

# Continuum deformation and stability analyses of a steep hillside slope under rainfall infiltration

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**Abstract** Rainfall weakens an earth slope in a number of ways. It increases the degree of saturation of the soil, thereby breaking the bonds created by surface tension between the soil particles. When the volume of infiltrating water is large enough to mobilize fluid flow inside the soil matrix, the fluid exerts a downhill frictional drag on the slope, creating a destabilizing effect. When excess fluid can no longer infiltrate the slope due to increased saturation in the soil, it is discharged as a surface runoff and erodes the slope. In this paper, we present a physics-based framework for continuum modeling of a hydrologically driven slope failure similar to what occurred in a steep experimental catchment CB1 near Coos Bay, Oregon. We quantify the rainfall-induced slope deformation and assess the failure potential of the slope using finite element modeling that couples solid deformation with fluid pressure in an unsaturated soil. Results of the studies suggest that for a steep hillside slope underlain by a shallow bedrock similar to the CB1 site, failure would occur by multiple slide blocks with the failure surfaces emerging on the slope face. These results suggest that an infinite slope mechanism would be insufficient to represent the failure kinematics for a slope similar to CB1.

**Keywords** Coupled formulation · Rainfall infiltration · Slope stability · Stabilized finite elements · Unsaturated soil

## 1 Introduction

Hydrologically driven slope instability threatens lives and property worldwide. Examples of large-scale slope failure all over the world are numerous. Landslides in the San Francisco Bay Area during the January 1982 storm resulted in 24 fatalities and millions of dollars in property damage [18, 61]. In January 4, 1982, a 0.22-m storm superimposed on approximately 0.6 m of pre-storm seasonal rainfall triggered thousands of landslides in the central Coast Ranges of California. In Mameyes, Puerto Rico, 1985, rainfall intensity as high as 0.56 m within a 24-h period, with rates as high as 70 mm/h, triggered debris flows and resulted in 129 deaths [31]. In Rio Limón, Venezuela, 1987, rainfall as much as 0.174 m in less than 5 h triggered numerous shallow landslides and debris flows resulting in 210 deaths [58]. In Antofagasta, Chile, 1991, rainfall rates as great as 60 mm/h during a 3-h period triggered landslides that resulted in 101 deaths [66]. In Vargas, Venezuela, 1999, a heavy rainfall exceeding 0.9 m over a 3-day period, with daily values greater than the 1,000-year return period [41], triggered thousands of landslides and resulted in an estimated 30,000 deaths [65]. And in 2006, a heavy rainfall in Guinsaugon, Philippines, triggered massive landslides burying an elementary school that had 246 students and 7 teachers [37].

Despite decades of extensive slope-stability model development, the fundamental controls connecting the hydrologic and geotechnical processes triggering slope failure are still not well quantified. This is evident from the La Conchita landslide of January 11, 2005, in southern California that occurred without warning. This lack of understanding is a direct result of the simplified physics in current models, with the omission of the effect of partial saturation from slope-stability calculations. It is known that

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increasing the degree of saturation decreases the capillary pressure, which in turn weakens the slope. Moreover, fluid flow generates frictional drag on the soil matrix, thus increasing the load that the soil is expected to carry. Despite the expected significant impact, such interplay between the increase in saturation accompanied by fluid flow and increase in potential for slope failure is yet to be fully quantified.

Rainfall-triggered slope instability has been the subject of intense research for many years. Several studies are available concerning field observations and laboratory experiments (e.g., [47]). The modeling of the slope failure process has been addressed in a variety of ways over the years. The most common approach is to uncouple the fluid flow and slope-stability problems, and instead treat them in a sequential fashion. First, a representative pore-pressure field is determined using either field-observations, analytical solutions, or numerical methods. The fixed pore-pressure field is then used to determine slope stability either analytically or numerically. Among these uncoupled methods, the most common treatment of the slope-stability sub-problem is through a limit equilibrium approach. For example, see [29, 59] where infinite slope approximations are used, and [17] where a simplified Janbu method of slices is used. In [35, 49], a finite element solution for the transient sub-surface seepage is combined with a method of slices to determine a slope's factor of safety. The key advantage of these methods is their simplicity. Because the solid and fluid sub-problems are uncoupled, sophisticated methods and software that have been developed over the years for the separate problems can be brought together. These models also have relatively few parameters to calibrate, and solutions can be computed inexpensively. Furthermore, it is easy to compute parameter sensitivities and understand basic trends in the slope failure process. On the downside, these models make many simplifying assumptions about the slope geometry, the coupled nature of the failure process, the constitutive behavior of the soil, and the in situ stress conditions.

In this paper, we develop and test a 3D physics-based slope deformation model that couples solid deformation with fluid flow in variably soils. We also assess the potential of the coupled model to realistically quantify stresses and deformation necessary to trigger slope failure. We emphasize the continuum nature of the modeling approach in that it does not quantify the factor of safety of the slope per se, unlike methods based on limit equilibrium concepts. Instead, our model predicts the spatial and temporal variations of internal stresses, pore water pressure, degree of saturation, and deformation within the slope, as functions of the spatially and temporally varying rainfall intensity. Thus, instead of having one scalar quantity called factor of safety, we assess the failure potential of a given

slope based on the stresses and deformation arising from a prescribed forcing function (i.e., rainfall intensity). Stability criteria based on deformation bands are used in this paper to assess the potential for slope failure.

To assess whether the proposed model can successfully integrate important variables in a physics-based characterization of the field conditions and still obtain a realistic description of slope failure, we test the approach with comprehensive and exhaustive data from the Coos Bay experimental catchment (CB1) [21, 22]. The highly instrumented site was originally chosen as a hillslope-scale "laboratory" for conducting sprinkling experiments aimed at developing and testing hydrologic response models. Experimental and field data generated from the site are plentiful, albeit most of them pertain to hydrologic response data [3, 43, 64]. However, the highly instrumented CB1 slope failed as a large debris flow in November 1996, raising some interesting questions related to the geotechnical aspects of the site. Given what we know about the topography, hydrologic constraints, and the geotechnical outcome at CB1, this case study seems ideal to test the proposed continuum slope model. However, it must be noted that despite much effort to constrain the site with extensive field instrumentation and investigation, much uncertainty remains particularly with respect to the geotechnical and hydrologic boundary conditions appropriate for the site. Therefore, to underscore what we still do not know about CB1, we emphasize that the analysis reported in this paper pertains only to a slope similar to CB1, and not to the slope at CB1 itself.

The slope at CB1 is steep, on the order of 43 degrees. Any critical state soil mechanics model would predict an initial stress condition within the slope that lies on the "dilatant side" of the critical state line because of the high shear stress to effective-mean-normal stress ratio generated by the steep slope condition [32, 44]. It would thus be reasonable to characterize the constitutive response of the soil skeleton with a Mohr–Coulomb plasticity or similar models, since the compression cap is unlikely to be activated particularly when the effective-mean-normal stress decreases further as a result of the loss of suction with increased saturation. A simpler plasticity model such as the Mohr–Coulomb model also requires fewer material parameters than any of the more sophisticated constitutive models available in the literature (see [76]). For the soil at CB1, which is mostly colluvium, laboratory-determined values of friction angle are available [53, 54]. Furthermore, representative values of lateral root cohesion in clearcut forests in the Oregon Coast Range have been estimated in [55]. Finally, the thickness of the colluvium at CB1 is known to be much smaller than the plan area of the mobilized slide, thus making a continuum analysis approach appropriate for this problem.

