers. A tentative point distribution (in % of the total) is provided in brackets. For most problems there is more than one valid way of solving them!

1. In this question, we consider a version of Tendermint, where the nodes, having acquired a lock, never release that lock. Suppose there are  $f$  adversarial nodes (Byzantine adversary) and  $n = 3f + 1$  nodes in total, and the quorum size is  $q = 2f + 1$ . We denote a client by the letter  $c$ , honest nodes by  $v_1^h, v_2^h, \dots, v_{2f+1}^h$ , and the adversarial nodes by  $v_1^a, \dots, v_f^a$  (the clients and honest nodes do not know which nodes are honest or adversarial). This version of Tendermint (just like the original Tendermint protocol) attempts to confirm a single block per height. Within each height  $h$ , it proceeds in *rounds*, each with a unique, known leader that proposes a block. Each of these round attempts to confirm a block for the height  $h$ .

At each round  $r$ , each honest node keeps track of the *stage* of the protocol within the round. It can be one of proposal, pre-vote, or pre-commit. Each stage lasts  $\Delta$  time, and thus, each round lasts  $3\Delta$  time.

At the beginning of the proposal stage (time  $t = 0$ ), an honest leader proposes a round- $r$  block. At the beginning of the pre-vote stage (time  $t = \Delta$ ), each honest node sends a round- $r$  pre-vote for the first round- $r$  block it observes. If an honest node does not observe a round- $r$  block, it sends a round- $r$  pre-vote for a special *nil* (empty) value. At the beginning of the pre-commit stage (time  $t = 2\Delta$ ), each honest node sends a round- $r$  pre-commit for the round- $r$  block, for which it has first observed  $2f + 1$  round- $r$  pre-votes by distinct nodes. If an honest node does not observe  $2f + 1$  pre-votes for any round- $r$  block, it sends a round- $r$  pre-commit for a special *nil* value. At the end of the round ( $t = 3\Delta$ ) or later, if an honest node observes  $2f + 1$  round- $r$  pre-commits for  $B$ , it confirms  $B$  for its height ( $h$ ), and terminates the protocol for height  $h$ . Otherwise, it goes into the next round  $r + 1$ .

A client  $c$  confirms a round- $r$  block  $B$ , if it observes (at any time)  $2f + 1$  round- $r$  pre-commits for  $B$  by distinct nodes. In that case, we say that the round- $r$  block  $B$  became confirmed by the round- $r$  pre-commits.

An honest node locks on a round- $r$  block  $B$  at round  $r$  upon sending a round- $r$  pre-

commit for  $B$ . In future rounds, the node does not send pre-votes for other blocks  $B' \neq B$ . If it is elected as a leader in a future round, it proposes the same block it is locked on.

- a) (%10) Draw the time-line for an execution of the protocol that lasts for two rounds, illustrating all the stages it has gone through.
- b) (%10) We first explore if this version of Tendermint is safe. Suppose two different blocks  $B$  and  $B'$  are proposed for the *same* round  $r$ . Is it possible for one client  $c$  to confirm  $B$ , while another client  $c'$  confirms  $B'$ ? (Here,  $c$  and  $c'$  can also be the same client.)
- c) (%10) Suppose a client  $c$  confirms a block  $B$  proposed for round  $r$ . Does this say anything about how many honest nodes must have locked on  $B$  at round  $r$ ?
- d) (%10) Now, suppose two different blocks  $B$  and  $B'$  are proposed for *different* rounds  $r$  and  $r' > r$  respectively. Is it possible for one client  $c$  to confirm  $B$ , proposed for round  $r$ , while another client  $c'$  confirms  $B'$ , proposed for round  $r'$ ? (Here,  $c$  and  $c'$  can also be the same client.)
- e) (%10) Is this protocol safe? If so, prove safety referring to the parts above. If not, describe an attack on safety referring to these parts.
- f) (%10) We next explore if the protocol is live. First, suppose at round 1, the leader is honest. Will a block become confirmed?
- g) (%10) Now suppose at some round  $r$ , there is an adversarial leader, which proposes a block  $B_1$ , but it initially shows  $B_1$  to only the  $f + 1$  honest nodes  $v_1^h, \dots, v_{f+1}^h$ , right before the pre-vote deadline. As a result, out of the  $2f + 1$  nodes, only these  $f + 1$  honest nodes send round- $r$  pre-votes for  $B_1$ . Now, right before the pre-commit deadline, the adversary shows  $f$  round- $r$  pre-votes for  $B_1$  by the adversarial nodes  $v_1^a, \dots, v_f^a$ , *only* to a single honest node,  $v_1^h$ . In this case, does block  $B_1$  become confirmed by the round- $r$  pre-commits? Which honest nodes send round- $r$  pre-commits for  $B_1$ ? Which honest nodes lock on  $B_1$  at round  $r$ ?
- h) (%10) At round  $r + 1$ , the honest node  $v_2^h$  becomes the leader and proposes a block  $B_2 \neq B_1$ . The adversarial nodes do not send any pre-votes or pre-commits at round  $r + 1$ . Does  $B_2$  become confirmed by the round- $(r + 1)$  pre-commits? Which honest nodes send round- $(r + 1)$  pre-votes for  $B_2$ ? Which honest nodes send round- $(r + 1)$  pre-commits for  $B_2$ ? Which honest nodes lock on  $B_2$  at round  $r + 1$ ?
- i) (%10) Now, suppose that instead of remaining silent, the adversary shows a single round- $(r + 1)$  pre-vote (by an adversarial node) for  $B_2$  to a single honest node,  $v_2^h$ , right before the pre-commit stage starts. Does  $B_2$  become confirmed by the round- $(r + 1)$  pre-commits? Which honest nodes send round- $(r + 1)$  pre-votes for  $B_2$ ? Which honest nodes send round- $(r + 1)$  pre-commits for  $B_2$ ? Which honest nodes lock on  $B_2$  at round  $r + 1$ ?
- j) (%10) Suppose the adversary remains silent after round  $r + 1$ . Is this protocol

live? If so, prove liveness referring to the parts above. If not, describe an attack on liveness referring to these parts.