CS 106B Lecture 24: Depth First and Breadth First Searching Friday, May 26, 2017

Programming Abstractions Spring 2017 Stanford University Computer Science Department

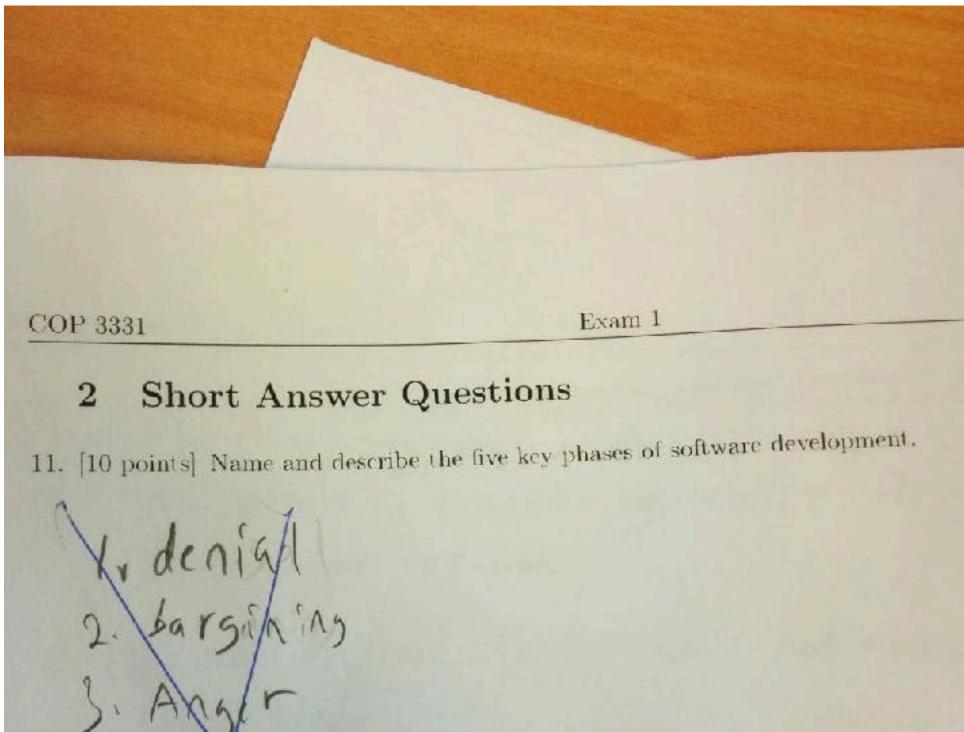
Lecturer: Chris Gregg

reading: Programming Abstractions in C++, Chapter 18.6

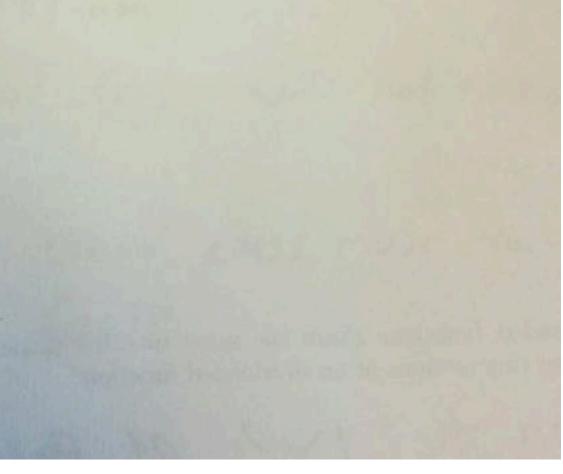




At this point in the quarter...