## 2 Continuum slope model

For a solid–water–air mixture the constitutive stress tensor  $\sigma'$  (positive for tension) may be defined as

$$\sigma' = \sigma + \left(1 - \frac{K}{K_s}\right) \bar{p} \mathbf{1}, \quad \bar{p} = \psi^w p_w + (1 - \psi^w) p_a, \quad (1)$$

where  $\sigma$  is the total Cauchy stress tensor,  $\psi^w$  is the degree of saturation,  $K$  and  $K_s$  are the elastic bulk moduli for the solid matrix and solid constituent, respectively,  $p_w$  and  $p_a$  are the intrinsic pore water and pore air pressures, respectively, and  $\mathbf{1}$  is the Kronecker delta tensor. Borja [11, 15] demonstrated this expression for the constitutive stress tensor to be energy-conjugate to the solid rate of deformation. Under special cases,  $\sigma'$  reduces to Bishop's stress when  $K/K_s = 0$  (incompressible solid grains) and  $\psi^w = \chi$ ; to the Skempton [60] and Nur-Byerlee [45] stress when  $\psi^w = 1$ ; and to the Terzaghi [62] stress when  $K/K_s = 0$  and  $\psi^w = 1$ . The Bishop parameter  $\chi$  can be determined experimentally [6, 40], and the substitution of degree of saturation  $\psi^w$  in lieu of this parameter is a simplified approximation derived from the volume averaging over a so-called representative elementary volume, REV. For purposes of constitutive modeling of the soil layer, we will use the Bishop stress ( $K/K_s = 0$ ), with  $\chi = \psi^w$ .

Ignoring inertia forces and setting  $p_a$  equal to the atmospheric pressure (i.e., zero) for near-surface condition, balance of linear momentum in the sub-surface is given by the equation

$$\nabla \cdot \sigma + \bar{p} \mathbf{g} = \mathbf{0}, \quad \bar{p} = \phi^s \rho_s + \phi^w \rho_w, \quad (2)$$

where  $\phi^s$  and  $\phi^w$  are the solid and water volume fractions in the REV, respectively;  $\rho_s$  and  $\rho_w$  are the intrinsic solid and water mass densities (i.e., mass of constituent  $\alpha$  per unit volume of constituent  $\alpha$ ), respectively;  $\bar{p}$  is the total mass density of the mixture (ignoring the mass of air phase); and  $\mathbf{g}$  is the gravity acceleration vector. Assuming that water is incompressible, balance of water mass in the sub-surface takes the form [10, 11]

$$\frac{d\phi^w}{dt} + \phi^w \nabla \cdot \mathbf{v} + \nabla \cdot \mathbf{q}^w = \pm \theta^b \pm \theta^e, \quad (3)$$

where  $\mathbf{v}$  is the velocity of the solid matrix,  $\mathbf{q}^w = \phi^w (\mathbf{v}^w - \mathbf{v})$  is the relative discharge velocity,  $\theta^b$  is the specified rate source/sink,  $\theta^e$  is the rate of water exchange with the surface continuum, and  $d(\cdot)/dt$  denotes a material time derivative following the solid motion. The relative discharge velocity is given by the constitutive equation

$$\mathbf{q}^w = k_{rw} \mathbf{K} \cdot \nabla \left( \frac{p_w}{\rho_w g} + z \right), \quad (4)$$

where  $\mathbf{K}$  is the hydraulic conductivity of the porous medium at complete saturation,  $k_{rw}$  is the relative permeability

that varies with degree of saturation  $\psi^w$ ,  $g$  is the gravity acceleration constant, and  $z$  is the vertical coordinate.

The two independent variables of the formulation are the solid velocity  $\mathbf{v}$  and pore water pressure  $p_w$  satisfying the two balance laws (2) and (3), along with the appropriate boundary and initial conditions. The solution is fully coupled in the sense that the independent variables are determined simultaneously. However, the governing equations must be closed by introducing a pair of constitutive laws determined from continuum principles of thermodynamics [10, 11, 15, 26, 27, 30, 34, 39, 46]: (a) a constitutive law relating the Cauchy effective stress rate tensor  $\dot{\sigma}'$  with the strain rate tensor  $\nabla^s \mathbf{v}$  for the solid matrix; and (b) a constitutive law relating the suction stress  $s = p_a - p_w$  with degree of saturation  $\psi^w$ . The second constitutive law is determined from the imbibition portion of the soil-water retention curve for a given soil [7, 67].

Continuum principles of thermodynamics suggest an elasto-plastic constitutive framework for the soil skeleton given by a yield function of the form [10, 11, 15, 26, 27]

$$F(\sigma', s, \bar{p}_c) = 0, \quad (5)$$

where  $\bar{p}_c$  is a stress-like plastic internal variable that determines the size of the compression cap. The suction stress has a positive value for negative pore water pressure (e.g., above the water table) and approaches zero as the soil approaches perfect saturation. However, as noted earlier, the compression cap is not likely to be activated for steep hillside slope conditions, and thus, this explicit dependence of the yield surface on the suction stress may be ignored when using the Mohr–Coulomb or similar yield criteria. We emphasize, however, that the yield function still depends on the suction stress through the Cauchy effective stress tensor  $\sigma'$ .

Mixed finite element (FE) equations may be readily developed from the variational forms of (2) and (3). The independent variables in the present case are the nodal solid displacement vector  $\mathbf{d}$  and nodal pore water pressure vector  $\mathbf{p}$ . The coupled FE equations take the form

$$\mathbf{F}_{\text{INT}}(\mathbf{d}) + \mathbf{G}\mathbf{p} = \mathbf{F}_{\text{EXT}}, \quad (6)$$

$$\mathbf{G}^T \dot{\mathbf{d}} + \mathbf{M}\dot{\mathbf{p}} + \Phi\mathbf{p} = \mathbf{G}_{\text{EXT}}, \quad (7)$$

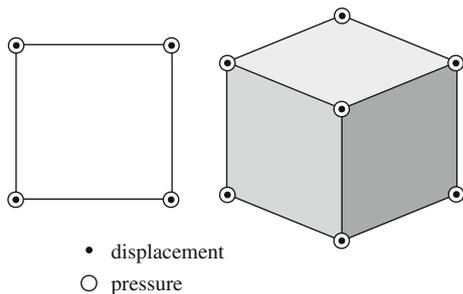
where  $\mathbf{F}_{\text{INT}}(\mathbf{d})$  is the internal nodal force vector arising from the effective stress  $\sigma'$ ,  $\mathbf{G}$  and  $\mathbf{G}^T$  are the discrete gradient and discrete divergence operators, respectively, which depend on  $\mathbf{p}$  through the degree of saturation  $S_r$  in the unsaturated regime,  $\mathbf{M}$  is a coupling matrix that vanishes at full saturation,  $\Phi$  is an effective conductivity matrix that also depends on the degree of saturation, and  $\mathbf{F}_{\text{EXT}}$  and  $\mathbf{G}_{\text{EXT}}$  are prescribed vectors of momentum and fluid supplies. Note that the degree of coupling implied by the earlier equations is more intricate than in the fully

saturated case because of the presence of  $\psi^w$  in many terms.

