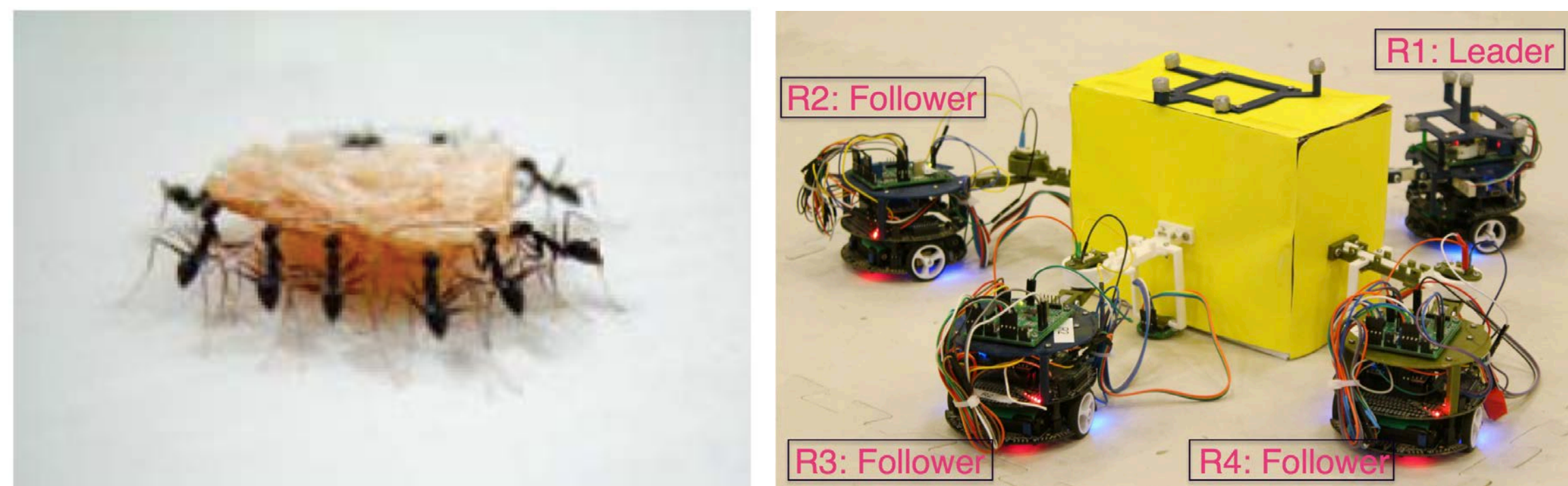


SUMMARY

- Cooperative manipulation with **no** communication
- Follower robots **measure object's motion** as an implicit way for force coordination.
- Leader steers the group, can be a human.
- Proof of force alignment of all robots.
- Custom-built robot prototype with 2D force sensor and laser velocity sensor.



