



Trees

Chris Piech

CS 106B
Lecture 18
Feb 8, 2016

Socratic



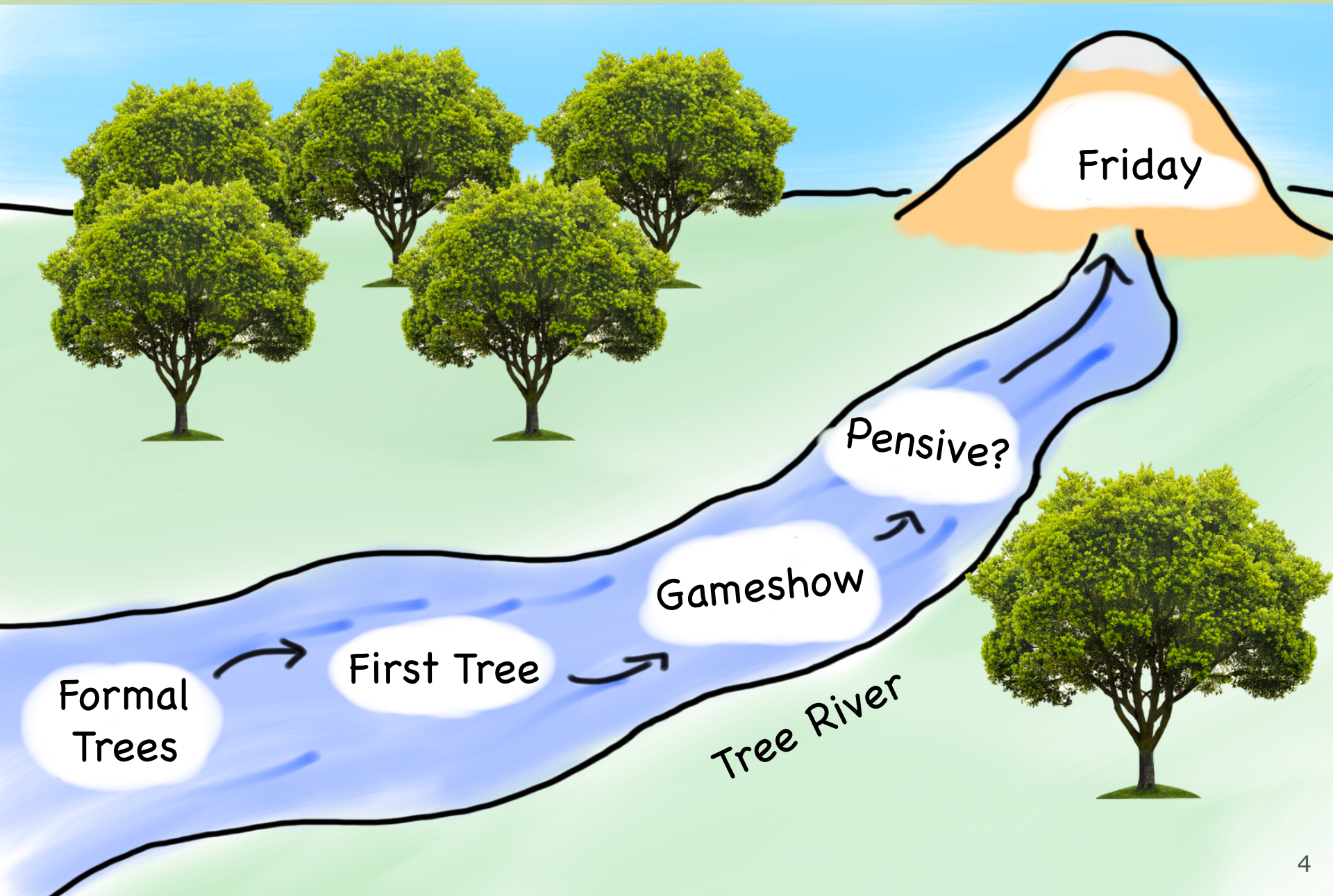
Room: **106BWIN16**

Today's Goal

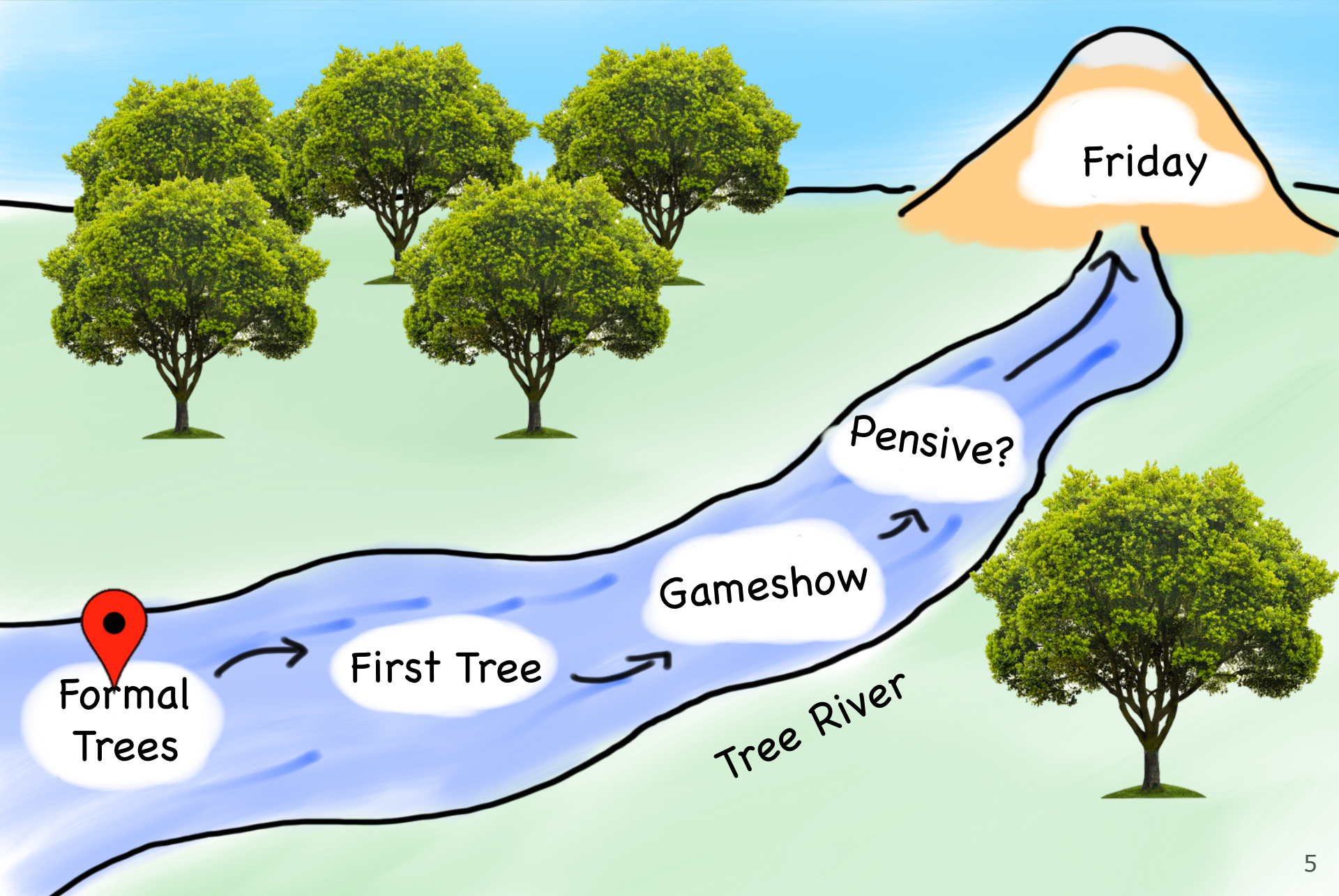
1. Be able to define a tree
2. Be able to traverse a tree



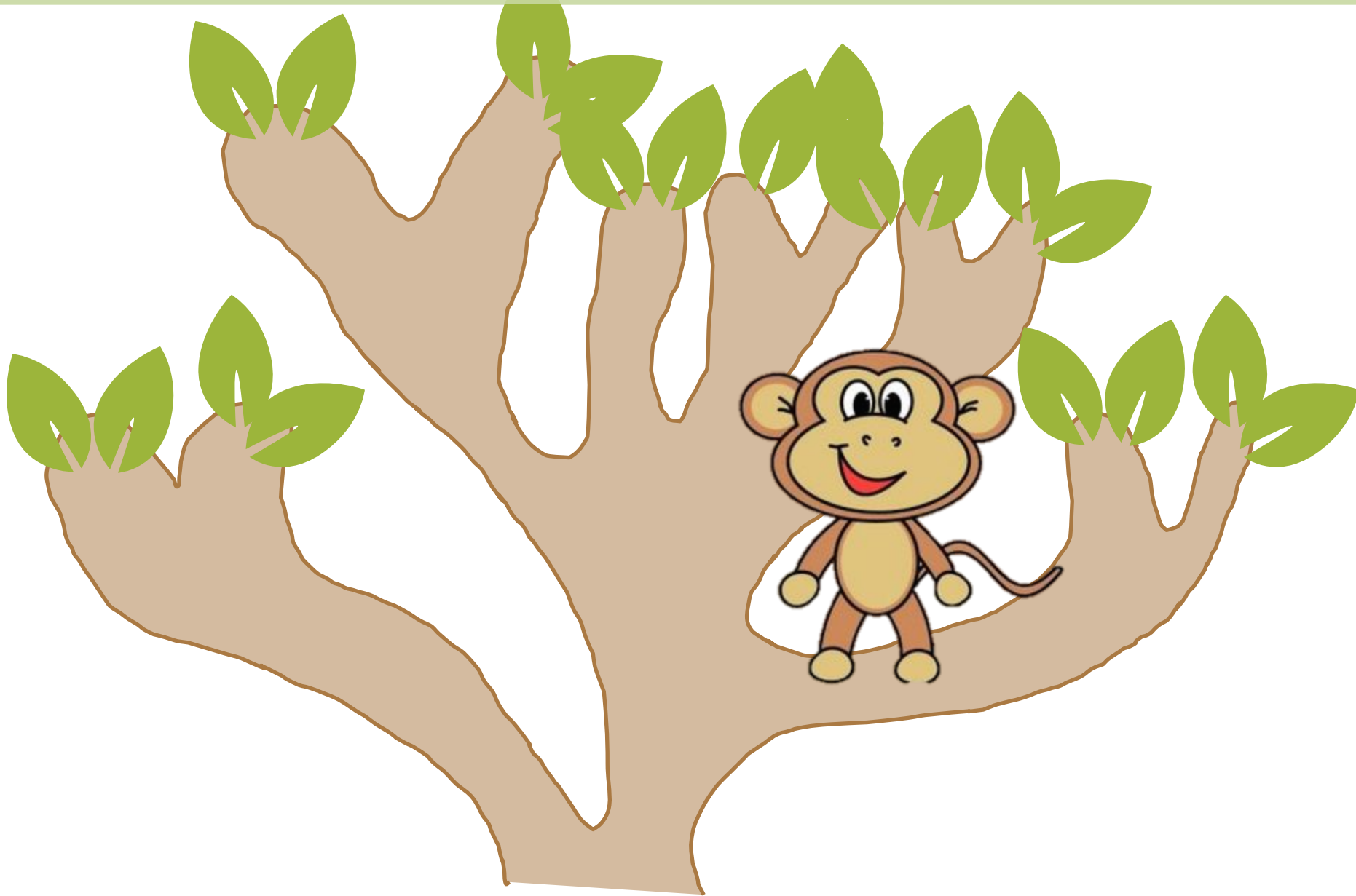
Today's Route



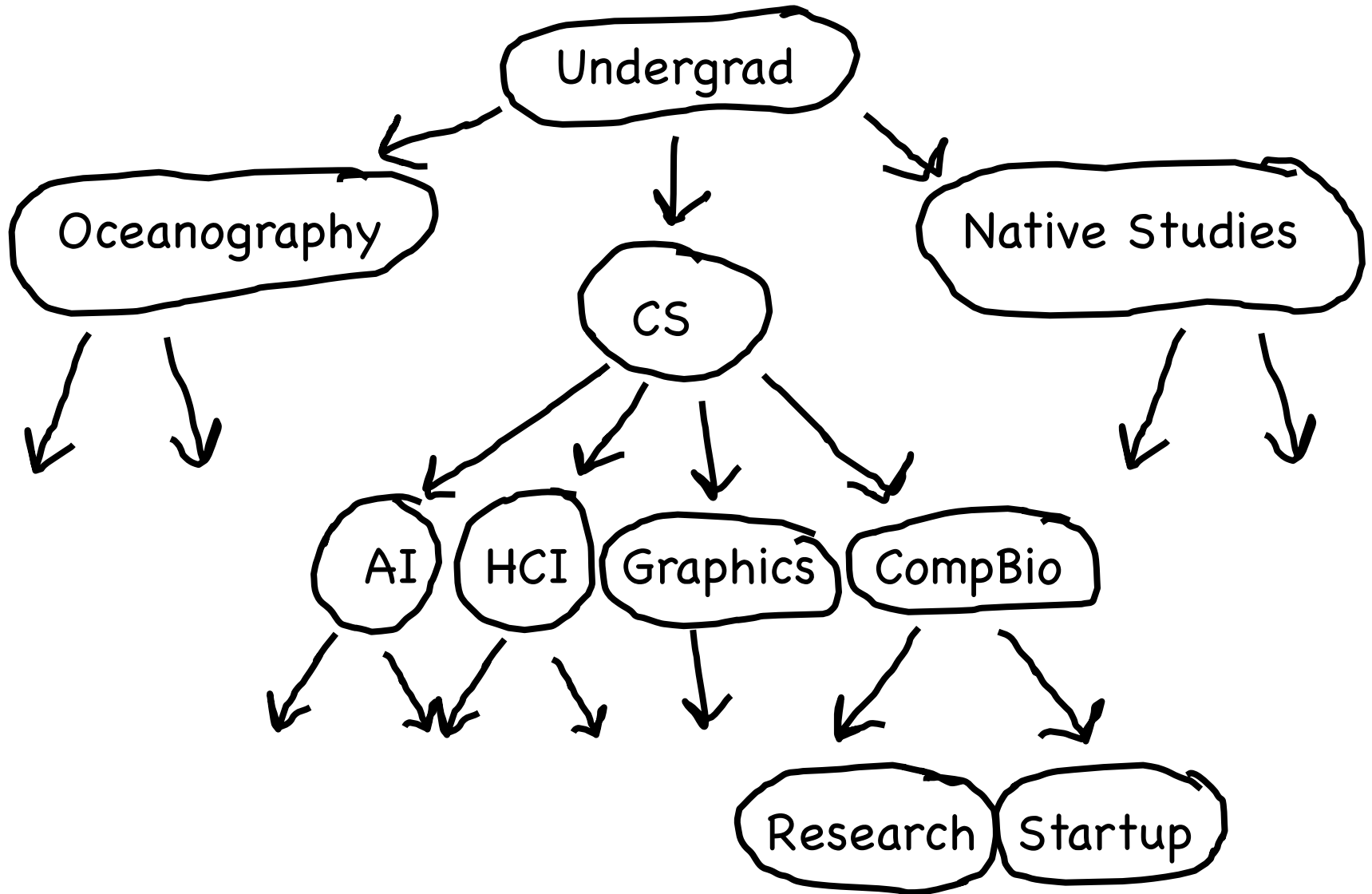
Today's Route



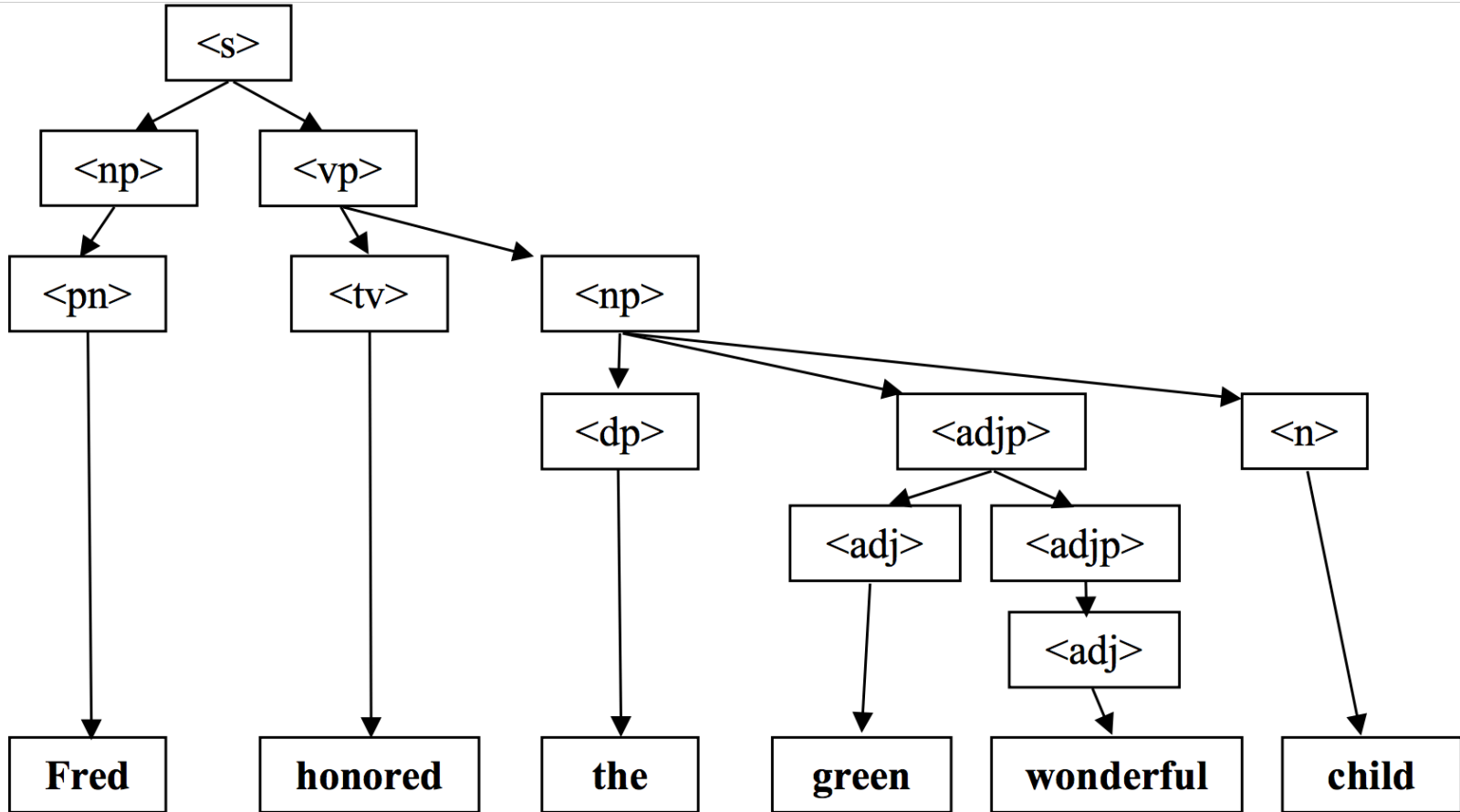
Recursive Exploration



Decision Trees

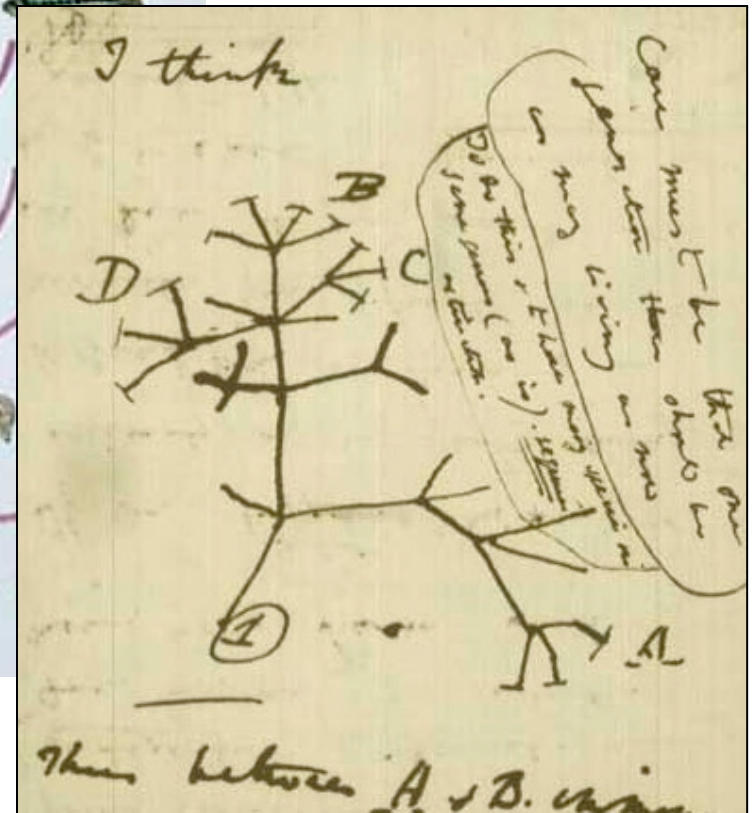
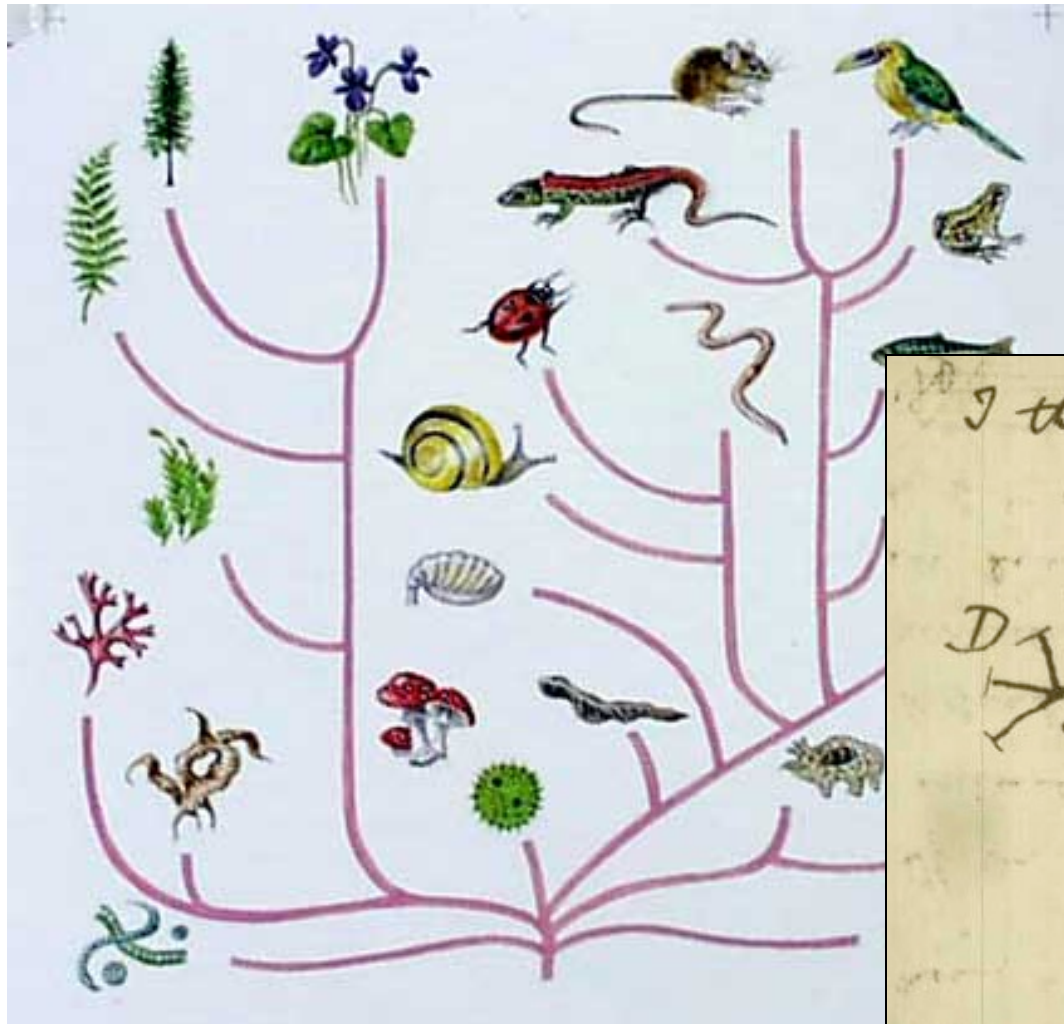


