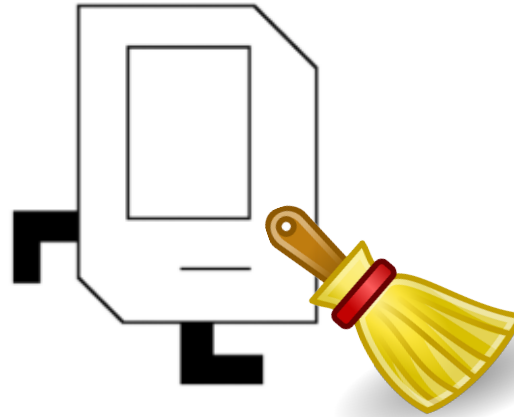


# Search Engines

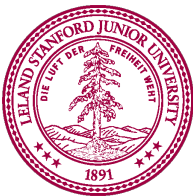
Chris Gregg

Based on slides by Chris Piech and Mehran Sahami  
CS106A, Stanford University

# Housekeeping



- Assignment 6: free one-day extension. Now due on Wednesday, August 4<sup>th</sup>, 10:30am.
- Final Diagnostic is this ~~Wednesday~~ Thursday, 10:30am-12:00pm, PDT
  - We have posted practice material
  - It will be on BlueBook, and will be similar to the week three diagnostic.
  - It will be more challenging, but doable
  - It will cover everything in class up to July 28th



# Learning Goals

1. Learning about search engines
2. Getting some hints on Assignment #7



And maybe some  
bonus story time!

# Search Engines



# How to Build a Web Search Engine

- Crawling
  - Find relevant documents to search over
- Indexing
  - Record which terms appear in which documents
- Search
  - Determine which documents match user's query
- Ranking
  - Sort matching documents by "relevance" to user's query
- Serving
  - Infrastructure to get queries and give results
- Interface
  - User interface for presenting results to the user

# In Assignment #7

- Crawling
  - We will provide document collection for you to search
- Indexing
  - You'll be writing this!
- Search
  - You'll be writing this!
- Ranking
  - Nothing fancy required, but great area for extensions
- Serving
  - Not required, but great area for extensions
- Interface
  - Give you basic text interface, but great area for extensions

# Indexing

- Inverted index (generally, just called an "index")
  - Similar to index in back of a book
  - For each word, you want to know where it is mentioned
- Mapping, where we have: term  $\rightarrow$  list of documents containing that term
  - **Term** is the generic way we refer to a word, name, number, etc. that we might want to look up
- Consider the example:
  - Term "burrito" appears in the documents "recipes.txt", "greatest eats.txt", "top 10 foods.txt", and "favorites.txt"
  - Term "sushi" appears in documents "favorites.txt" and "Japanese foods.txt"
  - Term "samosa" appears in document "appetizers.txt"

# Representing an Index in Python

- Consider the example:
  - term "burrito" appears in the documents "recipes.txt", "greatest eats.txt", "top 10 foods.txt", and "favorites.txt"
  - term "sushi" appears in documents "favorites.txt" and "Japanese foods.txt"
  - term "samosa" appears in document "appetizers.txt"
- In Python, use a dictionary to represent index
  - Map from term (key) to list of documents (value)

```
index = {  
    'burrito': ['recipes.txt', 'greatest eats.txt',  
               'top 10 foods.txt', 'favorites.txt'],  
    'sushi': ['favorites.txt', 'Japanese foods.txt'],  
    'samosa': ['appetizers.txt']  
}
```

# Building an Index in Assignment #7

- Given a set of documents
  - For each document, parse out all the terms:
    - Terms are separated from each other by space (or newline)
    - Terms should be converted to lowercase (for consistency)
    - Terms need to have punctuation stripped off start/end

```
>>> raw = '$$j.lo!'
```

```
>>> term = raw.strip(string.punctuation)
```

```
>>> term
```

```
'j.lo'
```

'doc1.txt':

<pre><b>*We*</b> are 100,000 <b>STRONG!</b> \$\$</pre>
--

- Example: Terms in 'doc1.txt':
  - '**\*We\***' should be converted to term '**we**'
  - '**are**' should be converted to term '**are**'
  - '**100,000**' should be converted to term '**100,000**'
  - '**STRONG!**' should be converted to term '**strong**'
  - '\$\$' should be ignored. Punctuation by itself is not a term.



# Building an Index in Assignment #7

'doc1.txt':

<b>*We*</b> <b>are</b> <b>100,000</b> <b>STRONG!</b> <b>\$\$</b>
---

- Example: Terms in 'doc1.txt':
  - '**\*We\***' should be converted to term '**we**'
  - '**are**' should be converted to term '**are**'
  - '**100,000**' should be converted to term '**100,000**'
  - '**STRONG!**' should be converted to term '**strong**'
  - '**\$\$**' should be ignored. Punctuation by itself is not a term.
- Resulting index (dictionary) in Python would be:

```
{  
    'we': ['doc1.txt'],  
    'are': ['doc1.txt'],  
    '100,000': ['doc1.txt'],  
    'strong': ['doc1.txt']  
}
```

Note: Python would print the dictionary all on one line. We just break it up on multiple lines in our examples for clarity.

