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Speech and Language Processing

**Chapter 6:**  
**Vector Semantics**



# What do words mean?

First thought: look in a dictionary

<http://www.oed.com/>

# Words, Lemmas, Senses, Definitions

**lemma**

**sense**

**definition**

pepper, *n.*

**Pronunciation:** BRIT. /'peɪpə/, U.S. /'peɪpər/

**Forms:** OE **peopor** (*rare*), OE **piþcer** (transmission error), OE **pipor**, OE **pipur** (*rare*).

**Frequency (in current use):**

**Etymology:** A borrowing from Latin. **Etymon:** Latin *piper*.

< classical Latin *piper*, a loanword < Indo-Aryan (as is ancient Greek *πίπερι*); compare Sar

**I.** The spice or the plant.

**1.**

**a.** A hot pungent spice derived from the prepared fruits (peppercorns) of the pepper plant, *Piper nigrum* (see sense 2a), used from early times to season food, either whole or ground to powder (often in association with salt). Also (locally, chiefly with distinguishing word): a similar spice derived from the fruits of certain other species of the genus *Piper*; the fruits themselves.

The ground spice from *Piper nigrum* comes in two forms, the more pungent *black pepper*, produced from black peppercorns, and the milder *white pepper*, produced from white peppercorns: see **BLACK adj.** and *n.* Special uses 5a, **PEPPERCORN n.** 1a, and **WHITE adj.** and *n.*<sup>1</sup> Special uses 7b(a).

**2.**

**a.** The plant *Piper nigrum* (family Piperaceae), a climbing shrub indigenous to South Asia and also cultivated elsewhere in the tropics, which has alternate stalked entire leaves, with pendulous spikes of small green flowers opposite the leaves, succeeded by small berries turning red when ripe. Also more widely: any plant of the genus *Piper* or the family Piperaceae.

**b.** Usu. with distinguishing word: any of numerous plants of other families having hot pungent fruits or leaves which resemble pepper (1a) in taste and in some cases are used as a substitute for it.

**c.** U.S. The California pepper tree, *Schinus molle*. Cf. **PEPPER TREE n.**

**3.** Any of various forms of capsicum, esp. *Capsicum annuum* var. *annuum*. Originally (chiefly with distinguishing word): any variety of the *C. annuum* Longum group, with elongated fruits having a hot, pungent taste, the source of cayenne, chilli powder, paprika, etc., or of the perennial *C. frutescens*, the source of Tabasco sauce. Now frequently (more fully **sweet pepper**): any variety of the *C. annuum* Grossum group, with large, bell-shaped or apple-shaped, mild-flavoured fruits, usually ripening to red, orange, or yellow and eaten raw in salads or cooked as a vegetable. Also: the fruit of any of these capsicums.

Sweet peppers are often used in their green immature state (more fully **green pepper**), but some new varieties remain green when ripe.

# Lemma pepper

Sense 1: spice from pepper plant

Sense 2: the pepper plant itself

Sense 3: another similar plant (Jamaican pepper)

Sense 4: another plant with peppercorns (California pepper)

Sense 5: *capsicum* (i.e. chili, paprika, bell pepper, etc)



A sense or “concept” is the meaning component of a word



There are relations between  
senses

# Relation: Synonymy

Synonyms have the same meaning in some or all contexts.

- filbert / hazelnut
- couch / sofa
- big / large
- automobile / car
- vomit / throw up
- Water / H<sub>2</sub>O

# Relation: Synonymy

Note that there are probably no examples of perfect synonymy.

- Even if many aspects of meaning are identical
- Still may not preserve the acceptability based on notions of politeness, slang, register, genre, etc.

## The Linguistic Principle of Contrast:

- Difference in form -> difference in meaning



# Relation: Synonymy?

Water/H<sub>2</sub>O

Big/large

Brave/courageous

# Relation: Antonymy

Senses that are opposites with respect to one feature of meaning

Otherwise, they are very similar!

dark/light

short/long

fast/slow rise/fall

hot/cold

up/down

in/out

More formally: antonyms can

- define a binary opposition
  - or be at opposite ends of a scale
- long/short, fast/slow
- Be *reversives*:
  - rise/fall, up/down

# Relation: Similarity

Words with similar meanings. Not synonyms, but sharing some element of meaning

car, bicycle

cow, horse

# Ask humans how similar 2 words are

word1	word2	similarity
vanish	disappear	9.8
behave	obey	7.3
belief	impression	5.95
muscle	bone	3.65
modest	flexible	0.98
hole	agreement	0.3

# Relation: Word relatedness

Also called "word association"

Words be related in any way, perhaps via a semantic frame or field

- car, bicycle: **similar**
- car, gasoline: **related**, not similar

# Semantic field

Words that

- cover a particular semantic domain
- bear structured relations with each other.

## **hospitals**

*surgeon, scalpel, nurse, anaesthetic, hospital*

## **restaurants**

*waiter, menu, plate, food, menu, chef),*

## **houses**

*door, roof, kitchen, family, bed*

# Relation: Superordinate/ subordinate

One sense is a **subordinate** of another if the first sense is more specific, denoting a subclass of the other

- *car* is a subordinate of *vehicle*
- *mango* is a subordinate of *fruit*

Conversely **superordinate**

- *vehicle* is a superordinate of *car*
- *fruit* is a superordinate of *mango*

<b>Superordinate</b>	vehicle	fruit	furniture
<b>Subordinate</b>	car	mango	chair



These levels are not symmetric

One level of category is  
distinguished from the others

The "basic level"

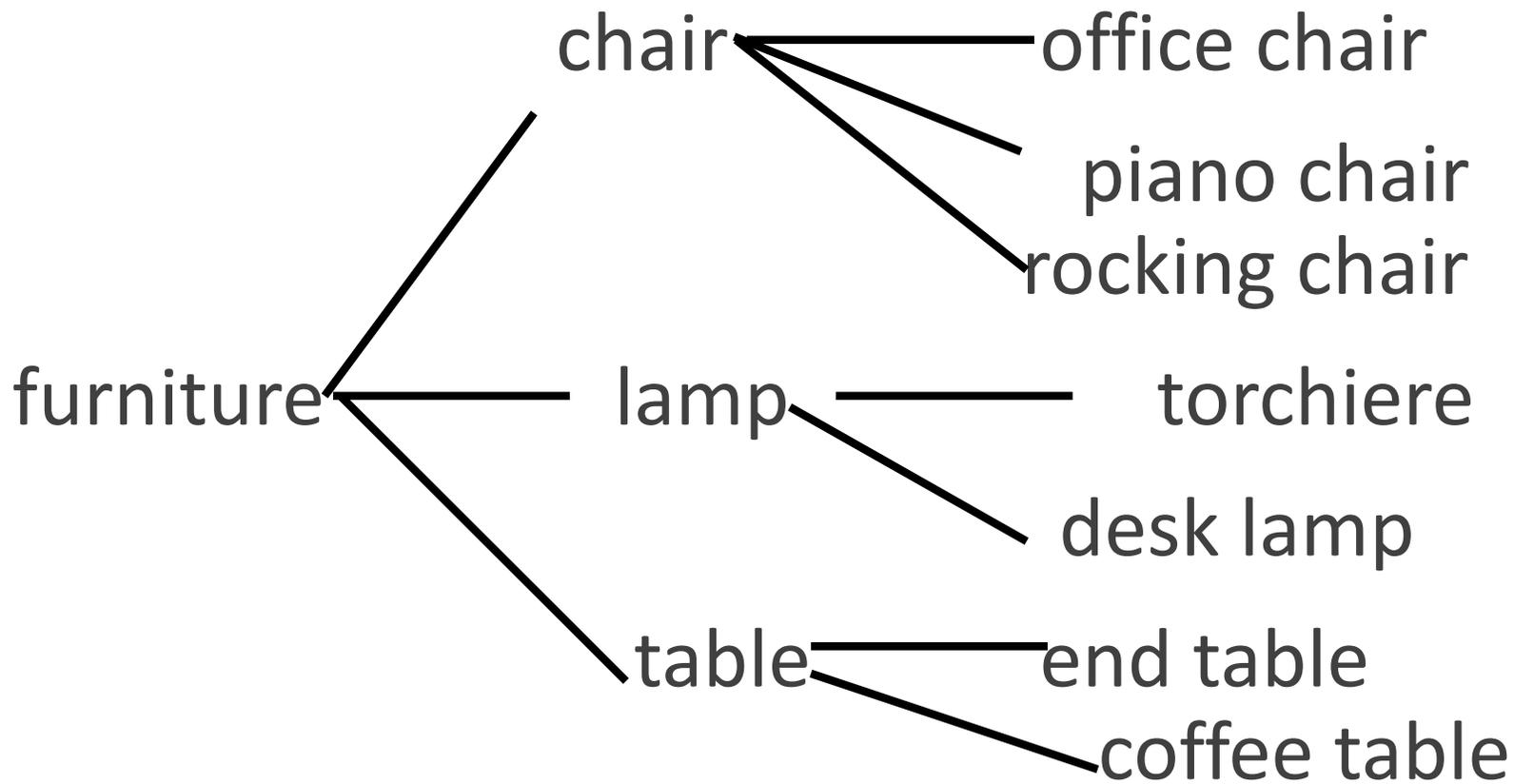
Name these items



**Superordinate**

**Basic**

**Subordinate**



# Cluster of Interactional Properties

Basic level things are “human-sized”

Consider chairs

- We know how to interact with a chair (sitting)
- Not so clear for superordinate categories like furniture
  - “Imagine a furniture without thinking of a bed/table/chair/specific basic-level category”



# The basic level

Is the level of distinctive actions

Is the level which is learned earliest and at which things are first named

It is the level at which names are shortest and used most frequently



# Connotation

Words have **affective** meanings

positive connotations (*happy*)

negative connotations (*sad*)

positive evaluation (*great, love*)

negative evaluation (*terrible, hate*).

# So far

## **Concepts** or word senses

- Have a complex many-to-many association with **words** (homonymy, multiple senses)

## Have relations with each other

- Synonymy
- Antonymy
- Similarity
- Relatedness
- Superordinate/subordinate
- Connotation



But how to define a concept?

# Classical (“Aristotelian”) Theory of Concepts

The meaning of a word:

a concept defined by **necessary and sufficient conditions**

A **necessary** condition for being an X is a condition C that X must satisfy in order for it to be an X.

- If not C, then not X
- “Having four sides” is necessary to be a square.

A **sufficient** condition for being an X is condition such that if something satisfies condition C, then it must be an X.

