

System Analysis of Power Transients in Advanced WDM Networks

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ABSTRACT

This paper considers dynamical transient effects in the physical layer of an optical circuit-switched WDM network. These transients of the average transmission power have millisecond time scales. Instead of studying detailed nonlinear dynamics of the network elements, such as optical line amplifiers, a linearized model of the dynamics around a given steady state is considered. System-level analysis in this paper uses modern control theory methods and handles nonlinearity as uncertainty. The analysis translates requirements on the network performance into the requirements to the network elements. These requirements involve a few gross measures of performance for network elements and do not depend on the circuit switching state. One such performance measure is the worst amplification gain for all harmonic disturbances of the average transmission power. Another, is cross coupling of the wavelength channel power variations. The derived requirements guarantee system-level performance for all network configurations and can be used for specifying optical components and subsystems.

Keywords: Optical network, physical layer, transient, dynamics, system analysis

1. INTRODUCTION

This paper considers dynamical transient effects in the physical layer of an optical WDM network. The physical layer dynamics include effects on different time scales. Dynamics of the transmission signal impulses have a scale of picoseconds. The timing recovery loops in the receivers operate in the nanoseconds time scale. Optical packet switching in the future networks will have microsecond time scale. Development of such optical networks is yet in its early stages. Most of the advanced development work in WDM networks is presently focused on circuit switching networks, where lightpath change events (such as wavelength add/drop or cross-connect configuration changes) happen on the time scale of seconds.

This paper is focused on the dynamics of the average transmission power related to the gain dynamics in Optical Line Amplifiers (OLA). These dynamics might be triggered by the circuit switching events and have millisecond time scale primarily defined by the Amplified Spontaneous Emission (ASE) kinetics in Erbium Doped Fiber (EDFA) amplifiers. The transmission power dynamics are also influenced by other active components of optical network, such as automatically tunable attenuators, spectral power equalizers, or other light processing components. When considering these dynamics, an average power of the lightpath transmission signal is considered. High bandwidth modulation of the signal, which in fact consists of separate information carrying pulses, is mostly ignored.

Ring WDM networks implementing communication between two fixed points are well established technology, in particular, for carrying SONET over the WDM. Such simple networks with fixed WDM lightpaths have been analyzed in most detail. Fairly detailed first principle models for transmission power dynamics exist for such networks, e.g., see papers^{2,4,6} describing models for EDFA gain dynamics. These models are implemented in industrial software allowing engineering design calculations and dynamical simulation of such networks. Such models can potentially have very high fidelity, but their setup, tuning (model parameter identification) and

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exhaustive simulations covering a variety of transmission regimes are potentially very labor intensive. Adding description of new network components to such model could require a major effort.

The difficulties with detailed first principle models will be greatly exacerbated for future mesh WDM networks. The future core optical networks will be transparent to wavelength signals on a physical layer. In such network, each wavelength signal travels through the optical core between electronic IP routers on the optical network edge with the information contents unchanged. The signal power is attenuated in the passive network elements and boosted by the optical amplifiers. The lightpaths will be dynamically provisioned by optical cross-connects, routers, or switches independently on the underlying protocol for data transmission. Such network is essentially a circuit switched network. It might experience complex transient processes of the average transmission power for each wavelength signal at the event of the lightpath add, drop, or re-routing. A combination of the signal propagation delay and channel cross-coupling might result in the transmission power disturbances propagating across the network in closed loops and causing lasting power oscillations. Such oscillations were observed experimentally.⁸ Additionally, the transmission power and amplifier gain transients can be excited by changes in the average signal power because of the network traffic burstliness.¹ If for some period of time the wavelength channel bandwidth is not fully utilized, this would result in a decrease of the average power (average temporal density of the transmitted information pulses).

First circuit switched optical networks are already being designed and deployed. This technology develops rapidly for metro area and long haul networks. Engineering design of circuit switched networks is complicated by the fact that performance has to be guaranteed for all possible combinations of the lightpaths. Further, as such networks develop and grow, they potentially have to combine heterogenous equipment from many different vendors. A system integrator of such network might be different from subsystems or component manufacturer. This creates a necessity of developing adequate methods for transmission power dynamics calculations that are suitable for the circuit switched network business. Ideally, these methods should be modular, independent on the network complexity, and use specifications on the component/subsystem level. The existing CAD tools for optical network³ do not address these issues. This paper attempts to address a need for such methods for analysis of the transmission power dynamic.