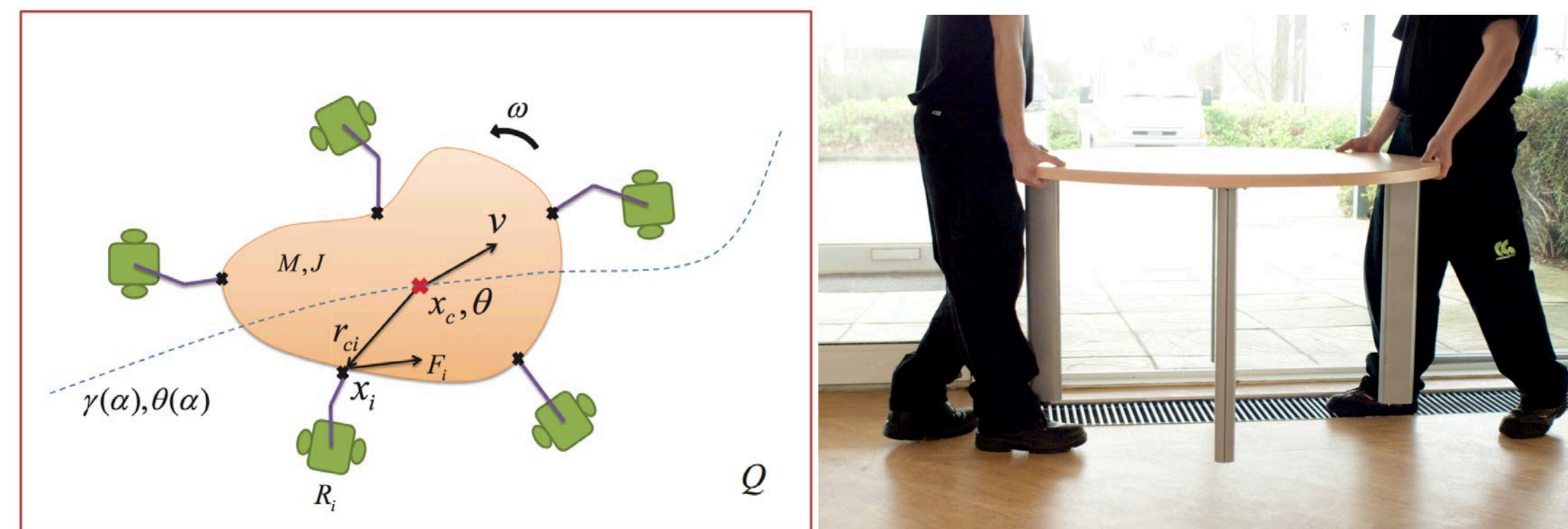
EXPERIMENT VIDEO



APPLICATION HIGHLIGHTS

- Scalable, fault tolerance
- No communication, no global localization, inexpensive individual robot
- Construction, manufacturing, disaster relief

DYNAMICS AND FORCE CONTROLLERS



• Object Dynamics

$$M\dot{\mathbf{v}} = \sum_{i=1}^N \mathbf{F}_i - \mu Mg \frac{\mathbf{v}}{\|\mathbf{v}\|}$$

• Followers' Force Controller

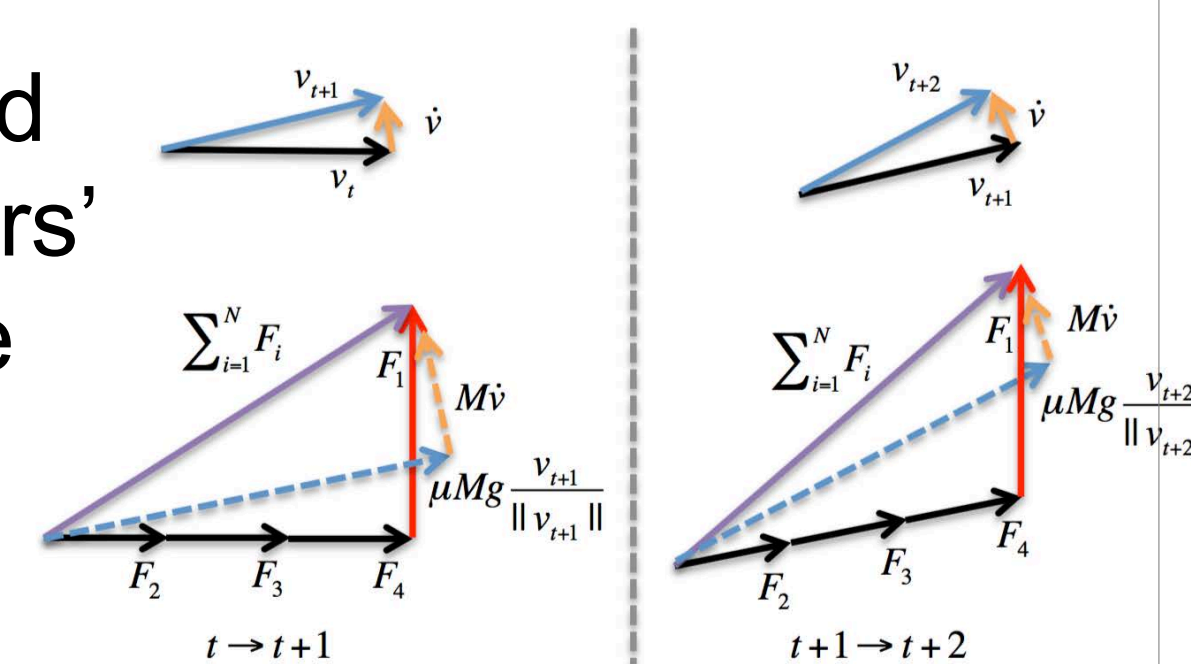
$$\mathbf{F}_i^i = \frac{\mu Mg}{N} \frac{\mathbf{v}^i}{\|\mathbf{v}^i\|}, \quad i = \{2, 3, \dots, N\}$$