- If and only if C, then X
- The following necessary conditions, jointly, are sufficient to be a square
  - x has (exactly) four sides
  - each of x's sides is straight
  - x is a closed figure
  - x lies in a plane
  - each of x's sides is equal in length to each of the others
  - each of x's interior angles is equal to the others (right angles)
  - the sides of x are joined at their ends

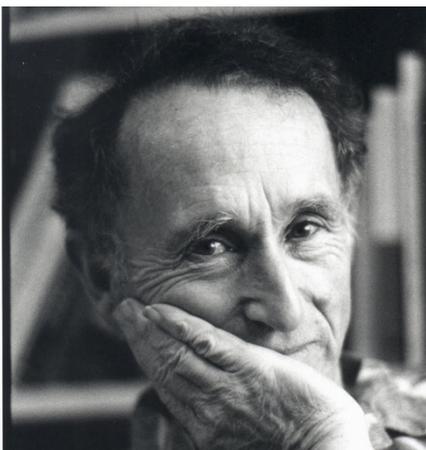
Example  
from  
Norman  
Swartz,  
SFU

# Problem 1: The features are complex and may be context-dependent

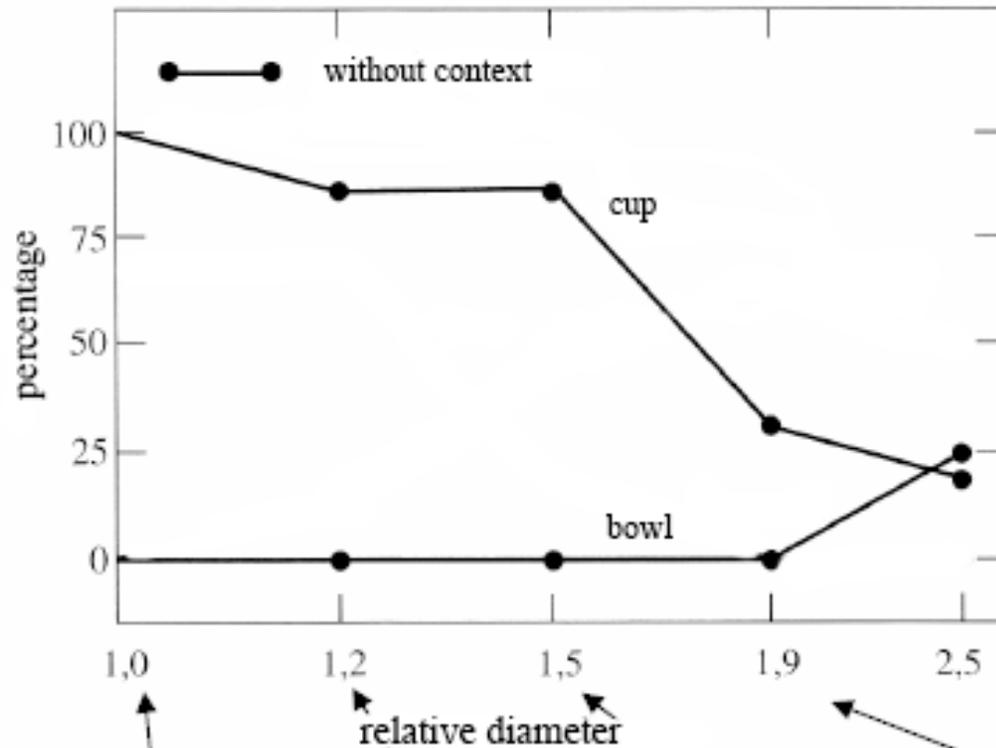
William Labov. 1975

What are these?

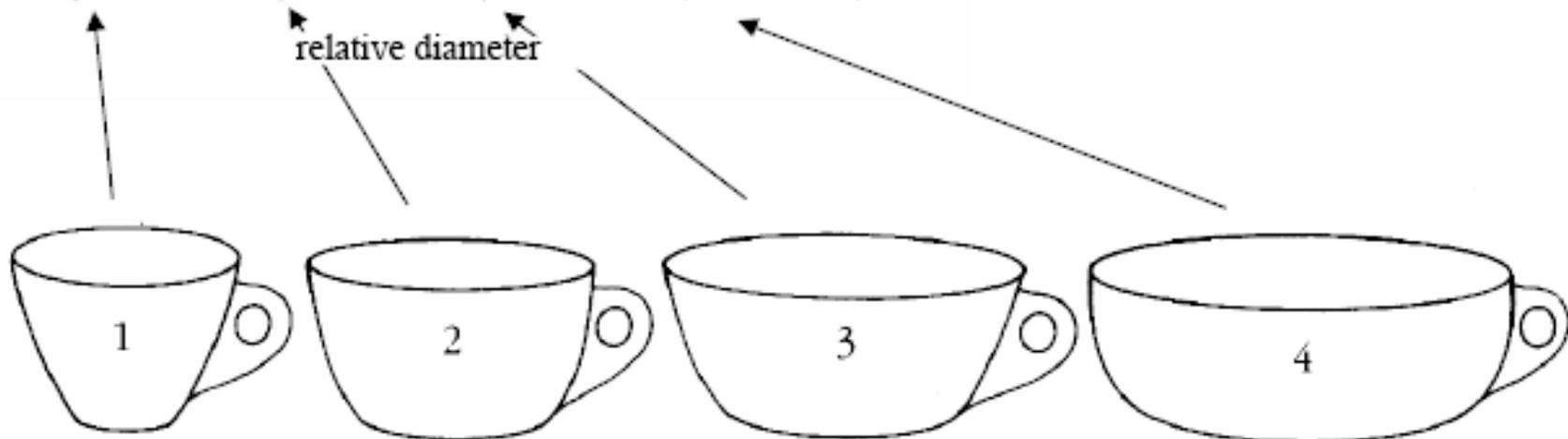
Cup or bowl?



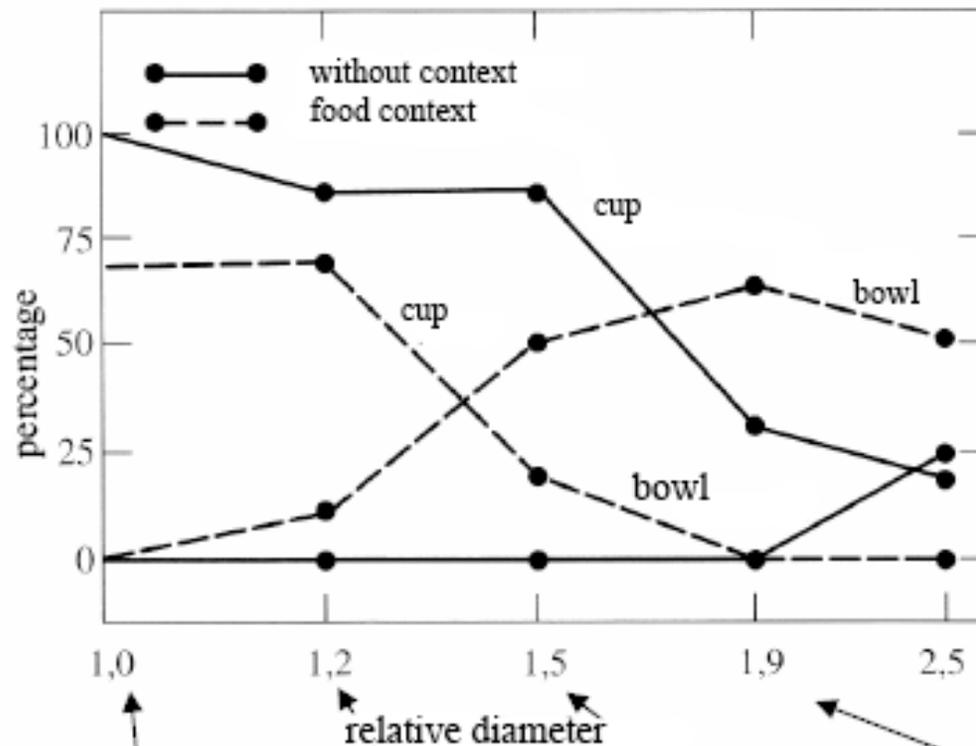
The category depends on complex features of the object (diameter, etc)



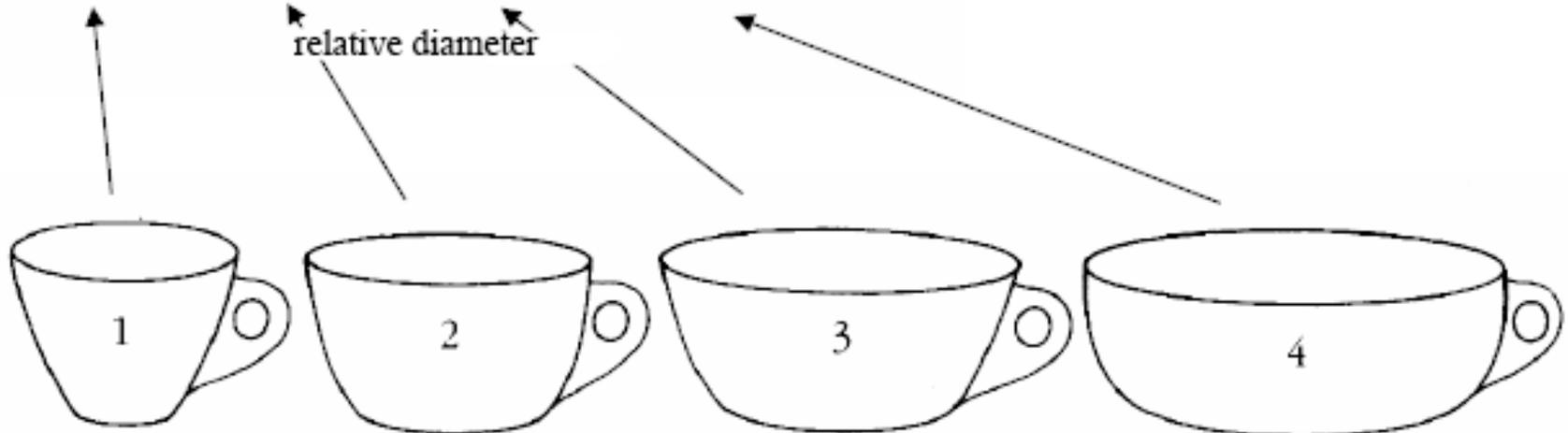
Where does the category „cup“ end?



The category depends on the context!  
(If there is food in it, it's a bowl)



Boundaries between  
cups and bowls  
are context sensitive



# Labov's definition of cup

The term *cup* is used to denote round containers with a ratio of depth to width of  $1 \pm r$  where  $r \leq r_b$ , and  $r_b = \alpha_1 + \alpha_2 + \dots + \alpha_n$  and  $\alpha_i$  is a positive quantity when the feature  $i$  is present and 0 otherwise.