# Building an Index in Assignment #7

'doc2.txt':

**Strong, you are!**  
**--Yoda--**

- Now, say we indexed 'doc2.txt':
  - 'Strong,' should be converted to term 'strong'
  - 'you' should be converted to term 'you'
  - 'are!' should be converted to term 'are'
  - '--Yoda--' should be converted to term 'yoda'
- Updating our previous index with this data should give:

```
{  
  'we': ['doc1.txt'],  
  'are': ['doc1.txt', 'doc2.txt'],  
  '100,000': ['doc1.txt'],  
  'strong': ['doc1.txt', 'doc2.txt'],  
  'you': ['doc2.txt'],  
  'yoda': ['doc2.txt']  
}
```

# A Final Note on Indexing

- Often, files have some information that we want to keep track of (such as a title) for later display
  - Here, first line of each file contains a title that we want to keep track of
  - The terms in the title line should still be indexed like every other line in the file
- Build a mapping (dictionary) from file names to titles (for later display):

```
{  
'quote1.txt': 'Yoda quote',  
'quote2.txt': "Gandhi's wisdom"  
}
```

'quote1.txt':

**Yoda quote**

**Strong, you are!**  
**--Yoda--**

'quote2.txt':

**Gandhi's wisdom**

**Be the change  
that you wish to  
see in the  
world.**  
**--Mahatma Gandhi**

Note: in the index of these files, **"gandhi's"** would be a term (with the apostrophe embedded) since the apostrophe is not at the end beginning/end of the term.

# Search

- Once you have an index, searching is straightforward
  - In the user interface, user enters a query
    - Note: Terms in query will be separated by spaces and converted to lowercase. (Can assume no punctuation before/after query terms.)
  - For each term in query, we use the index to look up the list of documents that the term appears in
    - This list of documents is called a "posting list"
- For one term queries, the posting list from the index directly provides the results to the query
- For multi-term queries, the way you combine posting lists for each term determines how the search works

# Multi-Term Queries

- Can add together the results (uniquely) of all the posting lists
  - This would be comparable to doing a union with sets
  - This corresponds to treating the query as a *disjunction*
    - We return any document that contains any of the terms in query
    - Logically, it's like using the connective "OR" between query terms
  - Recall index:

```
{  
  'we': ['doc1.txt'],  
  'are': ['doc1.txt', 'doc2.txt'],  
  '100,000': ['doc1.txt'],  
  'strong': ['doc1.txt', 'doc2.txt'],  
  'you': ['doc2.txt'],  
  'yoda': ['doc2.txt']  
}
```

Posting list:

- Query: "yoda strong"



# Multi-Term Queries

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  'strong': ['doc1.txt', 'doc2.txt'],  
  'you': ['doc2.txt'],  
  'yoda': ['doc2.txt']  
}
```

Posting list:

- Query: "yoda strong"

**['doc2.txt']**

# Multi-Term Queries

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  '100,000': ['doc1.txt'],  
  'strong': ['doc1.txt', 'doc2.txt'],  
  'you': ['doc2.txt'],  
  'yoda': ['doc2.txt']  
}
```

Posting list:

- Query: "yoda **strong**"

<code>['doc2.txt', 'strong.doc1.txt']</code>
--

# Multi-Term Queries

- Can take the overlap of the results (uniquely) of all the posting lists
  - This would be comparable to doing an intersection with sets
  - This corresponds to treating the query as a *conjunction*
    - We return documents that contain every term in query
    - Logically, it's like using the connective "AND" between query terms
  - This is what you'll implement for Assignment #7
  - Recall index:

```
{  
'we': ['doc1.txt'],  
'are': ['doc1.txt', 'doc2.txt'],  
'100,000': ['doc1.txt'],  
'strong': ['doc1.txt', 'doc2.txt'],  
'you': ['doc2.txt'],  
'yoda': ['doc2.txt']  
}
```
  - Query: "are you yoda"

Posting list:

# Multi-Term Queries

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'100,000': ['doc1.txt'],  
'strong': ['doc1.txt', 'doc2.txt'],  
'you': ['doc2.txt'],  
'yoda': ['doc2.txt']  
}
```
  - Query: "are you yoda"

Posting list:

`['doc1.txt', 'doc2.txt']`

# Multi-Term Queries

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  '100,000': ['doc1.txt'],
  'strong': ['doc1.txt', 'doc2.txt'],
  'you': ['doc2.txt'],
  'yoda': ['doc2.txt']
}
```
  - Query: "are **you** yoda"

Posting list:

**[ 'doc2.txt' ]**



# Multi-Term Queries

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'are': ['doc1.txt', 'doc2.txt'],  
'100,000': ['doc1.txt'],  
'strong': ['doc1.txt', 'doc2.txt'],  
'you': ['doc2.txt'],  
'yoda': ['doc2.txt']  
}
```
  - Query: "are you **yoda**"

Posting list:

**['doc2.txt']**

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- Can take the overlap of the results (uniquely) of all the posting lists
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'are': ['doc1.txt', 'doc2.txt'],  
'100,000': ['doc1.txt'],  
'strong': ['doc1.txt', 'doc2.txt'],  
'you': ['doc2.txt'],  
'yoda': ['doc2.txt']  
}
```
  - Query: "we are yoda"

Posting list:

# Multi-Term Queries

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'100,000': ['doc1.txt'],  
'strong': ['doc1.txt', 'doc2.txt'],  
'you': ['doc2.txt'],  
'yoda': ['doc2.txt']  
}
```
  - Query: "**we** are yoda"

Posting list:

**['doc1.txt']**

# Multi-Term Queries

- Can take the overlap of the results (uniquely) of all the posting lists
  - This would be comparable to doing an intersection with sets
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  '100,000': ['doc1.txt'],
  'strong': ['doc1.txt', 'doc2.txt'],
  'you': ['doc2.txt'],
  'yoda': ['doc2.txt']
}
```
  - Query: "we are yoda"