• Leader's Force Controller

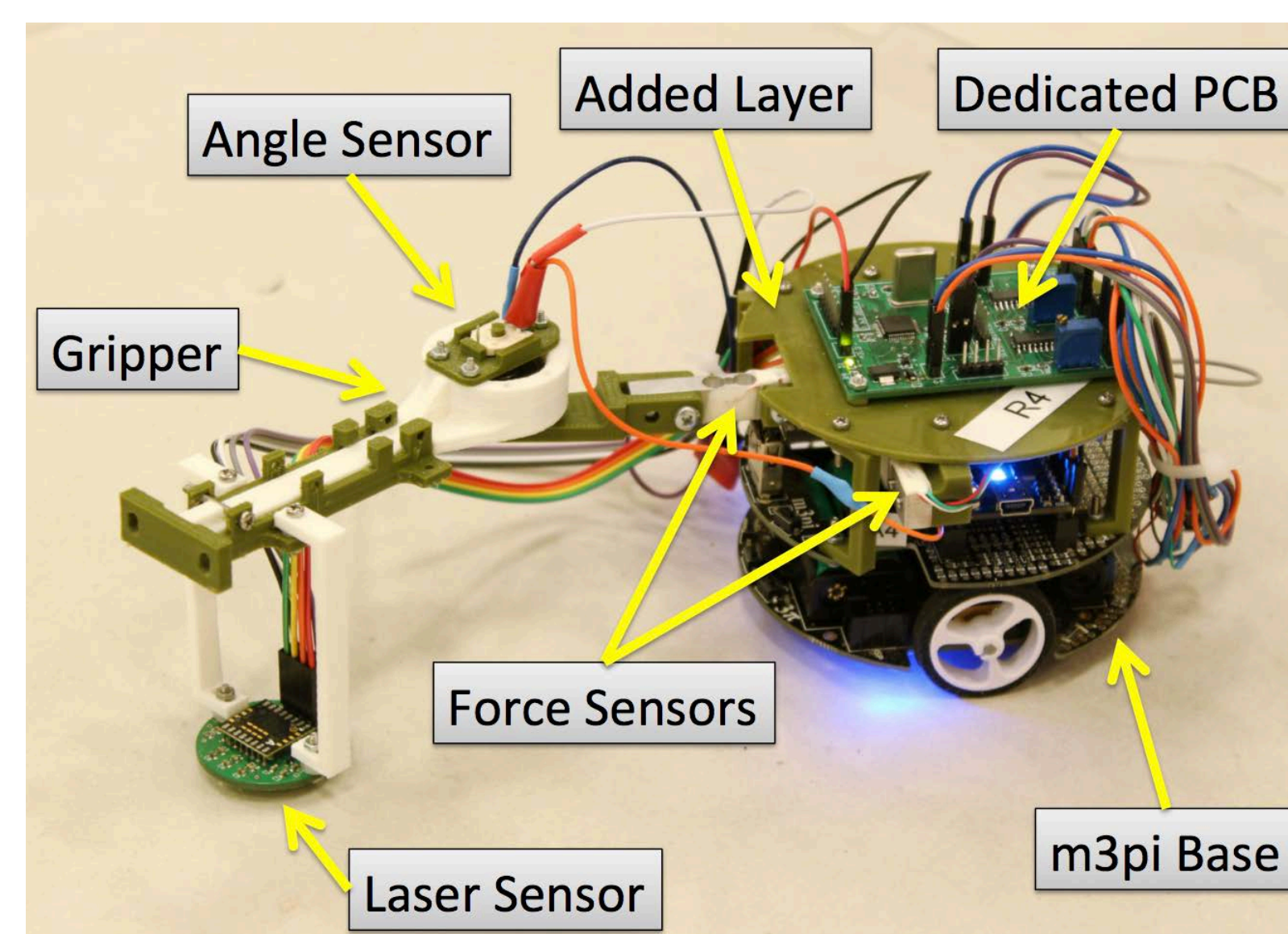
$$\mathbf{F}_1^1 = f_d \frac{\mathbf{v}_d^1}{\|\mathbf{v}_d^1\|} \quad f_d = K_p \max\{\|\mathbf{v}_d^1\| - \|\mathbf{v}^1\|, 0\}.$$