Syntax Tree

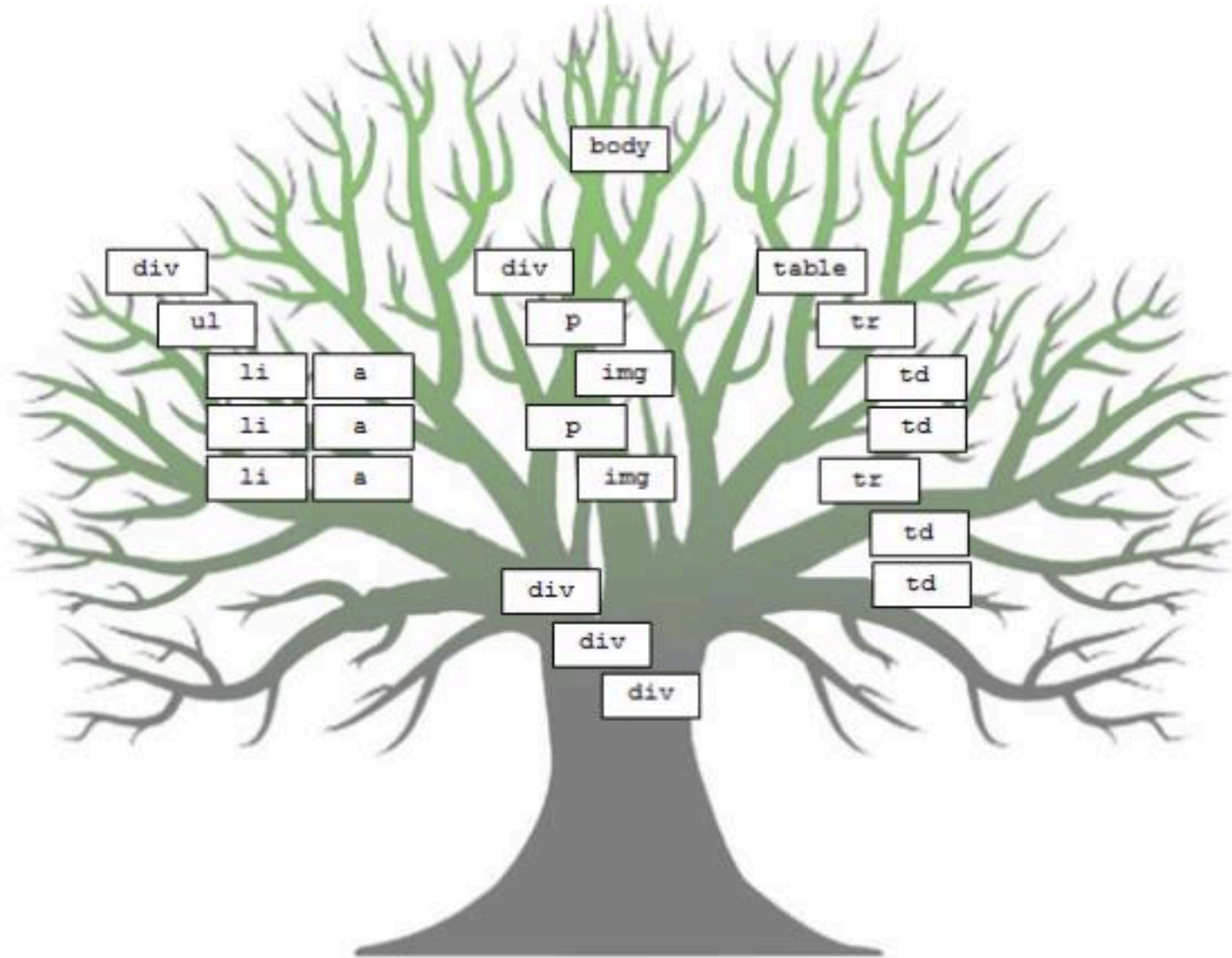


Random expansion from sentence.txt grammar for symbol "<s>"

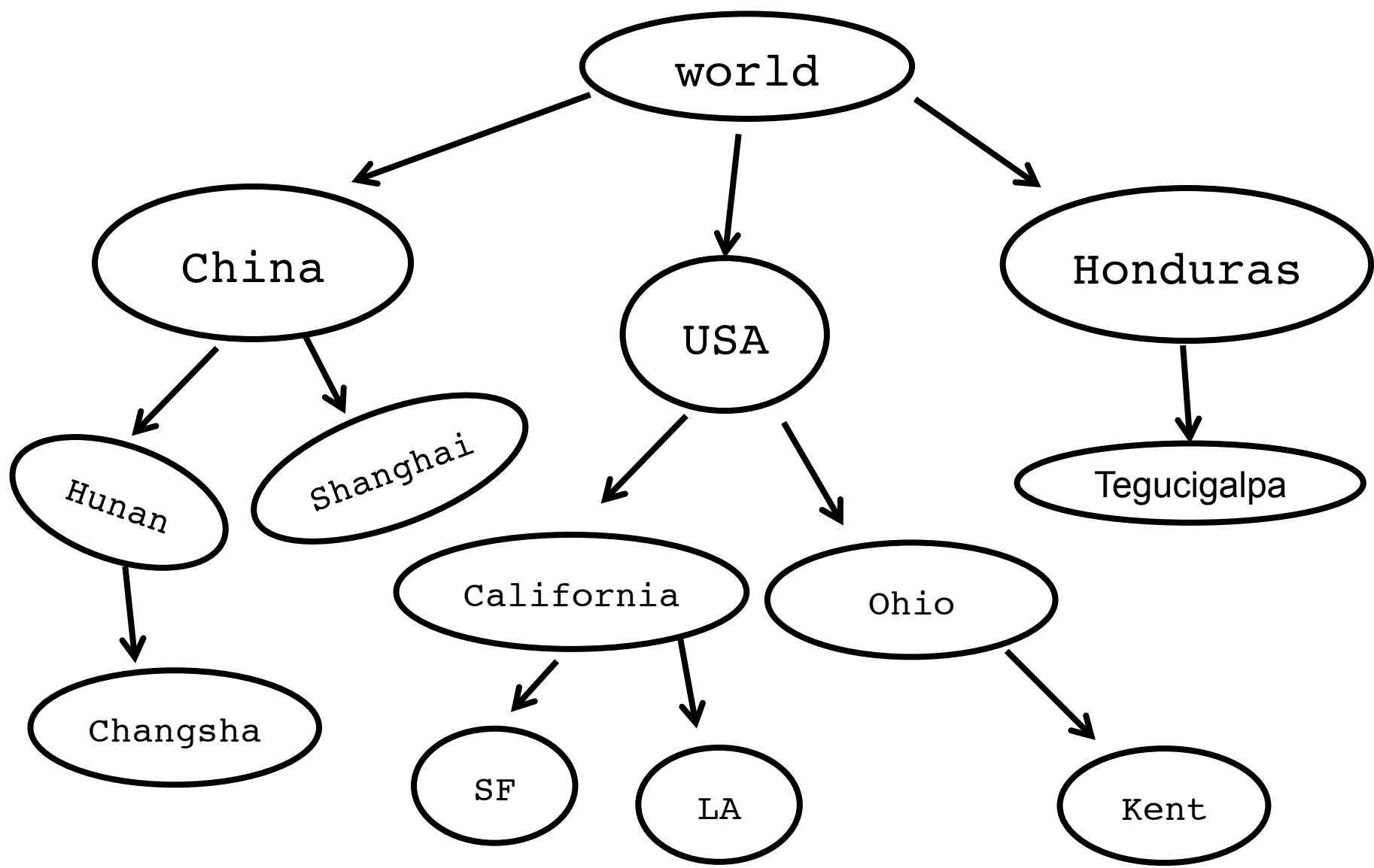
Animal Tree



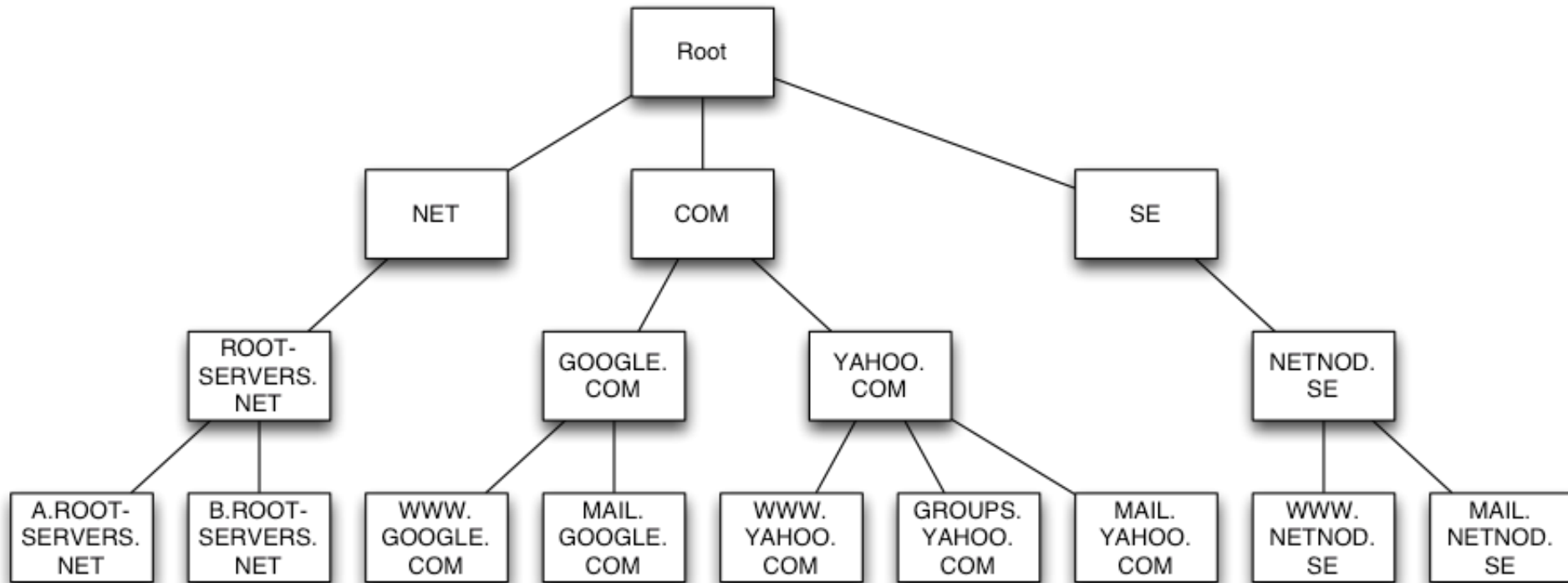
Websites



Hierarchies

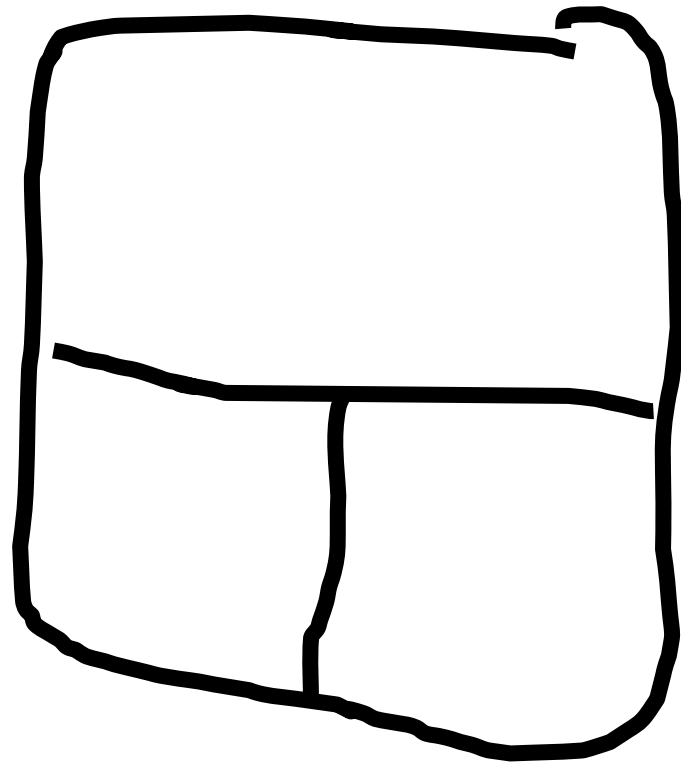


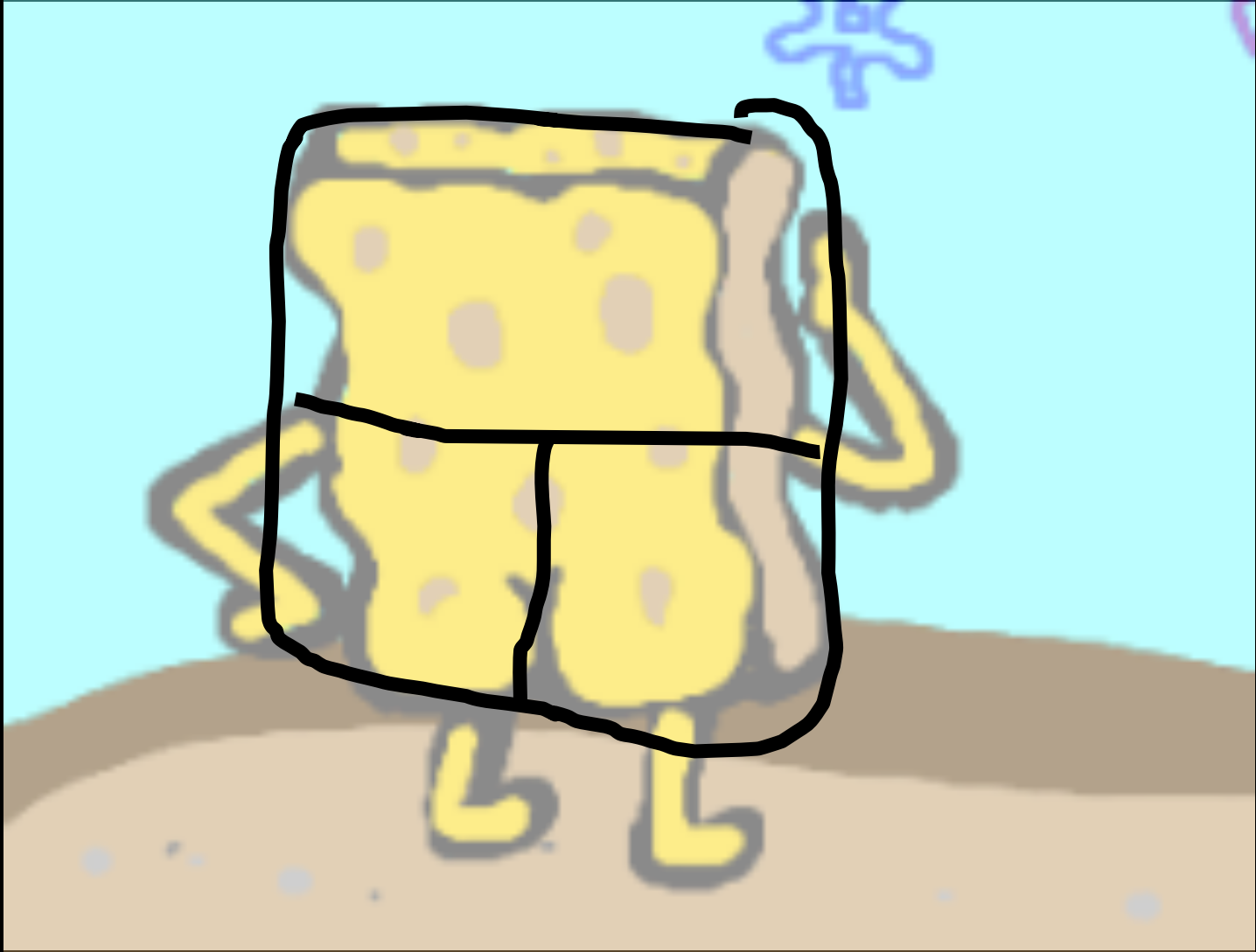
Internet Domains



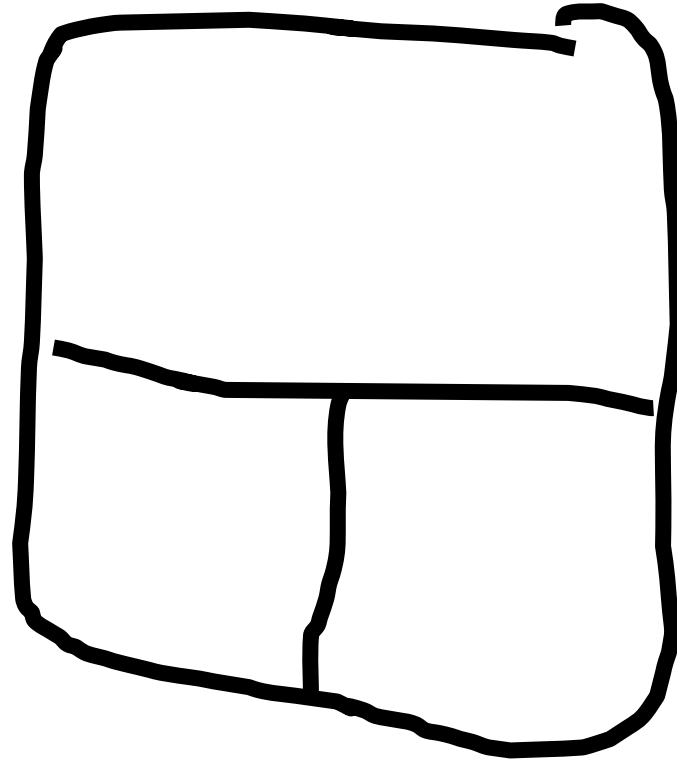
We have seen: Recursion on Trees

But How About Making a Tree Variable?

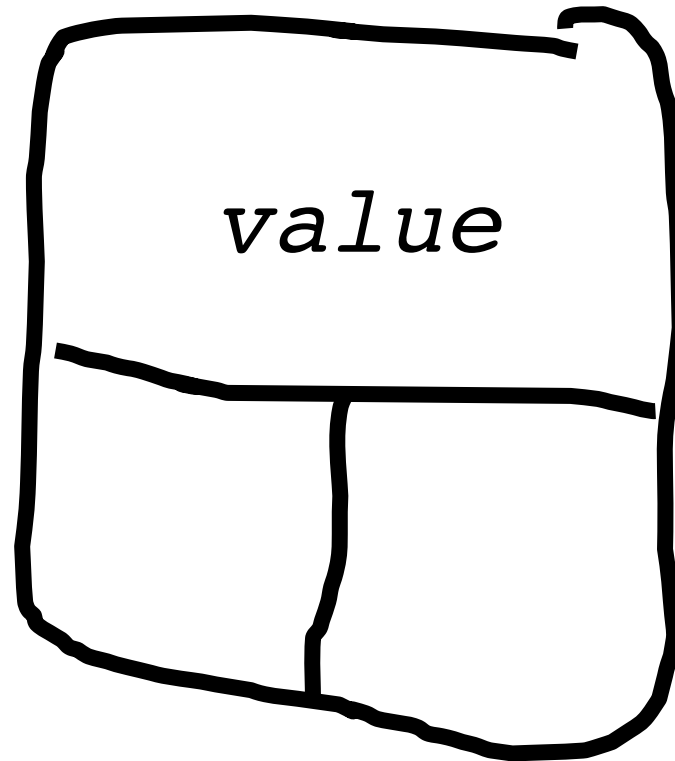




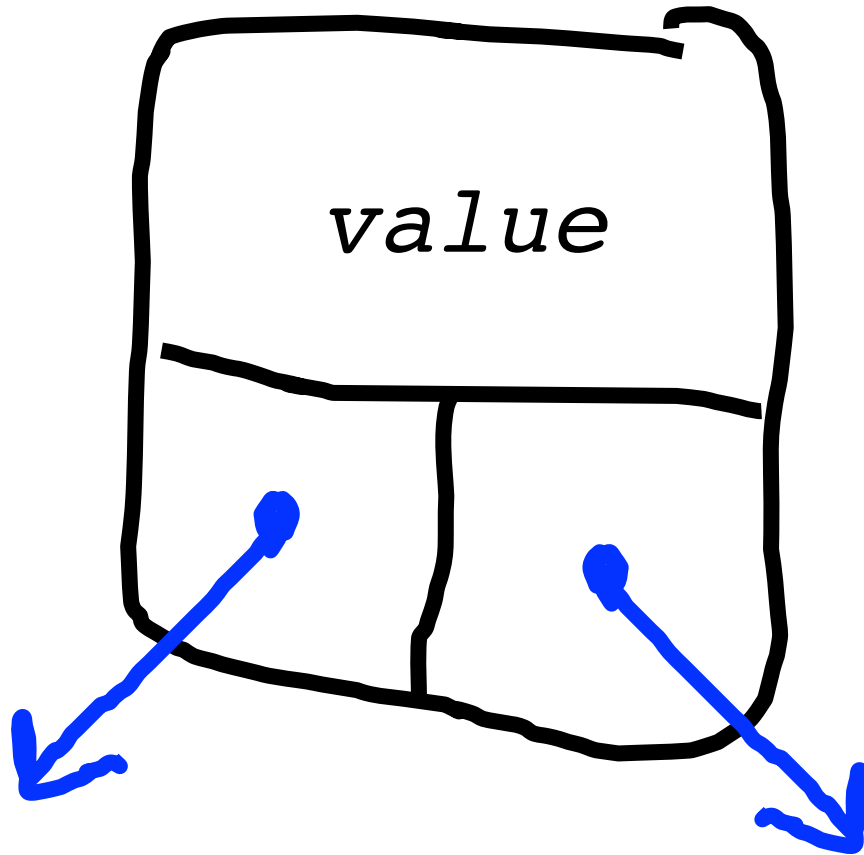
Binary Tree:

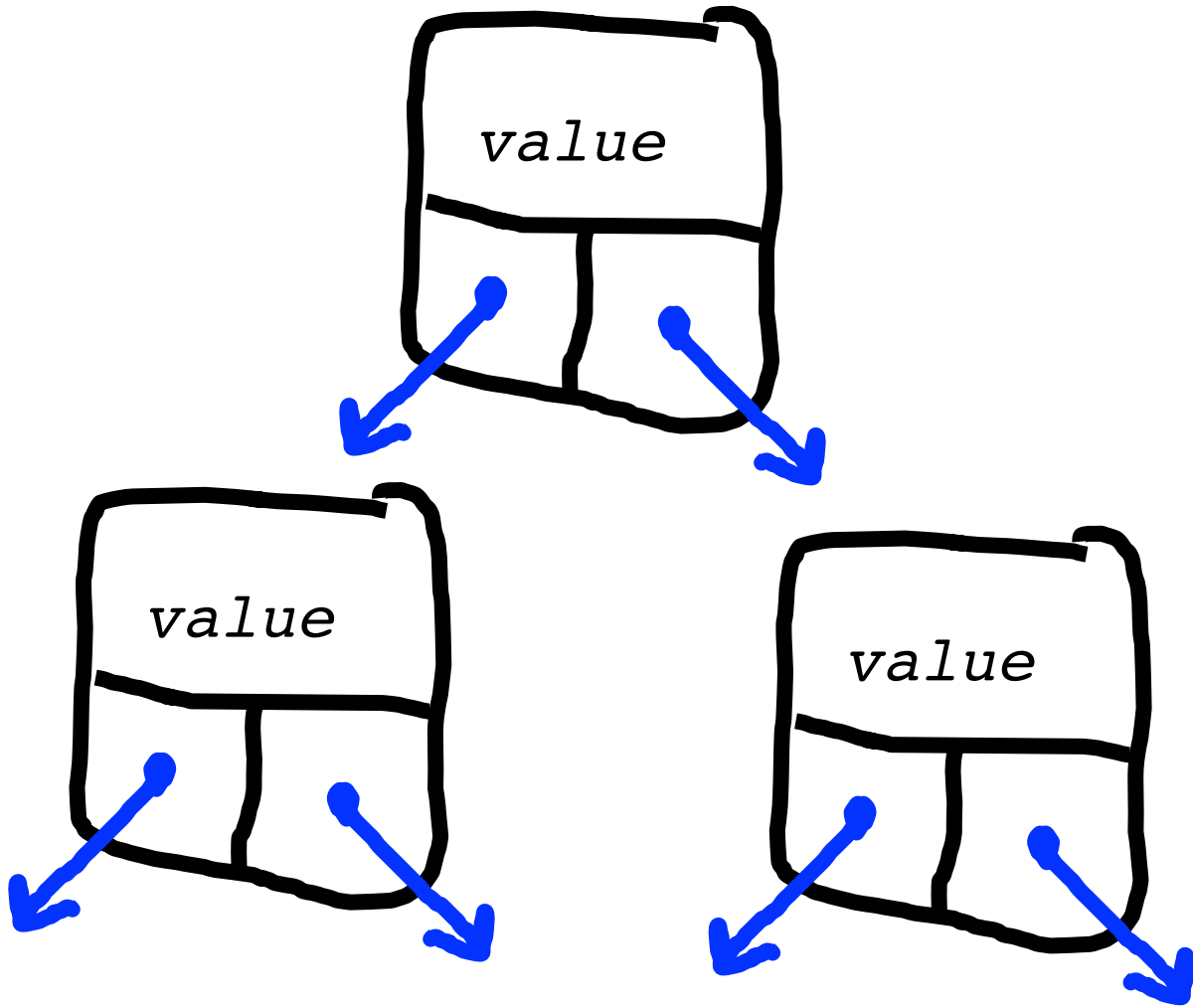


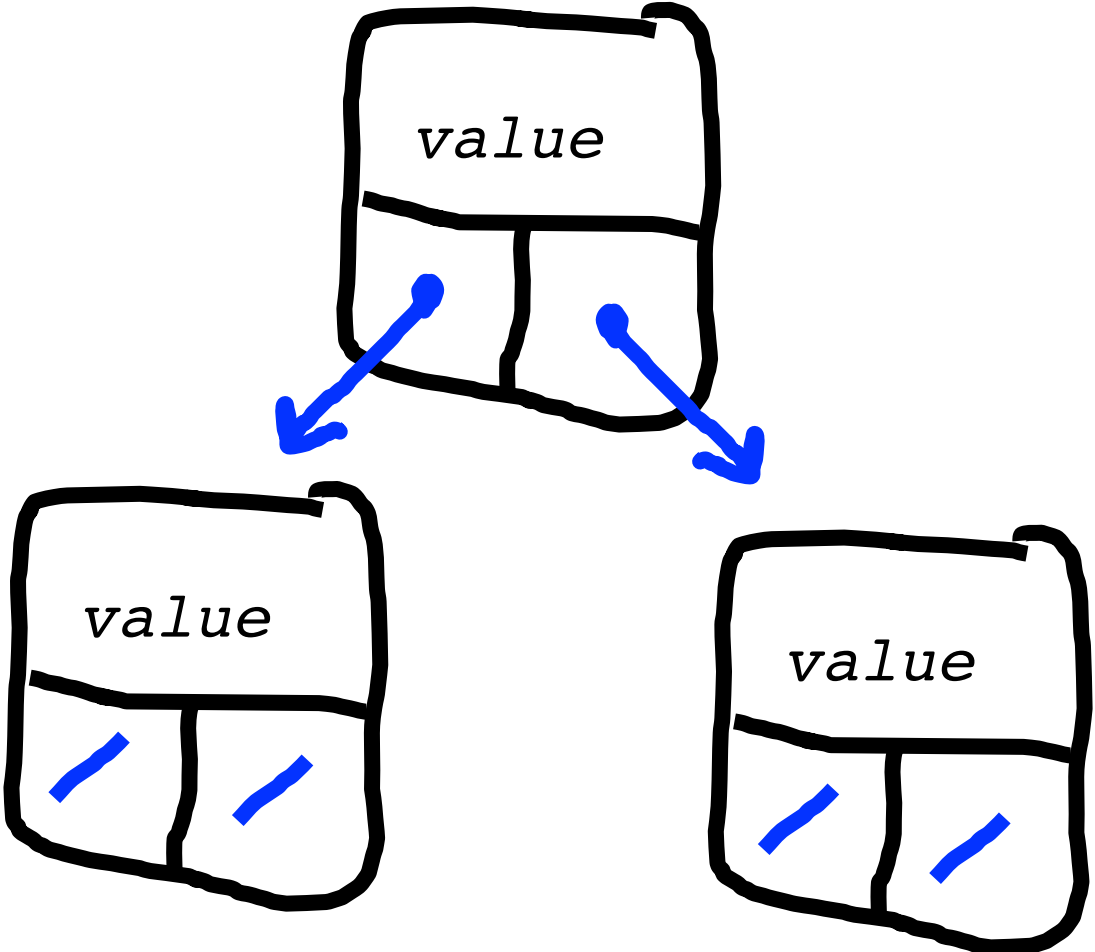
Binary Tree:



Binary Tree:



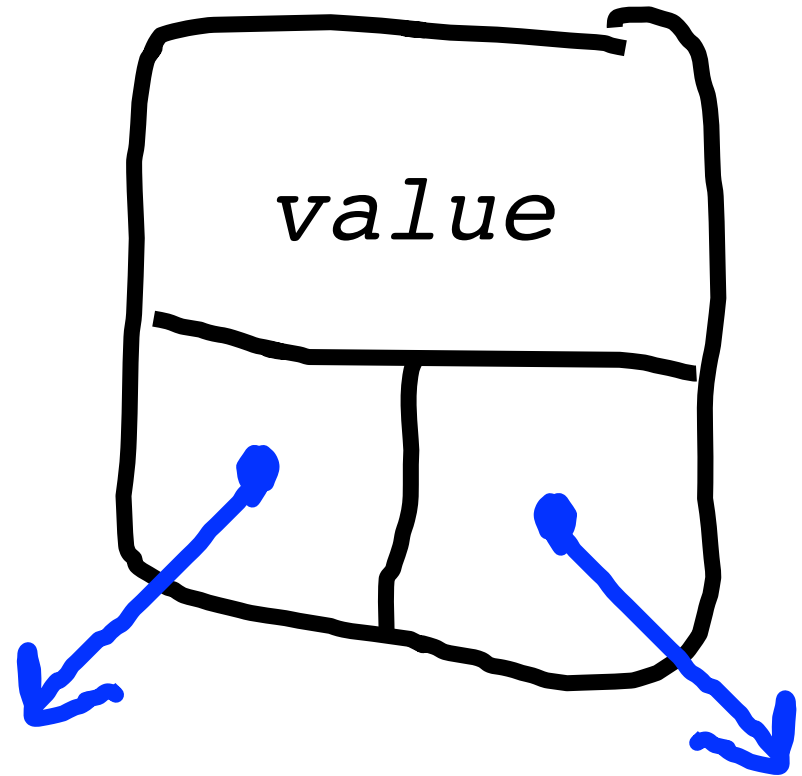




Most Important Slide

Binary Tree

```
struct Tree {  
    string value;  
    Tree * left;  
    Tree * right;  
};
```

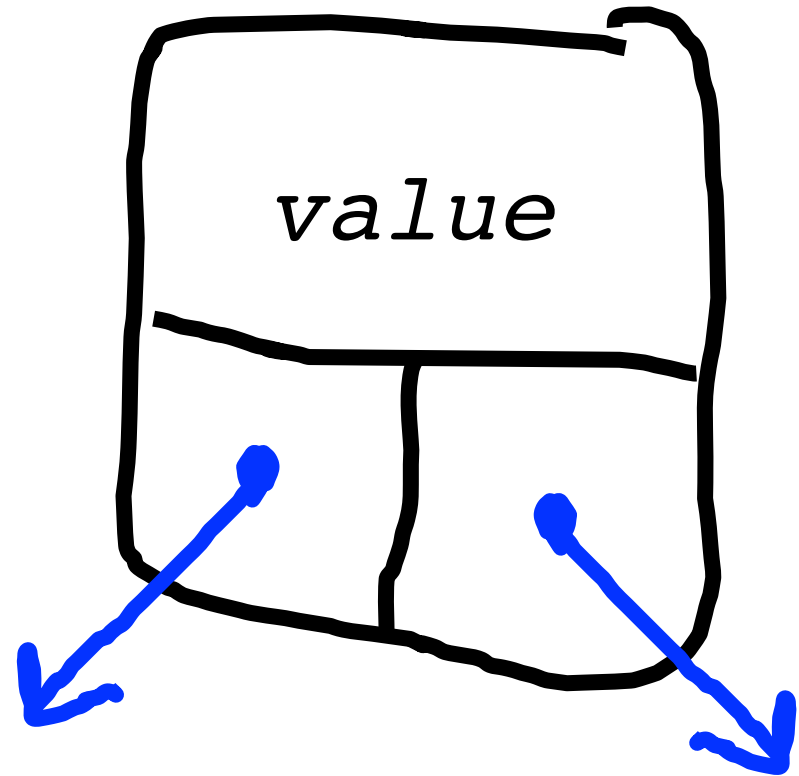


Does value have to be a string?

No

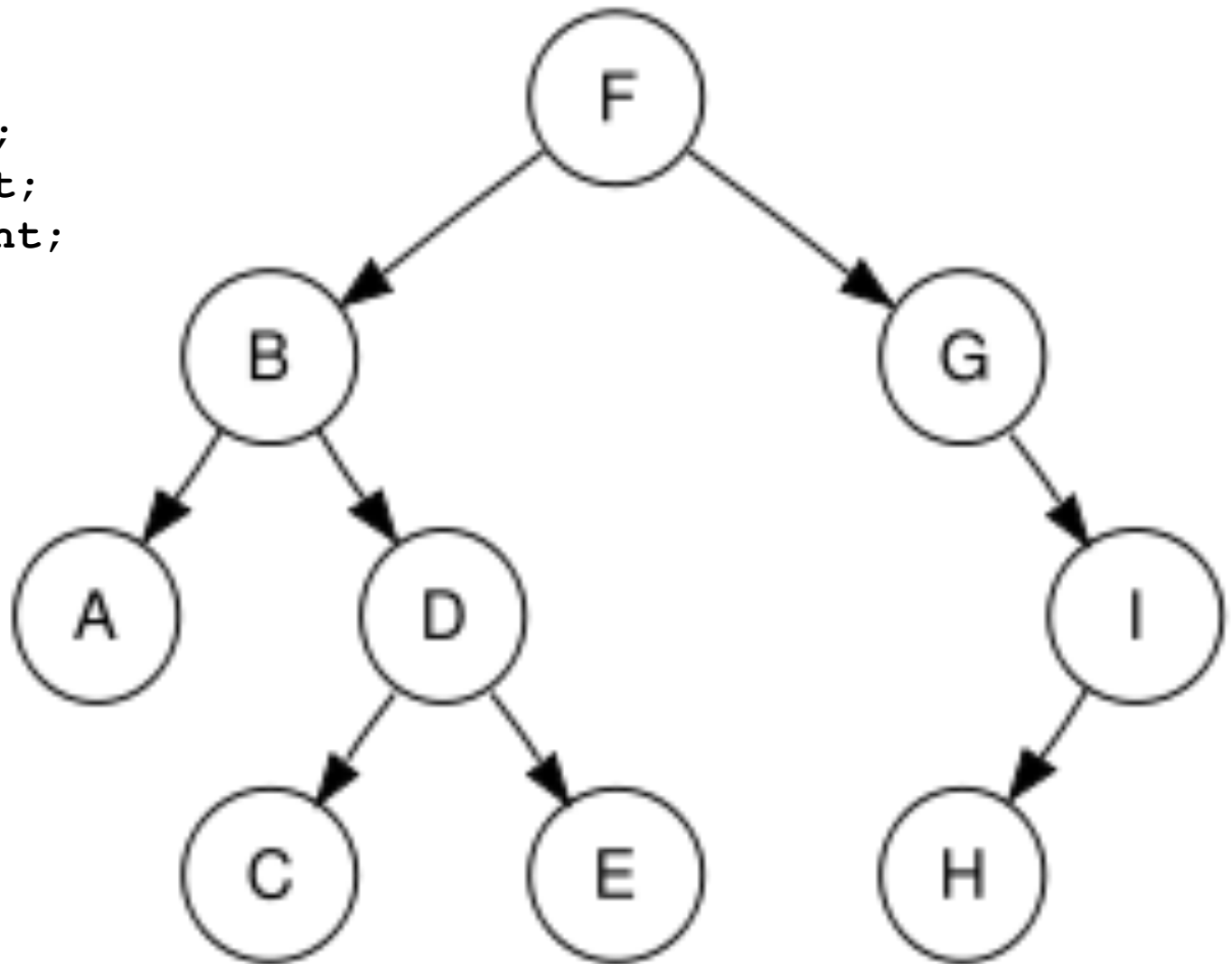
Binary Tree

```
struct Tree {  
    string value;  
    Tree * left;  
    Tree * right;  
};
```



Example Binary Tree

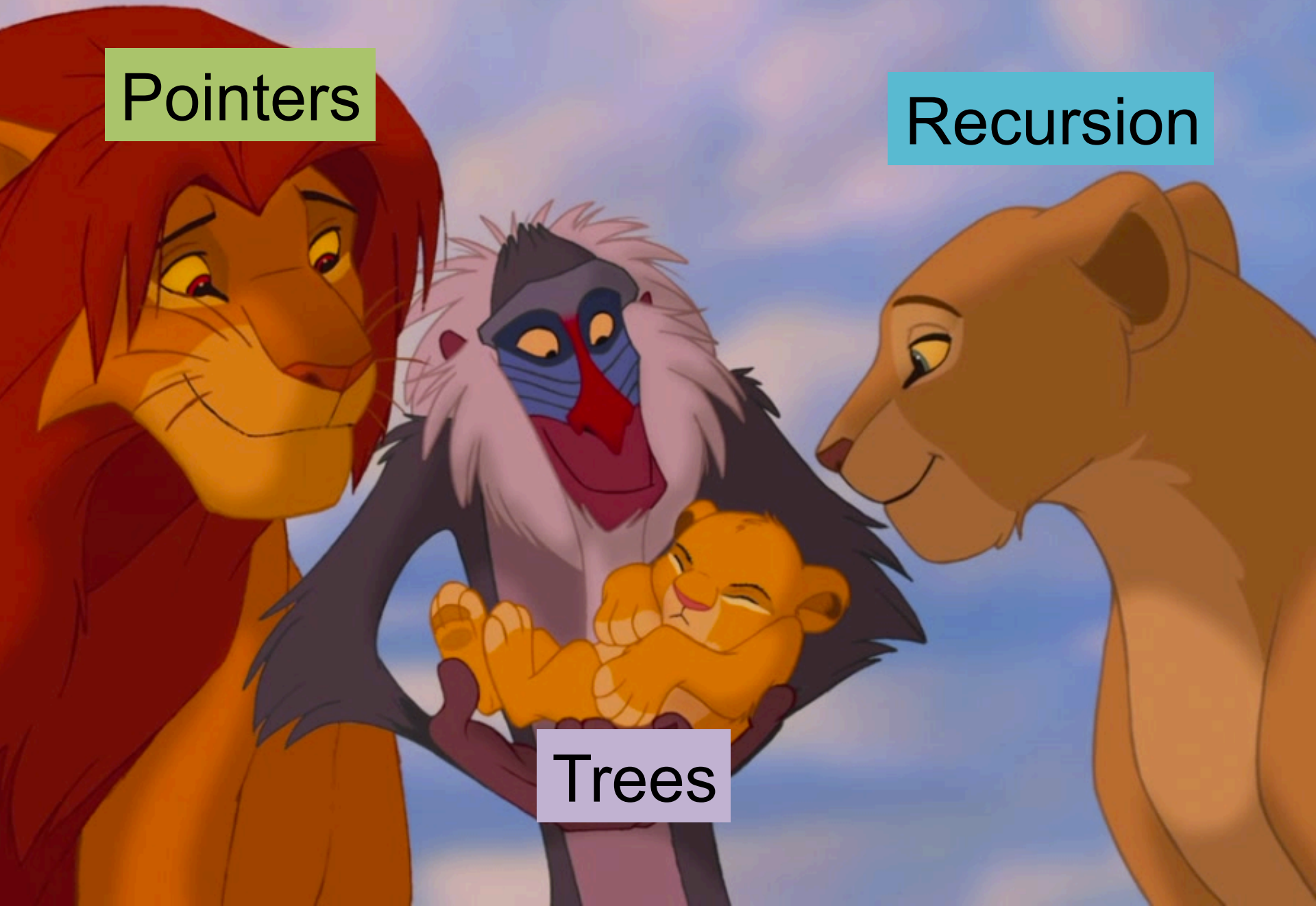
```
struct Tree {  
    char value;  
    Tree * left;  
    Tree * right;  
};
```



Pointers

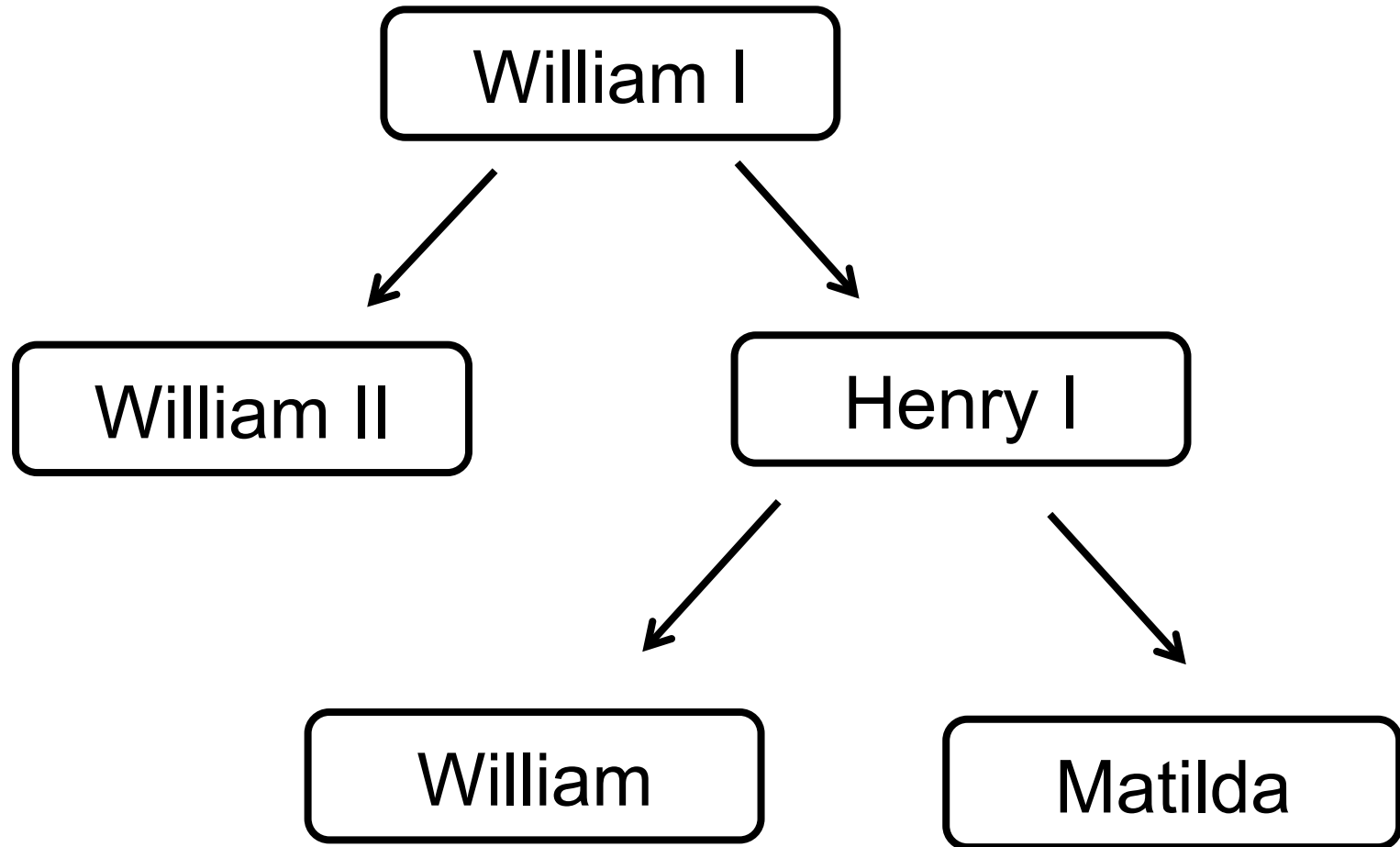
Recursion

Trees

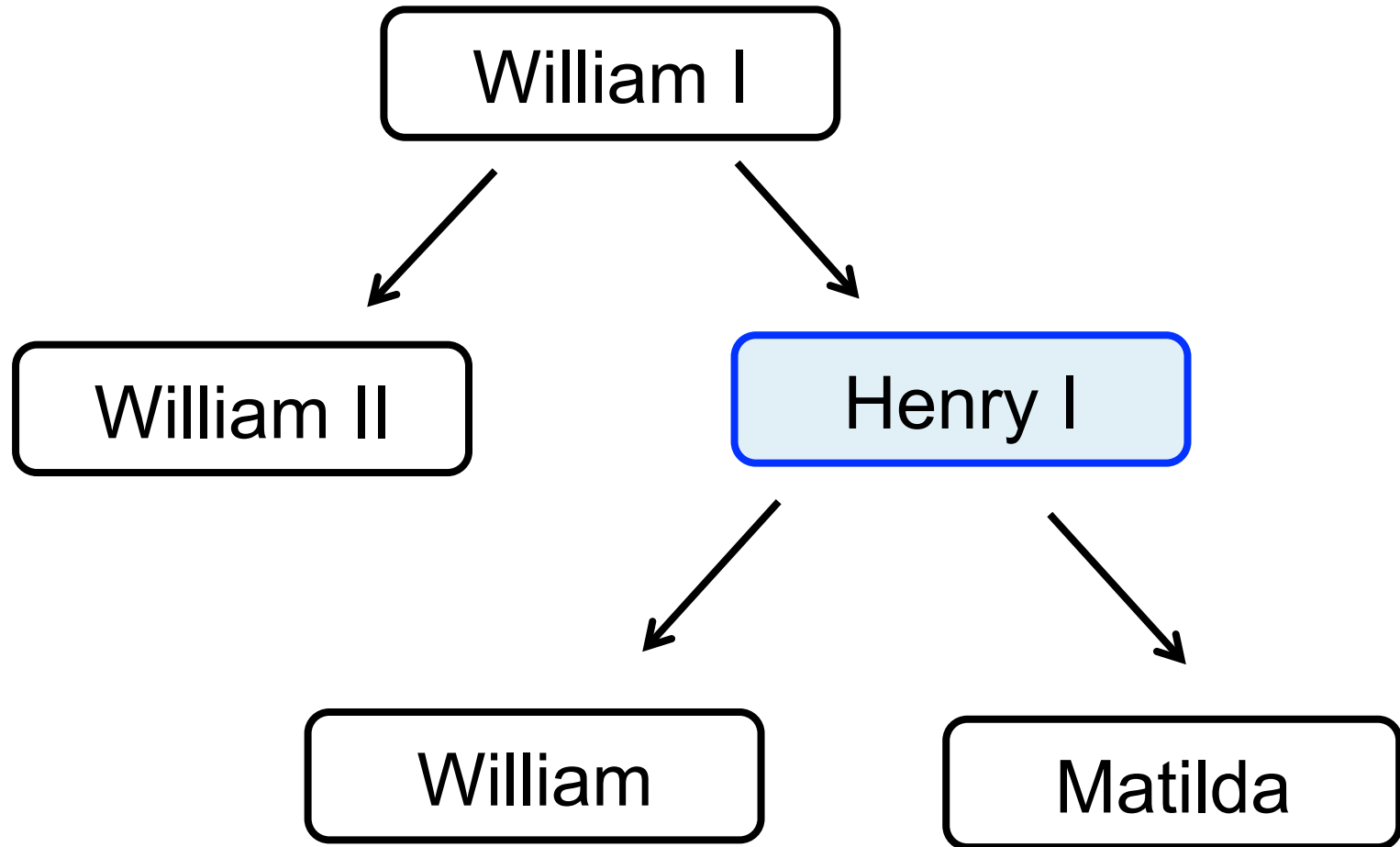


Terminology

Terminology

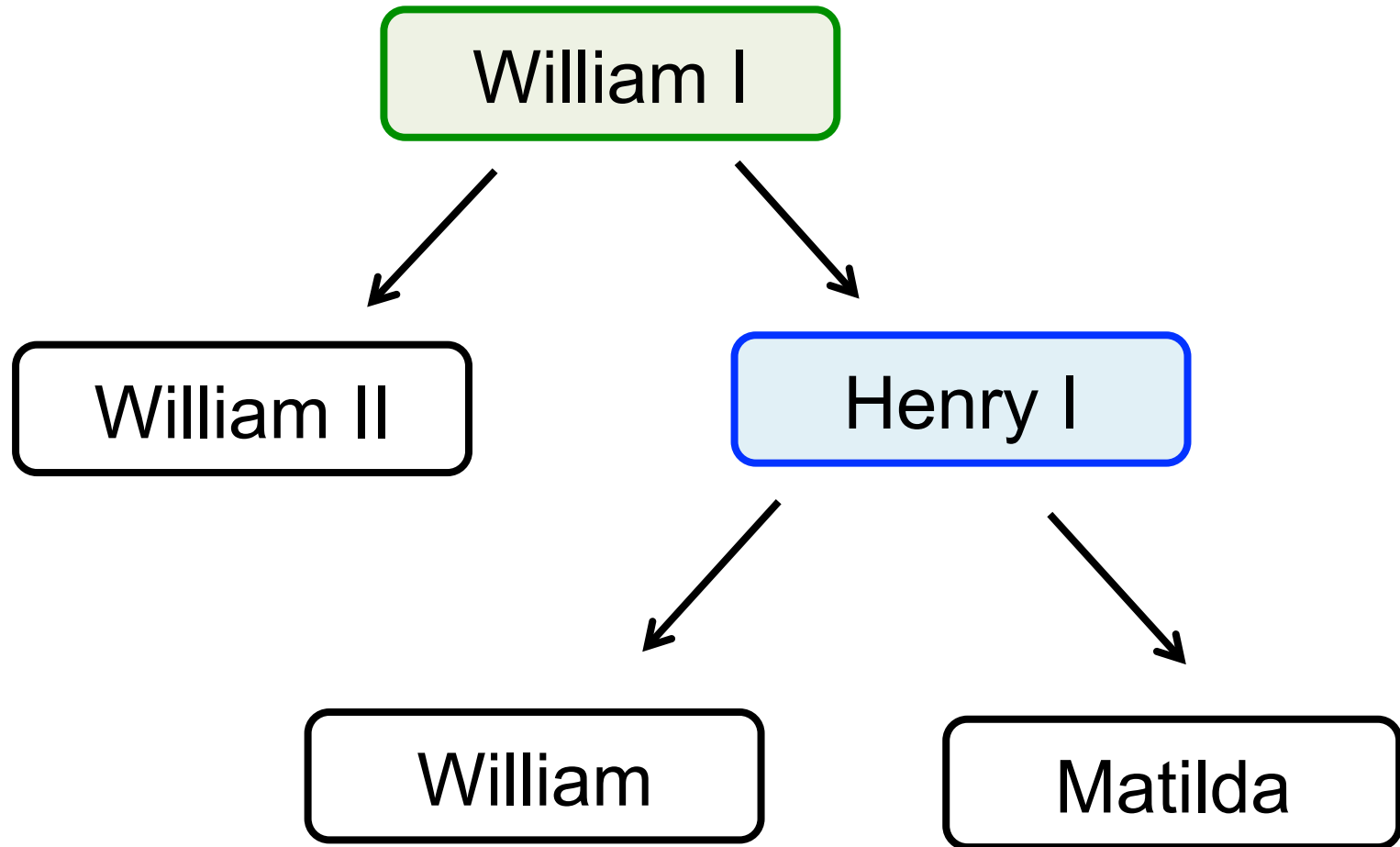


Terminology



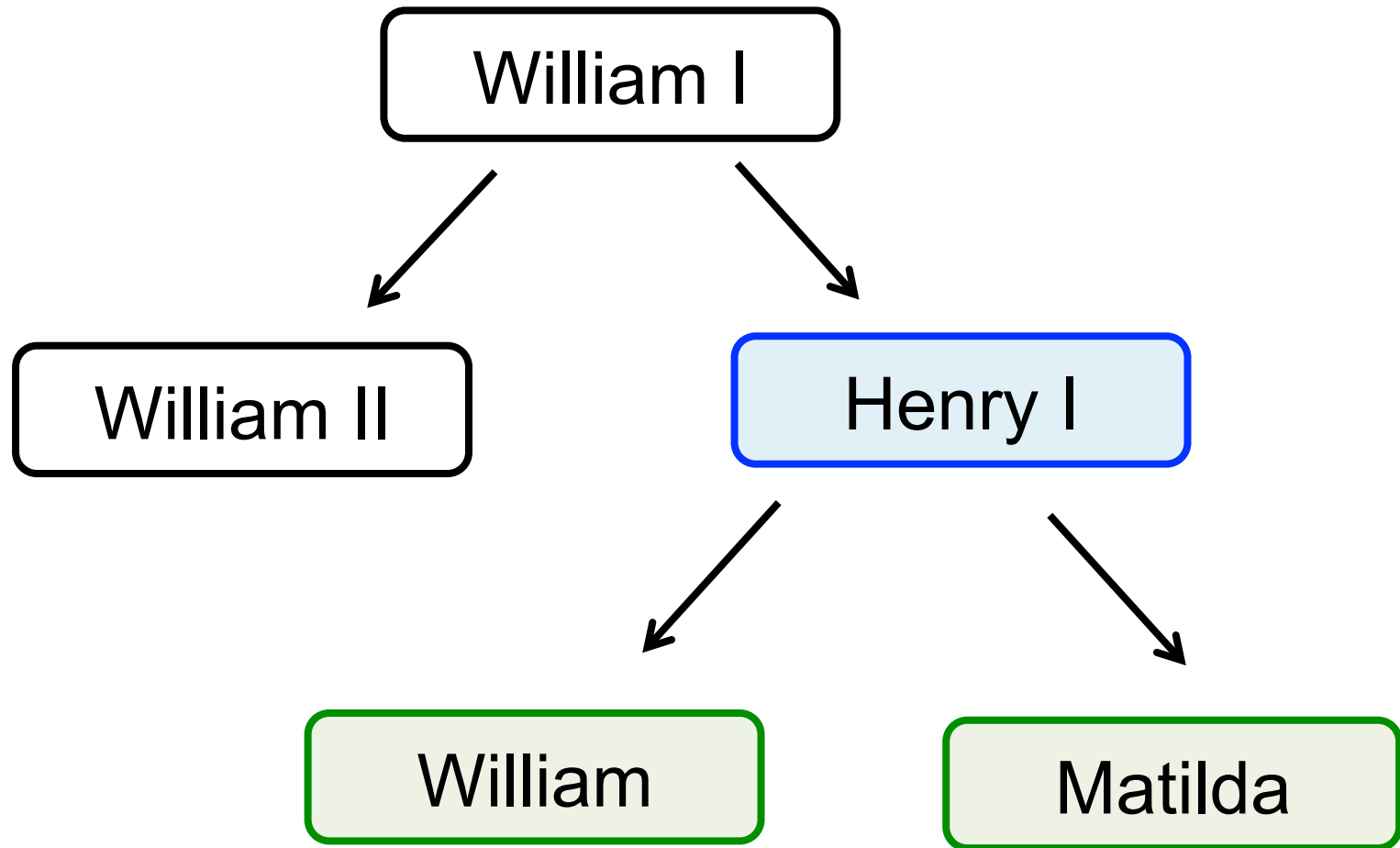
We call a single element a **“Node”** or **“Tree”**