Posting list:

**['doc1.txt']**

# Multi-Term Queries

- Can take the overlap of the results (uniquely) of all the posting lists
  - This would be comparable to doing an intersection with sets
  - This corresponds to treating the query as a *conjunction*
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  'strong': ['doc1.txt', 'doc2.txt'],
  'you': ['doc2.txt'],
  'yoda': ['doc2.txt']
}
```
  - Query: "we are **yoda**"

Posting list:

[ ]



Let's take it out for a spin:  
searchengine.py

# Ranking Documents

- In Assignment #7, you just display the documents that are considered matches to the query
  - You are not ranking them in any particular order
  - But, this is an area for cool extensions, so let's chat about it...
- One of the richest research areas in search is how to rank documents (i.e., sort them by relevance to user)
  - Doing this requires that we keep track of more information in the index (e.g., store lists/tuples rather than just file names)
  - Examples of additional information that's useful for ranking:
    - Number of times a term appears in a document
    - The positions of the terms in each document
    - How rare particular terms are in the whole collection of documents
    - How "popular" a document is (e.g., analyze link structure on the web)

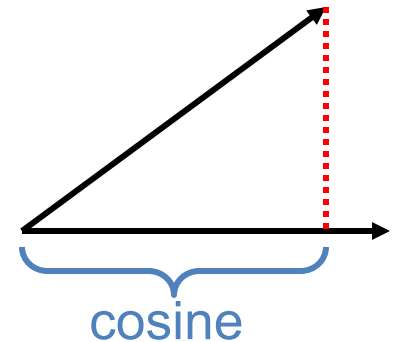
# Measures of Textual Similarity

- Classic approach: Documents/query similarity is a function of *term frequency within the document* and *across all documents*
- $TF(w)$  = frequency of term  $w$  in a document/query
  - Intuition: a word appearing more frequently in a document is more likely to be related to its “meaning”
- $IDF(w) = \log (N/n_w) + 1$ 
  - where  $N$  = total # documents,  $n_w$  is # documents containing  $w$
  - Intuition: words that appear in many documents (e.g., “the”) are generally not very informative/contentful terms
- TFIDF: contribution of each term is product of these:  
 $TFIDF(w) = TF(w) \times IDF(w)$

# Using TFIDF to Measure Similarity

- Consider each document as a list/vector:

	<b>dog</b>	<b>compute</b>	<b>window</b>	<b>...</b>
Doc. 1 = [	3.2,	0,	1.2,	... ]
Doc. 2 = [	0,	2.1,	5.4,	... ]
Doc. 3 = [	0,	1.7,	0,	... ]



- Lists/vectors are constructed such that
  - Each element of list/vector represents a term  $w_i$
  - Each element of list/vector has value:  $\text{TFIDF}(w_i)$
  - Normalize the vectors to unit length (using Euclidean norm)
- Document similarity to another document or query is measured using the cosine between the TFIDF vectors of the documents/queries
  - Cosine = vector dot product
  - Called "Vector Space Model"

# Learning Goals

1. Learning about search engines
2. Getting some hints on Assignment #7



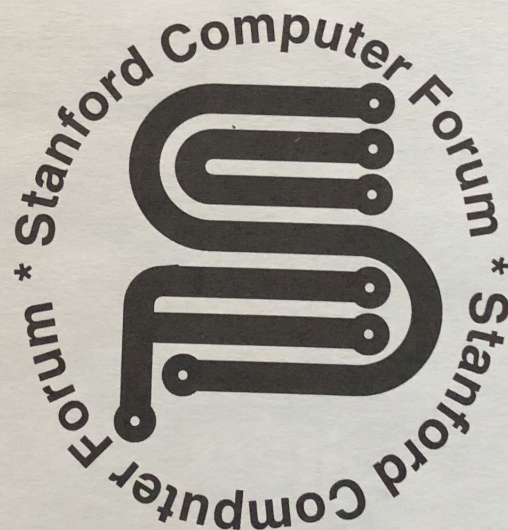
What about that  
bonus story time?!?

Bonus story time:  
Google  
(...before it was Google)



STANFORD COMPUTER FORUM  
TWENTY-NINTH ANNUAL MEETING

MARCH 19-20, 1997



Department of Computer Science  
Professor Jean Claude Latombe, Chair



**Thursday, March 20, 1997**

**1:30-3:00**

**Parallel Session III-A: Information Retrieval**

Professor Rajeev Motwani, Chair

H-P Auditorium

**1:30**

**Information Retrieval and the Web**

Larry Page

Professor Terry Winograd, Advisor

**2:00**

**Creating Personalized Yahoo!'s: Automated Hierarchical Clustering and Classification of Documents**

Mehran Sahami

Professor Daphne Koller, Advisor

**2:30**

**SenseMaker: An Information-Exploration Interface**

Michelle Baldonado

Professor Terry Winograd, Advisor

**3:00-3:15**

**Break**



**Thursday, March 20, 1997**

**10:30-12:00 Parallel Session II-A: Data Mining**  
Professor Nils Nilsson, Chair  
NEC Auditorium

**10:40 Adaptive Web Page Recommendation**  
Marko Balabanovic                      Professor Yoav Shoham, Advisor

**11:05 Problems in Data Mining**  
Sergey Brin                      Professor Hector Garcia-Molina, Advisor

**11:30 Association Rules**  
Craig Silverstein                      Professor Rajeev Motwani, Advisor

**12:00-1:30 Lunch**  
Gates Building, Room 104



**Wednesday, March 19, 1997**

**8:30-9:00      Registration and Continental Breakfast**  
Gates Building, Basement Lobby

**9:00-10:30    Opening Session**  
Gates Building, H-P Auditorium

**Welcoming Remarks**

Carolyn Tajnai, Director, Computer Forum  
Professor Yoav Shoham, Annual Meeting Program Chair

**Department Greetings**

Professor Jean-Claude Latombe, Chairman, Computer Science Department  
William F. Miller, Computer Forum Faculty Chair

**9:30            Keynote Address**  
Dr. Eric Schmidt, CTO, CEO, Sun Microsystems  
Evolution or Revolution? The Future of Network Computing

**10:30-11:00   Break**

# Google's Beginnings

- In mid-1990's, Larry Page and Sergey Brin did research as part of the Stanford Digital Library project
  - Original project was called "BackRub"
- Large parts of Google were originally built in Python
  - Here's some of that code (it's written in Python 1.4)