This paper applies modern dynamics and control system tools and practices to analysis of circuit switched optical networks. Instead of very accurate nonlinear models, linear models with uncertainty are used to guarantee integrated system performance. Such analysis might be somewhat conservative, but it is relatively easy to set up and yields easily understandable specifications for network components. Only very high-level knowledge about the components and subsystems is assumed. Unlike a detailed modeling and simulation approach, our robust analysis is independent of the wavelength routing. This ensures its applicability in the design of switched networks where a large number of different routings can be determined dynamically

Our technical approach to systems analysis is to linearize the nonlinear system around a fixed regime, describe the nonlinearity as a model uncertainty, and apply robust analysis that guarantees stability and performance conditions in the presence of the uncertainty. For a user of our approach, there is no need to understand the derivation and system analysis technicalities. The obtained results are very simple and relate performance to basic specifications of the network components. These specifications are somewhat different from those commonly used in the industry, but can be defined from simple experimentation with the components and subsystems. The obtained specification requirements can be used in development of optical amplifiers, equalizers, attenuators, other transmission signal conditioning devices, OADMs, OXCs, and any other optical network devices and subsystems influencing the transmission power. The analysis results could also provide specifications for component and subsystem choice when integrating the networks from commercially available hardware.

The analysis below assumes that the wavelength routing is fixed and considers signal power variations from the steady-state, average transmission power level. Such model linearization is a standard approach in systems control theory and practice and is commonly applied to nonlinear system analysis. It allows applying powerful tools of the control theory to the problem and achieving deeper insight into the dynamical transient effects and their criticality. The main issue with the linearization approach is that because of the nonlinearities the linearized model gains might change depending on the transmission signal power for each lightwave signal. This problem can be mitigated by performing robust analysis to obtain a guaranteed results for a range of the

linearized system gains obtained at different operating points. Such robust analysis might yield somewhat conservative results, but it also allows using low-fidelity models and is valid for unpredictably changing conditions, such as lightpath switching or introduction of additional wavelength add/drop points. The robust analysis is an effective alternative to a detailed large scale simulation. In addition to being much less expensive, it also provides better insight into the influence of network element parameters on the large scale WDM network system performance compared to the simulation.

2. MODELING POWER TRANSIENTS IN A TRANSMISSION CHANNEL

Consider a simple model of the transmission link neglecting the signal transients. A transmitted wavelength signal is characterized by its average power p_{in} at the link input and the average power p_{out} at the link output. The static model of the link has a general form of

$$p_{out} = F(p_{in}), \quad (1)$$

where $F(\cdot)$ is a nonlinear function. The models of the form (1) are commonly used in the optical network design practice. Such models describe attenuation of the transmission signal power in the fiber, filters, splitters, etc. and signal amplification in the OLA.

Let $p_{in,0}$ and $p_{out,0}$ be the steady-state equilibrium signal power values at the input and at the output of the link respectively. Let p_{in} and p_{out} be the ‘instantaneous’ values of the average power that could deviate from $p_{in,0}$ and $p_{out,0}$. The deviation is assumed to be relatively small. The power amplification/attenuation gain g of the link can be obtained by relating the dB values of the input and output power variations as

$$10 \log_{10} \frac{p_{out}}{p_{out,0}} = g \cdot 10 \log_{10} \frac{p_{in}}{p_{in,0}}, \quad (2)$$

$$g = \frac{p_{in,0}}{p_{out,0}} \frac{dF}{dp_{in}}(p_{in,0}), \quad (3)$$

where it is assumed that the dependence between the input and output power is purely static. In practice the gain g can be observed by applying a small variation of input power and registering the variation of the output power after the transients die out. The gain g describes propagation of the small average power disturbances in the network. These disturbances are with respect to a given steady state operation regime. Note that the gain g is conceptually different from the overall amplification gain as typically used in engineering of active optical network elements such as optical amplifiers.