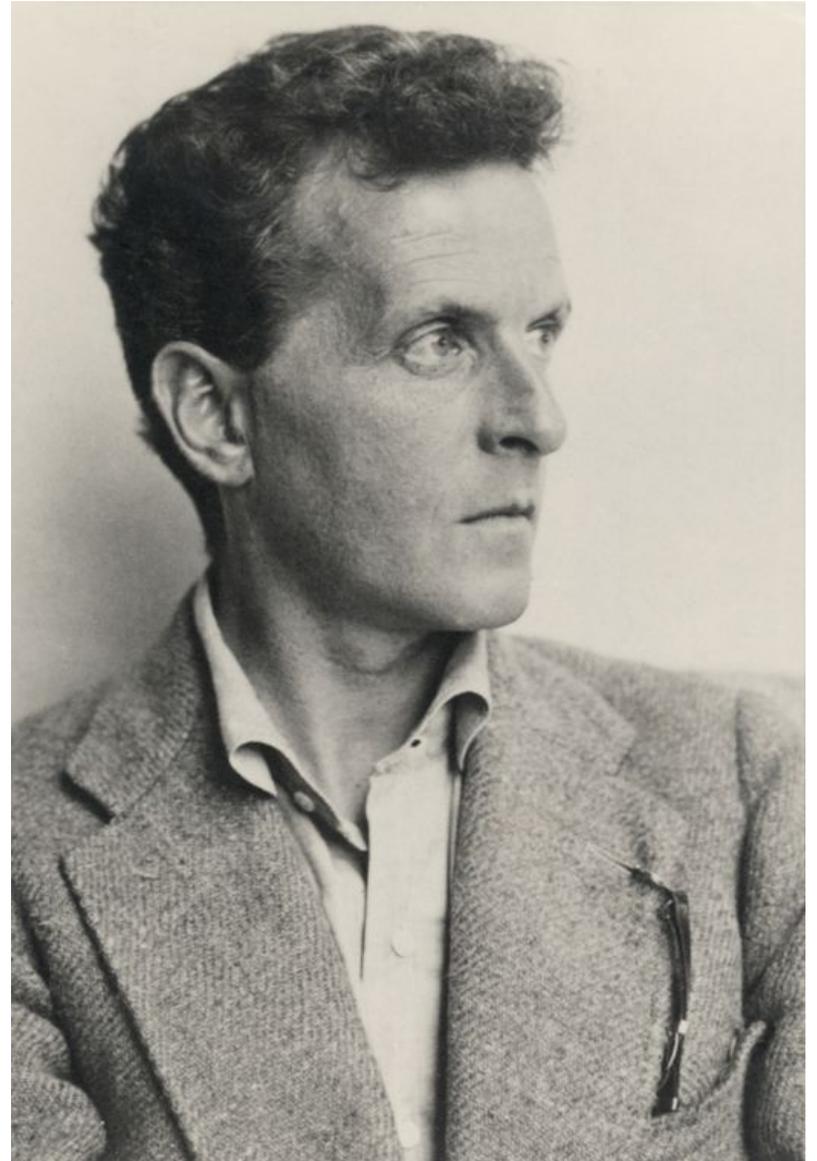
- feature
- 1 = with one handle
  - 2 = made of opaque vitreous material
  - 3 = used for consumption of food
  - 4 = used for the consumption of liquid food
  - 5 = used for consumption of hot liquid food
  - 6 = with a saucer
  - 7 = tapering
  - 8 = circular in cross-section

*Cup* is used variably to denote such containers with ratios width to depth  $1 \pm r$  where  $r_b \leq r \leq r_1$  with a probability of  $r_1 - r / r_1 - r_b$ . The quantity  $1 \pm r_b$  expresses the distance from the modal value of width to height.

# Ludwig Wittgenstein (1889-1951)

Philosopher of  
language

In his late years, a  
proponent of studying  
“ordinary language”



# Wittgenstein (1945)

## *Philosophical Investigations.*

### Paragraphs 66,67

66. Consider for example the proceedings that we call “games”. I mean board-games, card-games, ball-games, Olympic games, and so on. What is common to them all?—Don’t say: “There *must* be something common, or they would not be called ‘games’”—but *look and see* whether there is anything common to all.—For if you look at them you will not see something that is common to *all*, but similarities, relationships, and a whole series of them at that. To repeat: don’t think, but look!—Look for example at board-games, with their multifarious relationships. Now pass to card-games; here you find many correspondences with the first group, but many common features drop out, and others appear. When we pass next to ball-games, much that is common is retained, but much is lost.—Are they all ‘amusing’? Compare chess with noughts and crosses. Or is there always winning and losing, or competition between players? Think of patience. In ball games there is winning and losing; but when a child throws his ball at the wall and catches it again, this feature has disappeared. Look at the parts played by skill and luck; and at the difference between skill in chess and skill in tennis. Think now of games like ring-a-ring-a-roses; here is the element of amusement, but how many other characteristic features have disappeared! And we can go through the many, many other groups of games in the same way; can see how similarities crop up and disappear.

And the result of this examination is: we see a complicated network of similarities overlapping and criss-crossing: sometimes overall similarities, sometimes similarities of detail.

67. I can think of no better expression to characterize these similarities than “family resemblances”; for the various resemblances between members of a family: build, features, colour of eyes, gait, temperament, etc. etc. overlap and criss-cross in the same way.—And I shall say: ‘games’ form a family.

And for instance the kinds of number form a family in the same way. Why do we call something a “number”? Well, perhaps because it has a—direct—relationship with several things that have hitherto been called number; and this can be said to give it an indirect relationship to other things we call the same name. And we extend our concept of number as in spinning a thread we twist fibre on fibre. And the strength of the thread does not reside in the fact that some one fibre runs through its whole length, but in the overlapping of many fibres.

But if someone wished to say: “There is something common to all these constructions—namely the disjunction of all their common properties”—I should reply: Now you are only playing with words. One might as well say: “Something runs through the whole thread—namely the continuous overlapping of those fibres”.



What is a game?

# Wittgenstein's thought experiment on "What is a game":

PI #66:

"Don't say "there must be something common, or they would not be called `games'" —but *look and see* whether there is anything common to all"

Is it amusing?

Is there competition?

Is there long-term strategy?

Is skill required?

Must luck play a role?

Are there cards?

Is there a ball?

# Family Resemblance

Game 1	Game 2	Game 3	Game 4
ABC	BCD	ACD	ABD

“each item has at least one, and probably several, elements in common with one or more items, but no, or few, elements are common to all items” Rosch and Mervis



How about a radically different approach?



# Ludwig Wittgenstein

PI #43:

"The meaning of a word is its use in the language"



# Let's define words by their usages

In particular, words are defined by their environments (the words around them)

**Zellig Harris (1954): If A and B have almost identical environments we say that they are synonyms.**

# What does ongchoi mean?

Suppose you see these sentences:

- Ong choi is delicious **sautéed with garlic**.
- Ong choi is superb **over rice**
- Ong choi **leaves** with salty sauces

And you've also seen these:

- ...spinach **sautéed with garlic over rice**
- Chard stems and **leaves** are **delicious**
- Collard greens and other **salty** leafy greens

Conclusion:

- Ongchoi is a leafy green like spinach, chard, or collard greens

# Ong choy: *Ipomoea aquatica* "Water Spinach"



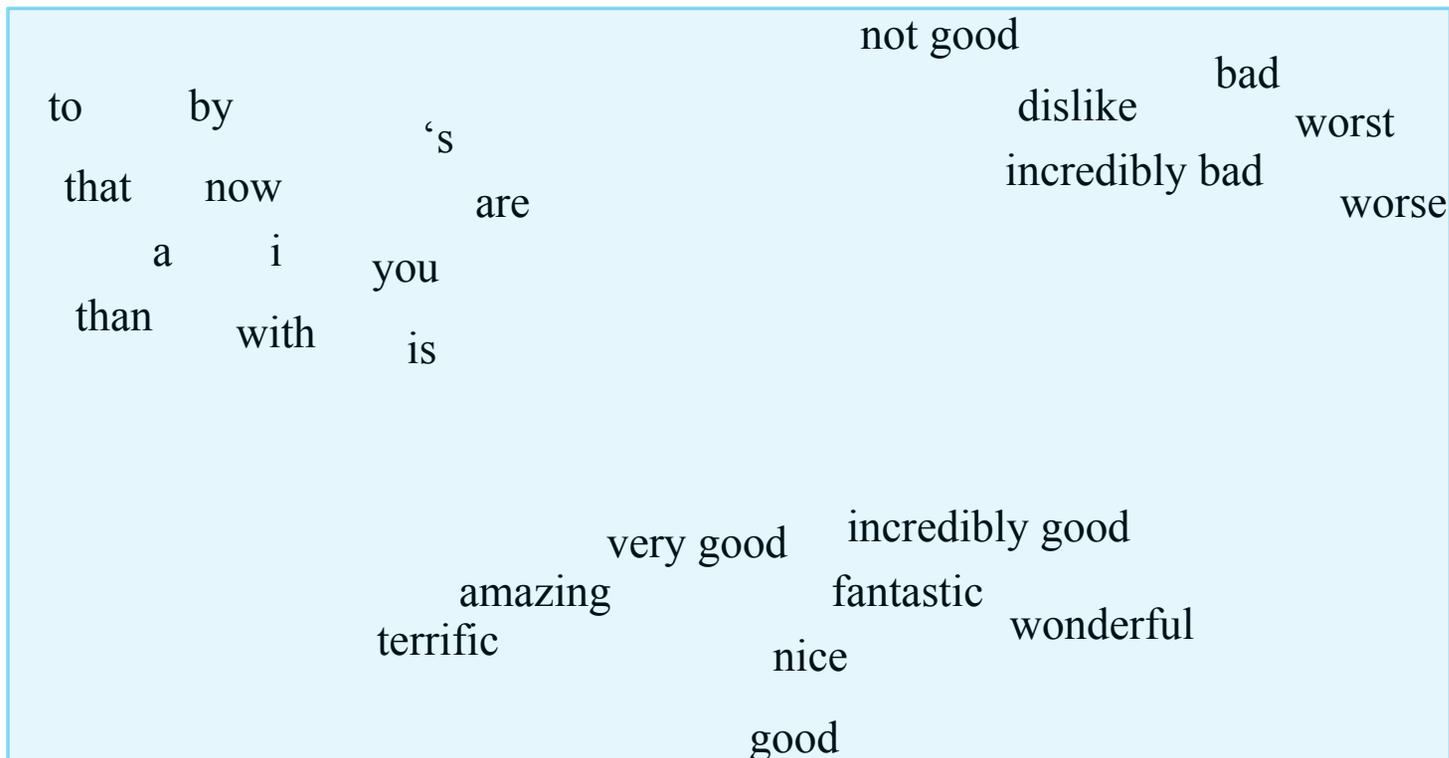
Yamaguchi, Wikimedia Commons, public domain

# We'll build a new model of meaning focusing on similarity

Each word = a vector

- Not just "word" or word45.