```
class RobotFileParser:
```

```
    def __init__(self):  
        self.rules = {}
```

```
    def parse(self, lines):  
        active = []  
        for line in lines:  
            # blank line terminates current record  
            if not line[:-1]:  
                active = []  
                continue  
            # remove optional comment and strip line  
            line = string.strip(line[:string.find(line, '#')])
```

```
    ...
```



**http://google.stanford.edu**

The image shows the original Google search engine interface. At the top is the word "Google!" in its iconic multi-colored font. Below it is a search bar with the text "Search the web using Google!". To the left of the search bar is a dropdown menu showing "10 results". To the right are two buttons: "Google Search" and "I'm feeling lucky". Below the search bar is the text "Index contains ~25 million pages (soon to be much bigger)". In the center is a link "About Google!". Below that are two links: "Stanford Search" and "Linux Search". At the bottom is a section for email updates with the text "Get Google! updates monthly!". It includes a text input field labeled "your e-mail", a "Subscribe" button, and an "Archive" link. At the very bottom, the copyright notice "Copyright ©1997-8 Stanford University" is highlighted with a red box.

Google!

Search the web using Google!

10 results Google Search I'm feeling lucky

*Index contains ~25 million pages (soon to be much bigger)*

[About Google!](#)

[Stanford Search](#) [Linux Search](#)

Get Google! updates monthly!

your e-mail Subscribe [Archive](#)

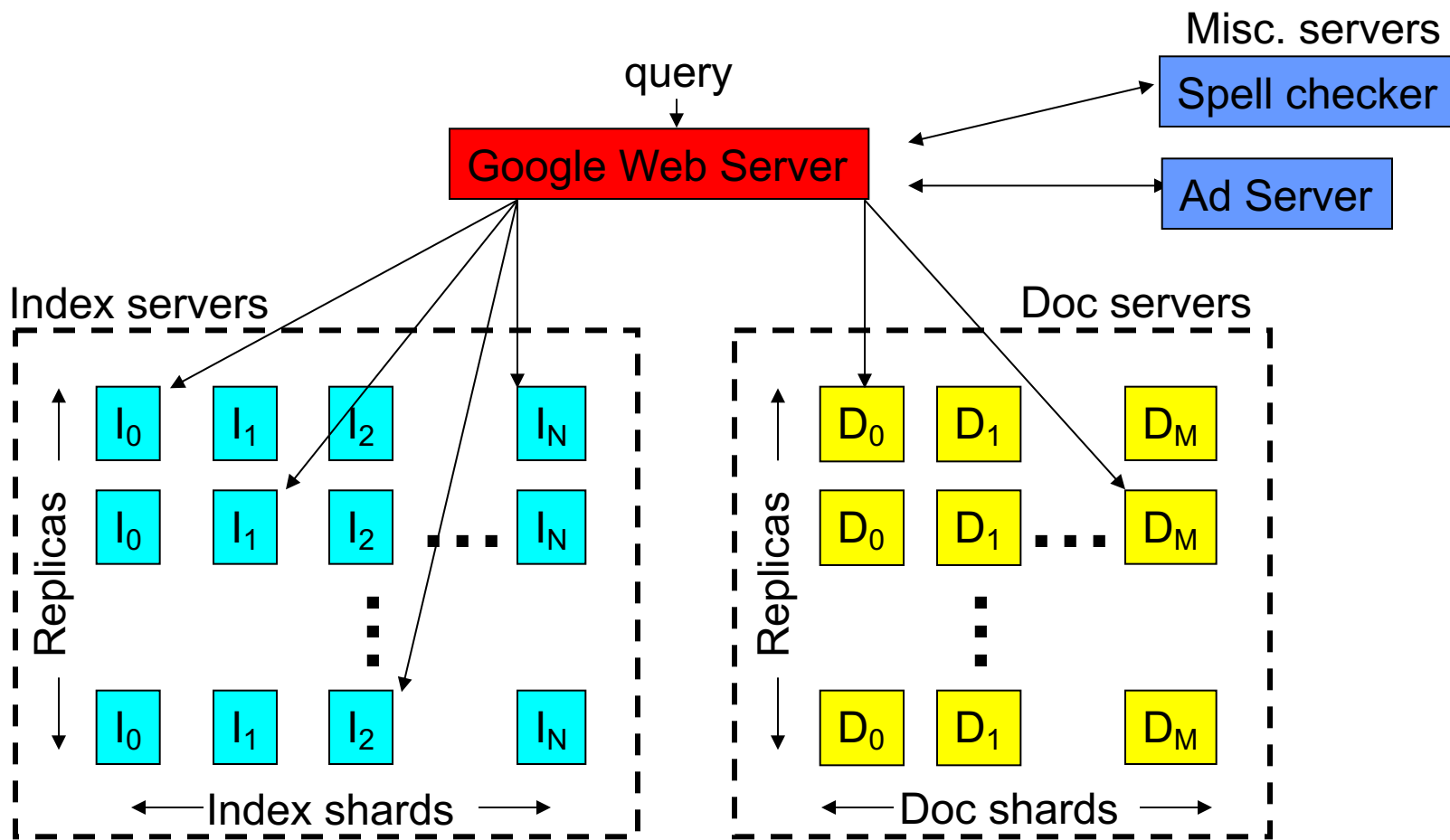
Copyright ©1997-8 Stanford University

*Image courtesy of Google*

# Google's Index (circa 2004)

- Too large to fit in memory for one machine
- Split index into pieces, called *shards*
  - Shards are small enough to have several per machine
  - Replicate the shards for robustness
- Need to still store original documents
  - Want to show users “snippets” of query terms in context
  - Use same sharding concept to store original documents