A more comprehensive model of the link might take into account dynamical effects manifested in the output power transients observed during a rapid change of the input power p_{in} as well as the external disturbances, such as transmission noise, that influence the signal power. To introduce a linearized dynamical model, consider the steady-state power levels $\bar{p}_{in,0}$, $\bar{p}_{out,0}$ at the input and output ports and their instantaneous values p_{in} , p_{out} that include deviations from these steady-state levels. The dynamical variables describing the variations of the signal power are

$$y_{out} = c \cdot 10 \log_{10} \frac{p_{out}}{p_{out,0}}, \quad (4)$$

$$y_{in} = \frac{c}{g} \cdot 10 \log_{10} \frac{p_{in}}{p_{in,0}}, \quad (5)$$

where c is the scaling factor and g is the gain (3). The same scaling factor c is introduced in (4) and (5) for both the input and output signals. This scaling factor does not change the linear dynamical model relating y_{out} to y_{in} and will be explained later on. The scaling factor $1/g$ in (5) is introduced such that the steady state (DC) small signal gain of the link is unity. The introduced scaling normalizes the considered dynamical effects with respect to the steady-state amplification or attenuation gain of the link. This allows separating the analysis of dynamical transient effects in the network from an analysis and design of the average power propagation for a transmission signal. For a long-haul transmission system each link might include an optical line amplifier (such

as EDFA) and a length of a fiber. This transmission system would be typically engineered such that the signal power gain in the amplifier compensates the power loss in the fiber. This means $g \approx 1$ and the scaling factor $1/g$ in (5) is close to unity.

Assuming the signal variations from the steady state are small, the dynamical relationship between the input and output signal power is linear and can be presented in the form

$$y_{out} = h(s)y_{in}, \quad (6)$$

where s is the Laplace transform variable and $h(s)$ is the link transfer function. The transfer function $h(s)$ describes the transient dynamics of the signal in the link. In accordance with (4), (5) this function is normalized such that $h(0) = 1$. The transfer function $h(s)$ might include the light propagation delay in the fiber length in the link, signal power attenuation in the fiber, the dynamical effects and channel power cross-interaction in the optical amplifiers, as well as influence of other active or passive optical devices, such as equalizers, filters, attenuators, and splitters, included in the link.

In modern control theory, the maximal gain $h(i\omega)$ is called an H_∞ norm of the transfer function $h(s)$ and usually denoted as

$$\|h(s)\|_\infty = \sup_{\omega \in \mathfrak{R}} |h(i\omega)|, \quad (7)$$

where a technical condition of transfer function $h(s)$ being stable and proper is assumed. This conditions always holds for the practical systems in question.

3. MODELING TRANSIENTS IN A WDM NETWORK

This section extends the model (6) towards a generic circuit-switched optical network configuration, such as one schematically depicted in Figure 1. The cross-influence of the power for individual wavelength signals can potentially result in the signal transients propagating along closed loop paths, despite the fact that none of individual wavelength signals follows a closed path. The closed-loop propagation of the transients might lead to sustained oscillations of the optical signal power. Such oscillations were observed experimentally.⁸ It is important to foresee possibility of such oscillations when designing a network and avoid them for all possible working regimes and switched circuit configurations.

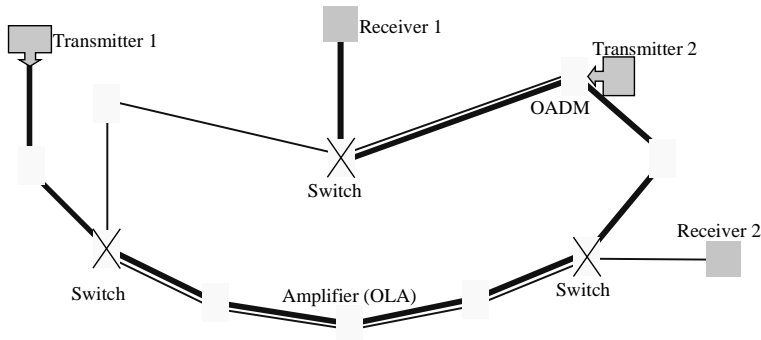


Figure 1: Optical network example

Consider a multivariable model for a single WDM transmission link carrying several wavelength signals, each characterized by its average power. For each wavelength signal, the scaled input and output variables $y_{in,k}$ and $y_{out,k}$ can be introduced similar to (4), (5), where k is the wavelength signal number for this link. These input signals are collected into a vector $Y_{in} \in \mathfrak{R}^N$, where N is the number of the signals in the link. The vector Y_{in} has components $y_{in,k}$. Similarly, the output signals of the link are described by the vector $Y_{out} \in \mathfrak{R}^N$ with the components $y_{out,k}$.