Similar words are "nearby in space"



# We define a word as a vector

Called an "embedding" because it's embedded into a space

The standard way to represent meaning in NLP

Fine-grained model of meaning for similarity

- NLP tasks like sentiment analysis
  - With words, requires **same** word to be in training and test
  - With embeddings: ok if **similar** words occurred!!!
- Question answering, conversational agents, etc

# We'll introduce 2 kinds of embeddings

## Tf-idf

- A common baseline model
- Sparse vectors
- Words are represented by a simple function of the counts of nearby words

## Word2vec

- Dense vectors
- Representation is created by training a classifier to distinguish nearby and far-away words



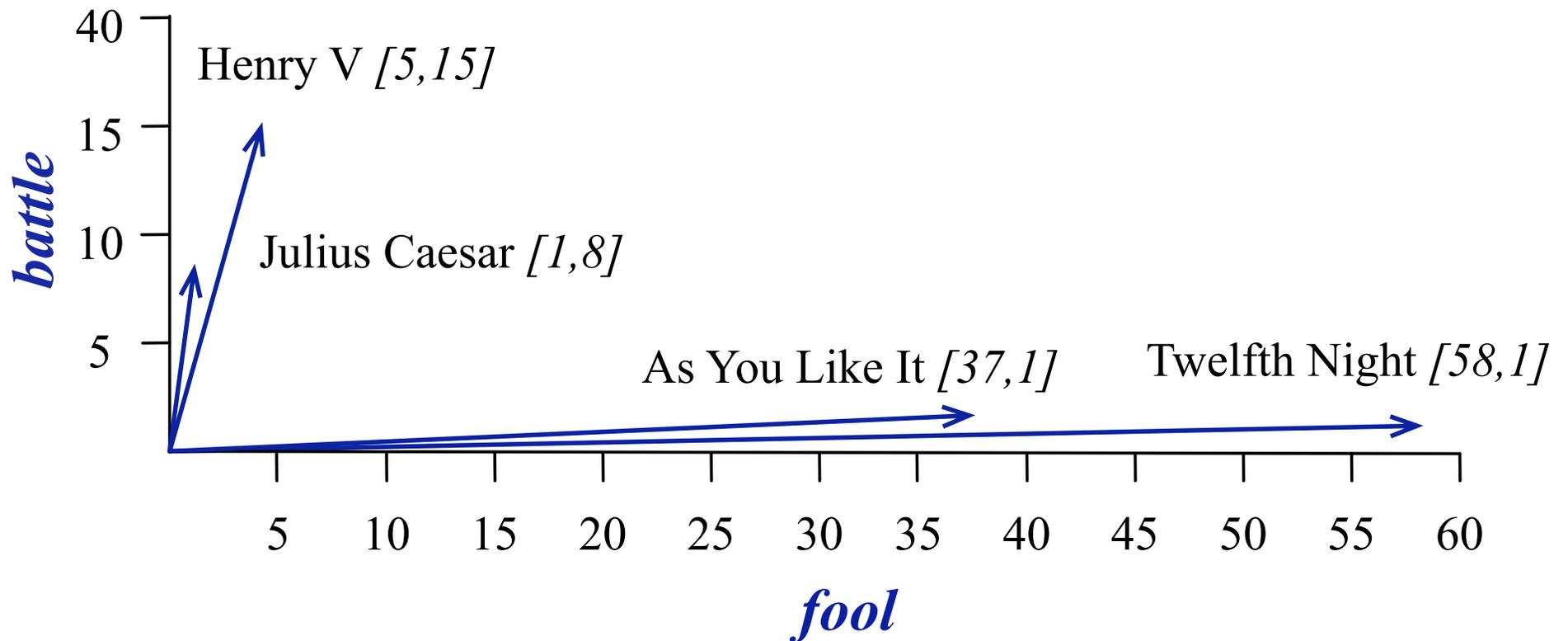
# Review: words, vectors, and co-occurrence matrices

# Term-document matrix

Each document is represented by a vector of words

	<b>As You Like It</b>	<b>Twelfth Night</b>	<b>Julius Caesar</b>	<b>Henry V</b>
<b>battle</b>	1	1	8	15
<b>soldier</b>	2	2	12	36
<b>fool</b>	37	58	1	5
<b>clown</b>	5	117	0	0

# Visualizing document vectors



# Vectors are the basis of information retrieval

	As You Like It	Twelfth Night	Julius Caesar	Henry V
<b>battle</b>	1	1	8	15
<b>soldier</b>	2	2	12	36
<b>fool</b>	37	58	1	5
<b>clown</b>	5	117	0	0

Vectors are similar for the two comedies

*As You like It* [1,2,37,5],

*Twelfth Night* [1,2,58,117]

Different than the history:

*Henry V* [15,36,5,0]

Comedies have more fools and clowns and fewer soldiers and battles.

# Words can be vectors too

	As You Like It	Twelfth Night	Julius Caesar	Henry V
<b>battle</b>	1	1	8	15
<b>soldier</b>	2	2	12	36
<b>fool</b>	37	58	1	5
<b>clown</b>	5	117	0	0
<b>fool</b>	37	58	1	5
<b>clown</b>	5	117	0	0

*Battle* is "the kind of word that occurs in Julius Caesar and Henry V"

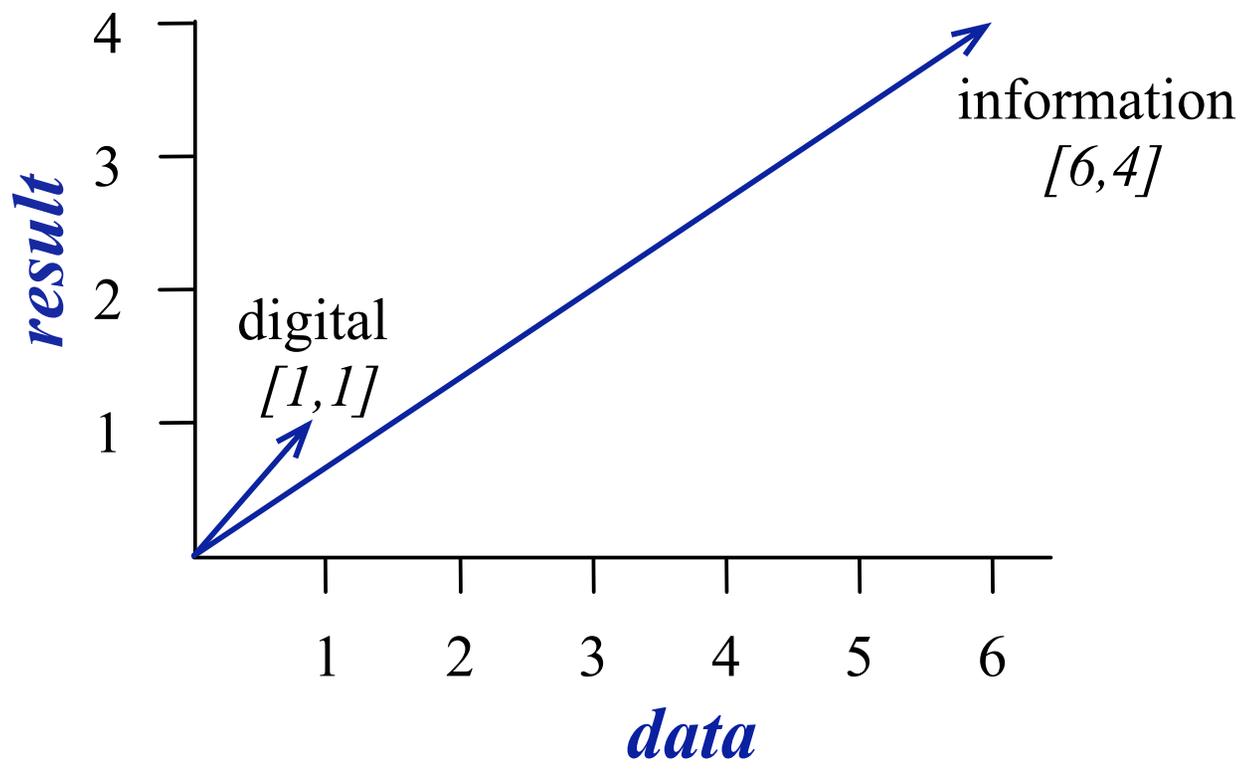
*Clown* is "the kind of word that occurs a lot in Twelfth Night and a bit in As You Like It"

# More common: word-word matrix (or "term-context matrix")

Two **words** are similar in meaning if their context vectors are similar

sugar, a sliced lemon, a tablespoonful of **apricot** jam, a pinch each of,  
their enjoyment. Cautiously she sampled her first **pineapple** and another fruit whose taste she likened  
well suited to programming on the digital **computer.** In finding the optimal R-stage policy from  
for the purpose of gathering data and **information** necessary for the study authorized in the

	aardvark	computer	data	pinch	result	sugar	...
apricot	0	0	0	1	0	1	
pineapple	0	0	0	1	0	1	
digital	0	2	1	0	1	0	
information	0	1	6	0	4	0	



# Reminders from linear algebra

$$\text{dot-product}(\vec{v}, \vec{w}) = \vec{v} \cdot \vec{w} = \sum_{i=1}^N v_i w_i = v_1 w_1 + v_2 w_2 + \dots + v_N w_N$$

$$\text{vector length } |\vec{v}| = \sqrt{\sum_{i=1}^N v_i^2}$$

# Cosine for computing similarity Sec. 6.3

$$\text{cosine}(\vec{v}, \vec{w}) = \frac{\vec{v} \cdot \vec{w}}{|\vec{v}| |\vec{w}|} = \frac{\sum_{i=1}^N v_i w_i}{\sqrt{\sum_{i=1}^N v_i^2} \sqrt{\sum_{i=1}^N w_i^2}}$$

$v_i$  is the count for word  $v$  in context  $i$

$w_i$  is the count for word  $w$  in context  $i$ .

→ →

Cos( $v, w$ ) is the cosine similarity of  $v$  and  $w$

→ →

$$\vec{a} \cdot \vec{b} = |\vec{a}| |\vec{b}| \cos \theta$$

$$\frac{\vec{a} \cdot \vec{b}}{|\vec{a}| |\vec{b}|} = \cos \theta$$

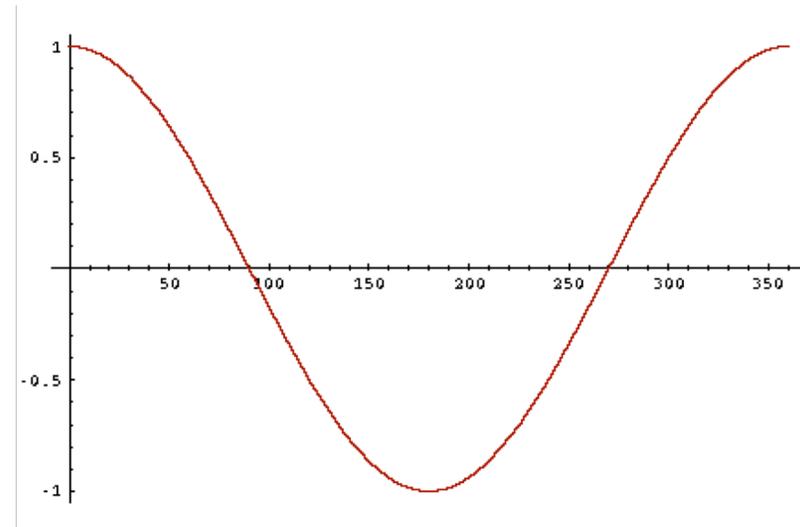
# Cosine as a similarity metric

-1: vectors point in opposite directions

+1: vectors point in same directions

0: vectors are orthogonal

Frequency is non-negative, so cosine range 0-1



$$\cos(\vec{v}, \vec{w}) = \frac{\vec{v} \cdot \vec{w}}{|\vec{v}| |\vec{w}|} = \frac{\vec{v}}{|\vec{v}|} \cdot \frac{\vec{w}}{|\vec{w}|} = \frac{\sum_{i=1}^N v_i w_i}{\sqrt{\sum_{i=1}^N v_i^2} \sqrt{\sum_{i=1}^N w_i^2}}$$

Which pair of words is more similar?