Terminology: Parent



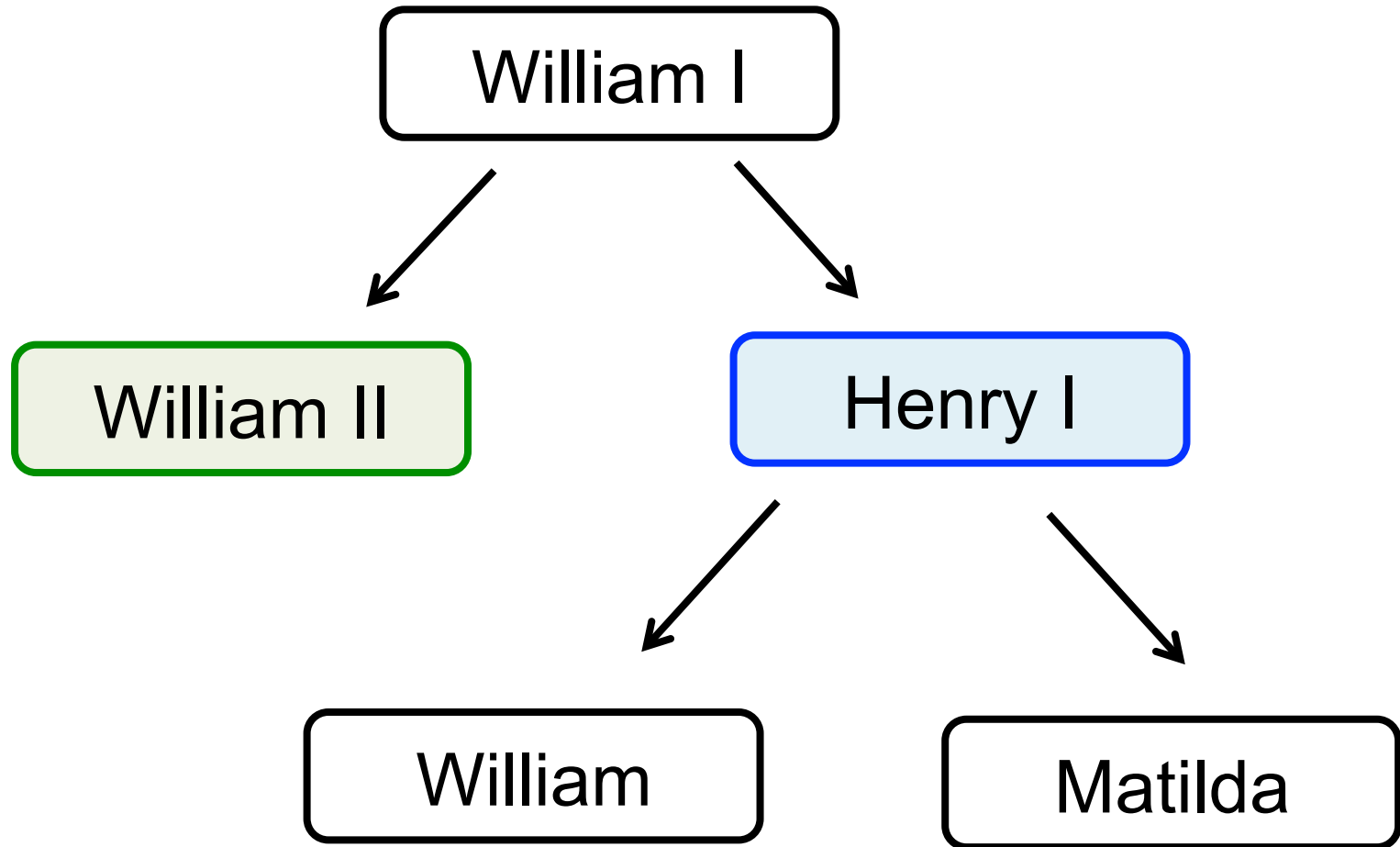
We call the Tree that points to us our **“Parent”**

Terminology: Children



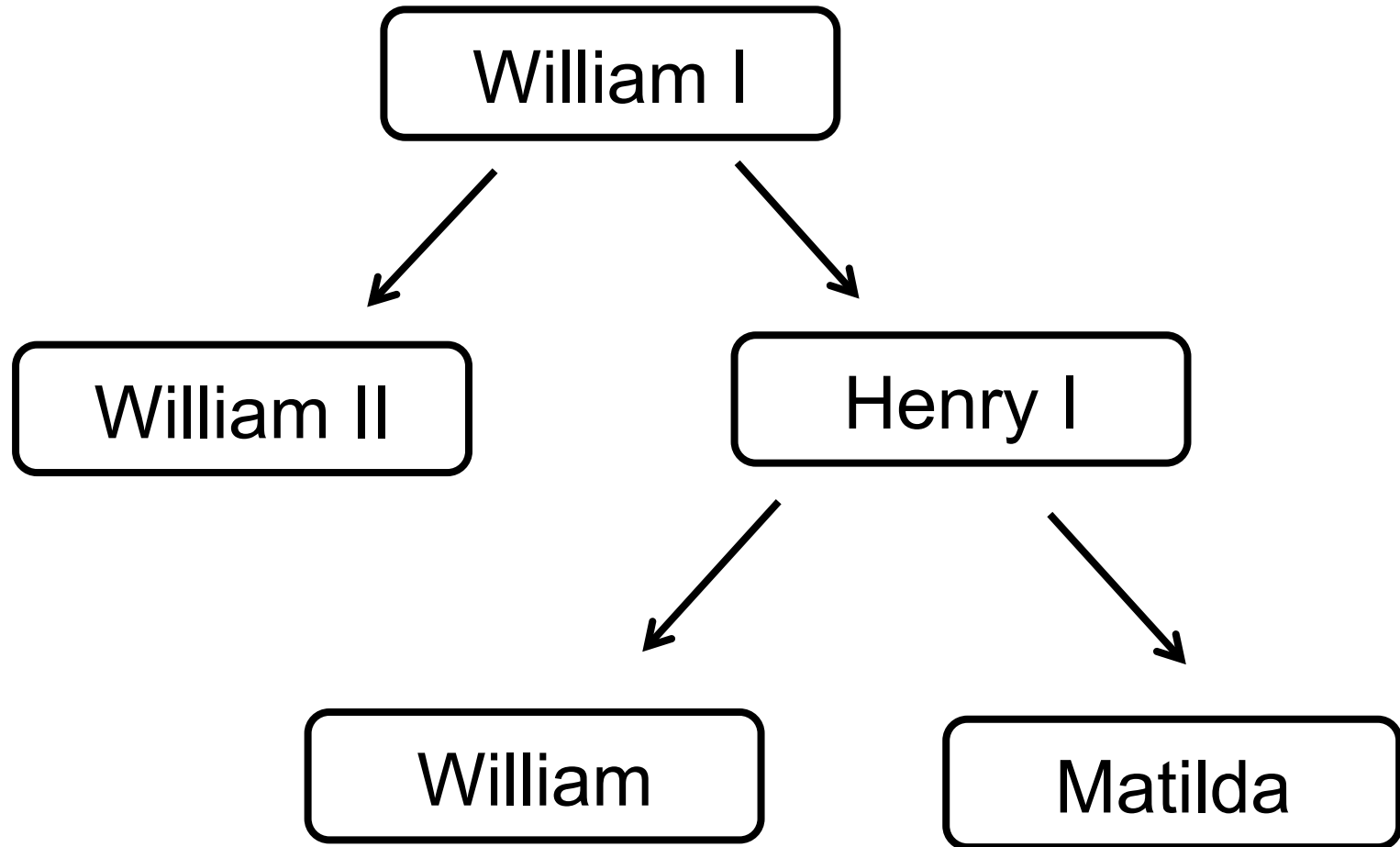
We call the nodes that we point to our **“Children”**

Terminology: Siblings

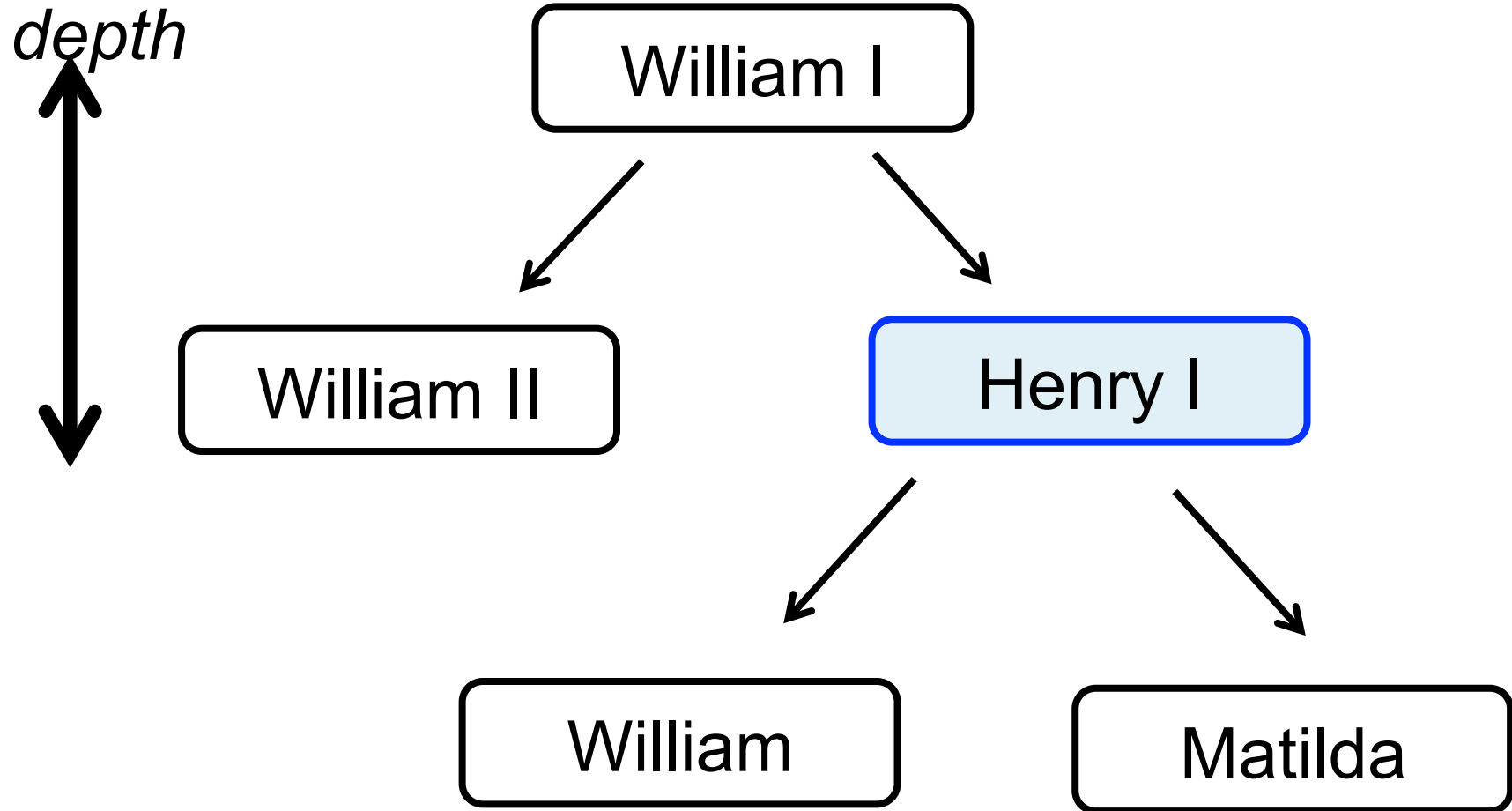


We call nodes that share the same parent **“Siblings”**

Terminology

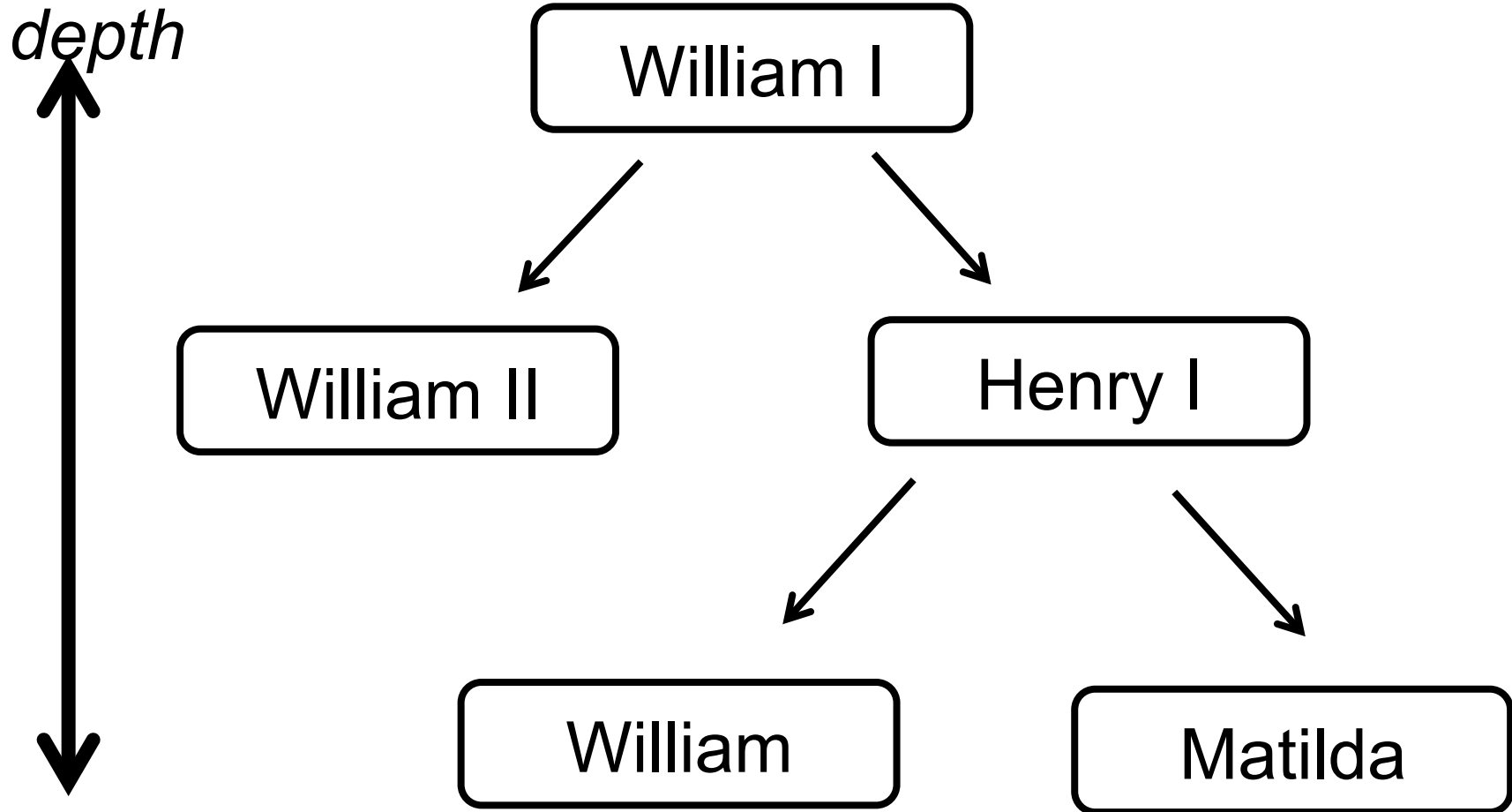


Terminology



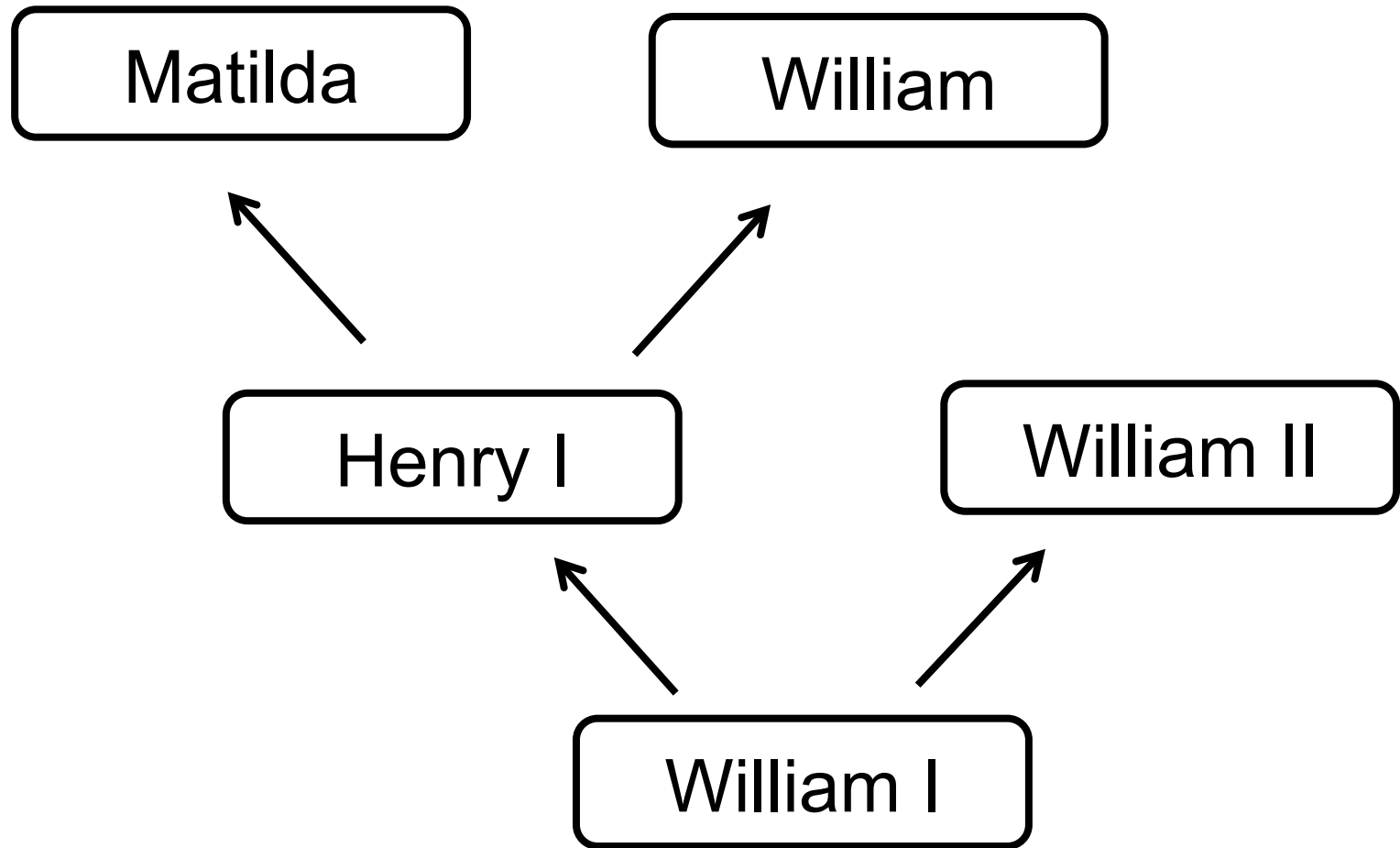
The depth of a node is the number of links from the root.

Terminology

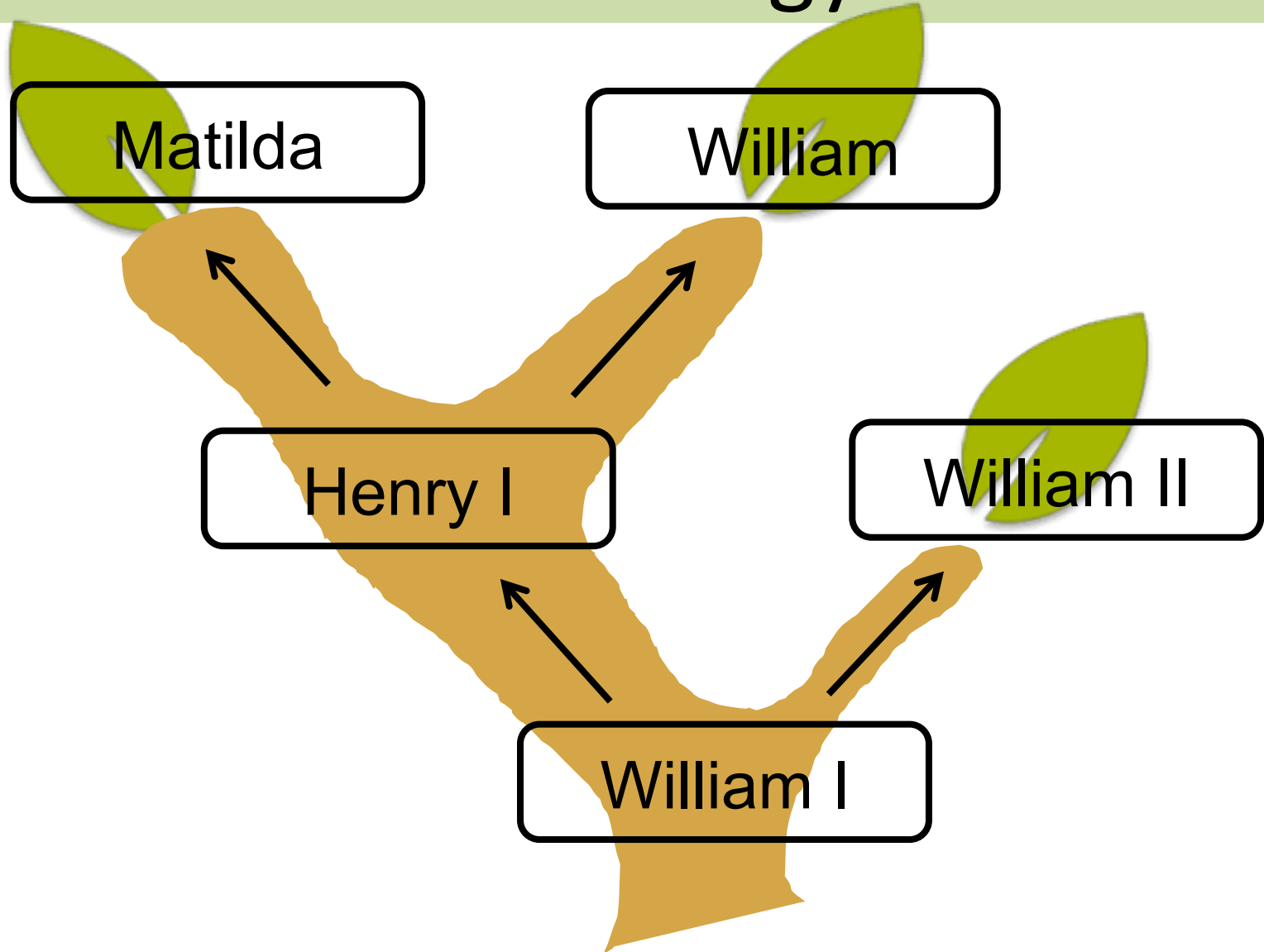


The depth of a tree is the maximum number of links from the root.