A multivariable extension of the linearized dynamical model (6) can be used to describe the relationship between the input and output signals in the link as

$$Y_{out} = H(s)Y_{in}, \quad (8)$$

where $H(s) \in \mathfrak{R}^{N,N}$ is a square transfer function matrix. The diagonal elements of $H(s)$ in (8) describe the transfer functions for each wavelength, similar to (6). The off-diagonal elements describe the cross-influence of an input power change in one wavelength signal onto the output power change for another wavelength signal.

The transfer function $H(s)$ can be split into two parts such that

$$H(s) = D(s) + T(s), \quad (9)$$

where $D(s)$ is a diagonal $N \times N$ matrix of the ‘nominal’ transfer function with the diagonal elements $d_k(s)$ and $T(s)$ is a $N \times N$ matrix describing the cross-influence of different wavelength signals. Note that in accordance with the scaling (4), (5) and similar with the model (6) the steady-state gains of the nominal transfer function are unity for each wavelength, i.e., $D(0) = I$, where I is the unity matrix.

In the control theory, it is well known that the maximal amplification gain of a dynamical linear operator (transfer function) can be computed as an H_∞ norm, a multivariable generalization of (7)

$$\|T(s)\|_\infty = \sup_{\omega \in \mathfrak{R}} \bar{\sigma}(T(i\omega)), \quad (10)$$

where $\bar{\sigma}(A)$ is the largest singular value of a matrix A , i.e., a square root of the largest eigenvalue of $A^T A$.

The operator gain (10) will be used in analysis of the transient stability and transmission disturbance amplification to follow. This analysis uses the bound $\|T(s)\|_\infty \leq t_*$ as the only information about the transfer function $T(s)$. Such analysis might be somewhat conservative but can be readily applied in practice. The $\|T(s)\|_\infty$ specification for the transfer function can be defined in practice with relative ease and without a need to have a detailed model of the cross-influence between powers of individual wavelength signals. The analysis to follow also includes a single parameter specification of the nominal transfer function model $D(s)$ through a maximal amplification gain with respect to the disturbances encountered in all the links along each lightpath.

Consider an alternative representation of a circuit switched WDM network, illustrated in Figure 1. For the sake of the analysis, the network is modeled as a collection of separate communication links. Each link receives a number of wavelength signals as its input. In the network, different wavelength signals on the output of one link are connected to the inputs of other links. By pulling the connections together, the network can be presented as in Figure 2

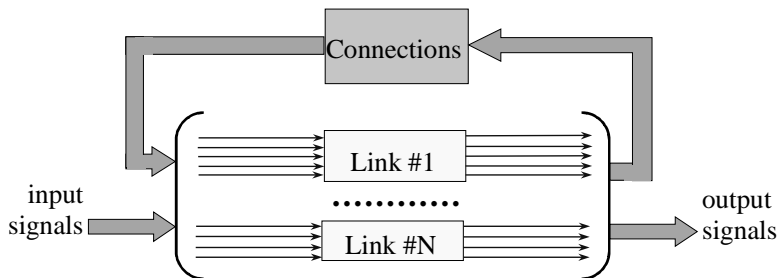


Figure 2: Network model as communication links and their connections

The network links in Figure 2 can be described by extending the model of the form (8), (9) towards all the links in question as follows

$$Y_{out}^{(n)} = H^{(n)}(s)Y_{in}^{(n)}, \quad (n = 1, \dots, N_L), \quad (11)$$

$$H^{(n)}(s) = D^{(n)}(s) + T^{(n)}(s), \quad (12)$$

where $Y_{in}^{(n)} \in \mathfrak{R}^{N_n}$ is the vector of the average input signal power variation for link n , $Y_{out}^{(n)} \in \mathfrak{R}^{N_n}$ is the vector of the output signal power variation, and $H^{(n)}(s)$ is the matrix transfer function describing link n . Similar to (6), the transfer matrix $H^{(n)}(s)$ for each link is split into the ‘nominal’ diagonal transfer matrix $D^{(n)}(s)$ and the ‘perturbation’ matrix $T^{(n)}(s)$ collecting the wavelength signal cross-coupling and other effects outside of the nominal model.