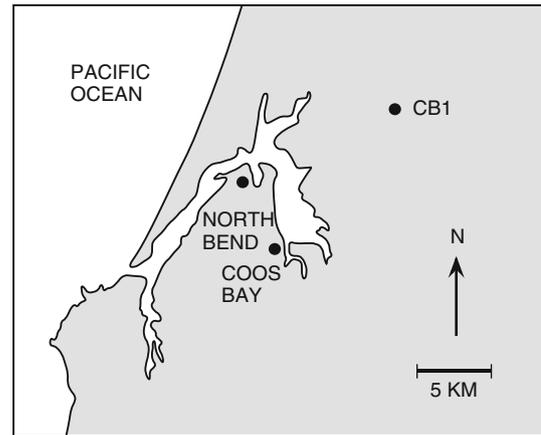
The coupled formulation presented earlier requires mixed finite elements with nodal pressure and displacement degrees of freedom. Low-order mixed finite elements, with equal order interpolation for displacement and pressure, would be ideal particularly in 3D when the number of equations can increase dramatically. Unfortunately, low-order mixed finite elements create a numerical difficulty in that in the limit of full saturation and either low permeability or fast loading rates, the pore fluid can impose near or exact incompressibility on the deformation of the solid matrix and create spurious pore-pressure oscillation. To address this difficulty, we use a stabilization scheme proposed by White and Borja [73] based on the concept of polynomial pressure projections (PPP), which was originally proposed in [8, 9, 20] to stabilize the Stokes problem. The primary motivation for using stabilization is computational efficiency: with this technique, it would now be possible to use low-order finite elements, such as those shown in Fig. 1, without the undesirable pore-pressure oscillation that otherwise afflicts the solution without stabilization.

### 3 Hydrologic and geotechnical conditions at CB1

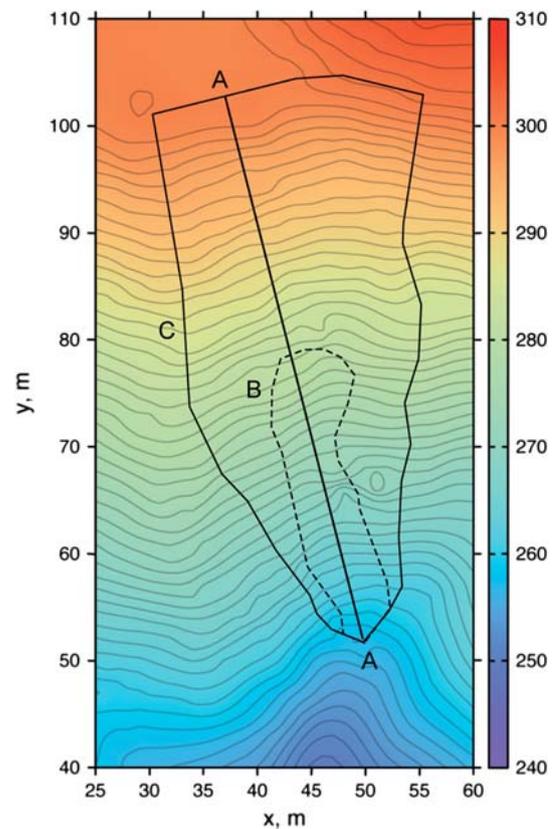
The CB1 experimental catchment [3, 43, 64], clearcut in 1987, is located along Mettman Ridge approximately 15 km north of Coos Bay in the Oregon Coast Range (Fig. 2). CB1 is a 51-m long (860 m<sup>2</sup>) unchanneled valley, with a north-facing aspect, that has an average slope of 43° (see Fig. 3). Three sprinkling experiments were conducted at CB1: experiment #1 conducted in May 1990 at 1.5 mm/h for 6 days; experiment #2 conducted in May 1990 at 3.0 mm/h for 4 days; and experiment #3 conducted in May 1992 at 1.7 mm/h for 7 days. The instrumentation at CB1 used to characterize the spatial and temporal variability in near-surface hydrologic response for the three experiments



**Fig. 1** Stabilized low-order mixed finite elements for coupled solid-deformation/fluid-diffusion: four-node quadrilateral for 2D (left), and eight-node hexahedral for 3D (right). After White and Borja [73]



**Fig. 2** Location map for CB1 experimental catchment near Coos Bay in the Oregon Coast Range, USA. Reproduced from Ebel et al. [21]



**Fig. 3** Topographic map for CB1 experimental catchment. Two-dimensional plane strain condition is assumed along section A-A for the coupled solid deformation-fluid flow analysis. *Dashed curve* B delineates the extent of debris flow zone at CB1 from event of November 1996. Larger region C defines the boundary of the Ebel et al. [22] 3D hydrologic FE model. *Color bar* is elevation in meters

included an exhaustive grid of rain gauges, piezometers, tensiometers, TDR wave guide pairs (for estimating soil-water content), lysimeters, meteorological sensors (on a tower), atmometers, and weirs. Continuous measurements

from rainfall, discharge, and total head (from selected piezometers) are available from 1990 through 1996. In November 1996, the CB1 slope failed as a large debris flow. The instrumentation at CB1 provides one of the most comprehensive hydrologic response data sets in existence for a steep, deforested catchment that has experienced slope failure.

The sediment at CB1 is colluvium, a surficial sediment derived from weathered or fresh bedrock, and the soil has no input from aeolian transport. The parent rock for the colluvium is an Eocene turbidite sandstone from the Tyee and Flournoy formations [55]. The soils are well mixed, non-plastic (plasticity index of 0), and gravelly sands [54]. The geometry and thickness of the colluvium are well defined from soil borings. Saturated hydraulic conductivity were determined from slug tests, soil-water content, and porosity from TDR measurements, and hysteretic capillary pressure relationships were established from experiments. Discharge chemistry data suggest that runoff generation occurs primarily from water stored in small, poorly connected pores, and fractures in the bedrock, and saprolite connecting with larger macropores during storms [42]. Tracer data (bromide and isotopically tagged water) suggest that the two most important flow paths at CB1 are rapid saturated flow through the shallow, fractured bedrock, and vertical percolation in the vadose zone [2]. Piezometer records show that sub-surface storm flow in the shallow, fractured-rock zone exerts the most significant control on pore-pressure development in the CB1 colluvium [42]. Tensiometer data indicate that the flux of water through the unsaturated zone provides an additional control on pore-pressure development and cannot be ignored in slope-stability assessment models [63].

Low confining stress triaxial shear tests demonstrate that the colluvium at CB1 is cohesionless (consisting of a sandy matrix with a friction angle of  $33^\circ$ ) [53, 54]. Lateral root cohesion in clearcut forests in the Oregon Coast Range was estimated to be uniformly less than 10 kPa [55] and may have explained how such a steep slope at CB1 could be sustained by the sediment (apart from the capillary tension that develops in the vadose zone). Low confining stress triaxial tests gave an internal friction angle of  $40^\circ$  and zero cohesion [55]. This is in agreement with other measurements near the site that gave internal friction angles ranging from  $35\text{--}44^\circ$  [19, 57, 74, 75] and zero cohesion [75]. The stress-strain behavior, observed in low confining stress triaxial strength testing, was approximately linear for low applied stresses with a distinct transition to a non-linear material behavior at axial strains greater than 1–2% [54]. The saturated density of the soil is about 1,600 kg/cu.m. [55], and the bulk density at soil water contents of

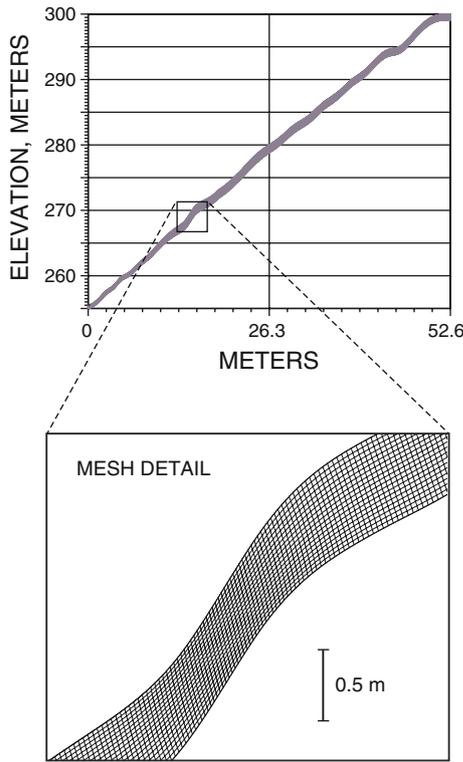
20–30% is around 1,200 kg/cu.m. [54]. The Van Genuchten [28, 67] parameters for the CB1 soil are discussed in the next section.