4. deptessi 5. accepta na



https://i.redd.it/e5uylwsqzizx.jpg





Logistics

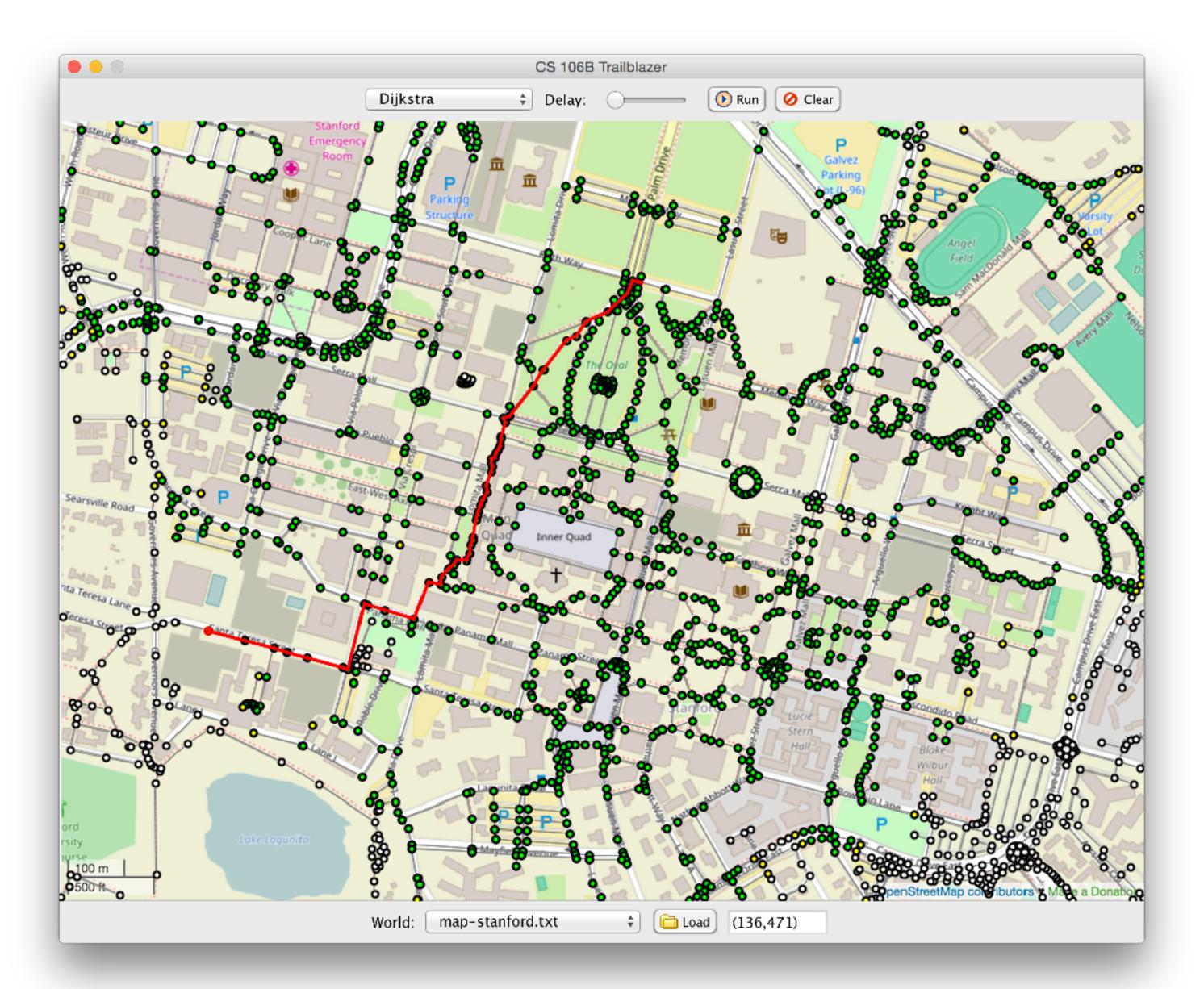
- •Trailblazer: Will be due on the last day of classes, no late days allowed.
- or use <u>sayat.me/chrisgregg</u> to let me know these things!
- More on Graphs (and a bit on Trees)
- Depth First Search
- •Breadth First Search

•There was some Tiny Feedback about an SL who "typically delays the grading" and feedback process a few weeks after the homework is due..." and "told us that in the beginning of the quarter that we can use late credit for the Assignment 7" this is **bad**. We need to know as early as possible if SLs aren't holding IGs or doing grading on time, or is passing on mis-information. Please email me directly,





Trailblazer



You create Google Maps!