To describe the complete model including the network inputs, outputs and link connection, introduce the following block-vector and block-matrix notations

$$\bar{Y}_{in} \equiv \begin{bmatrix} Y_{in}^{(1)} \\ \vdots \\ Y_{in}^{(N_n)} \end{bmatrix}, \quad \bar{Y}_{out} = \begin{bmatrix} Y_{out}^{(1)} \\ \vdots \\ Y_{out}^{(N_n)} \end{bmatrix}, \quad (13)$$

$$\bar{H}(s) = \text{block diag}\{H^{(1)}(s), H^{(2)}(s), \dots, H^{(N_n)}(s)\} \quad (14)$$

By using (11)–(14) the network model can be described through the following matrix equations

$$\bar{Y}_{out} = \bar{H}(s)\bar{Y}_{in}, \quad (15)$$

$$\bar{Y}_{in} = K \cdot \bar{Y}_{out} + BU, \quad (16)$$

$$Z = C\bar{Y}_{out}, \quad (17)$$

where $U \in \mathfrak{R}^M$ is the vector collecting the input signal power for all independent wavelength signals and $Z \in \mathfrak{R}^M$ is the vector collecting the output signal power for the same wavelengths; $M \leq N$. The block matrix $\bar{H}(s)$ is described in (14). The entries of the ‘connection’ matrix K are either zeros or off-diagonal ones. Each unity entry in K corresponds to a link output being connected to another link input in accordance with the row and column number of this entry. The rectangular selection matrix C consists mostly of zeros and has a single unity entry in each row. This entry describes the respective output signal of one of the transmission links observed as a signal delivered by the network to a final receiver device destination. The rectangular selection matrix B has structure similar to the structure of C . Each unity entry in B describes the network input signal (a component of U) connected to one of the network link inputs.

It is important to note at this point that potential changes in switching and routing of the individual wavelength signals in a transparent optical network would result in changing entries in the matrices K , B , and C . The models of the links (15) do not change. The analysis to follow uses only general properties of the matrices K , B , and C that do not depend on the particular signal routing configuration. Thus, this analysis is valid for the current network configuration independently of the current switch states.

From the model (15)–(17) the vector Z of the network output power for all independent wavelength signals can be found in the form

$$Z = CS(s)\bar{H}(s)BU, \quad (18)$$

$$S(s) = [I - \bar{H}(s)K]^{-1}, \quad (19)$$

where I is the identity matrix of the appropriate size and $S(s)$ is the sensitivity matrix for the network. The transfer matrix $S(s)$ defines the amplification effects for the transmission signal average power variations in the network as related to the connection of the links in the network.

In accordance with (6) and (14) the transfer matrix $\bar{H}(s)$ can be presented in the form

$$\bar{H}(s) = \bar{D}(s) + \bar{T}(s), \quad (20)$$

$$\bar{D}(s) = \text{block diag}\{D^{(1)}(s), D^{(2)}(s), \dots, D^{(N_n)}(s)\}, \quad (21)$$

$$\bar{T}(s) = \text{block diag}\{T^{(1)}(s), T^{(2)}(s), \dots, T^{(N_n)}(s)\}, \quad (22)$$

where $\bar{D}(s)$ is the composite diagonal nominal transfer matrix for all network links and $\bar{T}(s)$ is the composite transfer matrix incorporating the cross-coupling effects for all links.

By substituting (20) into (18), (19) one can derive the following representation of the network output signals

$$Z = CS_1(s)\bar{H}(s)BU, \quad (23)$$

$$S_1(s) = [I - S_0(s)\bar{T}(s)K]^{-1}S_0(s), \quad (24)$$

$$S_0(s) = [I - \bar{D}(s)K]^{-1}, \quad (25)$$

This representation explicitly shows the dependence of the output signal on the cross-coupling transfer matrix $\bar{T}(s)$ (22). If there is no cross-coupling, then $\bar{T}(s) = 0$, $S_1(s) = S_0(s)$, and the network output signals (23) are given by (18), where $S(s) = S_0(s)$.

4. ANALYSIS OF THE TRANSIENT PERFORMANCE

The analysis to follow is based on the assumption that the design of the network including the selection of the OLA gains is based on the nominal model of the network for each wavelength signal. In accordance with (12), such nominal models of the links are described by the diagonal transfer matrices $D^{(n)}(s)$ in (21) and they ignore the channel cross-coupling and other effects attributed to the transfer matrices $T^{(n)}(s)$ in (22). Note that in some practical cases the nominal models $D^{(n)}(s)$ might include only static amplification gains ignoring signal power transients. Such models are commonly used in the practical network design. In this case the unmodeled transient dynamics could be attributed to the transfer matrices $T^{(n)}(s)$.