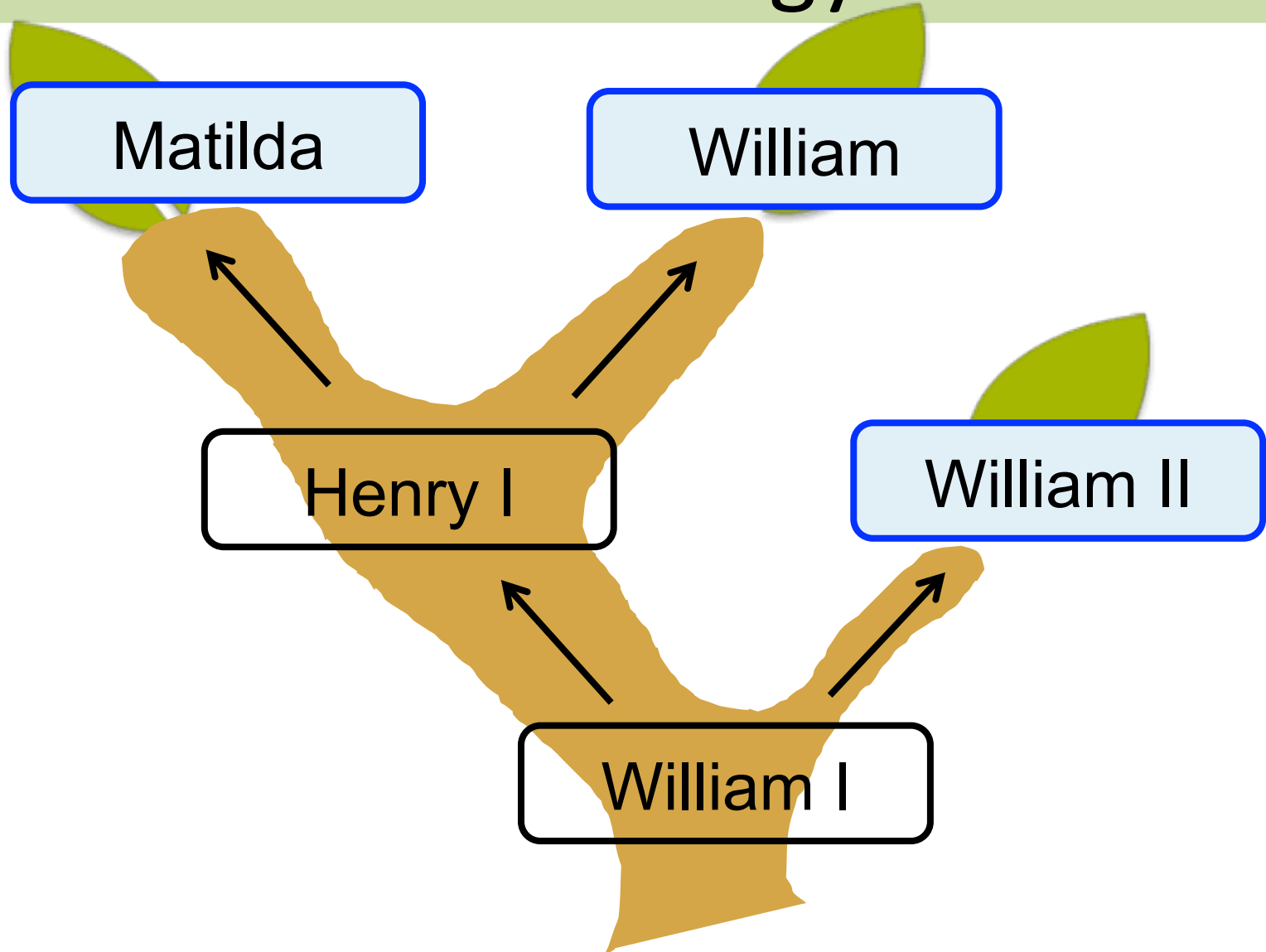
Terminology



Terminology

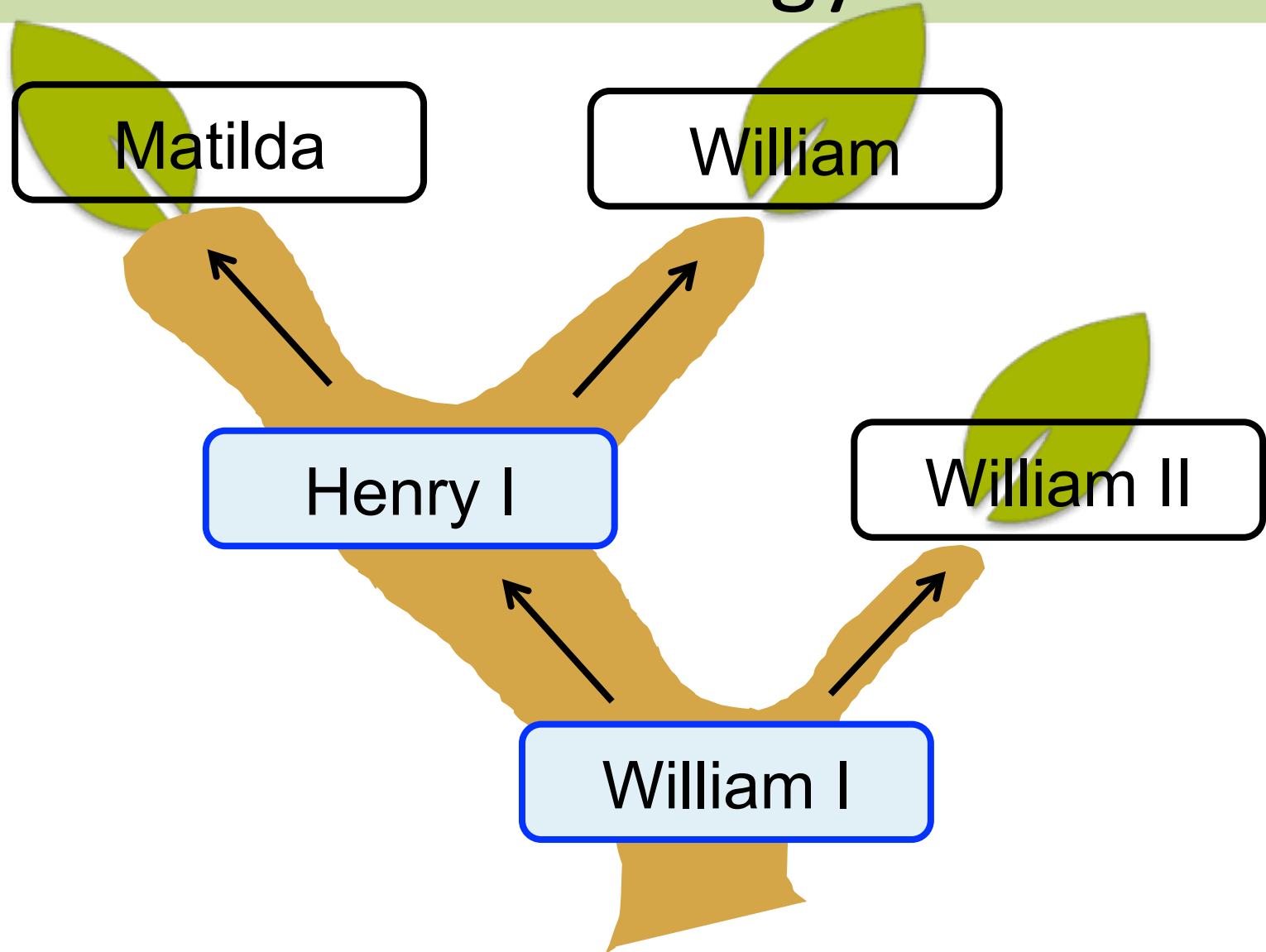


Terminology



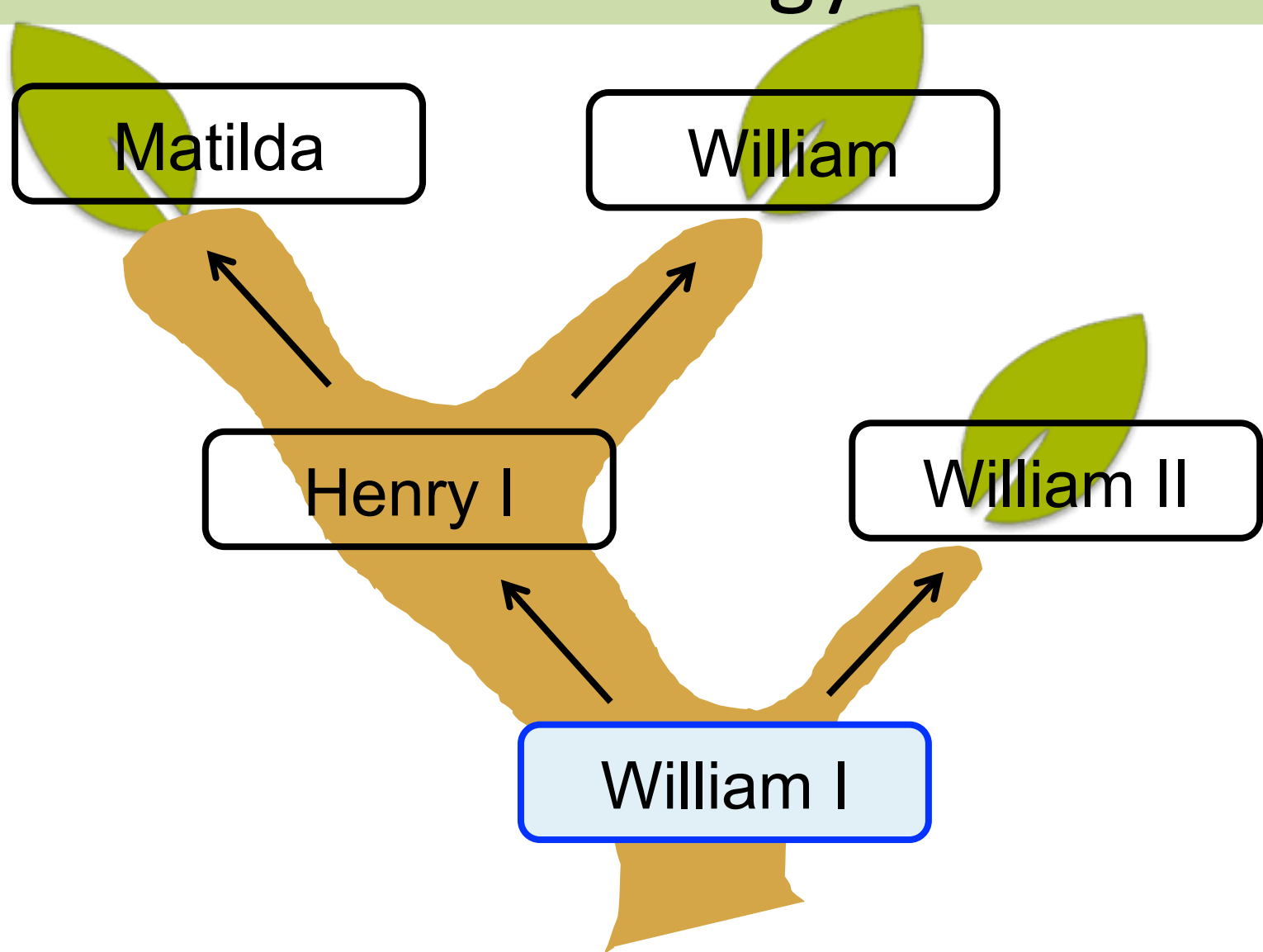
We call nodes that have no children **“Leaves”**

Terminology



We call nodes that have children **“Inner Nodes”**

Terminology



We call the node without parents the **“Root”**

Why Binary?

Exactly two children



End Terminology

Tree Definition

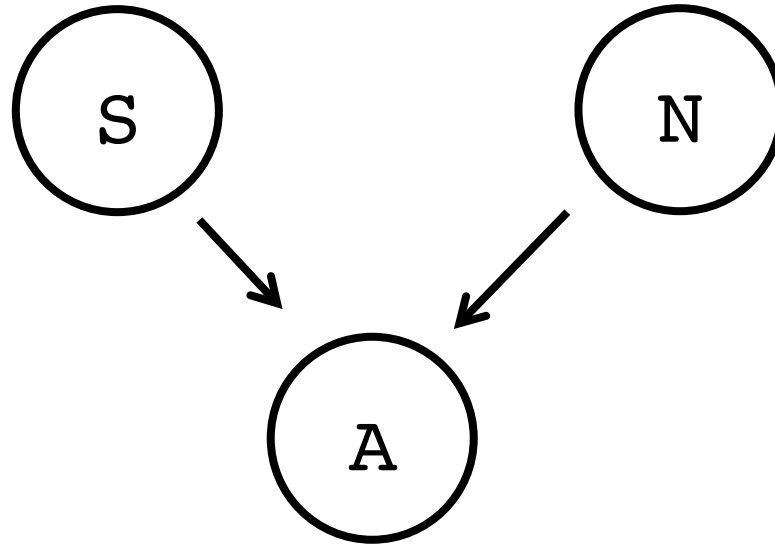


Only One Parent

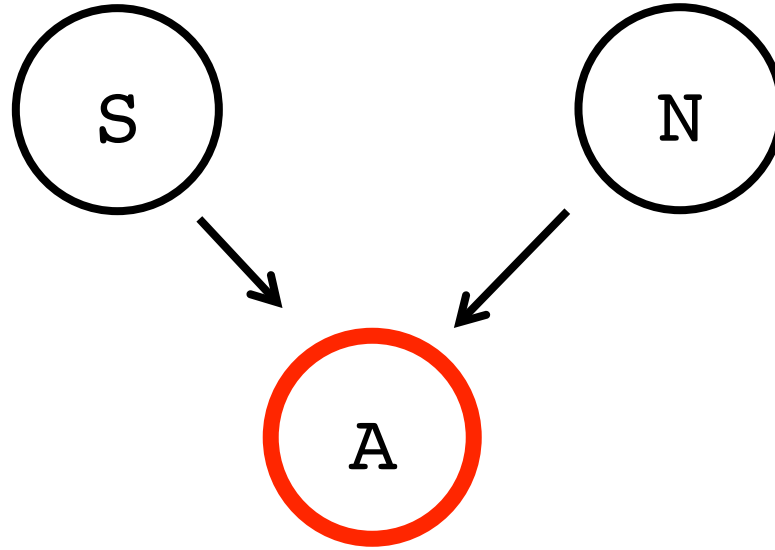


No Cycles

Only One Parent

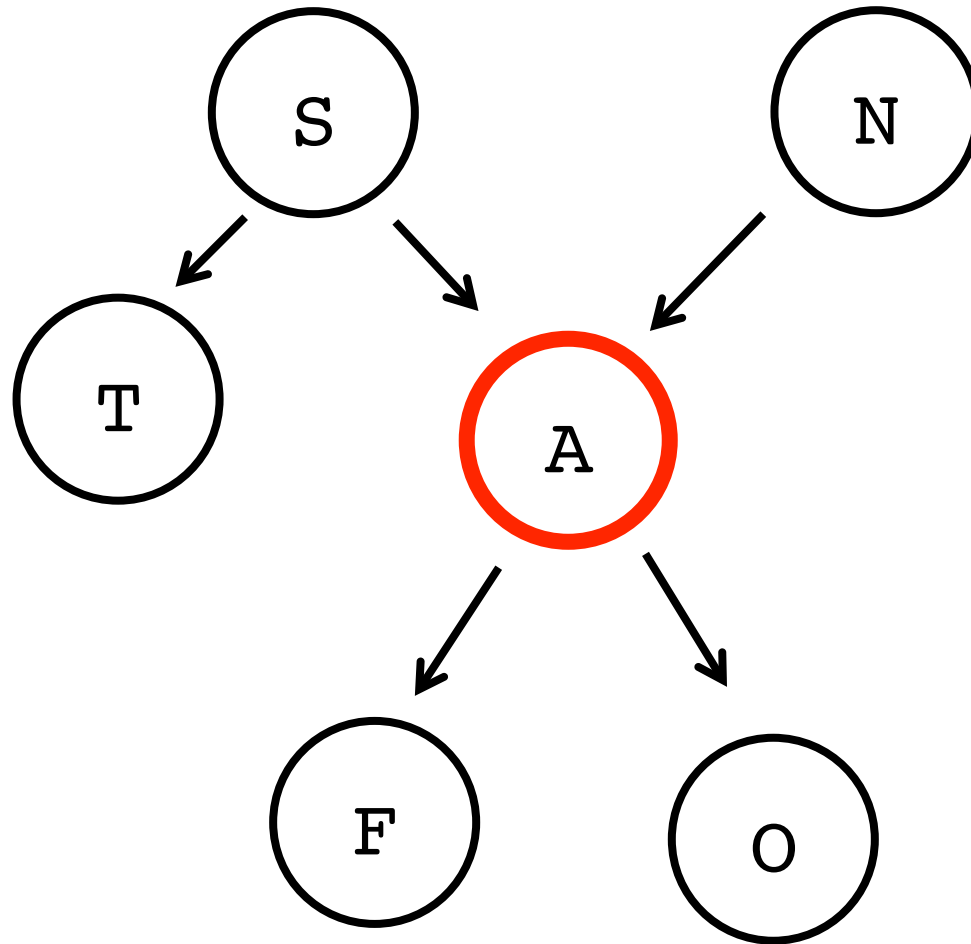


Only One Parent



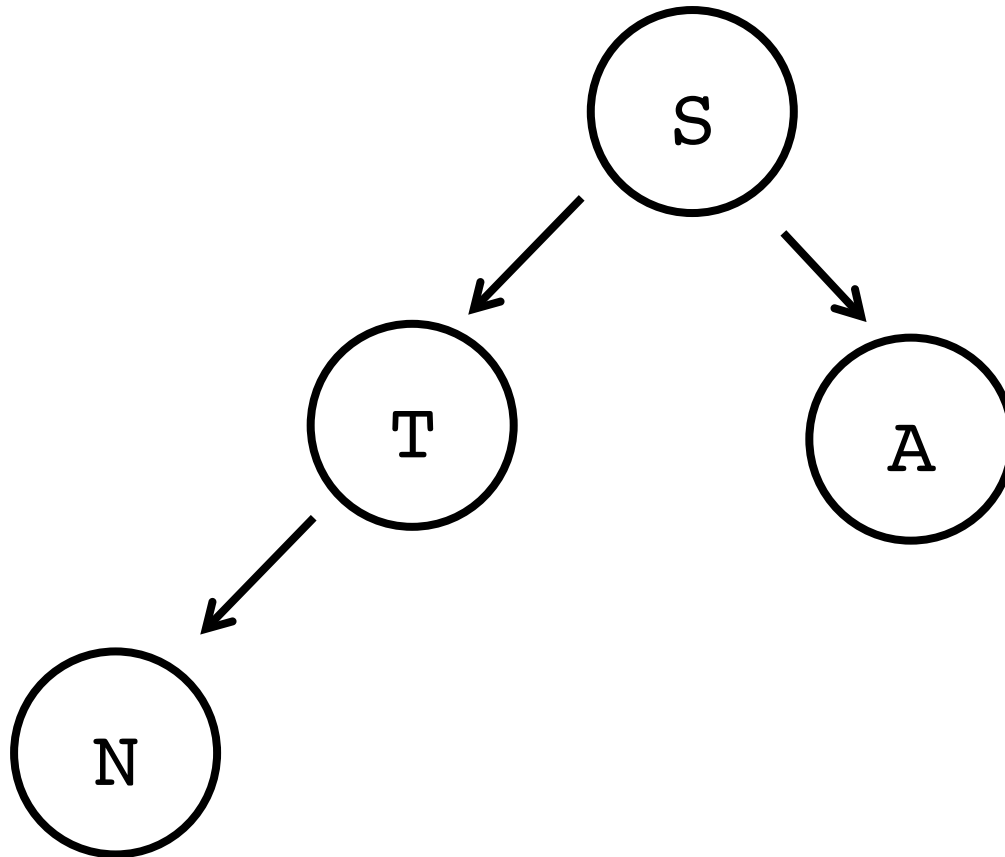
This is not a tree because the red node has two parents