You need to implement four different (but related) types of searches:

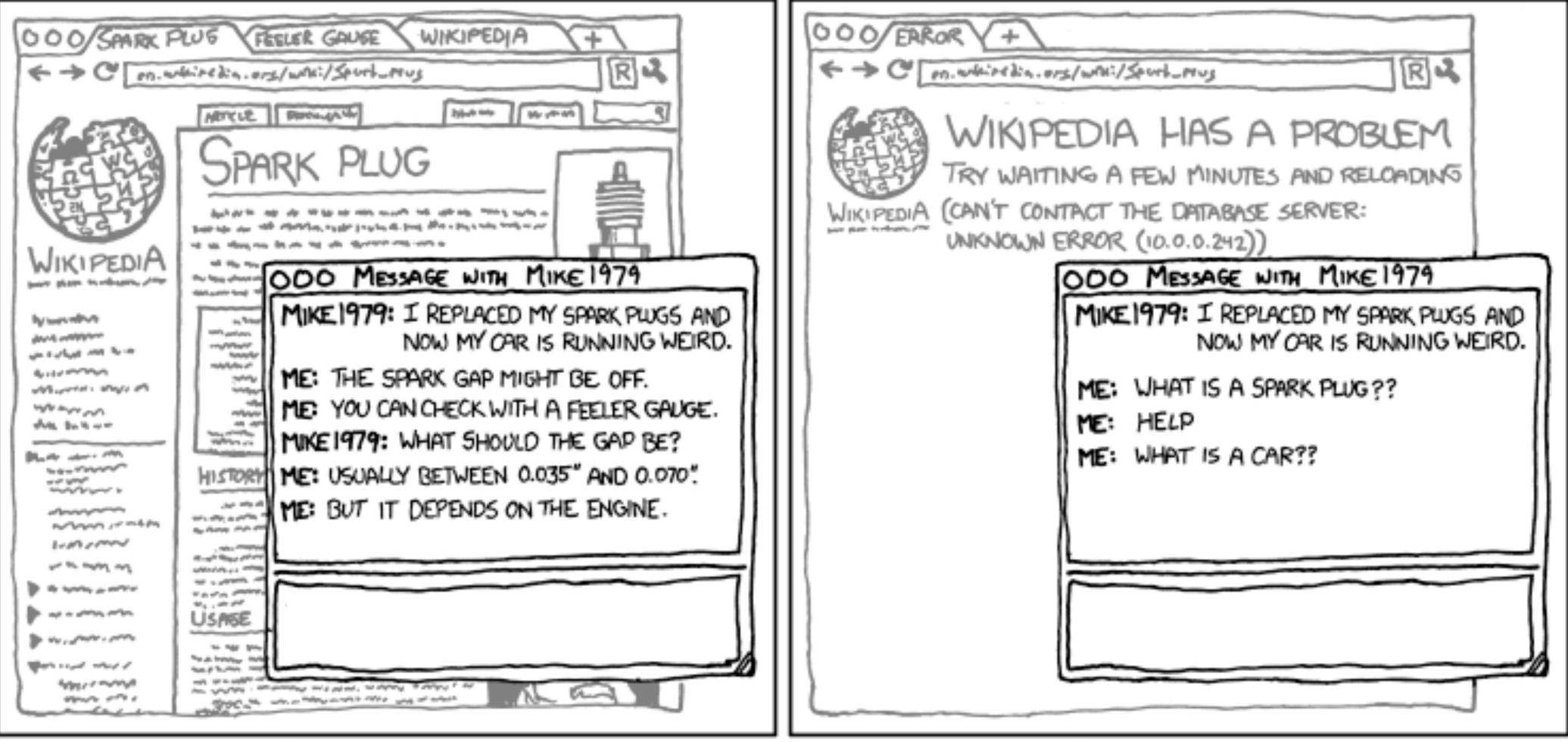
- Breadth First Search (today)
- Dijkstra (Wednesday, but will have an additional video by Saturday)
- A* (Wednesday, will also be covered in additional video)
- Alternate (you must determine algorithm)