Consider the expression (23) for the output signal power Z computed through the input signal power Z . In the presence of the cross-coupling, the transients in the input signal power U such as a channel add/drop or average power variation because of the traffic burstiness might cause large transients in the output signal power Z . This would happen in accordance with the amplification characteristics of the operator $S_1(s)$ in (24). The network design and the component specifications should guarantee that the signal amplification with the operator $S_1(s)$ is small over all frequencies.

Consider the following operator gains calculated in accordance with (10)

$$s_* = \|S_0\|_\infty, \quad (26)$$

$$t_* = \|\bar{T}(s)\|_\infty = \max_k \|T_k(s)\|_\infty, \quad (27)$$

$$s_1 = \|S_1\|_\infty, \quad (28)$$

where s_* is the gross measure of the nominal noise sensitivity S_0 (24), and t_* is the gross measure of the cross-coupling and other unmodeled effects. In accordance with (22), the norm t_* (27) corresponds to the worst cross-coupling in all of the network links. In accordance with (23), (24), and (26), the parameter s_* defines a measure of the external disturbance amplification in the nominal model of the network, i.e., the model that does not take the cross-influence of the wavelength signals into account.

For more detailed insight into evaluation of s_* , it must be noted that the matrix K in (16) is a projection matrix. It selects a subset of the input signals and permutes their order. Therefore,

$$\|K\| \equiv \bar{\sigma}(K) = 1 \quad (29)$$

From (23)–(29) it follows that the transient processes in the network are guaranteed to be stable as long as the cross-coupling is small enough, i.e., if $t_* < 1/s_*$. With the contribution of the cross-coupling effects is taken into account, the input power perturbation effect on the network output $S_0(s)U$ is replaced by $S_1(s)U$ in (23). The amplification gain s_1 in (28) can be estimated as follows

$$\|Z\|_\infty \leq s_1\|U\|_\infty \quad (30)$$

$$s_1 = \frac{s_*}{1 - t_*s_*} \quad (31)$$

where $\|U\|_\infty$ and $\|Z\|_\infty$ are the maximal spectral powers for the average power variations of the input and output transmission signals respectively. The inequality (30) follows from (28) and (23). The main advantage

of the estimate (31) of the sensitivity s_1 is its simple form. The estimate (31) shows that the power transient amplification can increase out of hand as t_* is getting closer to the stability boundary $1/s_*$. For $t_* \ll 1/s_*$ the cross-coupling effects are guaranteed to have little effect on the noise sensitivity. The expression (31) gives a convenient practical measure of the cross-coupling and other deviations from the nominal design behavior, which can be tolerated in the network links and devices included into this links. This shifts the emphasis from design and analysis of the entire optical network to the requirement specifications for individual network devices that might be provided by different OEM suppliers.

In the above analysis, the nominal network design is characterized by a single number – the nominal sensitivity s_* . This sensitivity depends on the nominal model of the network and can be evaluated at the stage of the nominal network design. In accordance with (24) and (26) the nominal sensitivity s_* depends on the lightpath connections, as defined by matrix K and the nominal network link gains as defined by the transfer matrix $D(s)$. The matrix K could be changing in a network because of the re-routing of the lightpaths. Therefore, it is desirable to characterize s_* in terms of specifications for the nominal network gains.

The nominal network gains can be characterized by a single H_∞ norm parameter

$$d_* = \|\bar{D}(s)\|_\infty = \max_k \|D_k(s)\|_\infty = \max_{k,j} \sup_{\omega \in \mathfrak{R}} |d_k^j(i\omega)|, \quad (32)$$

$$D_k(s) = \text{diag}\{d_k^1(s), d_k^2(s), \dots, d_k^{n_k}(s)\}, \quad (33)$$

where d_* can be considered as the largest input amplification gain of an wavelength signal over all network links at any frequency of the average input power modulation.

Clearly, the guaranteed value of the nominal sensitivity s_* grows with d_* . The question is: for a given value of d_* is it guaranteed that the sensitivity is less than s_* ? Let n_* be the maximal number of the links in the