#### 4 Hydro-mechanical model

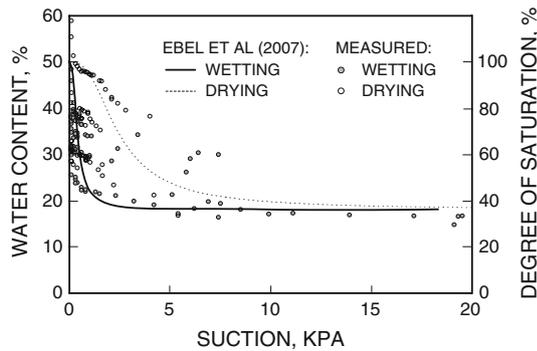
A challenging aspect of the numerical simulation of a hillslope-scale problem is determining the extent of the spatial and temporal discretizations, and what initial and boundary conditions to impose on the problem. Ebel et al. [22] conducted full 3D fluid flow simulations based on Richards equation of variably saturated flow in the subsurface [50] using a comprehensive FE code InHM (Integrated Hydrology Model) [68]. They simulated flow over a portion of the sediment and fractured bedrock delineated by vertical boundaries on which they believed they could reasonably impose a no-flow boundary condition. The spatial extent of their domain description is shown in Fig. 3.

For our purposes, the deformation in the bedrock would be too small to be of concern in the coupled solid deformation/fluid-flow analysis, and thus we only represent the sediment domain in our simulations. However, there are two important factors that make the present simulations significantly more demanding than the fluid-flow simulations conducted by Ebel et al. [22]: (a) each node in the FE mesh is now composed of 3 degrees of freedom (DOFs) in 2D (two displacement and one pressure), and 4 DOFs in 3D (three displacement and one pressure); thus, the number of equations increases very fast; and (b) the water retention curve typically exhibits a steep slope near the wetting front, necessitating a high-resolution mesh everywhere in the unsaturated zone (since the wetting front propagates through the unsaturated zone).

Considering the difficulty with modeling the exact CB1 conditions due to the uncertainties in defining what constitutes a ‘sufficient’ 3D representation of CB1 and what boundary conditions to impose on this model, we believe that it would be more enlightening to consider a much simpler 2D plane strain representation for now, where the boundary conditions can be constrained more easily. To this end, we selected a cross-section passing through the steepest portion of the CB1 catchment, shown as section A-A in Fig. 3, and constructed the FE mesh shown in Fig. 4. This 2D representation of the slope at CB1 is conservative in the sense that out-of-plane strengths from 3D effect emanating from lateral root cohesion, friction, etc. has been ignored. The mesh shown in Fig. 4 has 20,000 nodes and 18,981 (stabilized) quadrilateral mixed finite elements, resulting in a total of 60,000 DOFs.



**Fig. 4** Finite element mesh for CB1-like problem simulations (cf. section A-A in Fig. 3)

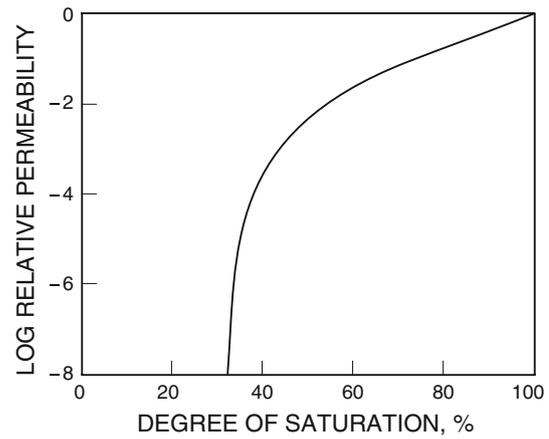


**Fig. 5** Soil-water retention curve data [64] and van Genuchten curves used by Ebel et al. [22] for hydrologic simulations. We use (approximately) the Ebel et al. [22] wetting curve for the saturation-suction relation to capture the mechanical response during the wetting phase of the numerical simulations

Figures 5 and 6 show the suction/saturation and saturation/relative permeability relationships used in the simulations. The degree of saturation  $S_r$  is determined from the Van Genuchten [67] model as

$$\psi^w(s) = \psi_1 + (\psi_2 - \psi_1) \left[ 1 + \left( \frac{s}{s_a} \right)^n \right]^{-m} \quad (8)$$

The model contains four parameters:  $\psi_1$  is the residual water saturation,  $\psi_2$  is the maximum water saturation,  $s_a$  is



**Fig. 6** Variation of relative permeability with degree of saturation based on the wetting curve

a scaling pressure, and  $n$  and  $m$  are empirical constants defining the shape of the saturation curve. The constants  $n$  and  $m$  are not independent but are rather related to one another as

$$m = \frac{n - 1}{n} \quad (9)$$

The water phase relative permeability is similarly defined as

$$k_{rw}(\theta) = \theta^{1/2} \left[ 1 - \left( 1 - \theta^{1/m} \right)^m \right]^2, \quad \theta = \frac{\psi^w - \psi_1}{\psi_2 - \psi_1} \quad (10)$$

The parameter values used in this work are given in Table 1. In order to calibrate the model, we have used the in situ retention curves as measured by Torres et al. [64] for the CB1 site. We ignored hysteretic effects and have only used the wetting measurements for calibration. The chosen values

**Table 1** Material parameters

Intrinsic permeability	$k$	$3.4 \times 10^{-11} \text{ m}^2$
Fluid viscosity	$\mu$	$1.0 \times 10^{-6} \text{ kPa s}$
Residual saturation	$\psi_1$	0.32
Maximum saturation	$\psi_2$	1.00
Shape constant	$n$	3.00
Scaling pressure	$s_a$	0.40 kPa
Bulk modulus	$K$	50 MPa
Poisson ratio	$\nu$	0.25
Cohesion	$c$	0–10 kPa
Friction angle	$\phi$	33–40°
Dilatancy angle	$\psi$	$\approx 25^\circ$
Porosity	$\phi^s$	0.50
Fluid density	$\rho_w$	1.0 Mg/m <sup>3</sup>
Solid density	$\rho_s$	2.2 Mg/m <sup>3</sup>

are nearly the same as those used by Ebel et al. [22] in their hydrologic model except for a slight adjustment in the scaling pressure. The steep geometry of the saturation and relative permeability relationships proved to be numerically challenging on the relatively coarse mesh, and a slight flattening of the curve improved the robustness of the model.

The elastic parameters  $K$  and  $\nu$  are typical for sand/gravel mixture subjected to a confining pressure comparable to those prevailing in the CB1 sediment [36]. The elastic parameters influence the displacements of the sediment but have little effect on the mechanism of failure, which is determined largely by the plasticity model. The parameters of the Mohr–Coulomb plasticity model are the cohesion  $c$ , friction angle  $\phi$ , and dilatancy angle  $\psi$ , and their range of values is also summarized in Table 1.