cosine(apricot, information) =

$$\frac{1+0+0}{\sqrt{1+0+0} \sqrt{1+36+1}} = \frac{1}{\sqrt{38}} = .16$$

cosine(digital, information) =

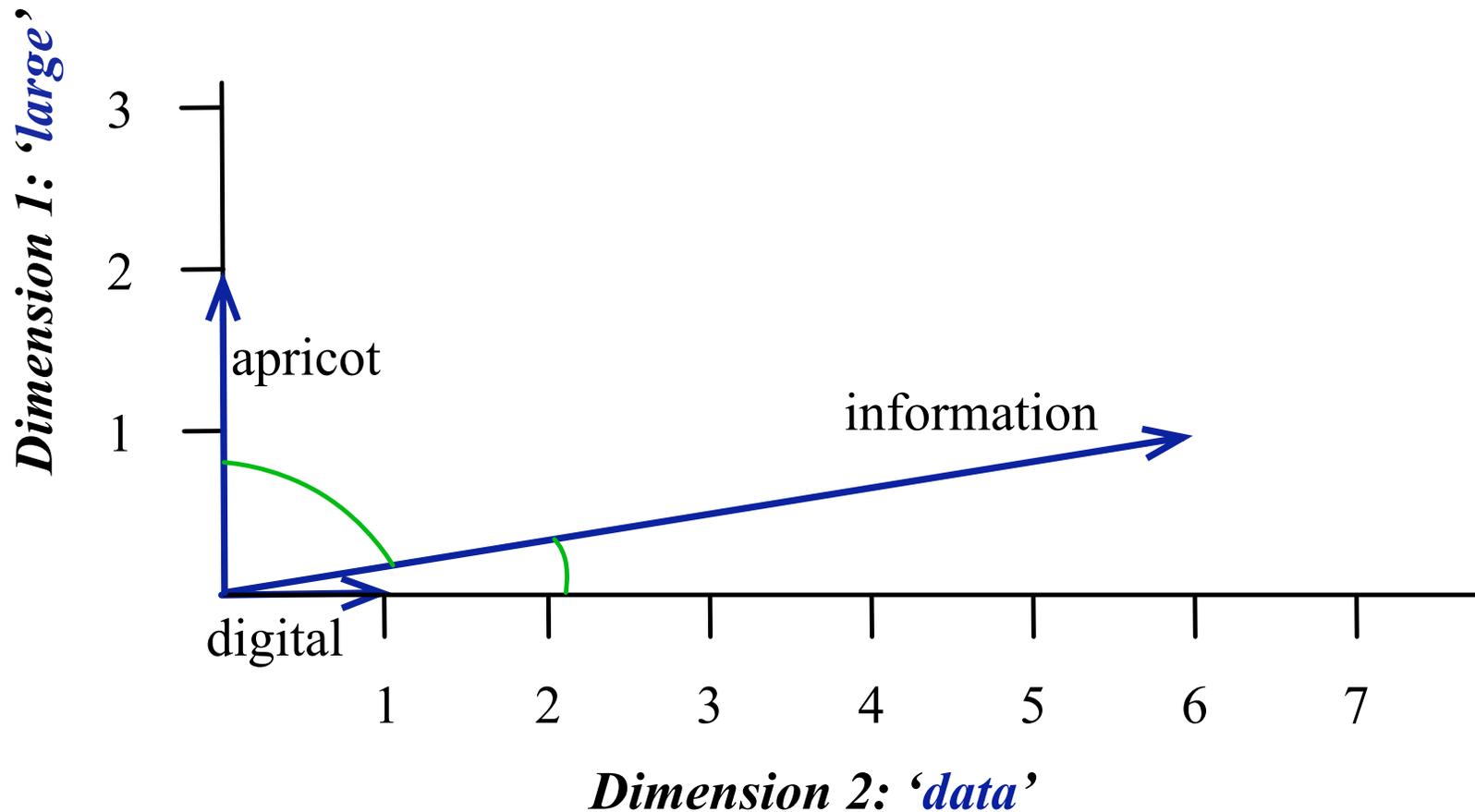
$$\frac{0+6+2}{\sqrt{0+1+4} \sqrt{1+36+1}} = \frac{8}{\sqrt{38}\sqrt{5}} = .58$$

cosine(apricot, digital) =

$$\frac{0+0+0}{\sqrt{1+0+0} \sqrt{0+1+4}} = 0$$

	large	data	computer
apricot	1	0	0
digital	0	1	2
information	1	6	1

# Visualizing cosines (well, angles)





# But raw frequency is a bad representation

Frequency is clearly useful; if *sugar* appears a lot near *apricot*, that's useful information.

But overly frequent words like *the*, *it*, or *they* are not very informative about the context

Need a function that resolves this frequency paradox!

# tf-idf: combine two factors

**tf: term frequency.** Just raw frequency count (or possible log frequency)

**Idf: inverse document frequency: tf-**

$$\text{idf}_i = \log \left( \frac{N}{\text{df}_i} \right)$$

Total # of docs in collection

# of docs that have word i

Words like "the" have very low idf

tf-idf value for word i in document j:

$$w_{ij} = \text{tf}_{ij} \text{idf}_i$$

# Summary: tf-idf

Compare two words using tf-idf cosine to see if they are similar

Compare two documents

- Take the centroid of vectors of all the words in the document
- Centroid document vector is:

$$d = \frac{w_1 + w_2 + \dots + w_k}{k}$$

# Tf-idf is a sparse representation

## Tf-idf vectors are

- **long** (length  $|V| = 20,000$  to  $50,000$ )
- **sparse** (most elements are zero)



# Alternative: dense vectors

vectors which are

- **short** (length 50-1000)
- **dense** (most elements are non-zero)

# Sparse versus dense vectors

## Why dense vectors?

- Short vectors may be easier to use as **features** in machine learning (less weights to tune)
- Dense vectors may **generalize** better than storing explicit counts
- They may do better at capturing synonymy:
  - *car* and *automobile* are synonyms; but are distinct dimensions
  - a word with *car* as a neighbor and a word with *automobile* as a neighbor should be similar, but aren't
- **In practice, they work better**

# Dense embeddings you can download!

Word2vec (Mikolov et al.)



<https://code.google.com/archive/p/word2vec/>

Glove (Pennington, Socher, Manning)

<http://nlp.stanford.edu/projects/glove/>





Word2vec

Popular embedding method

Very fast to train

Code available on the web

Idea: **predict** rather than **count**

# Word2vec

- Instead of **counting** how often each word  $w$  occurs near "*apricot*"
- Train a classifier on a binary **prediction** task:
  - Is  $w$  likely to show up near "*apricot*"?
- We don't actually care about this task
  - But we'll take the learned classifier weights as the word embeddings

# Brilliant insight: Use running text as implicitly supervised training data!

- A word  $s$  near *apricot*
  - Acts as gold ‘correct answer’ to the question
  - “Is word  $w$  likely to show up near *apricot*?”
- No need for hand-labeled supervision
- The idea comes from **neural language modeling**
  - Bengio et al. (2003)
  - Collobert et al. (2011)

# Word2Vec: Skip-Gram Task

Word2vec provides a variety of options. Let's do

- "skip-gram with negative sampling" (SGNS)

# Skip-gram algorithm

1. Treat the target word and a neighboring context word as positive examples.
2. Randomly sample other words in the lexicon to get negative samples
3. Use logistic regression to train a classifier to distinguish those two cases
4. Use the weights as the embeddings

# Skip-Gram Training Data

Training sentence:

... lemon, a **tablespoon of apricot jam** a pinch ...

c1            c2 target c3    c4

Assume context words are those in +/- 2  
word window

# Skip-Gram Goal

Given a tuple  $(t,c)$  = target, context

- (*apricot*, *jam*)
- (*apricot*, *aardvark*)

Return probability that  $c$  is a real context word:

$$P(+ | t,c)$$

$$P(- | t,c) = 1 - P(+ | t,c)$$

# How to compute $p(+ | t, c)$ ?

Intuition:

- Words are likely to appear near similar words
- Model similarity with dot-product!
- $\text{Similarity}(t, c) \propto t \cdot c$

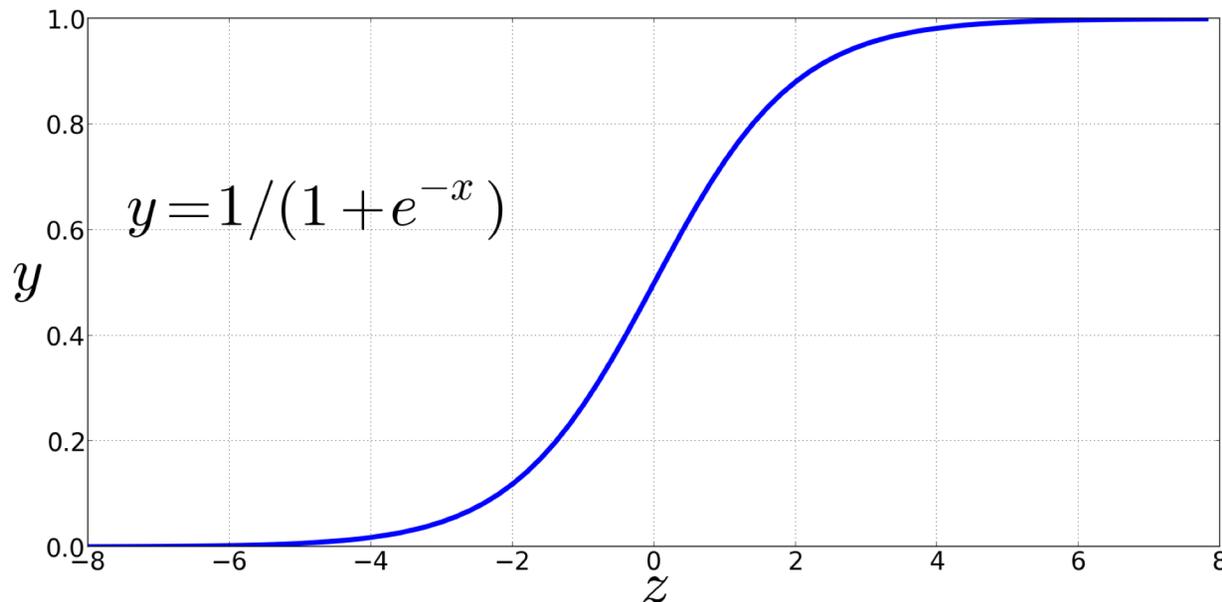
*Problem:*

- *Dot product is not a probability!*
  - *(Neither is cosine)*

# Turning dot product into a probability

The sigmoid lies between 0 and 1:

$$\sigma(x) = \frac{1}{1 + e^{-x}}$$



# Turning dot product into a probability

$$P(+|t, c) = \frac{1}{1 + e^{-t \cdot c}}$$

$$\begin{aligned} P(-|t, c) &= 1 - P(+|t, c) \\ &= \frac{e^{-t \cdot c}}{1 + e^{-t \cdot c}} \end{aligned}$$

For all the context words:

Assume all context words are independent

$$P(+|t, c_{1:k}) = \prod_{i=1}^{\kappa} \frac{1}{1 + e^{-t \cdot c_i}}$$

$$\log P(+|t, c_{1:k}) = \sum_{i=1}^k \log \frac{1}{1 + e^{-t \cdot c_i}}$$

# Skip-Gram Training Data

Training sentence:

... lemon, a **tablespoon of apricot jam** a pinch ...

c1                    c2    t            c3    c4

Training data: input/output pairs centering  
on *apricot*

Asssume a +/- 2 word window

# Skip-Gram Training

Training sentence:

... lemon, a **tablespoon of apricot jam** a pinch ...

c1

c2

t

c3

c4

**positive examples +**

t

c

---

apricot tablespoon

apricot of

apricot preserves

apricot or

- For each positive example, we'll create  $k$  negative examples.
- Using *noise* words
- Any random word that isn't  $t$

# Skip-Gram Training

Training sentence:

... lemon, a **tablespoon of apricot jam** a pinch ...

c1

c2

t

c3

c4

**positive examples +**

t

c

---

apricot tablespoon

apricot of

apricot preserves

apricot or

**negative examples -**

k=2

t

c

t

c

---

apricot aardvark apricot twelve

apricot puddle apricot hello

apricot where apricot dear

apricot coaxial apricot forever

# Choosing noise words

Could pick  $w$  according to their unigram frequency  $P(w)$

More common to chosen then according to  $p_\alpha(w)$

$$P_\alpha(w) = \frac{\text{count}(w)^\alpha}{\sum_w \text{count}(w)^\alpha}$$

$\alpha = \frac{3}{4}$  works well because it gives rare noise words slightly higher probability

To show this, imagine two events  $p(a) = .99$  and  $p(b) = .01$ :

$$P_\alpha(a) = \frac{.99^{.75}}{.99^{.75} + .01^{.75}} = .97$$

$$P_\alpha(b) = \frac{.01^{.75}}{.99^{.75} + .01^{.75}} = .03$$

# Setup

Let's represent words as vectors of some length (say 300), randomly initialized.

So we start with  $300 * V$  random parameters

Over the entire training set, we'd like to adjust those word vectors such that we

- Maximize the similarity of the **target word, context word** pairs (t,c) drawn from the positive data
- Minimize the similarity of the (t,c) pairs drawn from the negative data.

# Learning the classifier

Iterative process.

We'll start with 0 or random weights

Then adjust the word weights to

- make the positive pairs more likely
- and the negative pairs less likely

over the entire training set:

# Objective Criteria

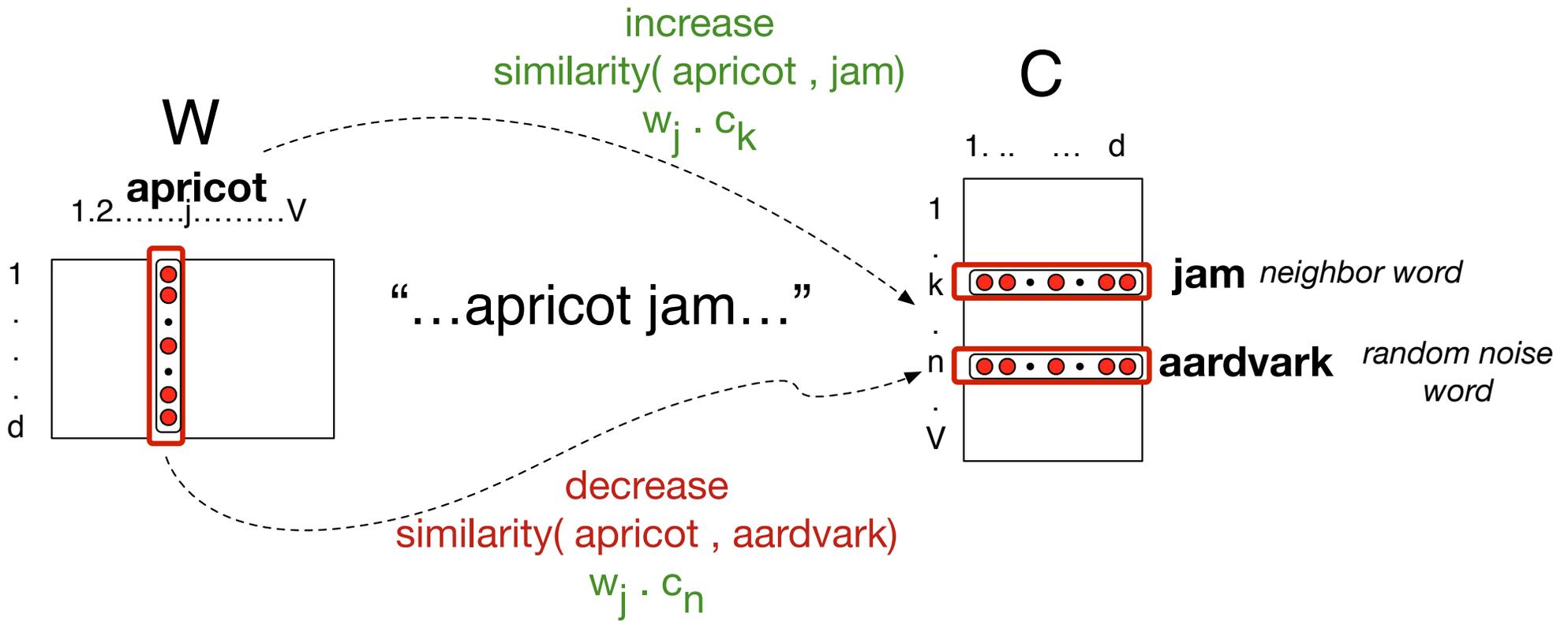
We want to maximize...

$$\sum_{(t,c) \in +} \log P(+|t, c) + \sum_{(t,c) \in -} \log P(-|t, c)$$

Maximize the + label for the pairs from the positive training data, and the – label for the pairs sample from the negative data.

Focusing on one target word  $t$ :

$$\begin{aligned} L(\theta) &= \log P(+|t, c) + \sum_{i=1} \log P(-|t, n_i) \\ &= \log \sigma(c \cdot t) + \sum_{i=1}^k \log \sigma(-n_i \cdot t) \\ &= \log \frac{1}{1 + e^{-c \cdot t}} + \sum_{i=1}^k \log \frac{1}{1 + e^{n_i \cdot t}} \end{aligned}$$





# Train using gradient descent

Actually learns two separate embedding matrices  $W$  and  $C$

Can use  $W$  and throw away  $C$ , or merge them somehow

# Summary: How to learn word2vec (skip-gram) embeddings

Start with  $V$  random 300-dimensional vectors as initial embeddings

Use logistic regression, the second most basic classifier used in machine learning after naïve bayes

- Take a corpus and take pairs of words that co-occur as positive examples
- Take pairs of words that don't co-occur as negative examples
- Train the classifier to distinguish these by slowly adjusting all the embeddings to improve the classifier performance
- Throw away the classifier code and keep the embeddings.

# Evaluating embeddings

Compare to human scores on word similarity-type tasks:

- WordSim-353 (Finkelstein et al., 2002)
- SimLex-999 (Hill et al., 2015)
- Stanford Contextual Word Similarity (SCWS) dataset (Huang et al., 2012)
- TOEFL dataset: *Levied is closest in meaning to: imposed, believed, requested, correlated*

# Properties of embeddings

Similarity depends on window size  $C$

$C = \pm 2$  The nearest words to *Hogwarts*:

- *Sunnydale*
- *Evernight*

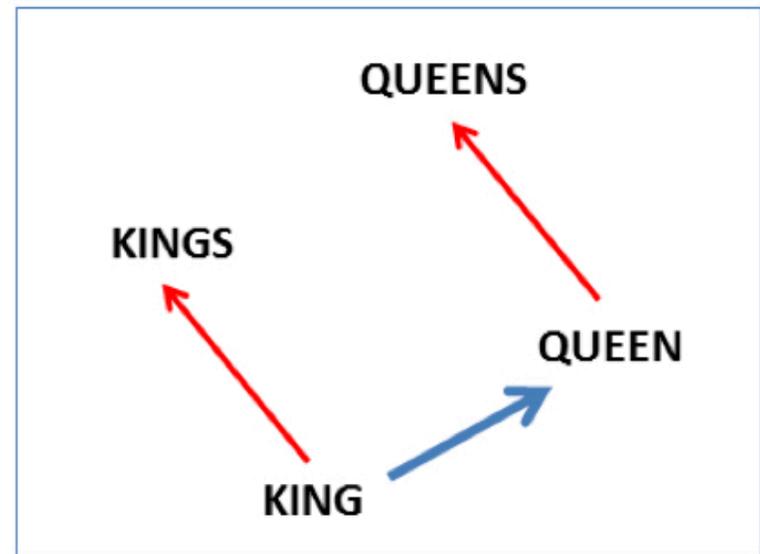
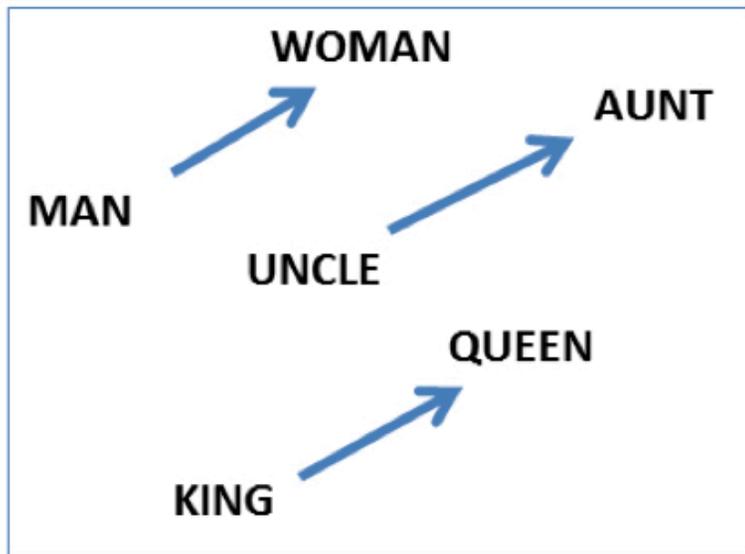
$C = \pm 5$  The nearest words to *Hogwarts*:

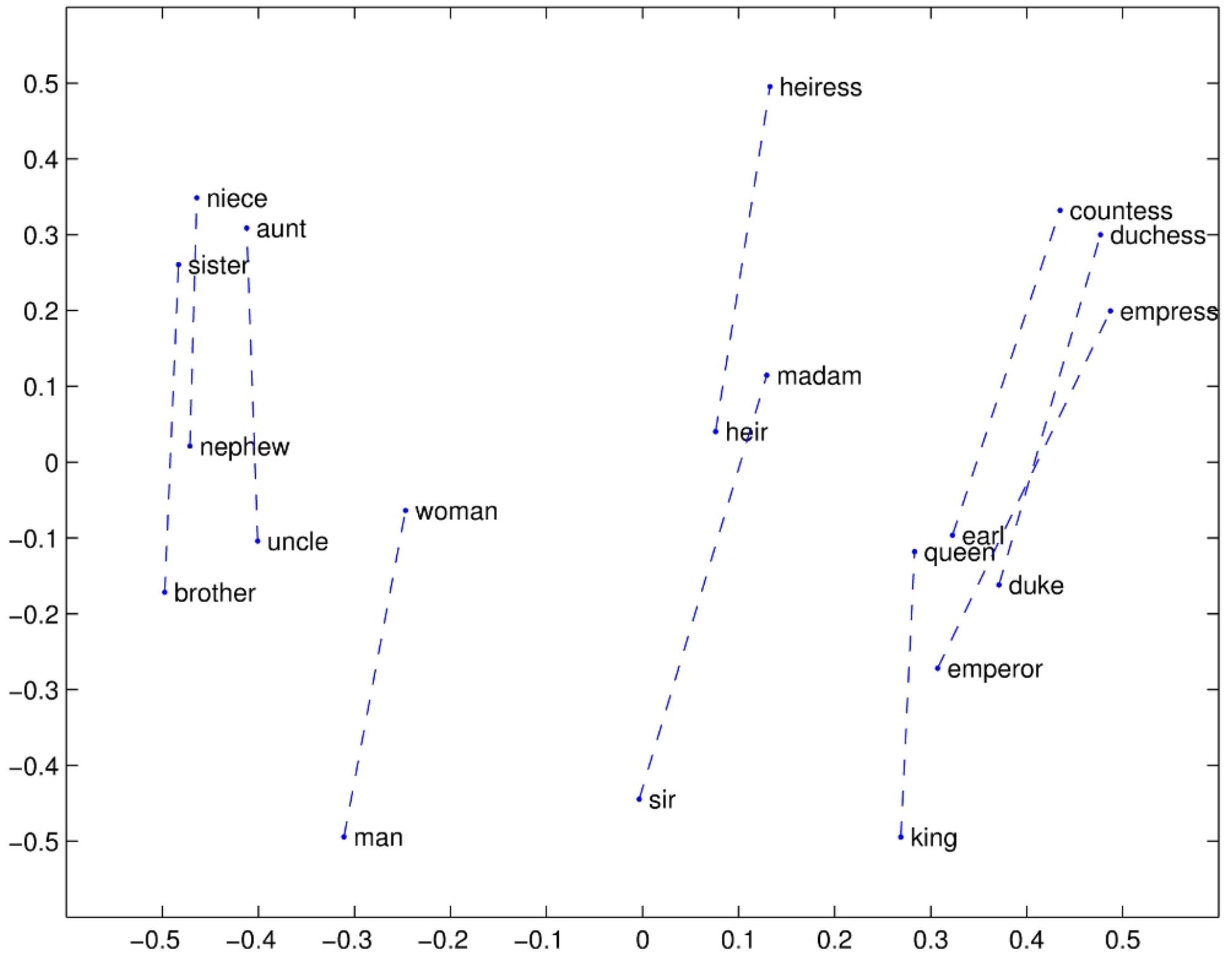
- *Dumbledore*
- *Malfoy*
- *halfblood*

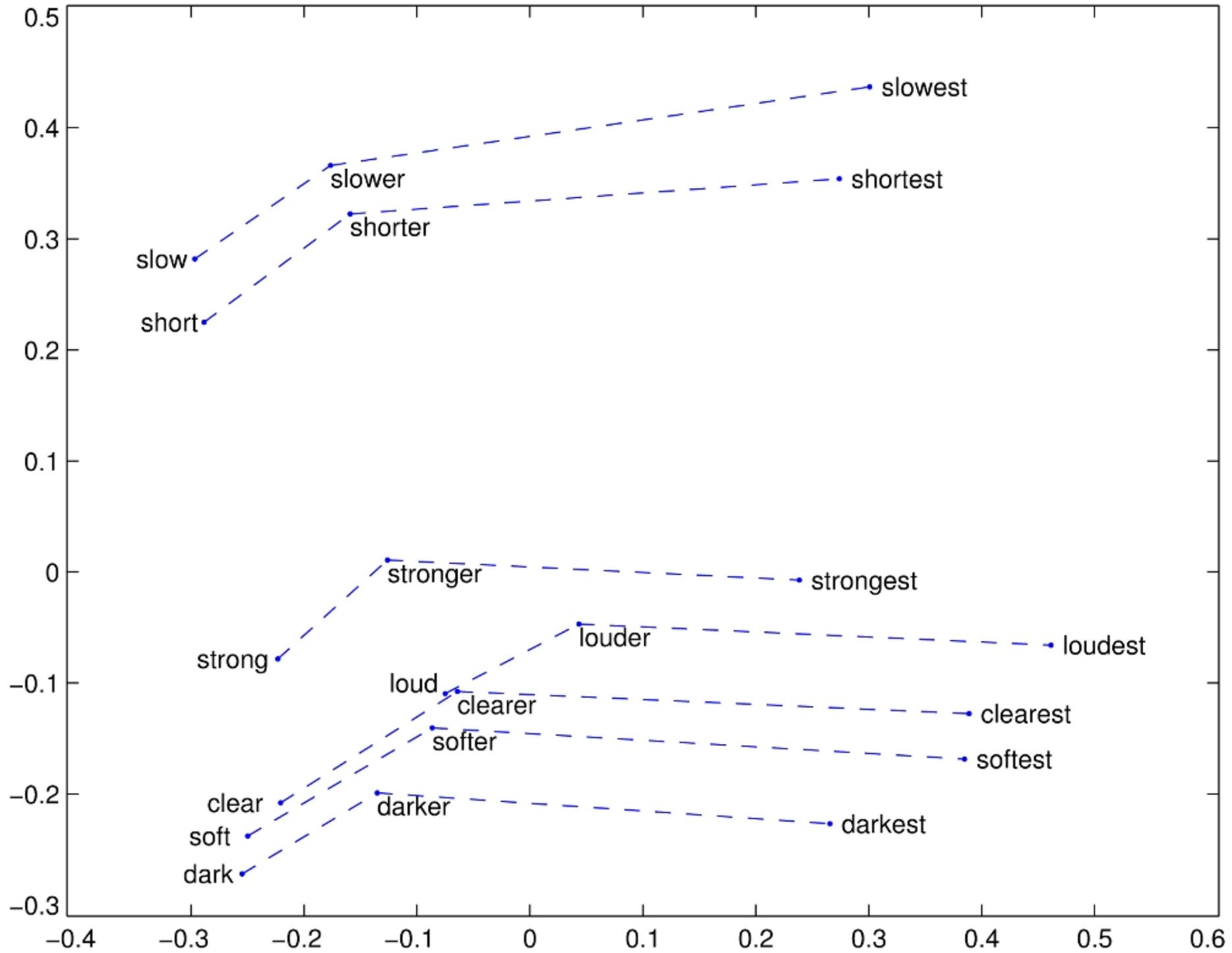
# Analogy: Embeddings capture relational meaning!

$\text{vector}('king') - \text{vector}('man') + \text{vector}('woman') \approx \text{vector}('queen')$

$\text{vector}('Paris') - \text{vector}('France') + \text{vector}('Italy') \approx \text{vector}('Rome')$







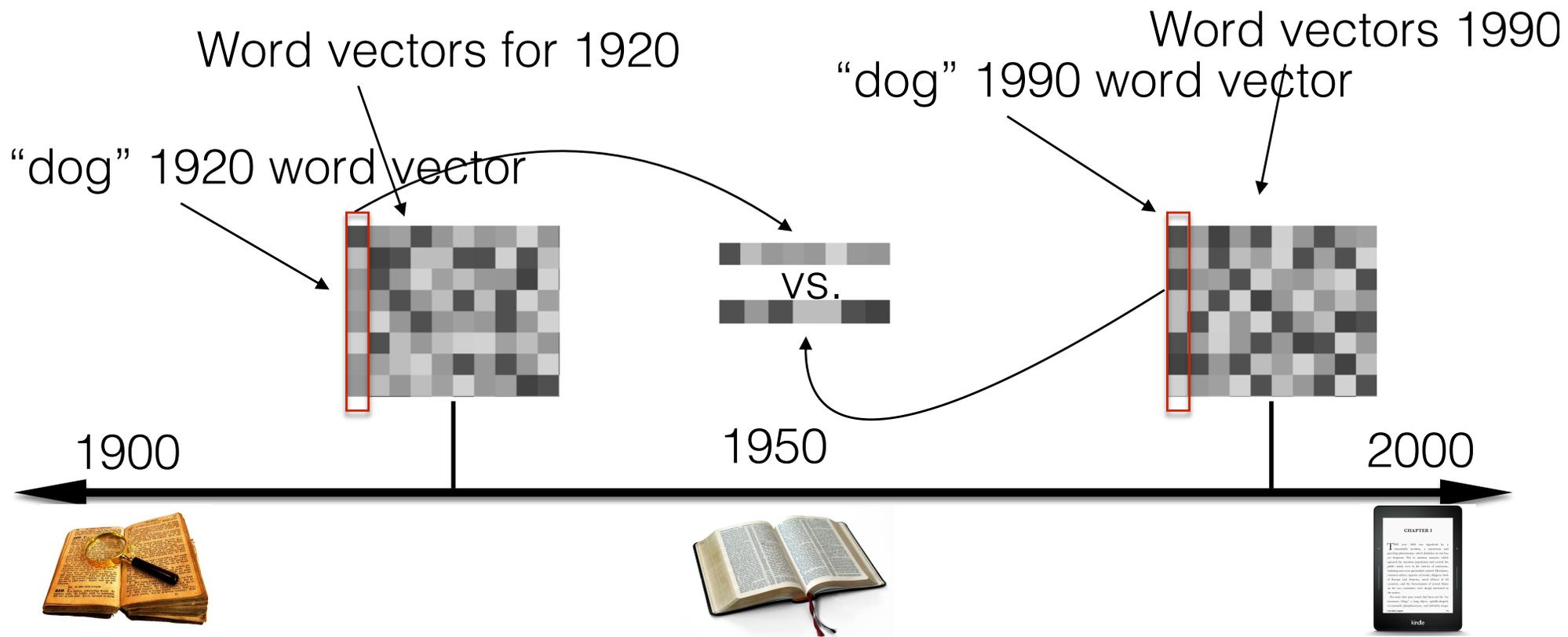
Embeddings can help study  
word history!

Train embeddings on old books to study  
changes in word meaning!!