- Replicate this whole structure within/across data centers

# Google Infrastructure (circa 2004)



Elapsed time: 0.25s, machines involved: 1000+

# Ranking Documents in Web Search

- Many early search engines used traditional techniques
  - TF x IDF vectors
  - Weight position on page (near top, in title better)
  - Weight proximity of terms on a page
- They were quickly “spammed” badly
  - Keyword stuffing (entire dictionaries in white/hidden text)
  - Word replacement in otherwise legitimate text
  - Cloaking: serving search engines one page and users another
- Anyone remember Alta Vista, Lycos, Infoseek...?

# Keyword Stuffing

- Put words in tiny white font on white background on the web page.
  - Search engine still indexes all those terms!

Rock n' roll t-shirts, Buy1Get1Free, Korn T-shirts, Metallica t-shirts, Metallica, Metallica Longsleeves, Metallica Sweatshirts, Metallica Flags, Limp Bizkit T-shirts, Limp Bizkit, Limp Bizkit Longsleeves, Limp Bizkit Sweatshirts, ... t-shert, t-shirts, the biggest T-shirt store on this planet, t-sit, T-SIT, t-shiitrt, T-SHIIRT, t-shiirts, T-SHIIRTS, t-sshirt, T-SSHIRT, t-sshirts, T-SSHIRT, tt-shirt, TT-SHIRT, tt-shirts, TT-SHIRTS, T-SHIRT, t--shirt, T--SHIRT, t--shirts, T--SHIRTS, t-shhirt, T-SHHIRT, t-shhirts, T-SHHIRTS, t-shirrt, T-SHIRRT, t-shirrts, T-SHIRRTS, t-shirtt, T-SHIRTt, t-shirtts, T-SHIRTTS, tshirt, TSHIRT, tshirts, TSHIRTS, tshits, TSHITS, tshit, TSHIT, tsir, TSIR, t tsirts, T TSIRTS, shirt, SHIRT, tshaert, TSHAERT, tshert, TSHERT, TSHEART, tshurt, t-shurt, t-shert, tee-shert, tee shert, tee short, tee shurt



# New Method for Ranking on the Web

- Content of a page is under editorial control of writer
- Using only content on page to rank documents puts ranking in hands of page *writer*
- Google made two innovations early on (using links):
  - Anchor text
    - Use text in link pointing to a page
  - Spectral link analysis
    - Use graph structure of the web to infer importance of page
    - PageRank algorithm
- Assumption: it is harder to manipulate pages not under your own control

# Leverage Anchor Text Information