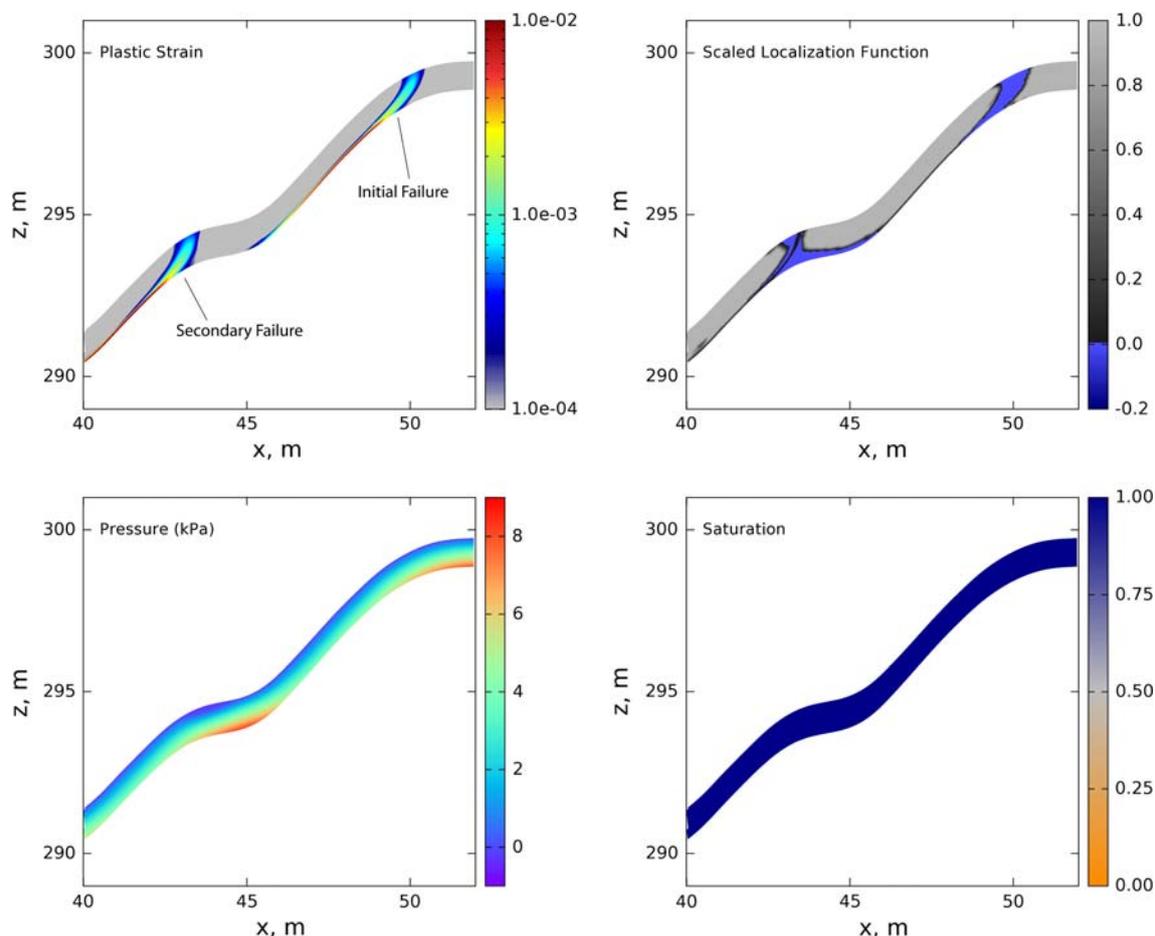
## 5 Results

In general, failure mechanisms generated by the 2D slope model are complex and very much dependent on the

imposed flow boundary conditions. Furthermore, the timing and location of initial failure are dependent on the intensity of rainfall and local flow conditions, such as the presence of a source or sink. In this section, we summarize the results of numerical simulations on the 2D slope model. The section is divided into two parts. In the first part, we show the impact of flow boundary conditions on the resulting deformation and failure patterns. In the second part, we conduct parametric studies to investigate the sensitivity of the calculated deformation and failure patterns to variation in material parameters.

### 5.1 Impact of flow boundary conditions

We consider three fluid-flow boundary conditions—Case A: a zero fluid pressure is prescribed on the slope surface; Case B: rainfall infiltration is prescribed on the slope surface in the form of fluid flux; and Case C: fluid infiltration into the sediment is prescribed on the interface between the sediment and fractured bedrock. The materials parameters are summarized in Table 1. For the present simulations, baseline

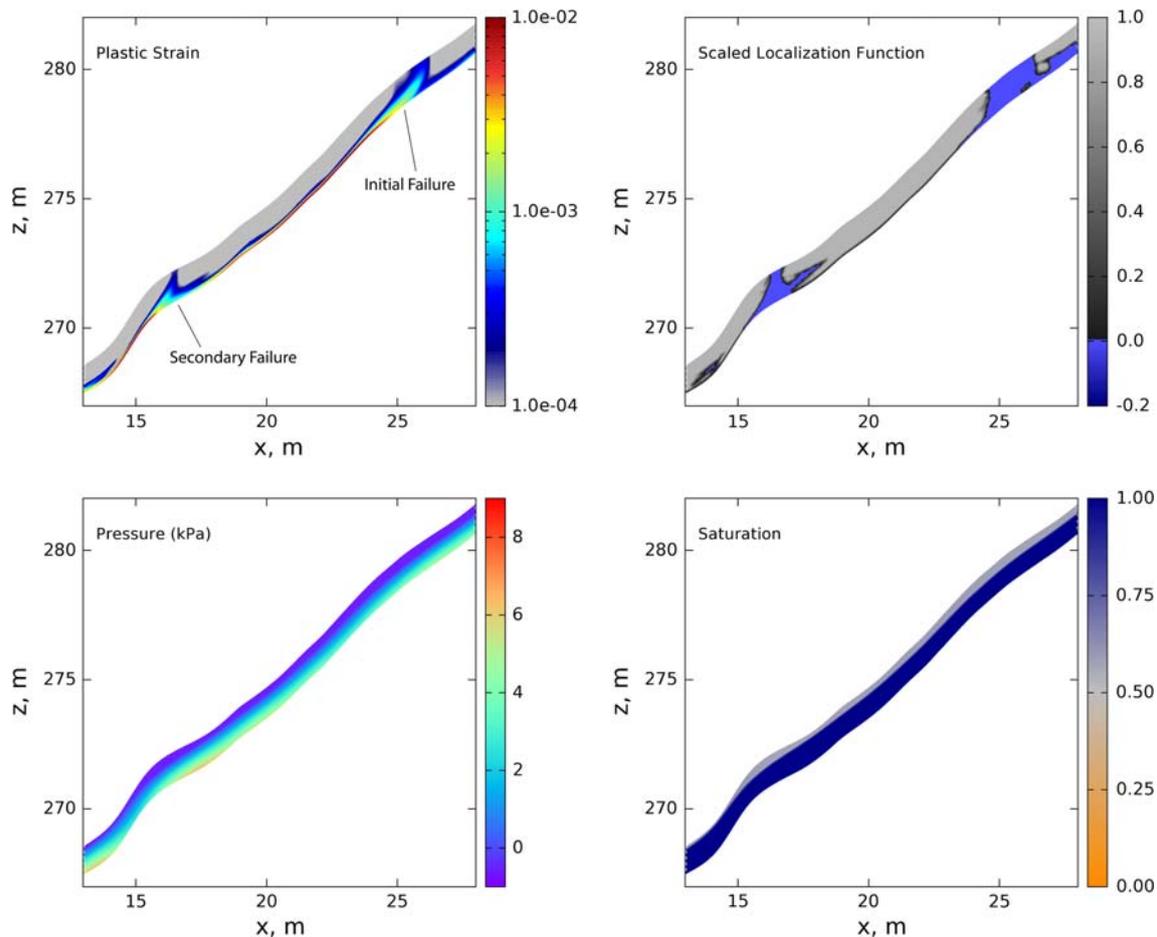


**Fig. 7** Multiple slide block mechanism in a steep hillside slope subjected to rising pore water pressure boundary condition from  $-1.5$  kPa up to  $0$  kPa in  $3$  h on slope surface

values of  $c = 4$  kPa for cohesion,  $\phi = 40^\circ$  for friction angle, and  $\psi = 25^\circ$  for dilatancy angle were used.