Will Hamilton

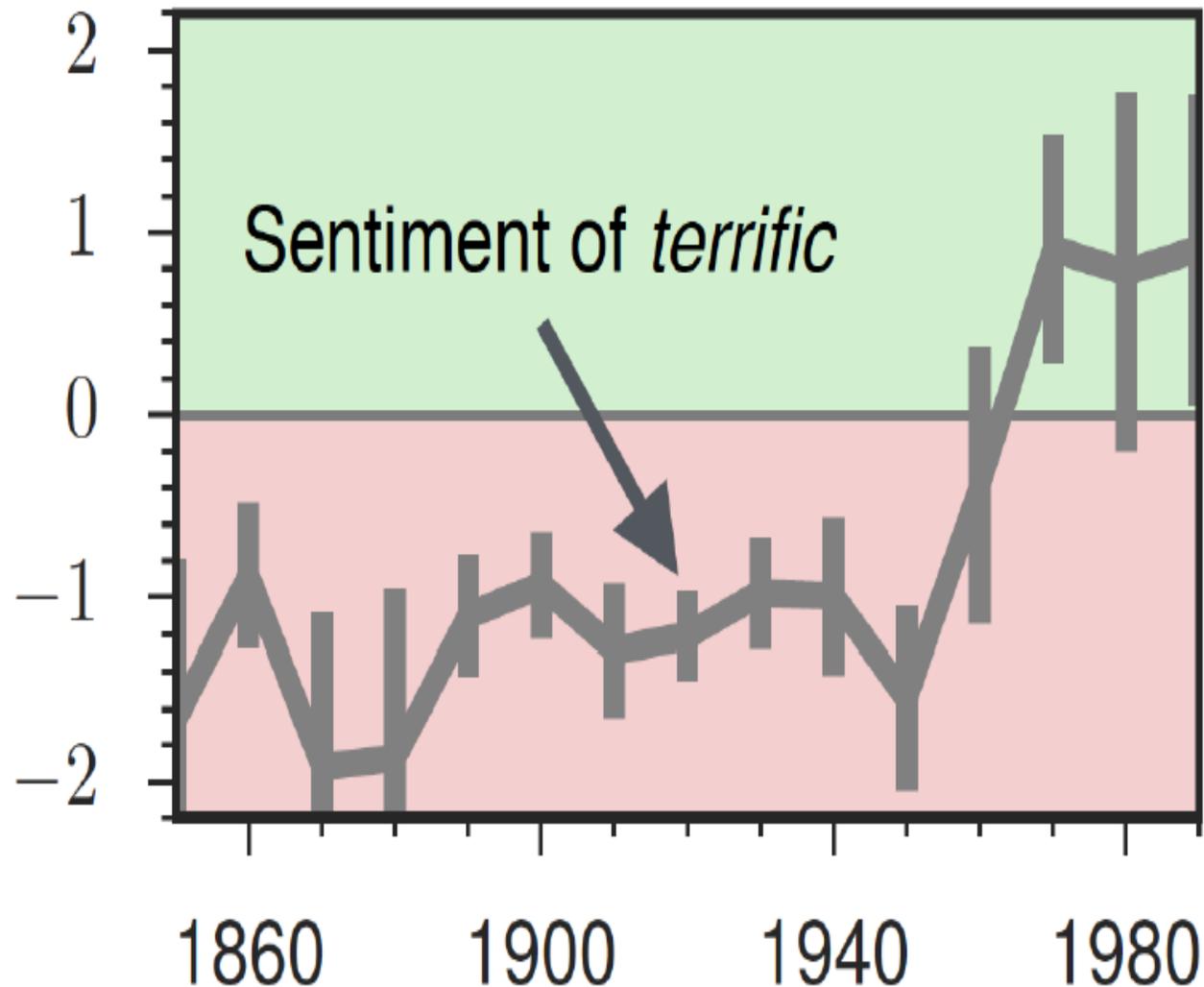
# Diachronic word embeddings for studying language change!





# The evolution of sentiment words

Negative words change faster than positive words





# Embeddings and bias

# Embeddings reflect cultural bias

Bolukbasi, Tolga, Kai-Wei Chang, James Y. Zou, Venkatesh Saligrama, and Adam T. Kalai. "Man is to computer programmer as woman is to homemaker? debiasing word embeddings." In *Advances in Neural Information Processing Systems*, pp. 4349-4357. 2016.

Ask “Paris : France :: Tokyo : x”

- x = Japan

Ask “father : doctor :: mother : x”

- x = nurse

Ask “man : computer programmer :: woman : x”

- x = homemaker

# Embeddings reflect cultural bias

Caliskan, Aylin, Joanna J. Bruson and Arvind Narayanan. 2017. Semantics derived automatically from language corpora contain human-like biases. *Science* 356:6334, 183-186.

Implicit Association test (Greenwald et al 1998): How associated are

- concepts (*flowers, insects*) & attributes (*pleasantness, unpleasantness*)?
- Studied by measuring timing latencies for categorization.

Psychological findings on US participants:

- African-American names are associated with unpleasant words (more than European-American names)
- Male names associated more with math, female names with arts
- Old people's names with unpleasant words, young people with pleasant words.

Caliskan et al. replication with embeddings:

- African-American names (*Leroy, Shaniqua*) had a higher GloVe cosine with unpleasant words (*abuse, stink, ugly*)
- European American names (*Brad, Greg, Courtney*) had a higher cosine with pleasant words (*love, peace, miracle*)

Embeddings reflect and replicate all sorts of pernicious biases.

# Directions

## Debiasing algorithms for embeddings

- Bolukbasi, Tolga, Chang, Kai-Wei, Zou, James Y., Saligrama, Venkatesh, and Kalai, Adam T. (2016). Man is to computer programmer as woman is to homemaker? debiasing word embeddings. In *Advances in Neural Information Processing Systems*, pp. 4349–4357.

Use embeddings as a historical tool to study bias

# Embeddings as a window onto history

Garg, Nikhil, Schiebinger, Londa, Jurafsky, Dan, and Zou, James (2018). Word embeddings quantify 100 years of gender and ethnic stereotypes. *Proceedings of the National Academy of Sciences*, 115(16), E3635–E3644

## Use the Hamilton historical embeddings

The cosine similarity of embeddings for decade X for occupations (like teacher) to male vs female names

- Is correlated with the actual percentage of women teachers in decade X

# History of biased framings of women

Garg, Nikhil, Schiebinger, Londa, Jurafsky, Dan, and Zou, James (2018). Word embeddings quantify 100 years of gender and ethnic stereotypes. *Proceedings of the National Academy of Sciences*, 115(16), E3635–E3644

Embeddings for competence adjectives are biased toward men

- *Smart, wise, brilliant, intelligent, resourceful, thoughtful, logical, etc.*

This bias is slowly decreasing

# Embeddings reflect ethnic stereotypes over time

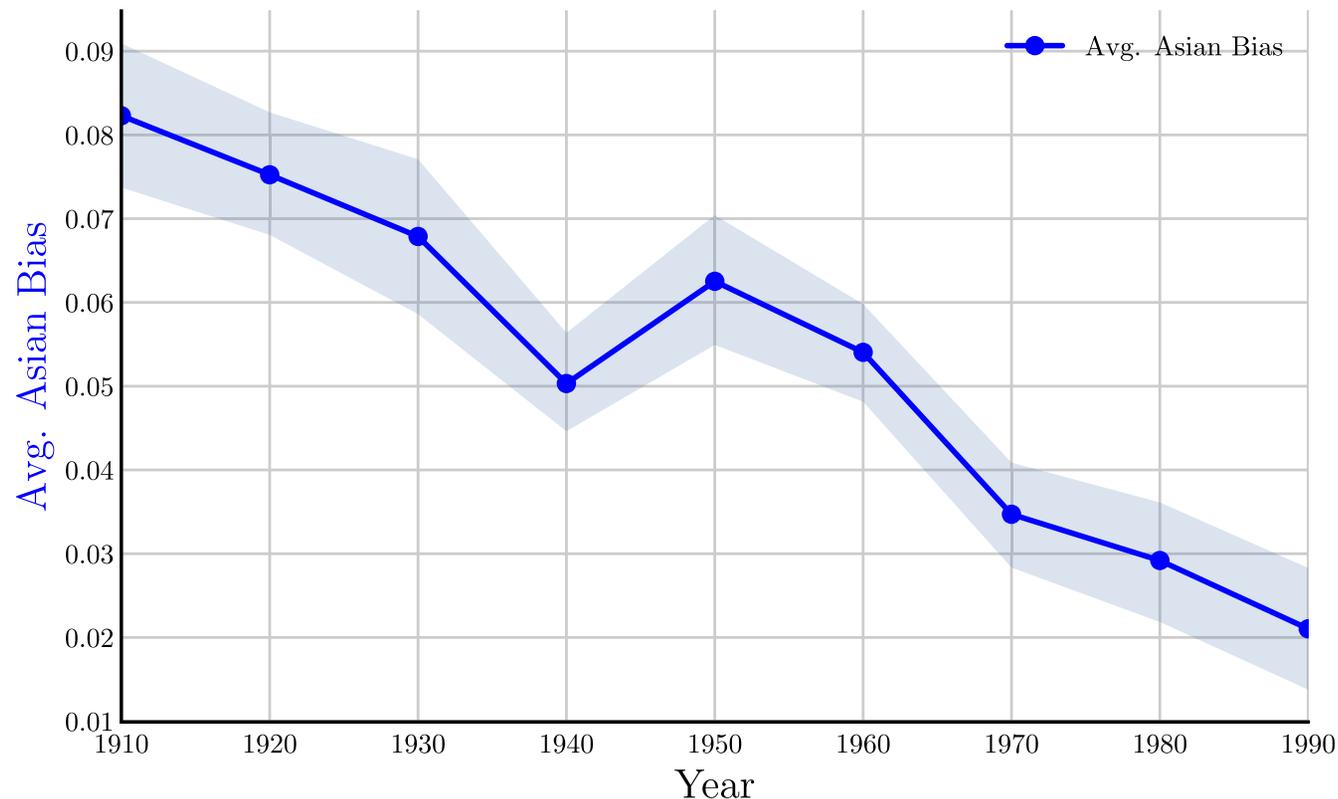
Garg, Nikhil, Schiebinger, Londa, Jurafsky, Dan, and Zou, James (2018). Word embeddings quantify 100 years of gender and ethnic stereotypes. *Proceedings of the National Academy of Sciences*, 115(16), E3635–E3644

- Princeton trilogy experiments
- Attitudes toward ethnic groups (1933, 1951, 1969) scores for adjectives
  - *industrious, superstitious, nationalistic, etc*
- Cosine of Chinese name embeddings with those adjective embeddings correlates with human ratings.

# Change in linguistic framing 1910-1990

Garg, Nikhil, Schiebinger, Londa, Jurafsky, Dan, and Zou, James (2018). Word embeddings quantify 100 years of gender and ethnic stereotypes. *Proceedings of the National Academy of Sciences*, 115(16), E3635–E3644

## Change in association of Chinese names with adjectives framed as "othering" (*barbaric, monstrous, bizarre*)



# Changes in framing: adjectives associated with Chinese

Garg, Nikhil, Schiebinger, Londa, Jurafsky, Dan, and Zou, James (2018). Word embeddings quantify 100 years of gender and ethnic stereotypes. *Proceedings of the National Academy of Sciences*, 115(16), E3635–E3644

1910

1950

1990

---

Irresponsible

Disorganized

Inhibited

Envious

Outrageous

Passive

Barbaric

Pompous

Dissolute

Aggressive

Unstable

Haughty

Transparent

Effeminate

Complacent

Monstrous

Unprincipled

Forceful

Hateful

Venomous

Fixed

Cruel

Disobedient

Active

Greedy

Predatory

Sensitive

Bizarre

Boisterous

Hearty

---

# Conclusion

## **Concepts** or word senses

- Have a complex many-to-many association with **words** (homonymy, multiple senses)
- Have relations with each other
  - Synonymy, Antonymy, Superordinate
- But are hard to define formally (necessary & sufficient conditions)

## **Embeddings** = vector models of meaning

- More fine-grained than just a string or index
- Especially good at modeling similarity/analogy
  - Just download them and use cosines!!
- Can use sparse models (tf-idf) or dense models (word2vec, GLoVE)
- Useful in practice but know they encode cultural stereotypes