```
<A href=http://www.stanford.edu>
```

Stanford University home page

```
</A>
```



- Anchor text tells us what link author thinks of page being pointed to
- Link text is generally not in the control of the same author that wrote the page being pointed to
- Quality of the referring page allows us to estimate the quality of the target page

# Analyzing Link Reference Structure

- Simple citation counting doesn't work
  - Easy to outwit
  - Just create lots of links to a page from any other page
  - E.g., Create a page A with 10,000 links to page B
- Quality of citing page is a factor
  - Page A:

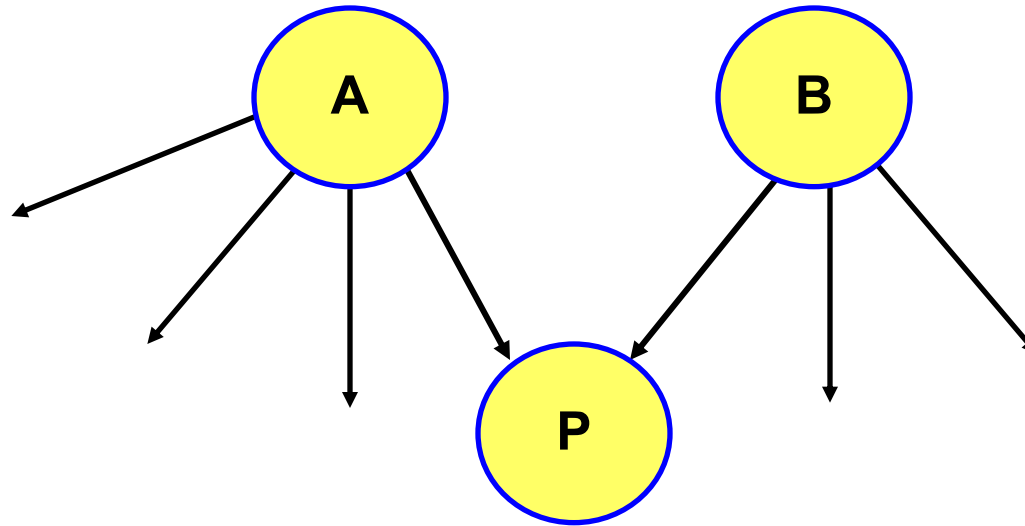
I have 5 links and you have only 2 links so I must be better.
  - Page B:

Oh yeah, but **New York Times** points to me!

# PageRank Algorithm

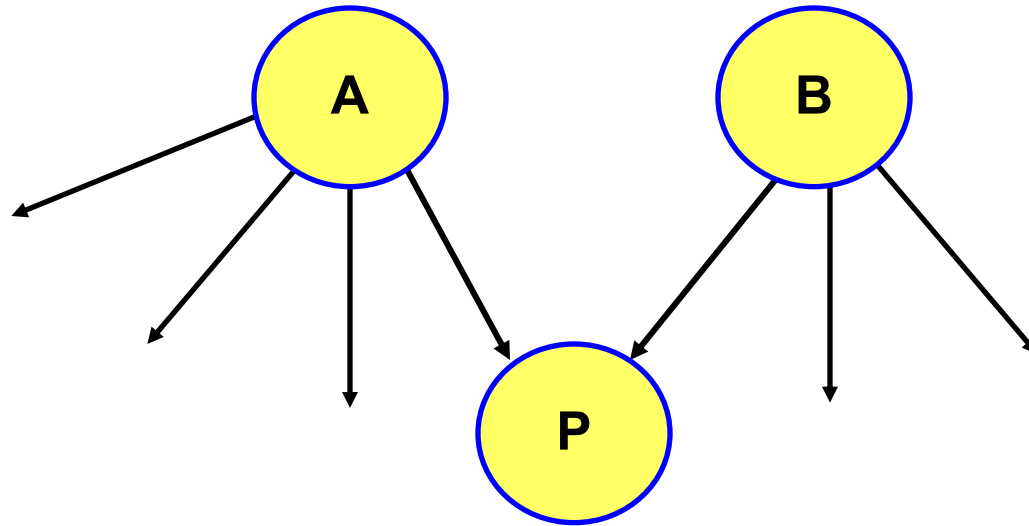
- Ranking technology based on link structure analysis
  - Invented by Larry Page (the “Page” in PageRank) in 1997
  - Stanford actually owns the patent (licensed by Google)
- Provides measure of a web page’s “importance”
  - Measures not just how many links point to a page, but how important the pages are that contain those links
- Analyzes the web as a graph