Only One Parent

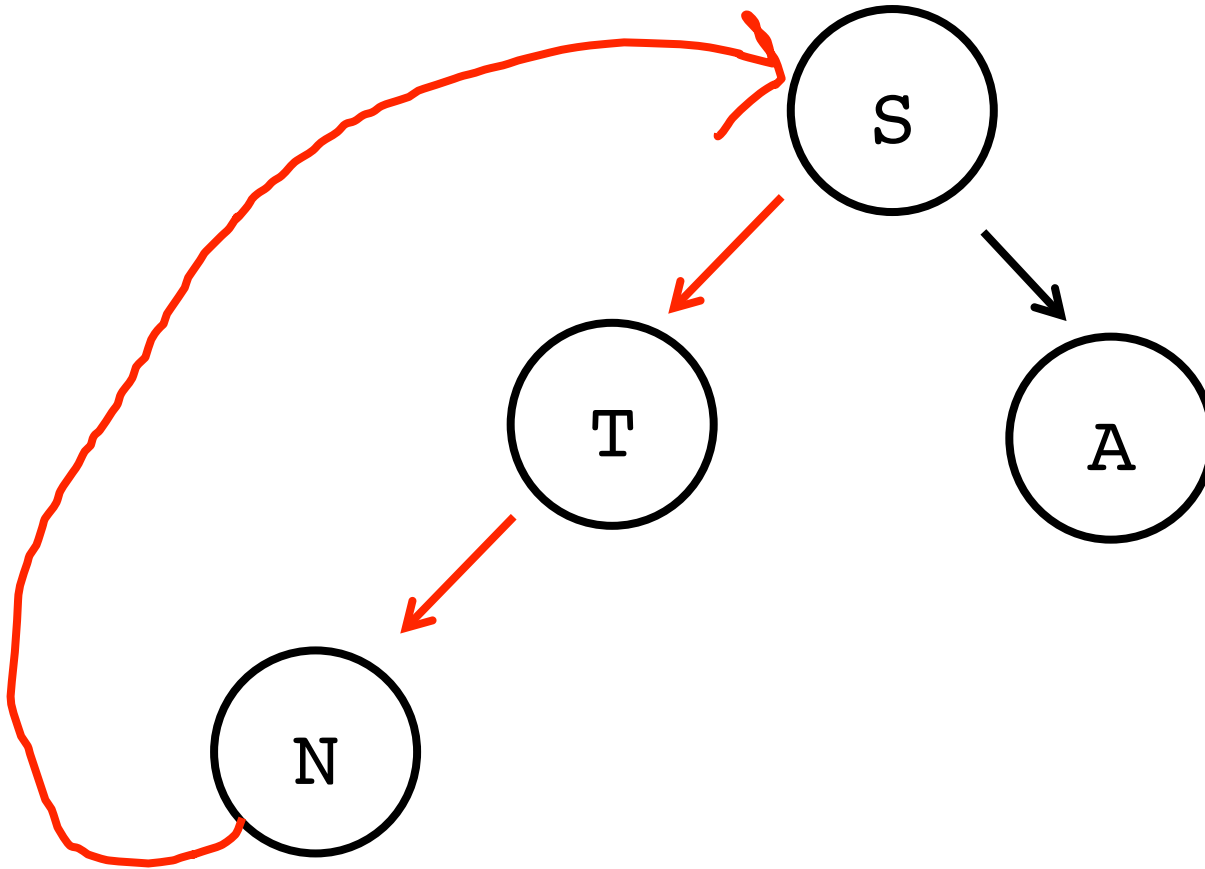


This is not a tree because the red node has two parents

No Cycles

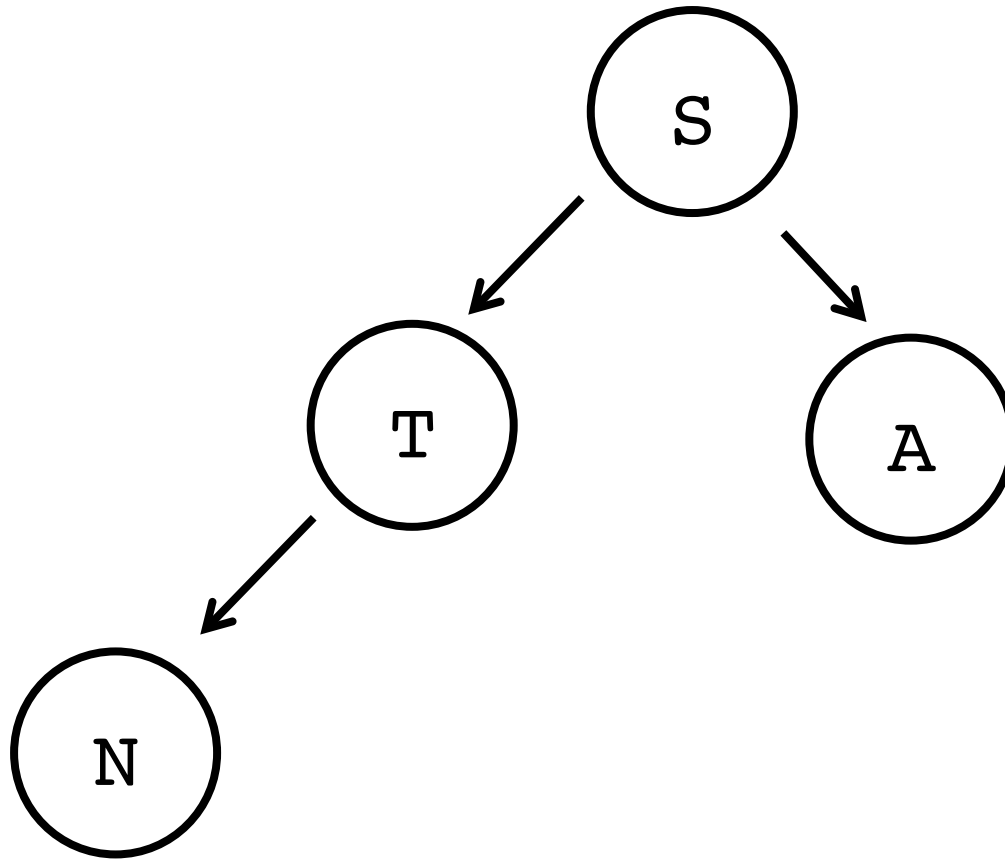


No Cycles

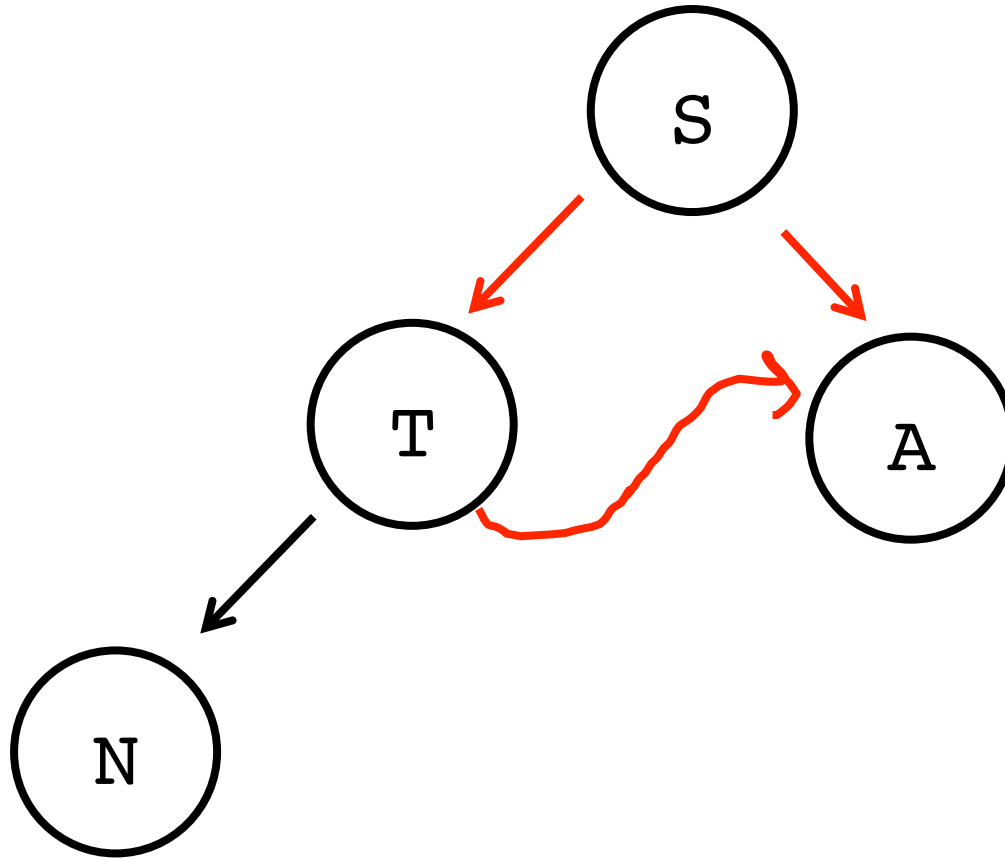


This is not a tree because the red edges make a cycle

No Cycles



No Cycles



This is not a tree because the red edges make a cycle

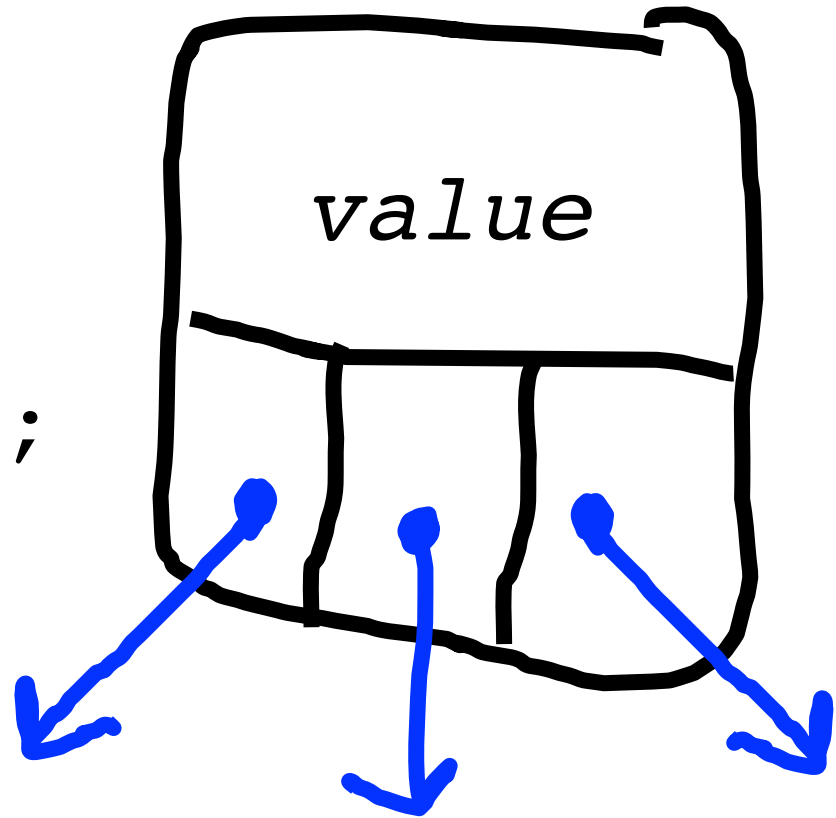
Other Kinds of Trees



One of my favorite trees

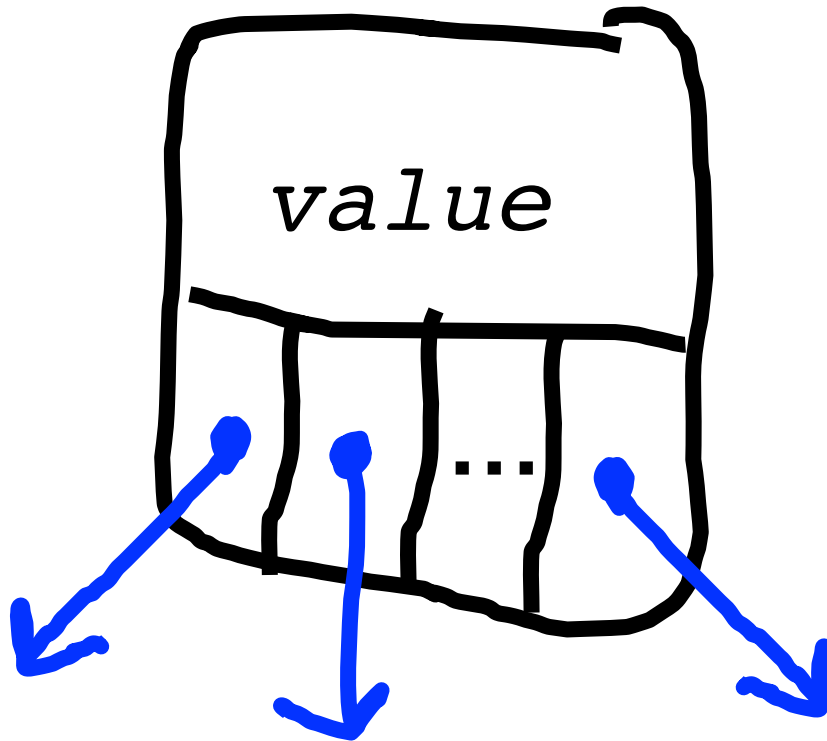
Trinary Tree

```
struct Tree {  
    string value;  
    Tree * left;  
    Tree * middle;  
    Tree * right;  
};
```



Tree

```
struct Tree {  
    string value;  
    Vector<Tree *> children;  
};
```



Structs or Classes

```
struct Tree {  
    string value;  
    Tree * left;  
    Tree * right;  
};
```

```
class Tree {  
private:  
    string value;  
    Vector<Tree *> children;  
};
```

How Many Valid Binary Trees?

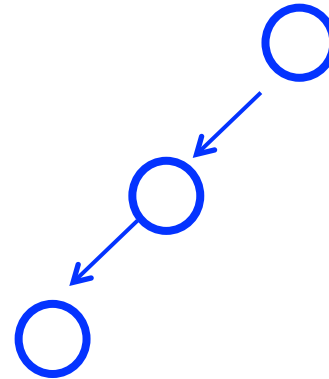
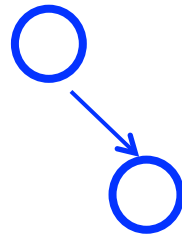
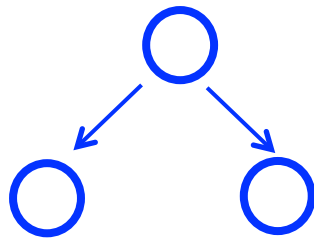
A) 3

B) 4

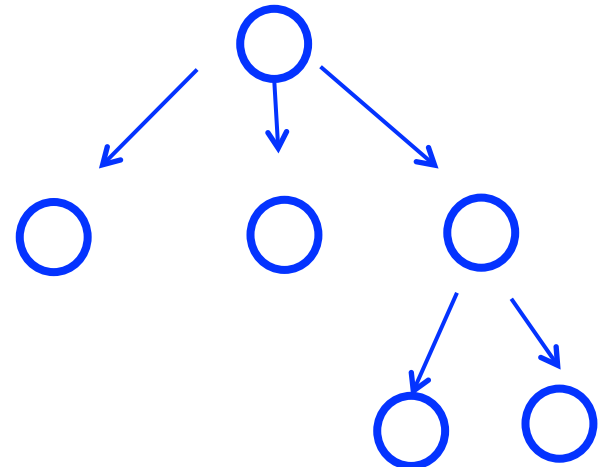
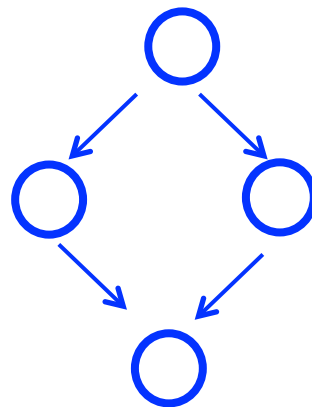
C) 5

D) 6

E) 7

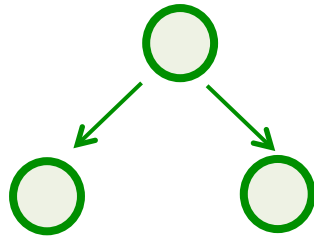


NULL

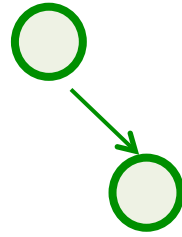


How Many Valid Binary Trees?

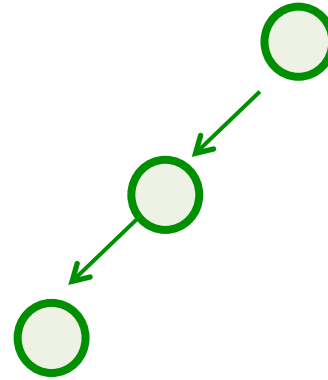
A) 3



B) 4



C) 5

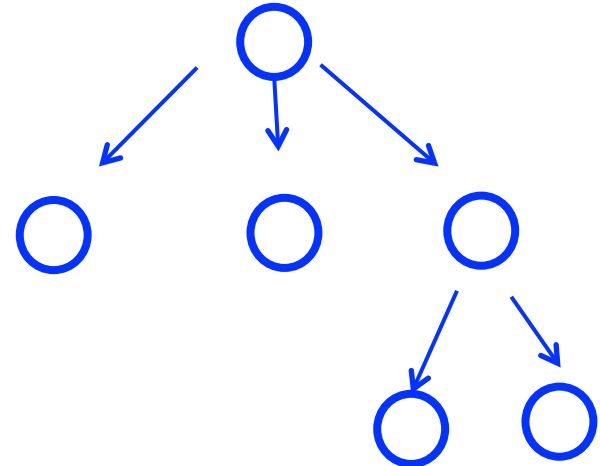
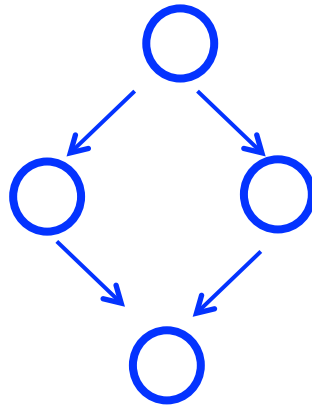


D) 6



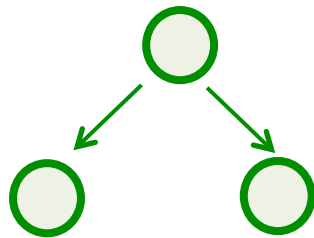
E) 7

NULL

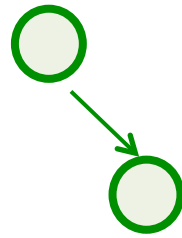


How Many Valid Binary Trees?

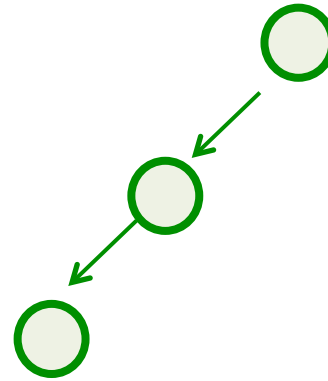
A) 3



B) 4



C) 5

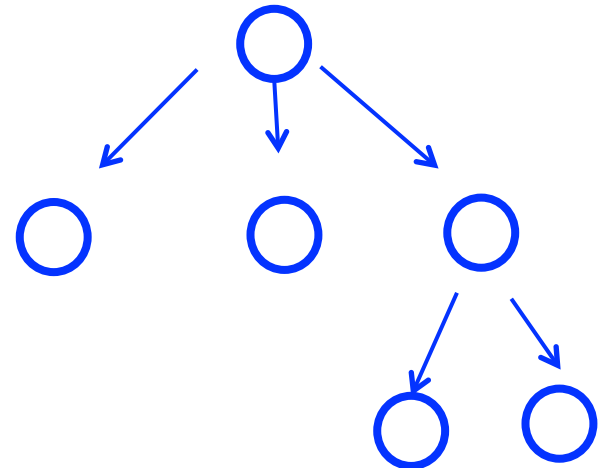
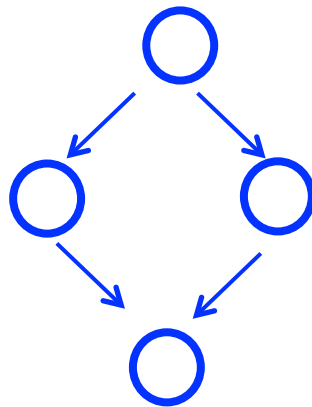


D) 6



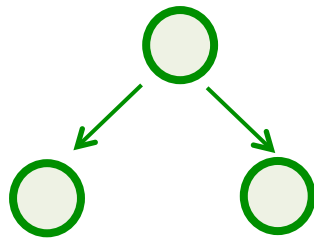
E) 7

NULL

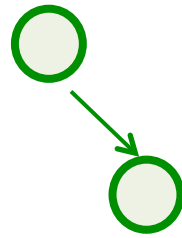


How Many Valid Binary Trees?

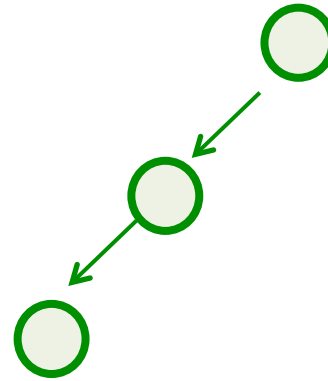
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C) 5

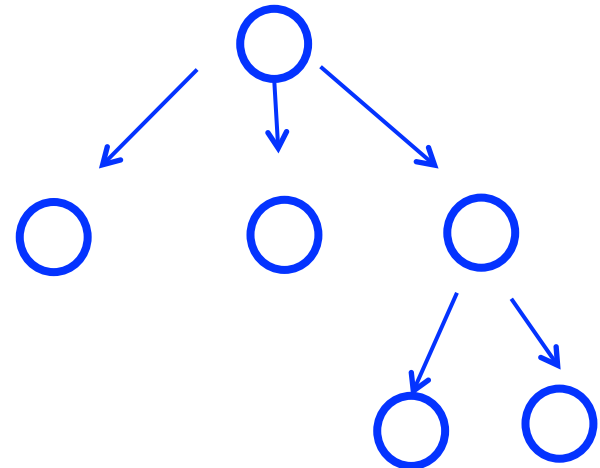
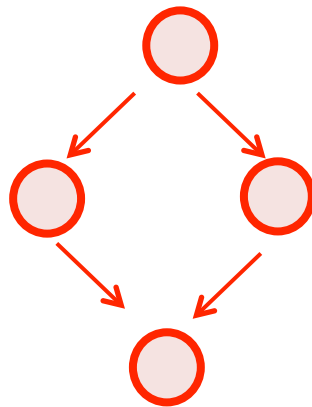


D) 6



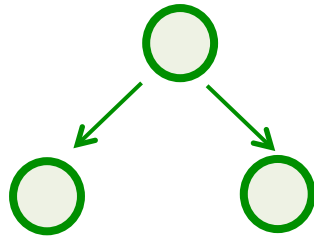
E) 7

NULL

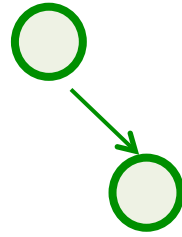


How Many Valid Binary Trees?

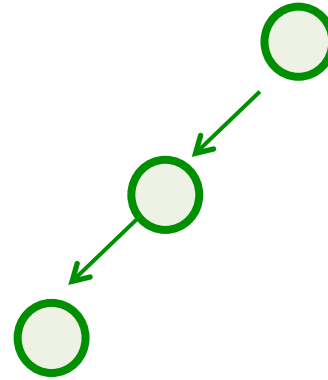
A) 3



B) 4



C) 5

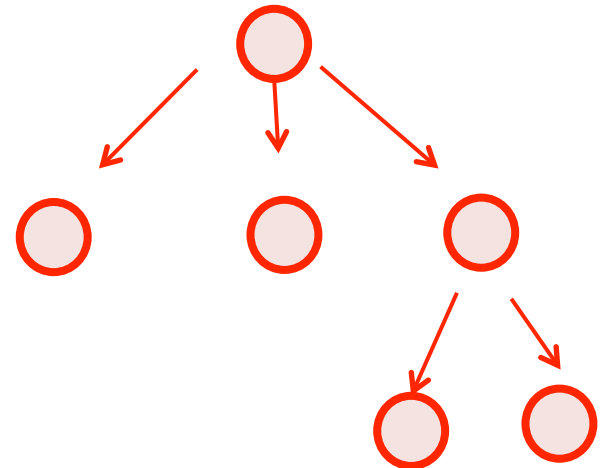
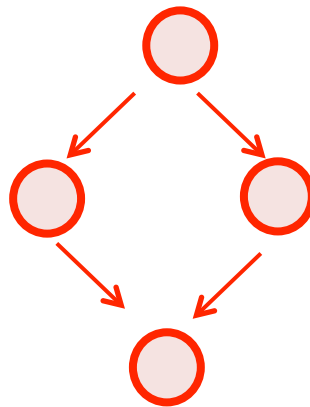


D) 6



E) 7

NULL



How Many Valid Binary Trees?

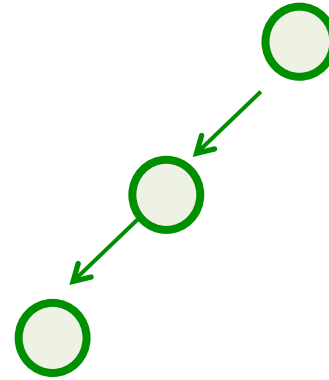
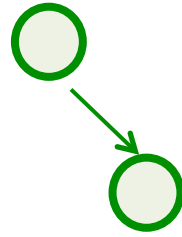
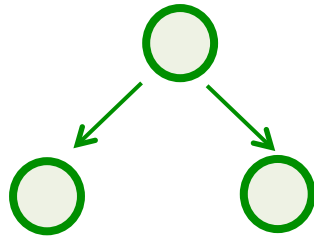
A) 3

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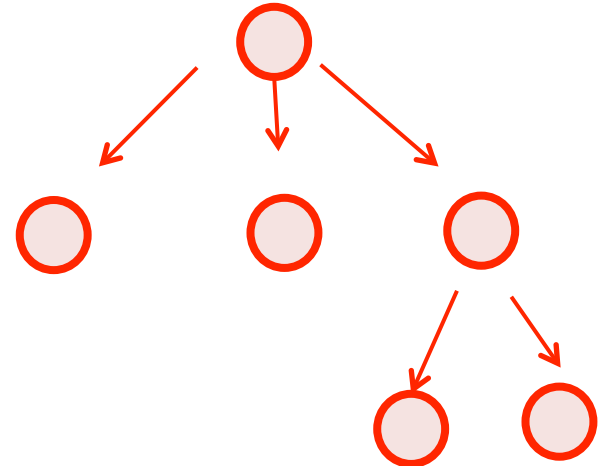
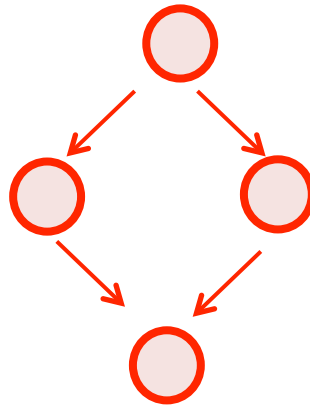
C) 5