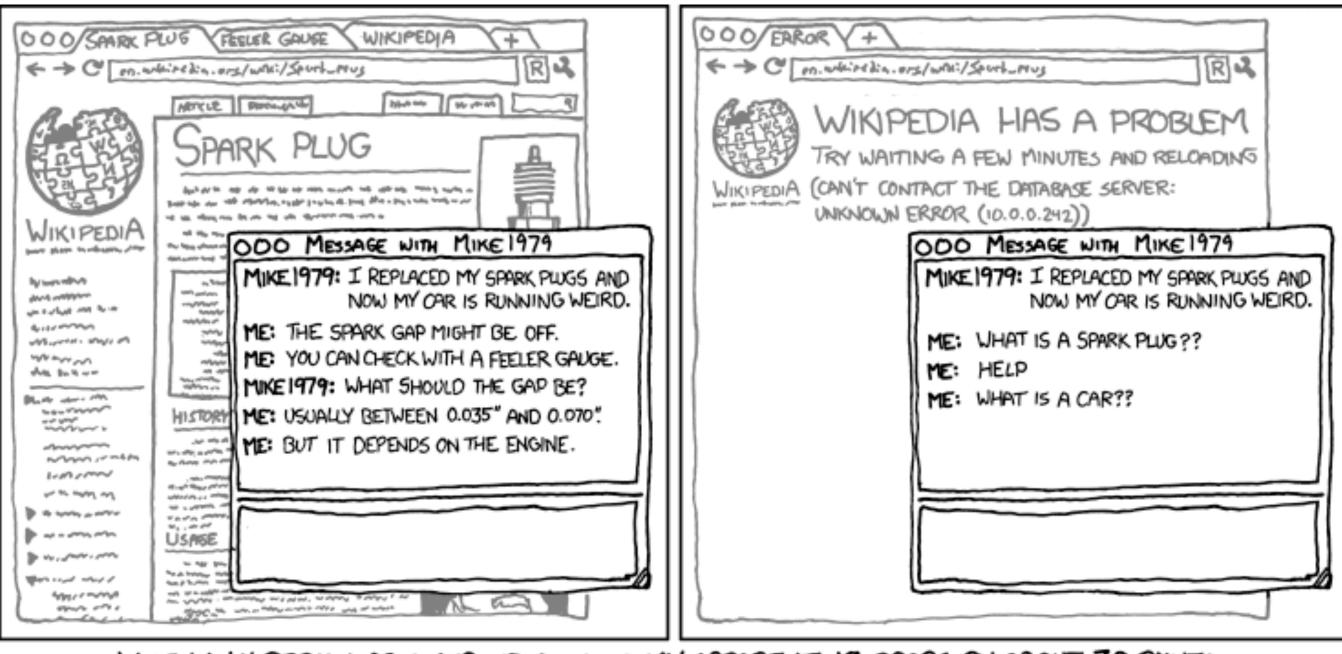
Wikipedia



WHEN WIKIPEDIA HAS A SERVER OUTAGE, MY APPARENT 1Q DROPS BY ABOUT 30 POINTS,

XKCD 903, Extended Mind, <u>http://xkcd.com/903/</u>





WHEN WIKIPEDIA HAS A SERVER OUTAGE, MY APPARENT IQ DROPS BY ABOUT 30 POINTS.

XKCD 903, Extended Mind, http://xkcd.com/903/

Wikipedia

When you hover over an XKCD comic, you get an extra joke:

Wikipedia trivia: if you take any article, click on the first link in the article text not in parentheses or italics, and then repeat, you will eventually end up at "Philosophy".