PROOF OF FORCE CONVERGENCE

- **Theorem 1:** the proposed controllers cause followers' forces synchronize to the leader's
- Proof: Vector-based



ROBOT DESIGN



- 2D force sensors
- Optical velocity sensor
- 1-DOF gripper

FORCE FEEDBACK CONTROL

- Reference frame conversion

$$\mathbf{v}^i = R(\theta_i)\mathbf{v}$$

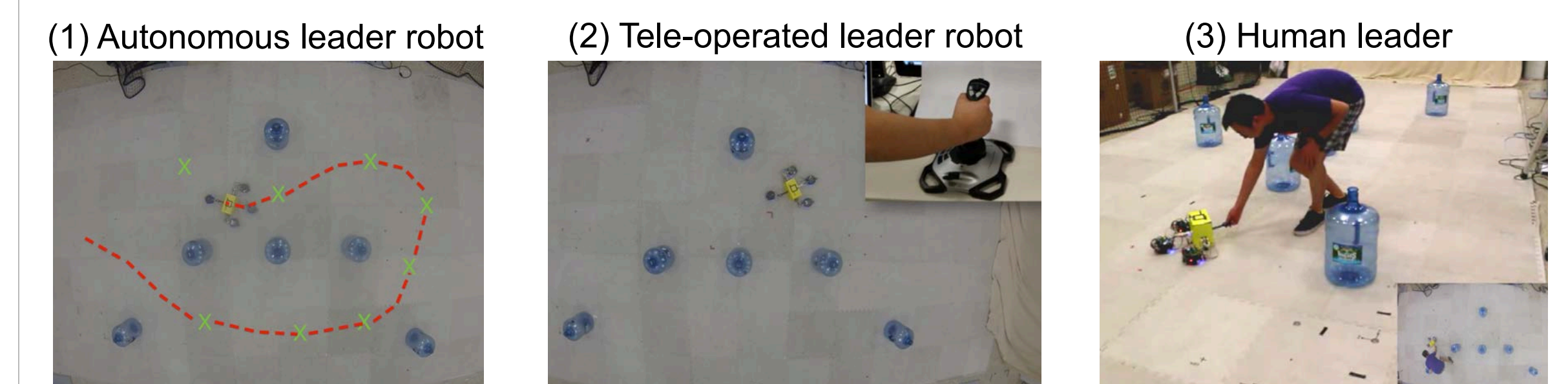
- Linear force generation model