D) 6

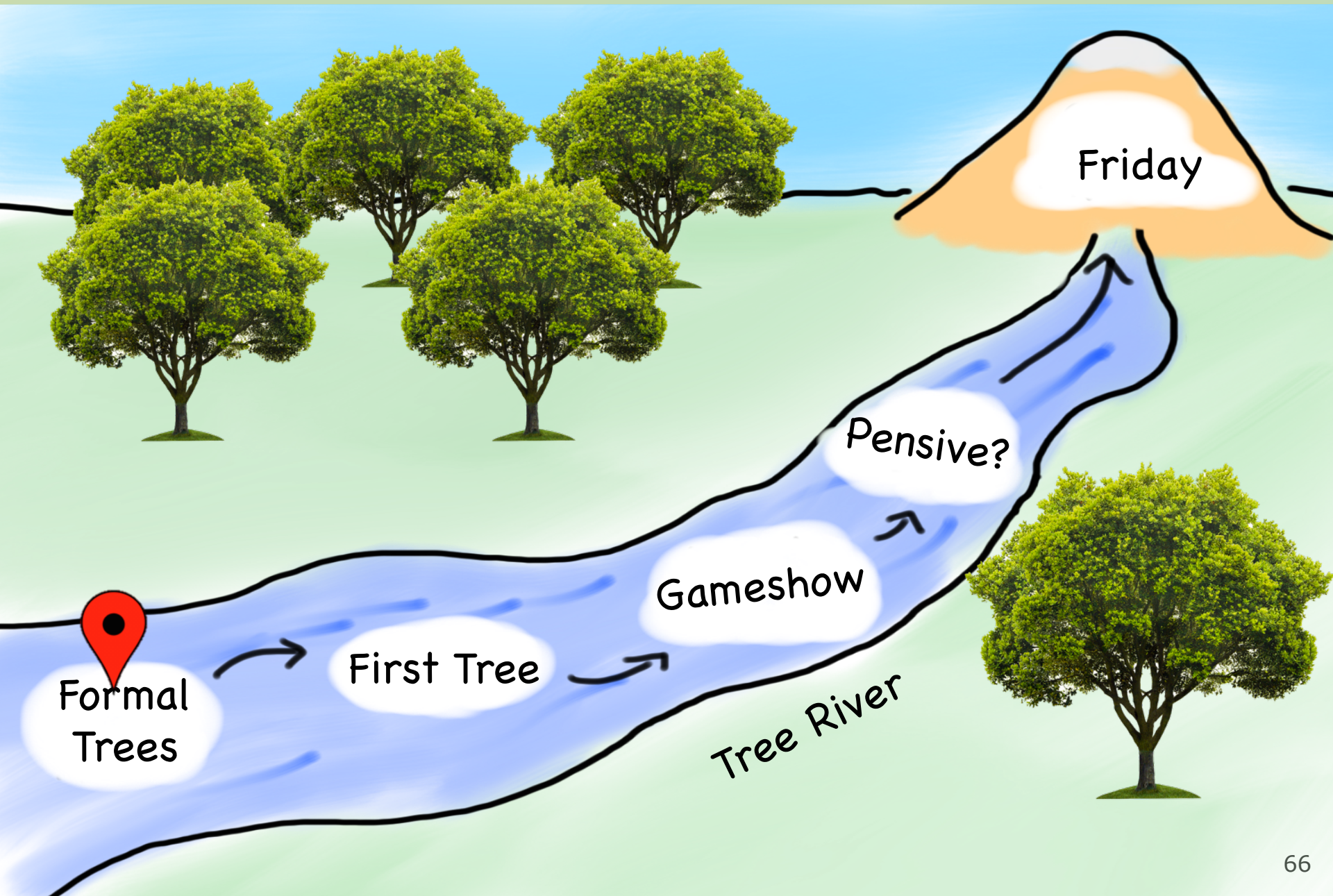
E) 7



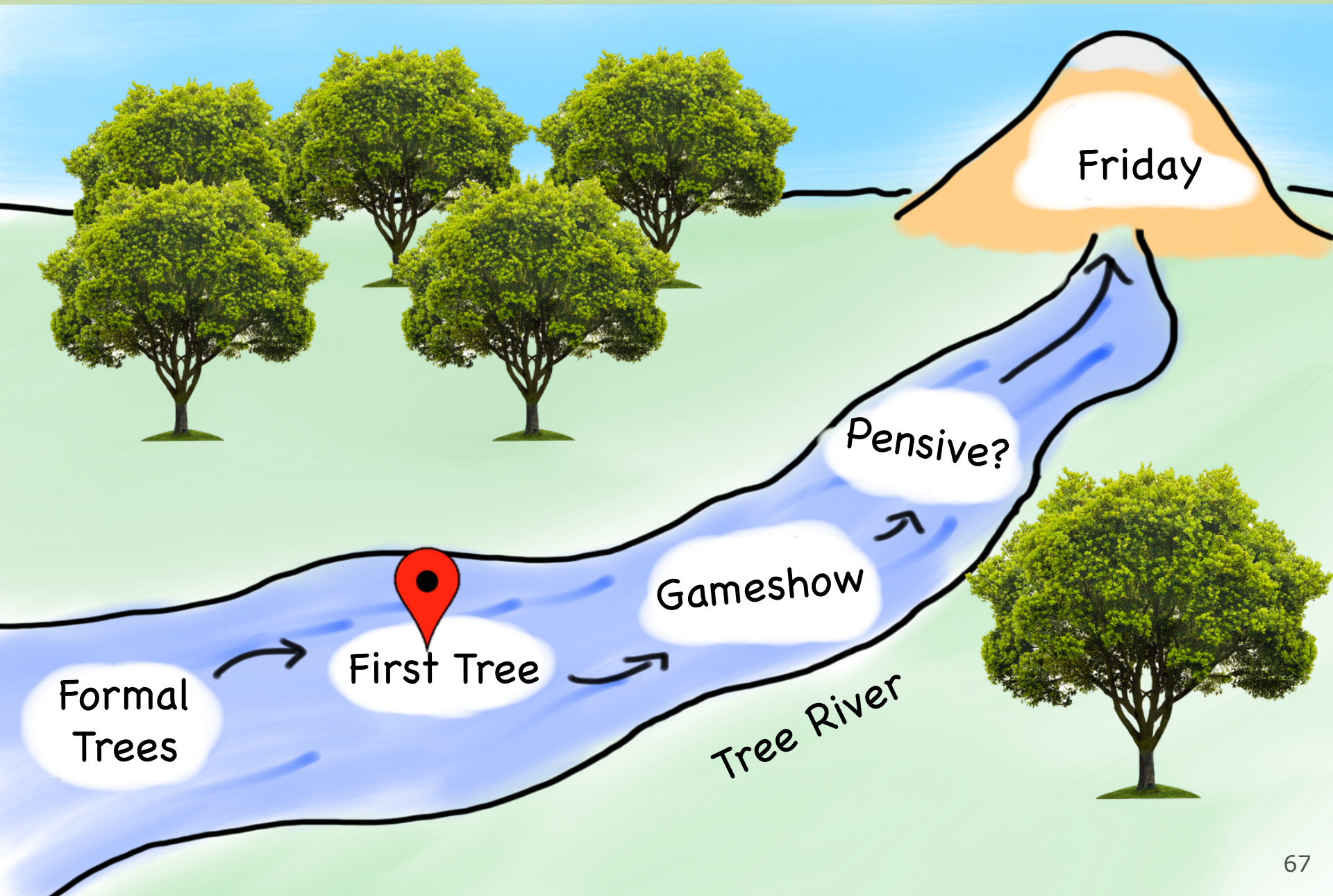
NULL



Today's Route



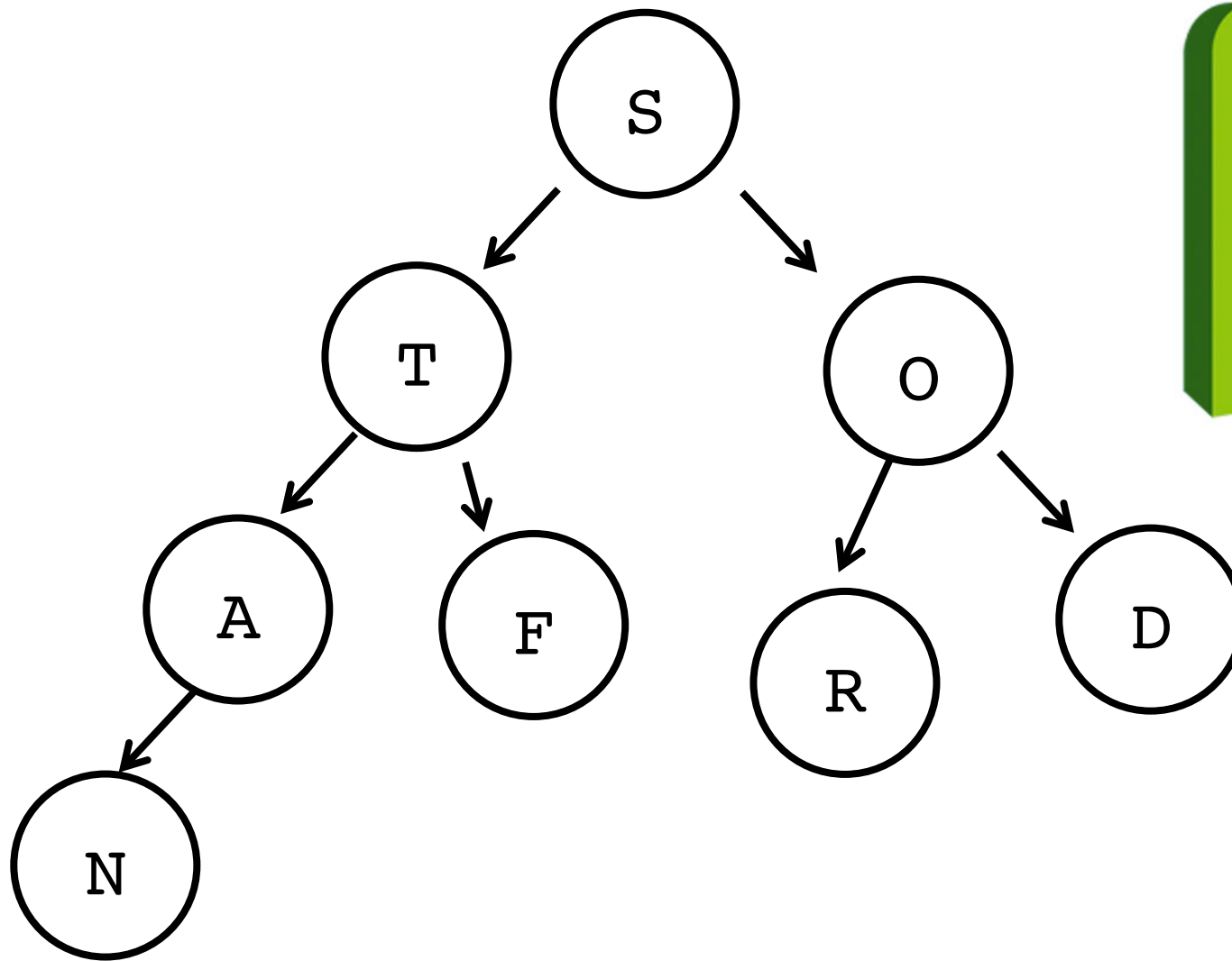
Today's Route



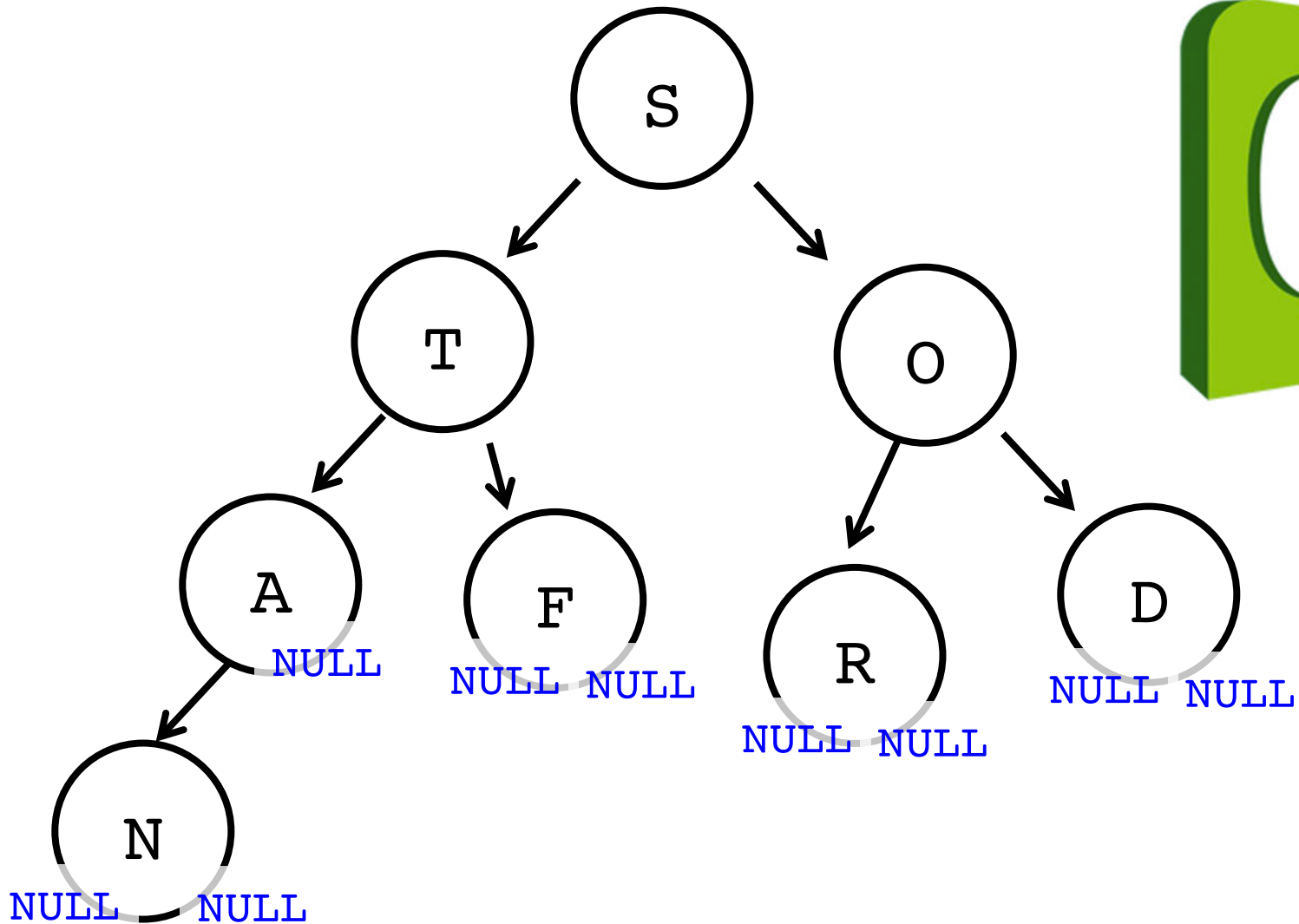




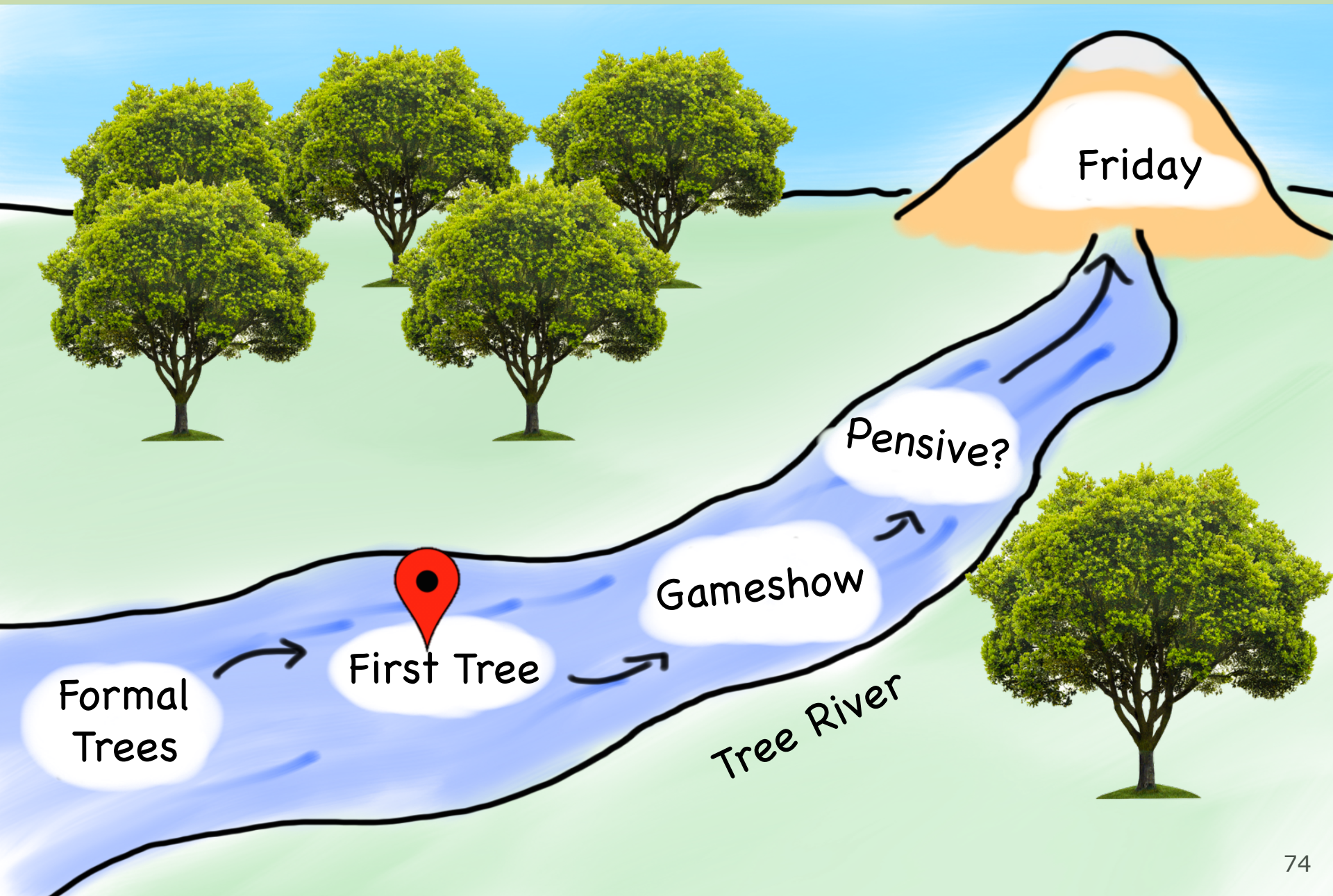
Count This Tree



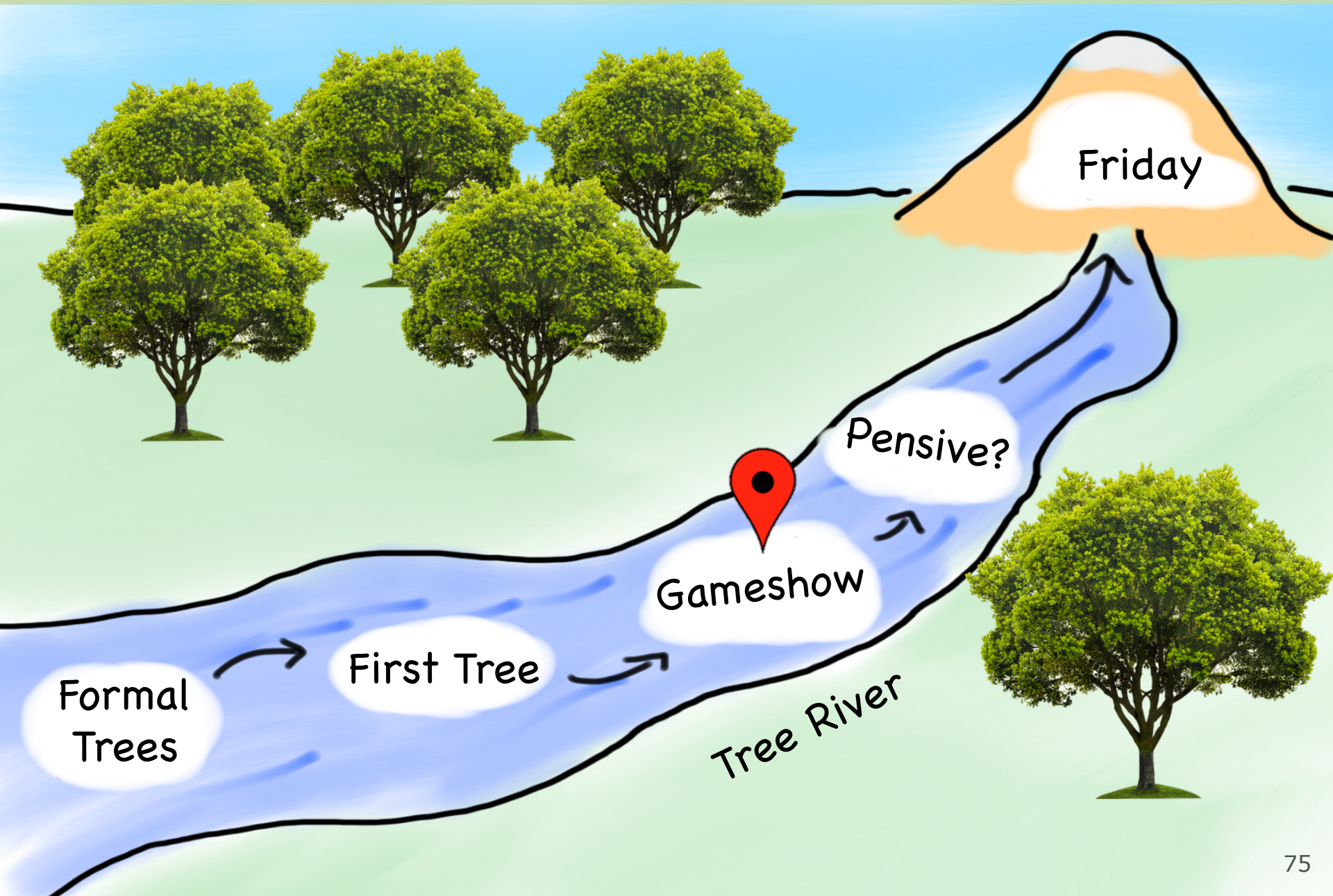
NULL Children



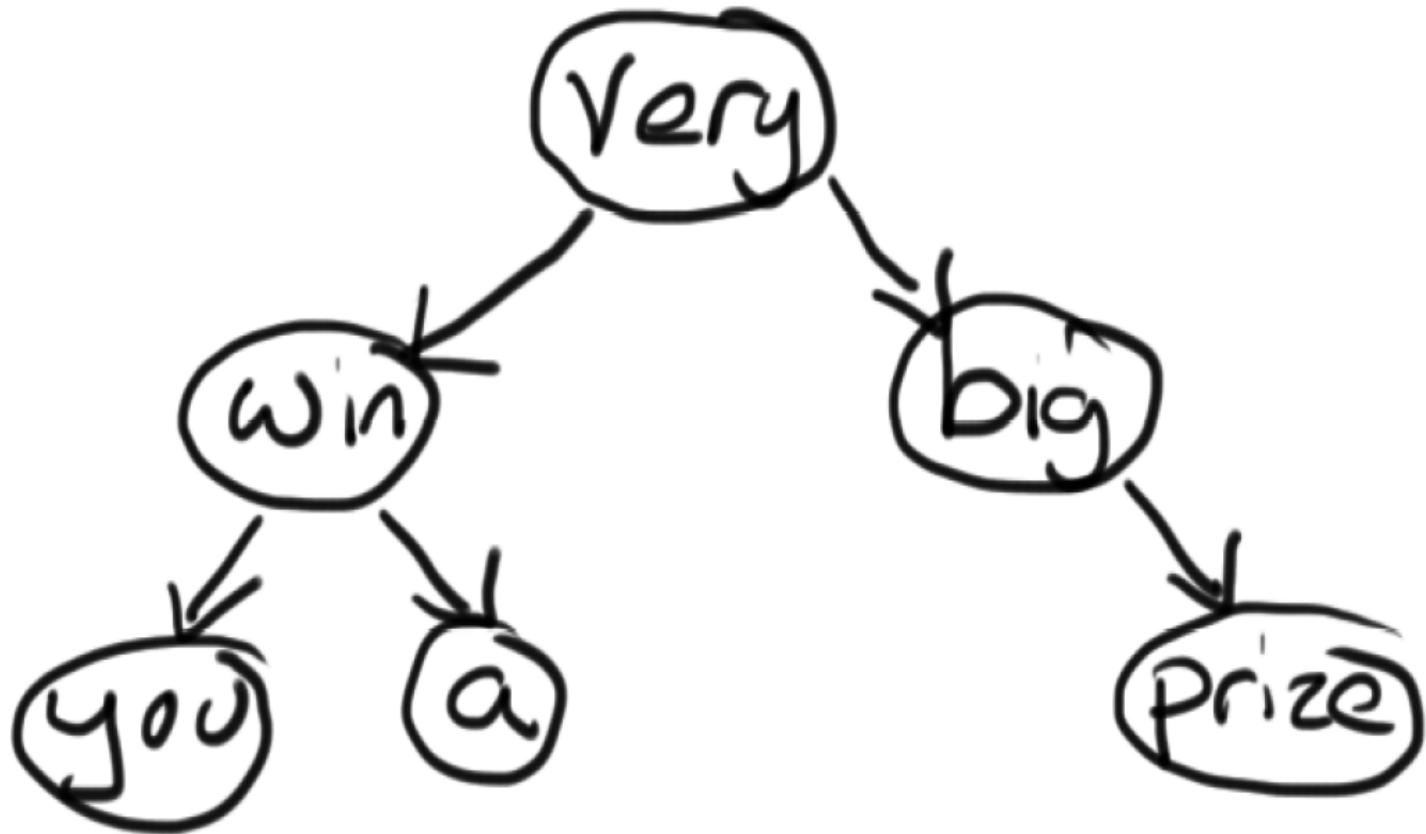
Today's Route



Today's Route



Game Show Tree



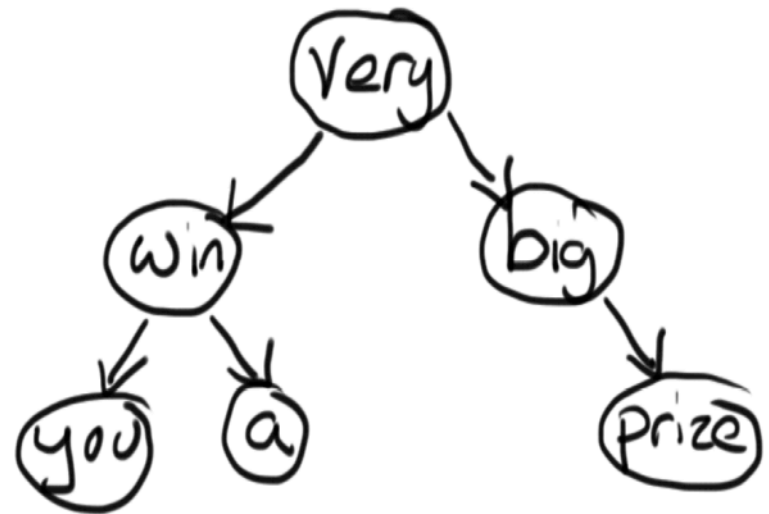
Game Show Tree

I VOLUNTEER

AS TRIBUTE

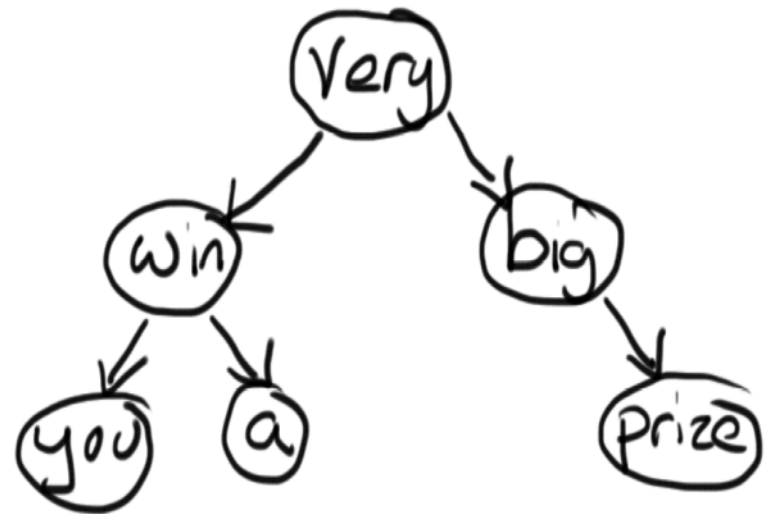
Game Show Tree

```
struct Tree {  
    string value;  
    Tree * left;  
    Tree * right;  
};
```