Is this true??

According to the Wikipedia article "Wikipedia:Getting to Philosophy" (so meta), (https://en.wikipedia.org/wiki/Wikipedia:Getting_to_Philosophy):

As of February 2016, 97% of all articles in Wikipedia eventually lead to the article Philosophy.

How can we find out? We shall see!

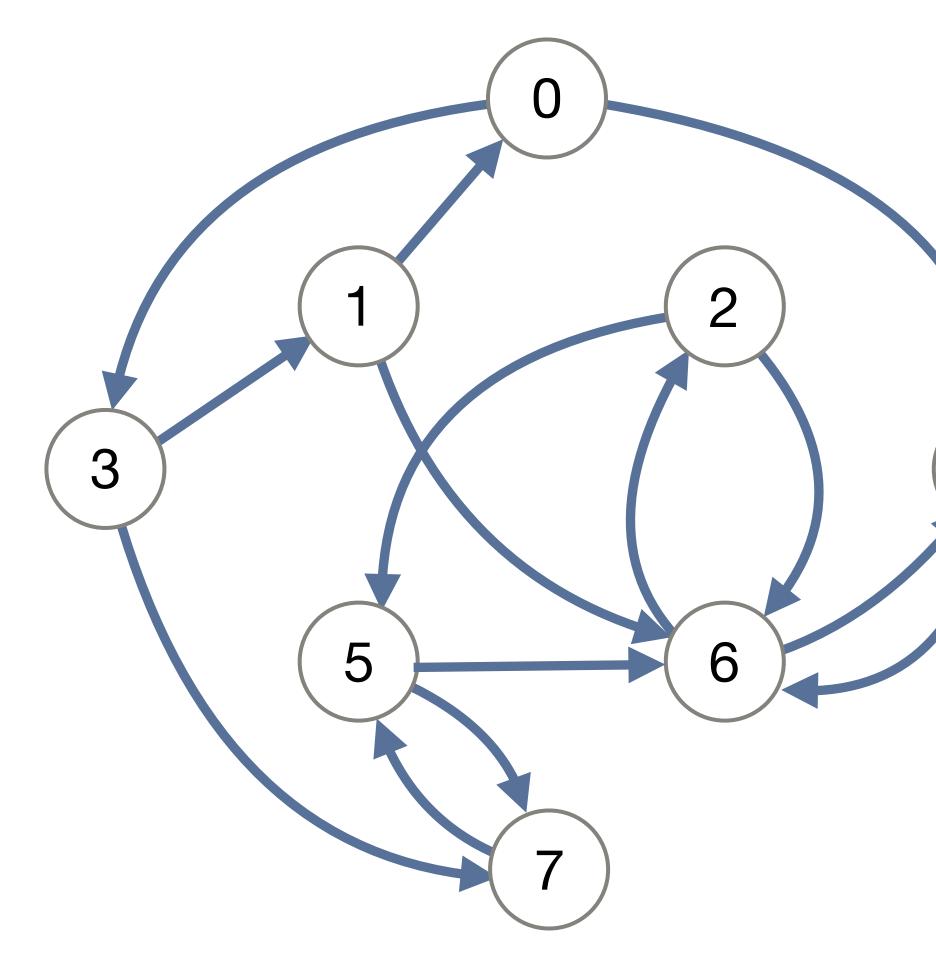
Wikipedia

Wikipedia trivia: if you take any article, click on the first link in the article text not in parentheses or italics, and then repeat, you will eventually end up at "Philosophy".





Recall from the last couple of lectures that a graph is the "wild west of trees" graphs relate vertices (nodes) to each other by way of edges, and they can be directed or undirected. Take the following directed graph:



Graph Searching

A search on this graph starts at one vertex and attempts to find another vertex. If it is successful, we say there is a path from the start to the finish vertices.

What paths are there from 0 to 6?