  - Not dependent on contents of single page
  - Linkers, not page author, are judge of page
  - Spam resistant
  - Shows a truly innovative application of graph theory

# The Web as a Graph



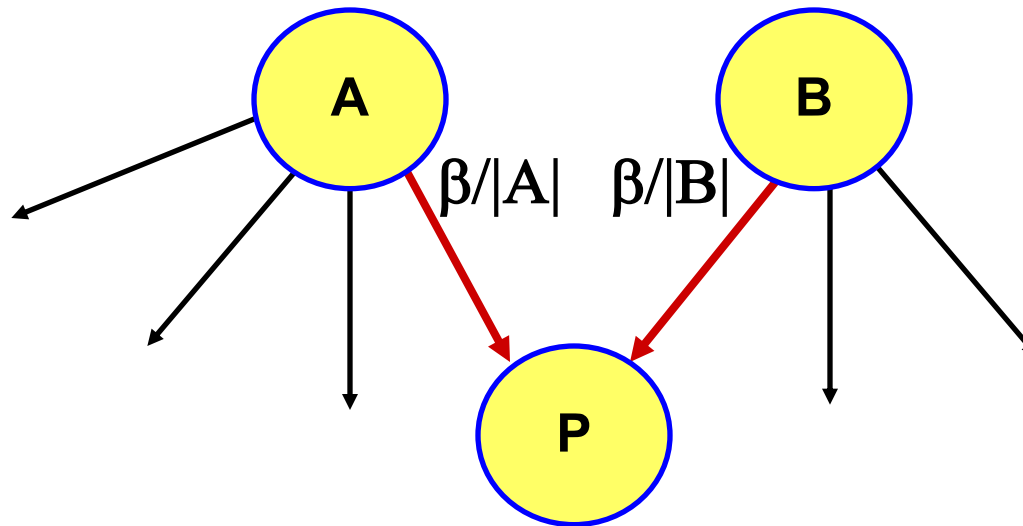
- **Vertices:** web pages
- **Edges:** links from one page to another
- Consider the web as a weighted graph
- **Weights:** numbers associated with each edge

# PageRank: Show Me the Randomness!



PageRank measures the probability that a “random surfer” will be at a given page in the following surfing model

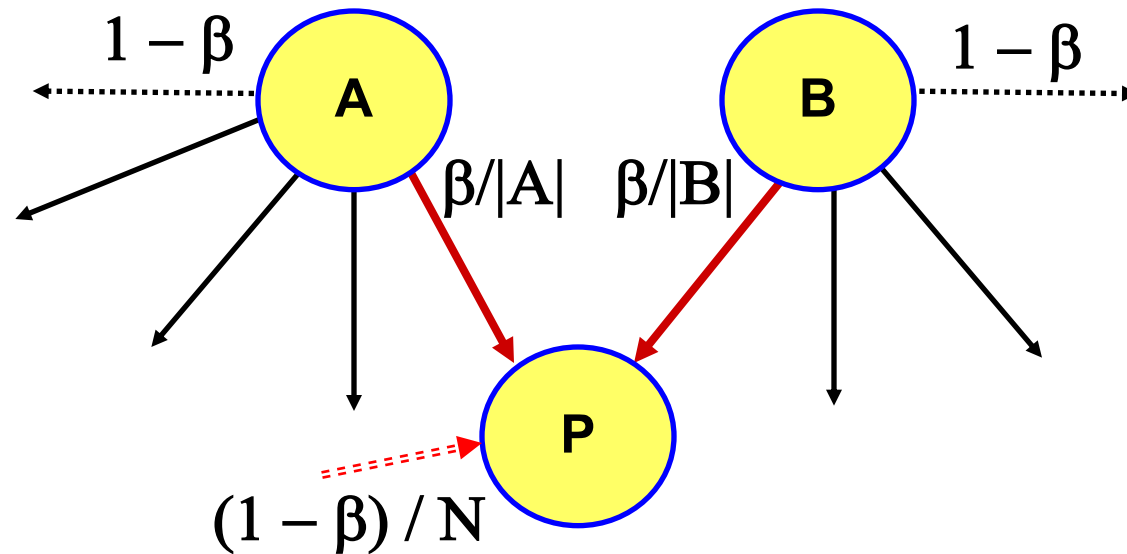
# PageRank: Random Surfer Model



At every clock tick the surfer surfs:

- forward over a random out-link with probability  $\beta$

# PageRank: Random Surfer Model

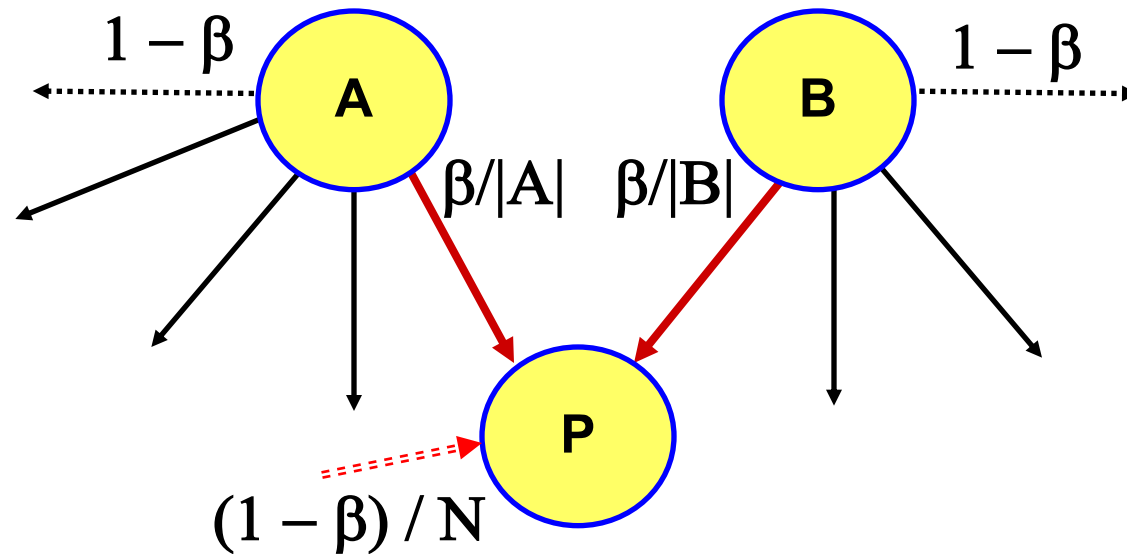


At every clock tick the surfer surfs:

- forward over a random out-link with probability  $\beta$
- and otherwise jumps to random web page (probability  $1 - \beta$ )



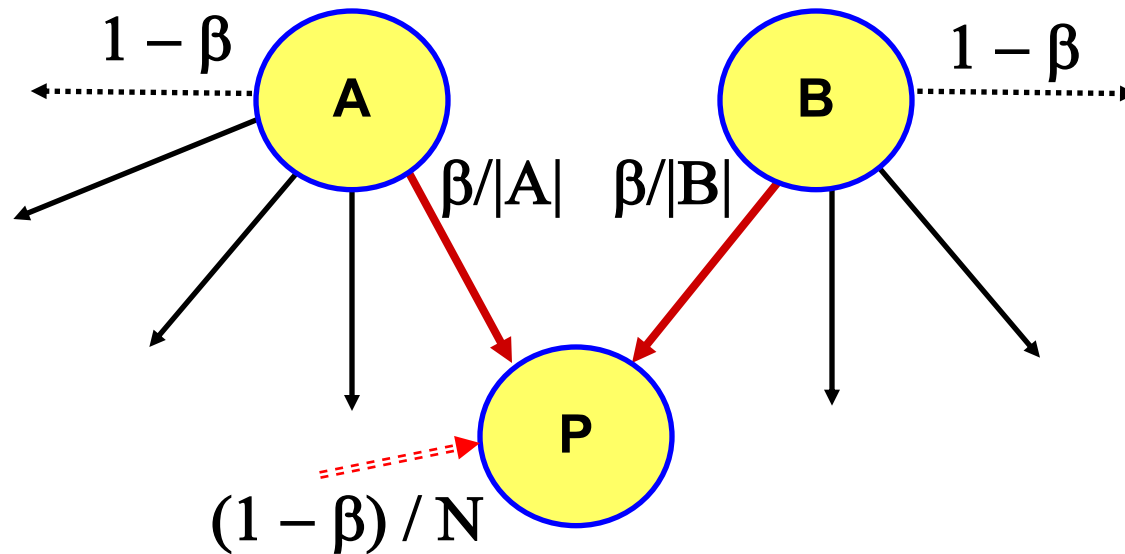
# PageRank: Random Surfer Model



PageRank of P =

$$\beta[(1/4)(\text{PageRank of A}) + (1/3)(\text{PageRank of B})] + (1 - \beta)/N$$

# PageRank: Random Surfer Model



At every clock tick the surfer surfs:

- forward over a random out-link with probability  $\beta$
- and otherwise jumps to a random web page (probability  $1 - \beta$ )
- PageRank is fixed point of this model
- Intuitively: the total fraction of time a surfer spends on a page

# For Those Who Really Dig Matrices

$$\mathbf{M}' = (1 - \beta)\mathbf{R} + \beta\mathbf{M}$$

$$\mathbf{P} = \mathbf{M}'^T \mathbf{P}$$

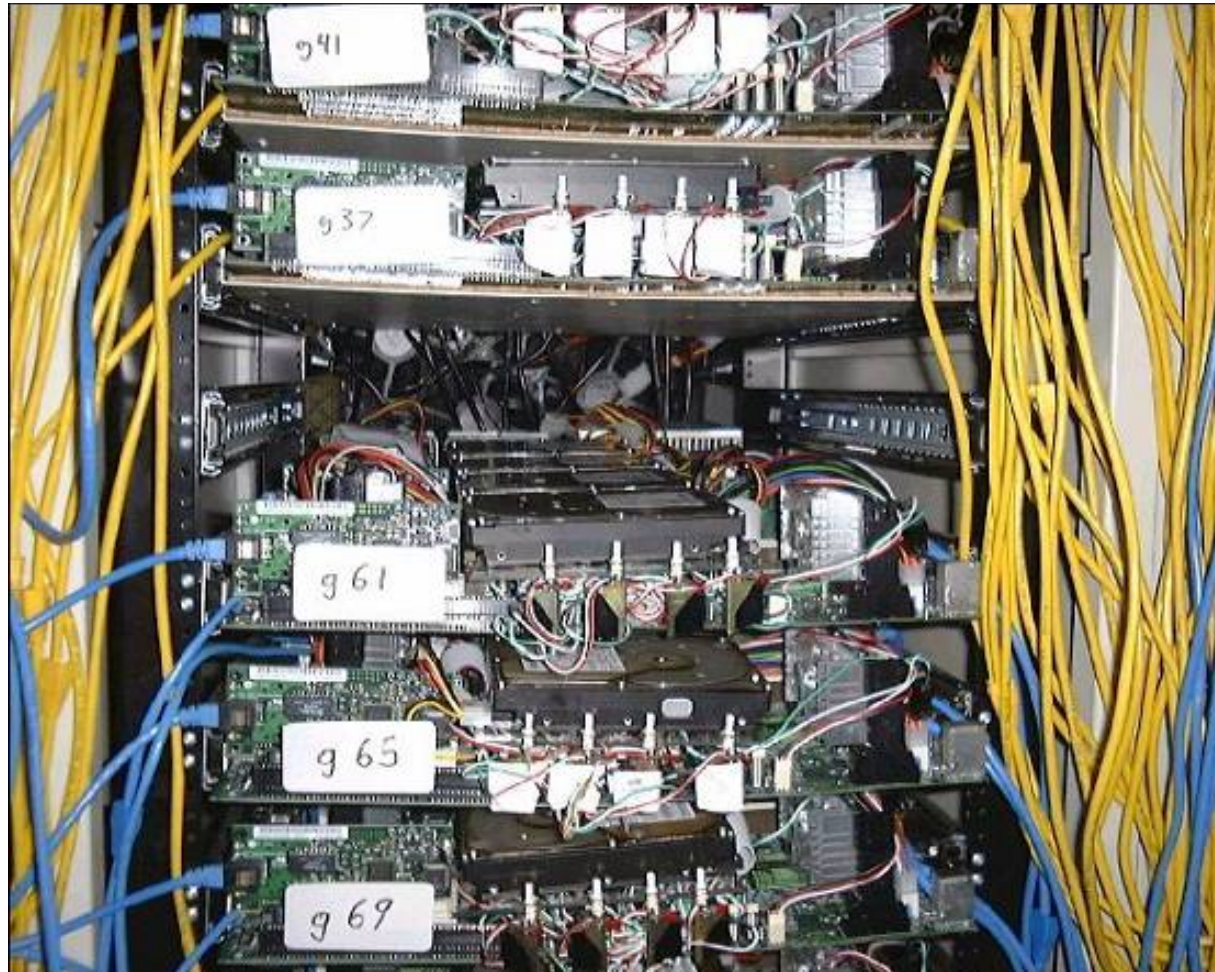
- Where:
  - $\mathbf{M}$  = normalized web-adjacency (probability) matrix
  - $(1 - \beta)$  = reset probability
  - $\mathbf{R}$  = “reset” matrix ( $= [1/N]_{N \times N}$ )
  - $\mathbf{P}$  = PageRank vector
  - $\mathbf{P}$  is the principal eigenvector of  $\mathbf{M}'$  (bonus)

google.stanford.edu (circa 1997)



*Image courtesy of Google*

# google.com (1999)



*Image courtesy of Google*



# Google Data Center (circa 2000)



*Image courtesy of Google*

# Empty Google Data Center (2001)



*Image courtesy of Google*



# 3 Days Later...



*Image courtesy of Google*



# A Day in the Life of Google

A picture is worth a few hundred million search queries...

Thu Aug 14 00:00:00 PDT 2003



*Image courtesy of Google*