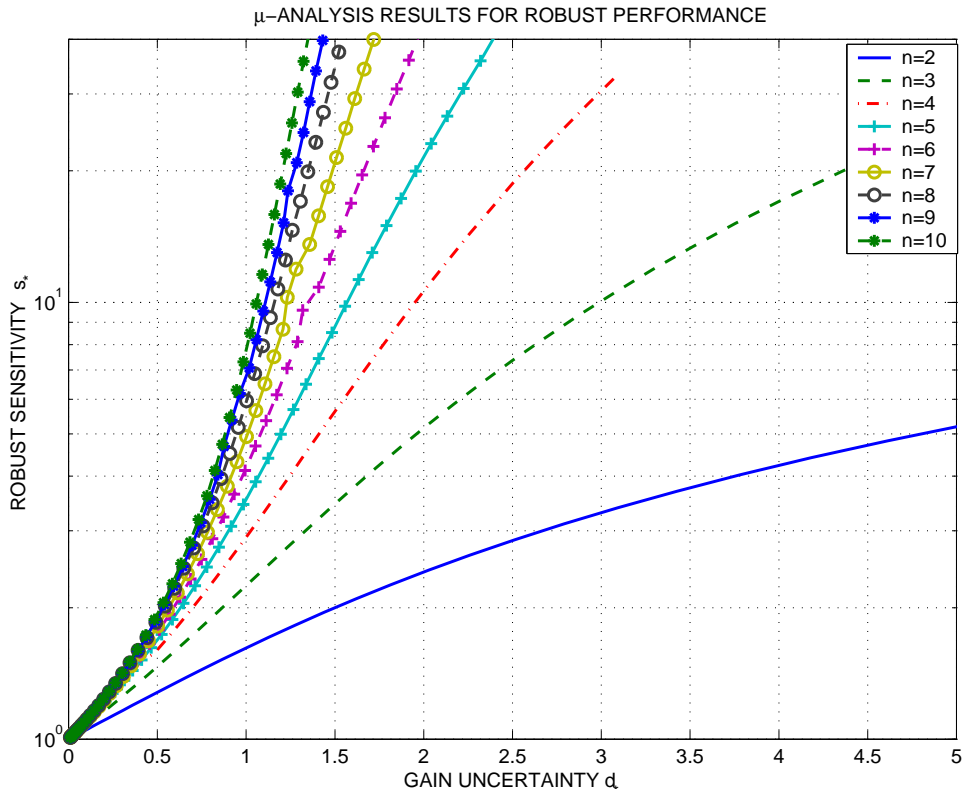


Figure 3: The dependence $s_*(d_*, n_*)$ computed for $n_* \leq 10$

path for any wavelength. The function $s_*(d_*, n_*)$ describing the maximal (worst case) sensitivity s_* that can be possibly achieved for given d_* and n_* can be evaluated with help of μ -analysis.⁹ The detailed discussion of the calculation is beyond the scope of this paper. Figure 3 shows the curves $s_*(d_*, n_*)$ computed for $n_* \leq 10$. These curves cover the case of the networks with up to 9 OXCs encountered for each wavelength.

5. DISCUSSION AND CONCLUSION

To recap, the robust characterization of the transient amplification in the network in (30), (31) describes the entire WDM network with help of only three parameters: (i) the channel cross coupling parameter t_* in (27), (ii) the maximal nominal amplification gain d_* (32) for the network links, and (iii) the maximal number n_* of links in a lightpath in the network. All these parameters can be easily obtained for a network being analyzed. The robust sensitivity s_1 in (31) takes into account the cross-coupling effects and can be computed from the nominal robust sensitivity s_* . The latter is defined by d_* and n_* and can be evaluated from the plots in Figure 3.

The described robust sensitivity analysis automatically takes care of the potential presence of closed loops and lightpath changes (switching). Of course, there is a price to pay for the analysis convenience - it might be somewhat conservative. A detailed model of the network might give a more accurate prediction of the transient amplification. A big advantage of our approach, however, is that the estimates of the amplification gain d_* and the signal cross-coupling t_* parameters can be considered as hardware specifications for each of the network links. As long as the network design complies with these specifications, the robust bound on the transient amplification holds, even as the lightpaths are switched, network configuration is modified, or some of the equipment replaced.

Our analysis implicitly assumes that the phase of the dynamic amplification gain $d_k^j(i\omega)$ and the cross-coupling $T(i\omega)$ are worst possible. This assumption is particularly reasonable if the propagation delays in the network links are comparable with or larger than the time constants of the lightpath switching transients. Future optical core networks will have very fast lightpath switching times, while the signal propagation delays are defined by the fiber link lengths and cannot be reduced. This means our analysis is most relevant for these future networks.

The analysis results obtained in the paper do not depend on the network or switched circuit configuration. Though the analysis is based on control theory techniques, using its the results does not require a deep background in the control theory. Engineering specifications of the network subsystems and components used for analysis are easy to understand and use.

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