$$\mathbf{v}_c^i - \mathbf{v}^i = K_f(\mathbf{F}_i - \mathbf{f}_i)$$

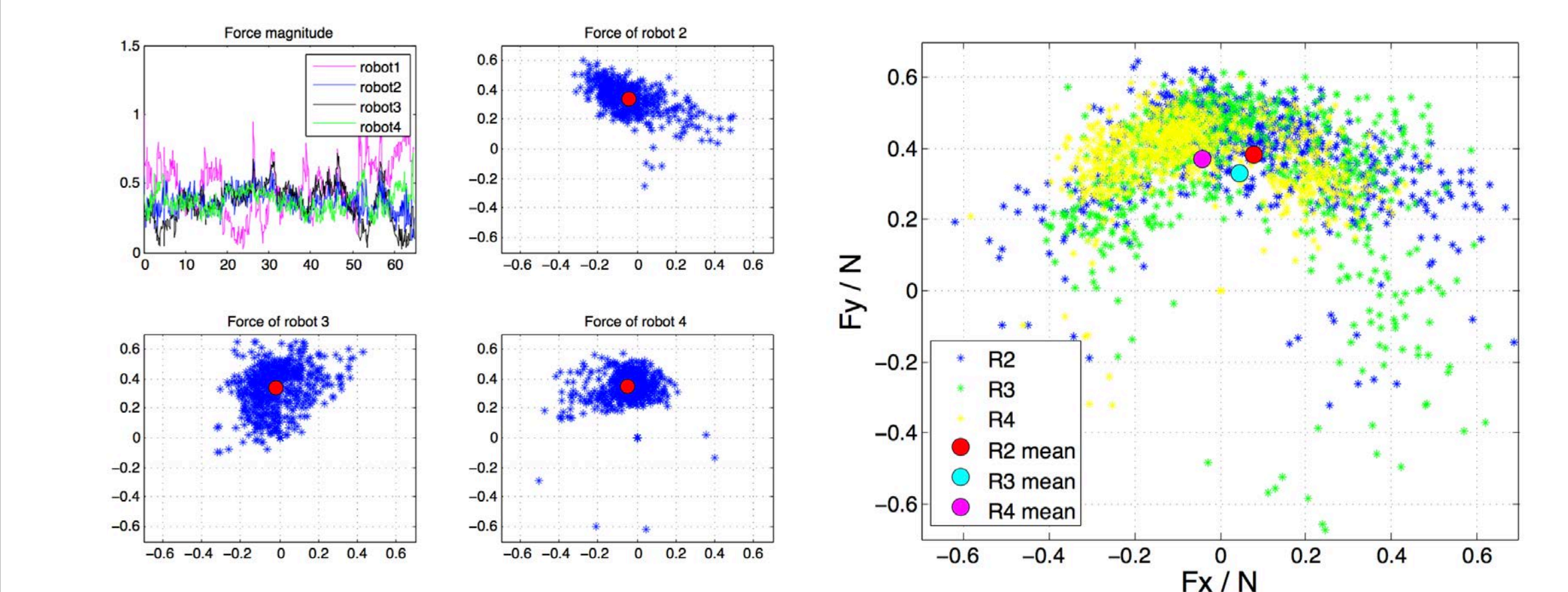
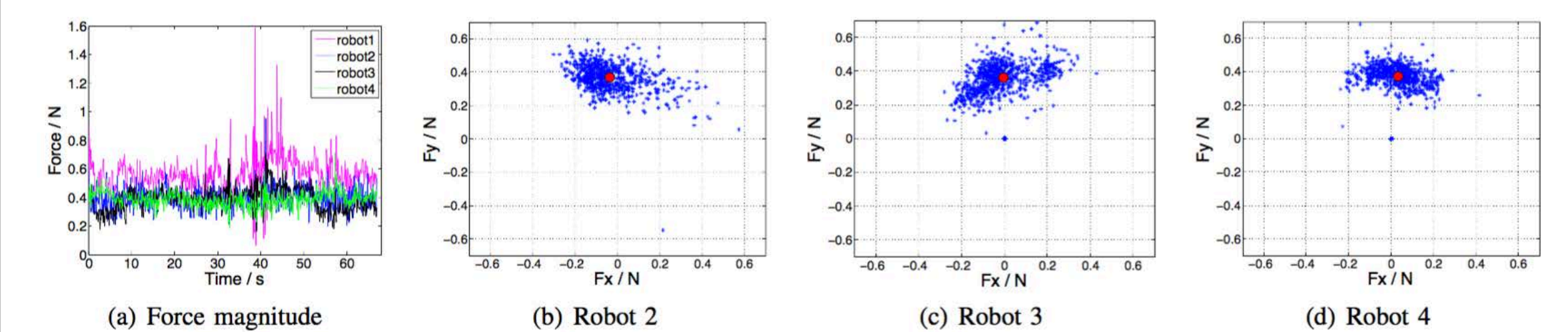
- Point offset control (overcome non-holonomic)

$$\mathbf{v}_p^i = \left[\frac{(\omega_l - \omega_r)r_w l}{d_w}, \frac{(\omega_l + \omega_r)r_w}{2} \right]$$

RESULTS



Experiments with different leaders, same follower robots.



PAPER QR CODE (SCAN)



Paper (PDF)



Video (YouTube)