In all the simulations, the sediment was assumed fixed to the bedrock, and any relative sliding between the sediment and bedrock may only take place in the form of plastic deformation on the sediment. The slope is very thin compared to its length, so the displacement boundary conditions on the top and bottom ends of the slope are expected to play a very minor role on the calculated mechanical responses. Thus, in the present simulations, we simply assumed the top and bottom ends of the slope to be fixed to the support. However, initial conditions do play a significant role on the hydro-mechanical responses, particularly the initial value of negative pore water pressure within the sediment. Based on the hydrologic simulations of Ebel et al. [22], we assumed an initial pore water pressure of  $-1.5$  kPa throughout the sediment. Gravity load was turned on along with this initial pore water pressure to obtain the initial effective stresses, after which the nodal displacements were reset to zero. A standard  $2 \times 2$  Gauss integration rule was used for the stabilized quadrilateral mixed elements, and a backward implicit scheme was used for time integration.

For Case A, we assumed the pore water pressure on the slope surface to ramp up linearly from  $-1.5$  kPa at  $t = 0$ , to  $0$  kPa at  $t = 3$  h (Dirichlet boundary condition), with all other fluid-flow boundaries assumed to be impermeable (Neumann boundary condition). This represents a heavy rainfall, enough to saturate the slope surface within a period of 3 h and keep it saturated thereafter. Figure 7 summarizes the calculated hydro-mechanical responses at the inception of primary and secondary failure mechanisms within the slope. The general mechanism is as follows. As the sediment becomes saturated, local plastic zones develop on the base and stretch the slope segments unevenly. Eventually, plastic zones curve upwards due to local stretching of the slope segments and emerge on the ground surface approximately at coordinates  $x = 43$  and  $50$  m. The resulting slope failure mechanism is similar to multiple slide block described by Varnes [69]. Drained bifurcation analyses based on the Rudnicki and Rice [51] procedure allowed the calculation of localization function [4, 5, 11, 12, 13, 14, 52], showing negative values. This suggests that a shear band-type bifurcation is likely to occur where the plastic deformation concentrates. On a related note, Borja [10] demonstrated that



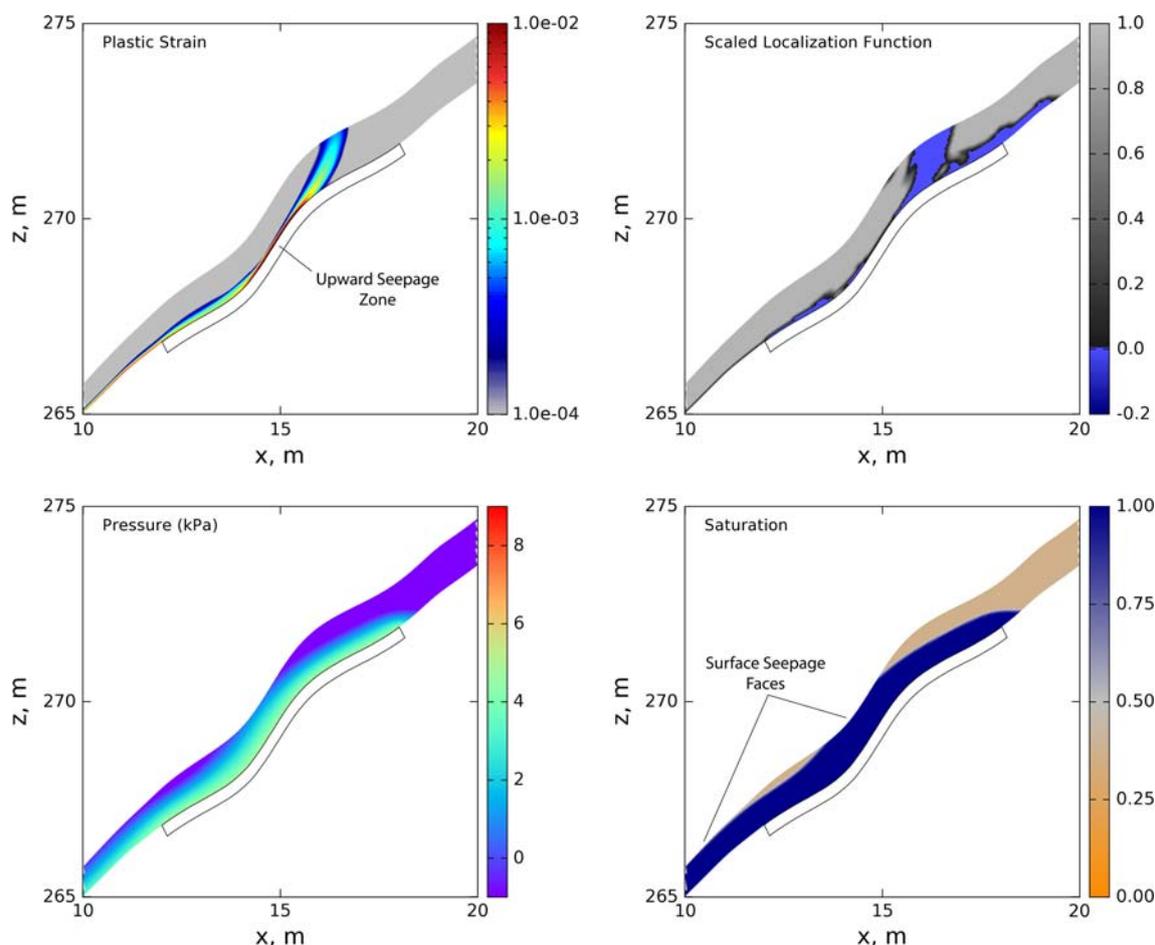
**Fig. 8** Multiple slide block mechanism in a steep hillside slope subjected to rainfall infiltration of 15 mm/h on slope surface

drained shear-band bifurcation is likely to be more critical than undrained bifurcation in partially saturated dilatant frictional materials. At the inception of initial and secondary failure mechanisms, the critical slope segment is nearly saturated, and the pore water pressure is approximately hydrostatic relative to the slope surface.

For Case B, we specified a seepage infiltration of 15 mm/h on the slope surface (Neumann boundary condition) while maintaining the same flow boundary conditions on the other faces as in Case A (an initial all-Neumann set of flow boundary conditions). This eventually caused the bottom end of the slope to become saturated and the pore water pressure there to rise indefinitely. Since the pore water pressure cannot exceed zero on the slope surface, the boundary condition switched from a seepage type (Neumann) to a pressure-type (Dirichlet) on the slope surface where the pore water pressure reached zero. Figure 8 shows the calculated hydro-mechanical responses. The failure mechanism is similar to a multiple block type as in Case A, but note that the new boundary conditions have mobilized failure within a different segment of the slope (at  $x = 16$  and 25 m). The

localization function also shows a propensity of the sediment to develop shear strain localization where plastic deformation concentrates. Furthermore, even though the sediment is saturated all throughout the depth near the bottom end of the slope, initial failure still developed upslope, at  $x = 25$  m where the sediment is still partially saturated. This suggests that the sediment does not have to be completely saturated to experience failure by plastic deformation and shear strain localization.