Game Show Tree

```
int main() {  
    introduction();  
    Tree * tree = initTree();  
    int choice = getUserChoice();  
    suspense();  
    switch (choice) {  
        case 1: doorOne(tree); break;  
        case 2: doorTwo(tree); break;  
        case 3: doorThree(tree); break;  
    }  
    return 0;  
}
```

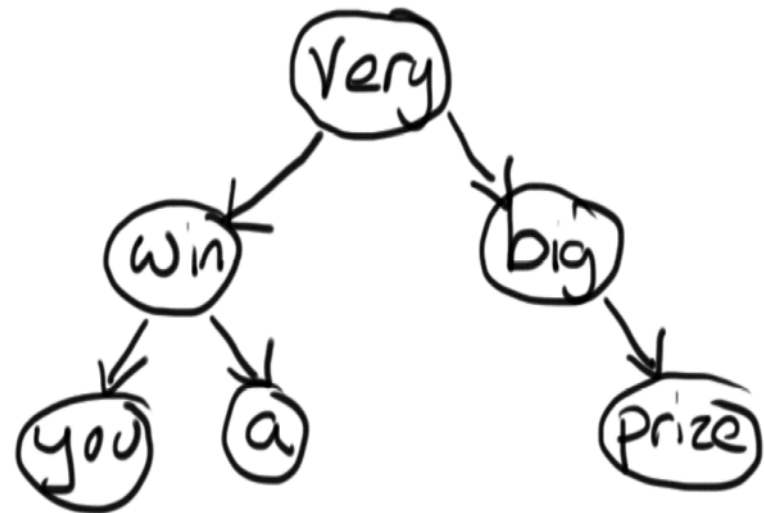


Game Show Tree

```
void doorOne(Tree * tree) {  
    if(tree == NULL) return;  
    cout<<tree->value<<" ";  
    doorOne(tree->left);  
    doorOne(tree->right);  
}
```

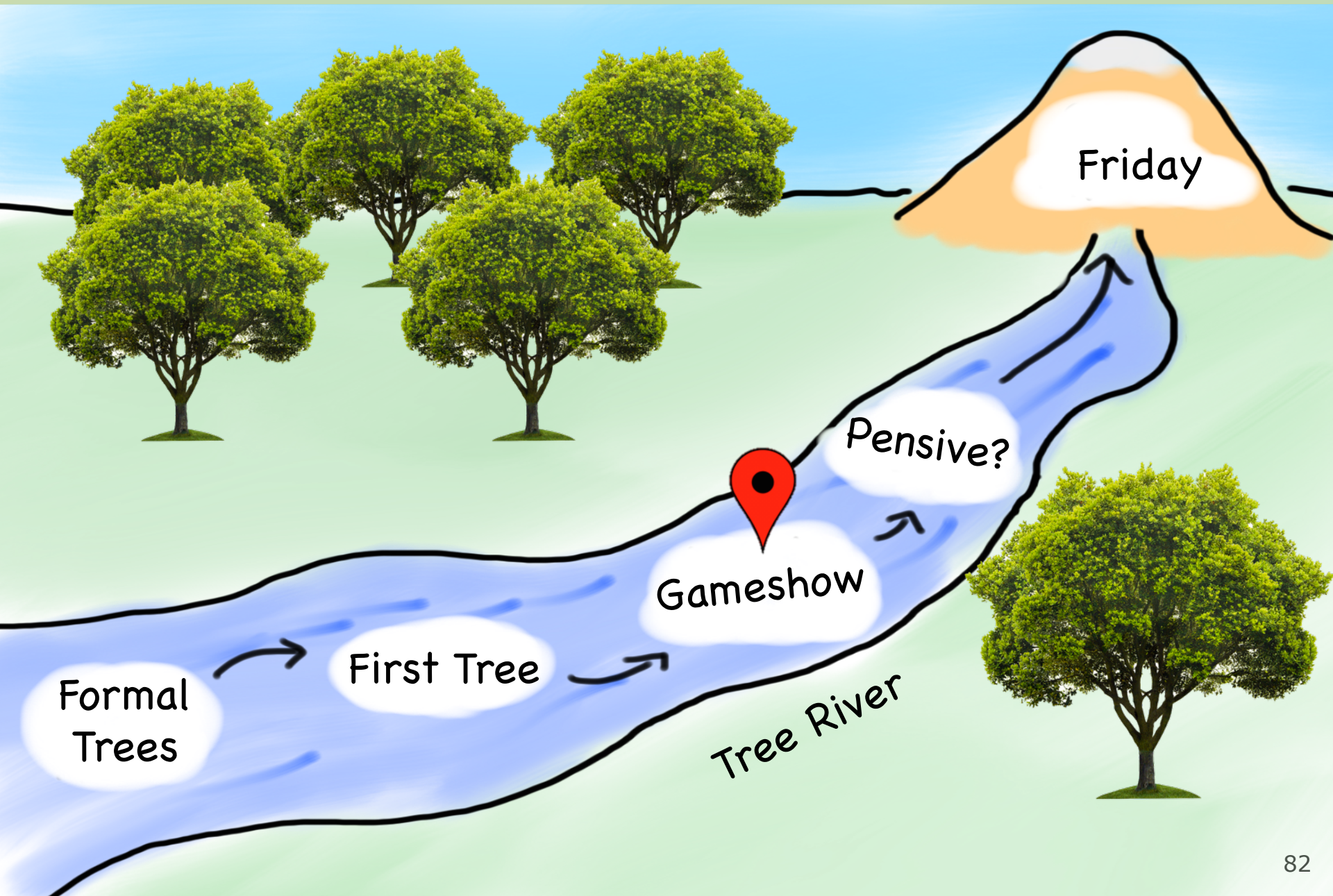
```
void doorTwo(Tree * tree) {  
    if(tree == NULL) return;  
    doorTwo(tree->left);  
    cout<<tree->value<<" ";  
    doorTwo(tree->right);  
}
```

```
Void doorThree(Tree * tree) {  
    if(tree == NULL) return;  
    doorThree(tree->left);  
    doorThree(tree->right);  
    cout<<tree->value<<" ";  
}
```

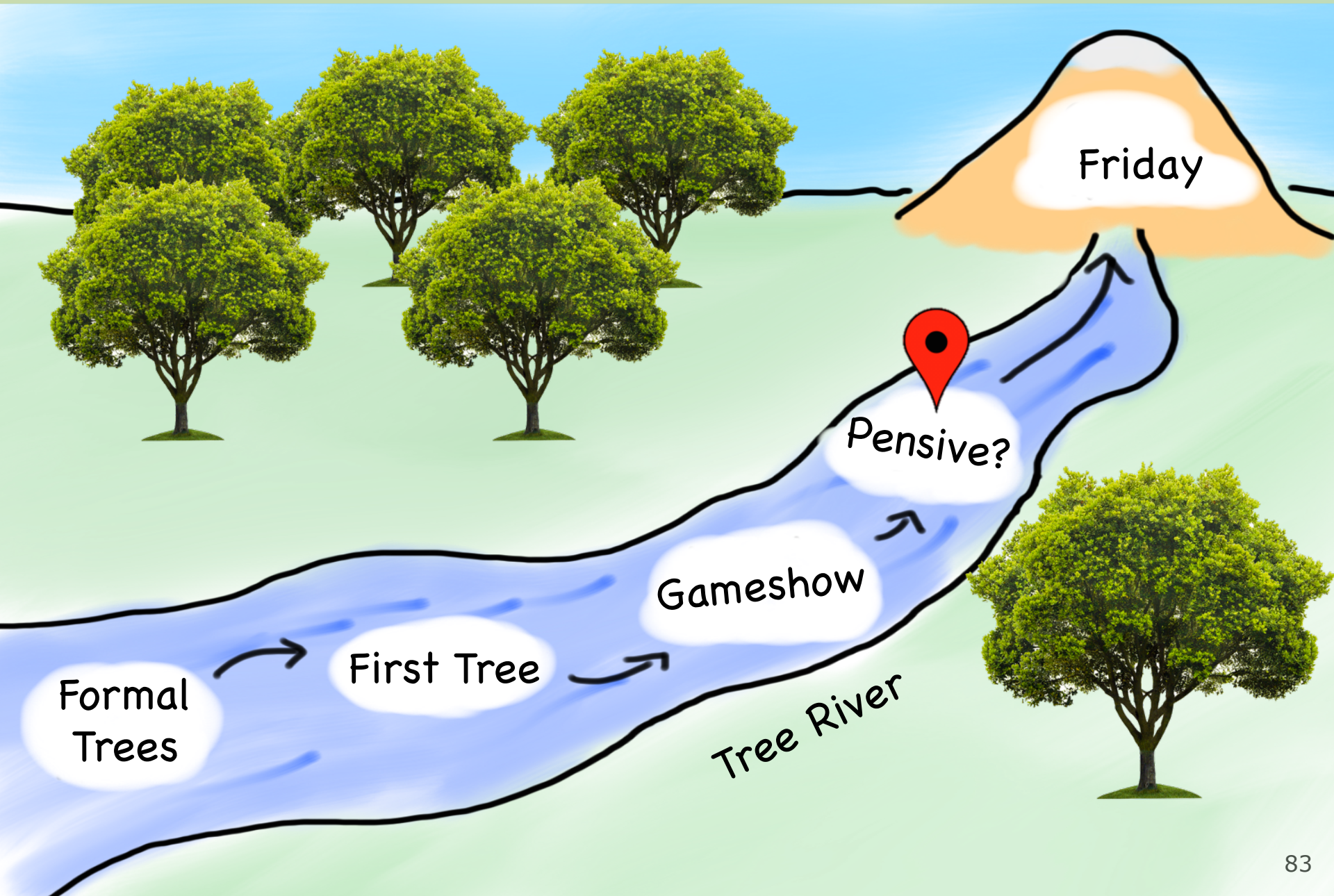




Today's Route



Today's Route



DUMBLEDORE IS SO EPIC



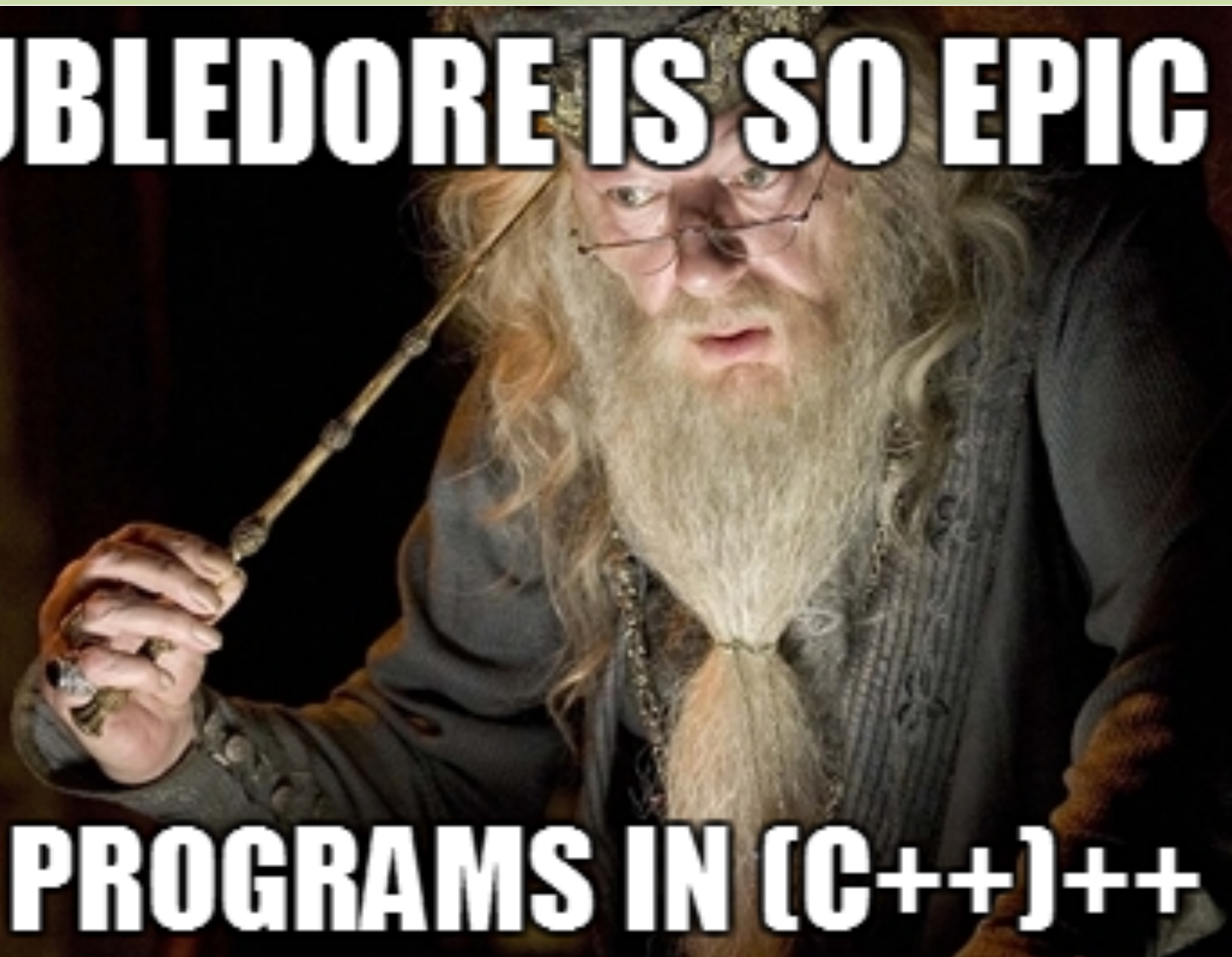
HE CAN SORT IN $O(N)$ TIME

DUMBLEDORE IS SO EPIC



HE BEAT WATSON AT JEOPARDY

DUBLEDORE IS SO EPIC




HE PROGRAMS IN (C++)++

DUMBLEDORE IS SO EPIC

**HE SOLVED P VS NP BUT DIDN'T TELL
ANYONE**

DUMBLEDORE IS SO EPIC

A close-up photograph of Albus Dumbledore from the Harry Potter series. He has a long, flowing white beard and is wearing his signature round glasses. He is holding his wand in his right hand, looking directly at the camera with a serious expression. The background is dark and out of focus.

**HE ENTERED THE CS106B
PROGRAMMING CHALLENGE**

How come Dumbledore knows everything?

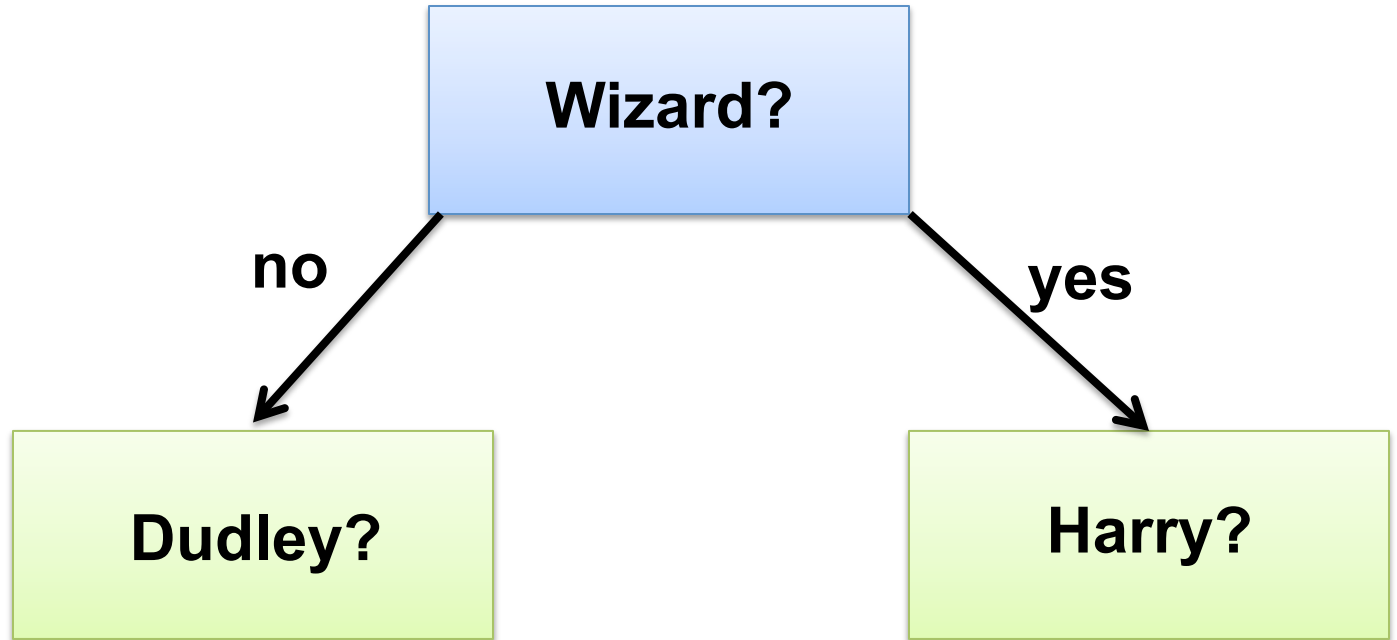
Pensive



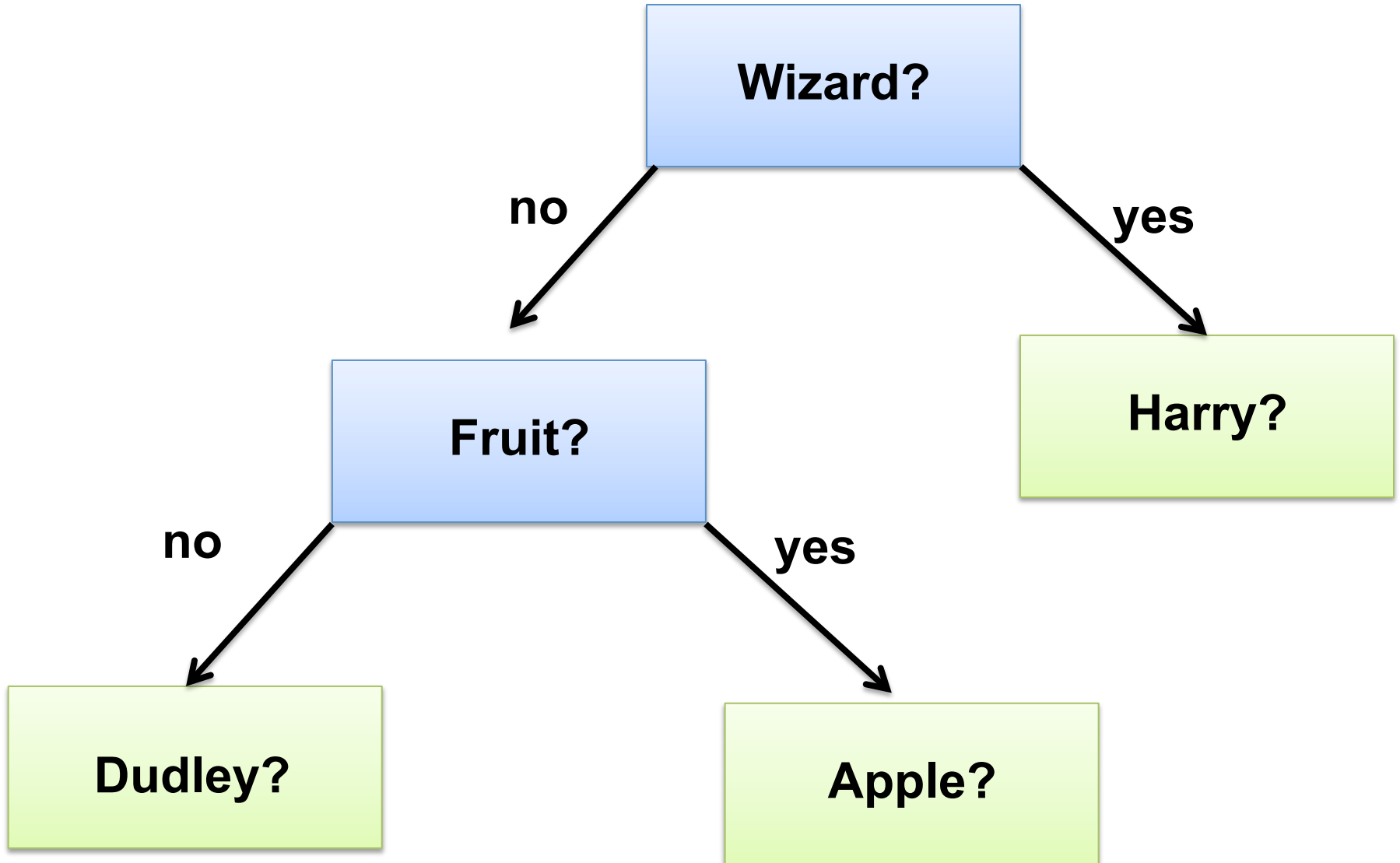
Pensive Demo



Pensive



Pensive



"Do, or do not.

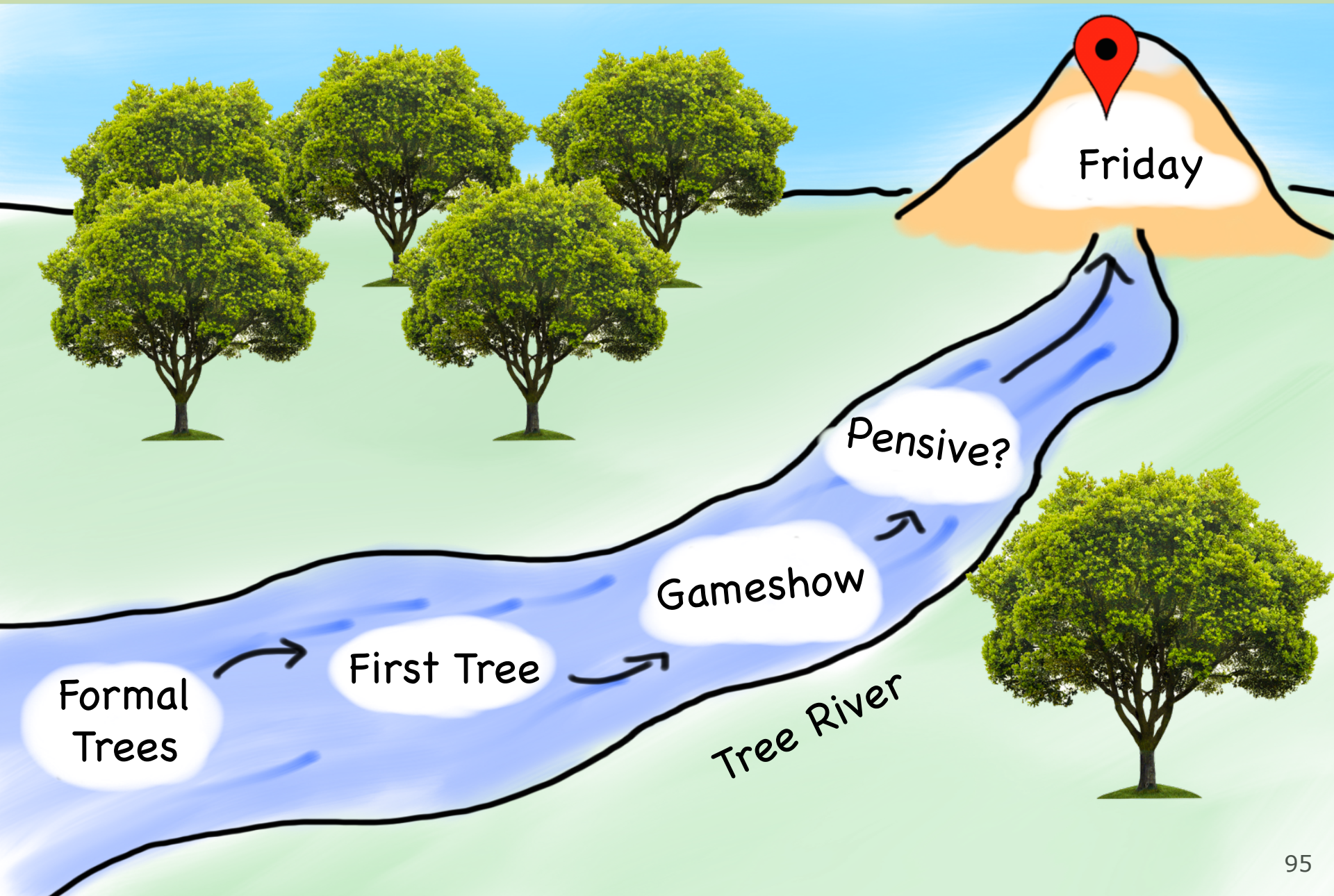
There is no try."

-Dumbledore

* actually Yoda. But what ever



Today's Route



Today's Goal

1. Be able to define a tree
2. Be able to traverse a tree