For Case C, we also assumed an initial all-Neumann boundary condition with zero flux on all surface boundaries except over a finite segment between  $x = 12$  and 18 m on the sediment–bedrock interface. Thus, this segment of the fractured bedrock was assumed to be a fluid source. There has been much speculation about the fluid flux from the fractured bedrock at CB1. Whereas its importance on the hydrologic aspects has been elucidated from previous fluid-flow simulations [22], its impact on the sediment mechanical responses is poorly understood. To isolate the effect of fluid infiltration from the fractured bedrock, we assumed the top surface to be a no-flux boundary unless the pressure plume



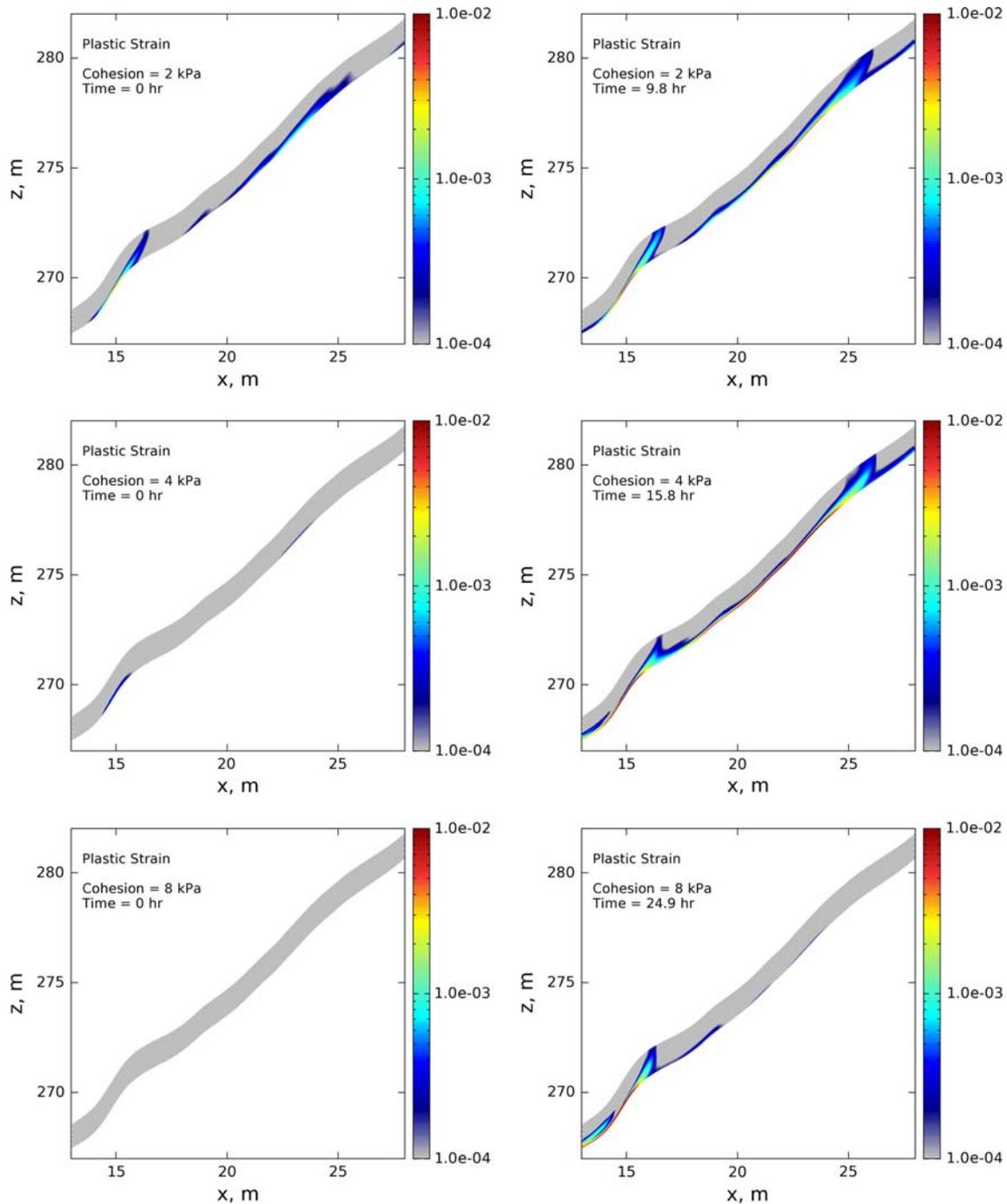
**Fig. 9** Failure mechanism in a steep hillside slope subjected to upward seepage on the base of the slope

reaches it, at which point it switches to a  $p = 0$  face. Figure 9 suggests that with only fluid influx from the fractured bedrock, it takes a large amount of seepage to build up enough pressure to fail the slope. Note that the pressure plume extends all the way to the surface, implying that upward seepage would be observed at the surface. It thus appears that upward seepage is unlikely to be the primary failure mechanism for a slope similar to CB1. However, upward seepage

could certainly aggravate a slope that has already been weakened by other infiltration.

## 5.2 Impact of strength parameters variation on failure mechanism

The comprehensive hydrologic FE simulations conducted by Ebel et al. [22] highlighted the importance of being able



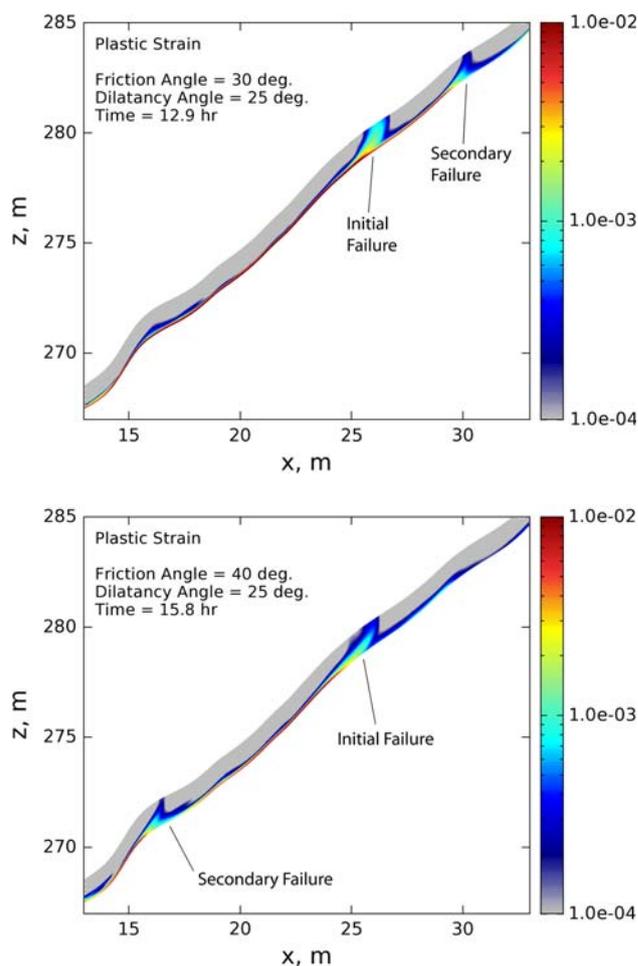
**Fig. 10** Variation of failure mechanism and timing of failure with cohesion

to constrain the parameters of the fluid-flow model in general, and the soil-water retention curve in particular, for a realistic prediction of the field responses at CB1. In this section, we address the implications of uncertain strength parameters on the predicted failure mechanism and the timing of such mechanism for a steep hillside slope similar to CB1. Fortunately, the perfectly plastic Mohr–Coulomb model has only three strength parameters: cohesion  $c$ , friction angle  $\phi$ , and dilatancy angle  $\psi$ , and thus the parametric studies can be conducted with relative ease. Any unknown hardening or softening responses may be viewed as part of the uncertainties in these strength parameters.

Figure 10 shows the impact of an uncertain cohesion on the failure mechanism for the 2D slope model. The friction and dilatancy angles were fixed at 40 and 25°, respectively, and the loading condition was defined by Case B (prescribed seepage on the slope face). We recall that at the CB1 site, the parameter  $c$  was derived mainly from lateral root cohesion, which could vary in space and time. For example, as the sediment is stretched, the root strength could be mobilized, resulting in an increase in  $c$ , but it could also subsequently decrease when the roots are pulled from the host sediment. The figure shows the failure mechanisms and timing of failure at cohesion of 2, 4, and 8 kPa. At 2 kPa the slope failed for the initial configuration, just under its own self-weight. The observed trends are what one would expect: larger cohesion delays the timing of failure. However, at  $c = 8$  kPa, only a single plastic zone emerged on the slope face, not multiple ones.

Figure 11 shows the impact of an uncertain friction angle  $\phi$  on the failure mechanism for the 2D slope model. In the simulations,  $c$  was fixed at 4 kPa, and the loading condition was again defined by Case B. For the two values of friction angle tested ( $\phi = 30$  and 40°), the initial plastic zone emerged on the slope face at approximately the same location (at  $x = 25$  m). However, for  $\phi = 30^\circ$ , the secondary failure zone developed at an earlier time and above the initial failure zone (at  $x = 30$  m), whereas for  $\phi = 40^\circ$ , the secondary plastic zone emerged on the slope face at a later time and below the initial failure zone (at  $x = 17$  m).

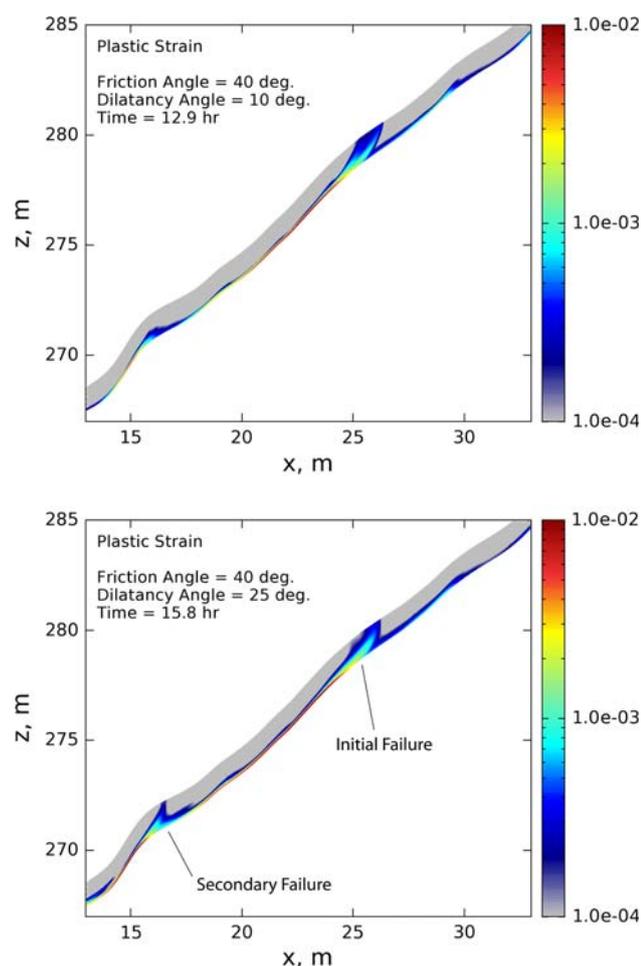
Finally, we consider the effect of the dilatancy angle on the predicted failure kinematics. Figure 12 compares the plastic strain distribution in the slope using two dilatancy angles, 10 and 25°, while the friction angle remains fixed at the baseline value of 40°. In both cases, a failure surface extending to slope surface is observed at approximately  $x = 25$  m, suggesting that this failure mode is insensitive to dilatancy. In the low dilatancy angle simulation, however, the secondary failure in the  $x = 16$  m region is suppressed. There is some indication that with additional deformation, a secondary failure may initiate at this point, but the timing of the two would not be as closely linked as in the high dilatancy angle case. Close examination of the plastic strain contours in both simulations



**Fig. 11** Variation of failure mechanism and timing of failure with friction angle

also indicate that the plastic zone in the low dilatancy case is less “diffuse” than in the high dilatancy case.

We remark that many interesting features of the coupled physics in this problem are spatially localized. For example, consider the sharp wetting front that moves through the domain, or the localized plastic shear deformation. From a computational perspective, this suggests that an adaptive mesh refinement algorithm could be quite useful for this class of problems. This assessment is particularly true as one considers fully three-dimensional analyses in complex domains. However, there are at least two non-trivial issues that must be addressed in order to apply this algorithm to coupled fluid-flow/solid-deformation problems. The first is that an appropriate refinement/coarsening criterion must be developed that accounts for the coupled nature of the fluid-solid problem, see [23, 56]. The second consideration is that applying adaptive mesh refinement to a plastic medium introduces additional questions about how to handle the treatment of internal plastic variables. When an element is refined or coarsened, new quadrature points are created, and the internal plastic history of the material must be



**Fig. 12** Variation of failure mechanism and timing of failure with dilatancy angle

transferred to these new points. For a simple plasticity model (such as MC), a straightforward projection/interpolation method may be sufficient, but for more complex models (say, a critical state soil model) with several internal parameters, we must develop a refinement strategy that ensures that the plastic variables remain self-consistent with one another as projection or interpolation operations proceed, see [16, 38, 48].

## 6 Summary and conclusions

We have presented a continuum physics-based framework for analysis of coupled solid deformation-fluid-flow processes in partially saturated earthen slopes. The formulation for constitutive modeling of the unsaturated sediment is based on the use of an effective stress measure that represents the sole stress state variable responsible for deforming the solid skeleton, and on direct use of suction in the constitutive relations [10, 11, 15, 33]. Other

alternative approaches exist, in which different pairs of stress state variables are chosen instead of a single effective stress, such as the net stress and matric suction [1, 24, 25, 70–72]. However, the effective stress used in this work appears to have an advantage in terms of FE implementation, since the coupled formulation follows exactly the same lines as those developed for the fully saturated case. This implies that stabilized low-order mixed FE elements can be used just as well for the unsaturated case.

We have used the coupled continuum FE model to analyze the deformation and stability of a steep hillside slope similar to the CB1 site. Despite the simplified 2D plane strain representation adopted by the model, the predicted failure mechanisms are complex and nowhere near what one would normally obtain from an infinite slope assumption. For a steep hillside slope similar to CB1, it appears that failure mechanism would likely initiate in the form of multiple failure blocks, which could transform into a debris flow similar to what was observed at the CB1 site during the November 1996 event. An obvious advantage of the proposed continuum modeling approach lies in its ability to integrate important hydro-mechanical processes responsible for triggering rainfall-induced movement of earthen slopes, including increased saturation, fluid flow, and inelastic solid deformation. Work is currently underway to incorporate 3D effects into the numerical model.

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