() 🕼 4 🕼 6

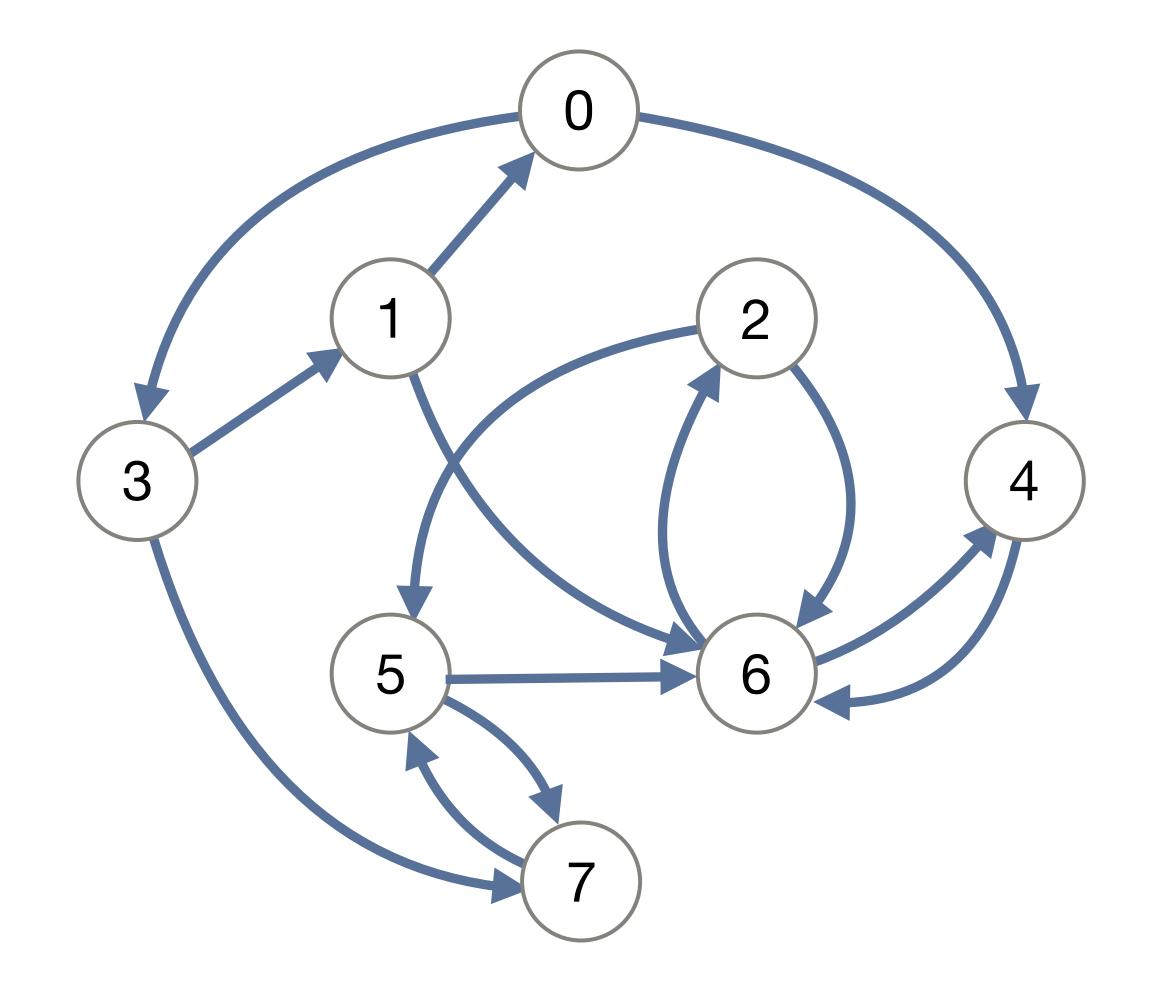
0 @ 3 @ 1 @ 6

0 @ 3 @ 7 @ 5 @ 6





What paths are there from 3 to 2?



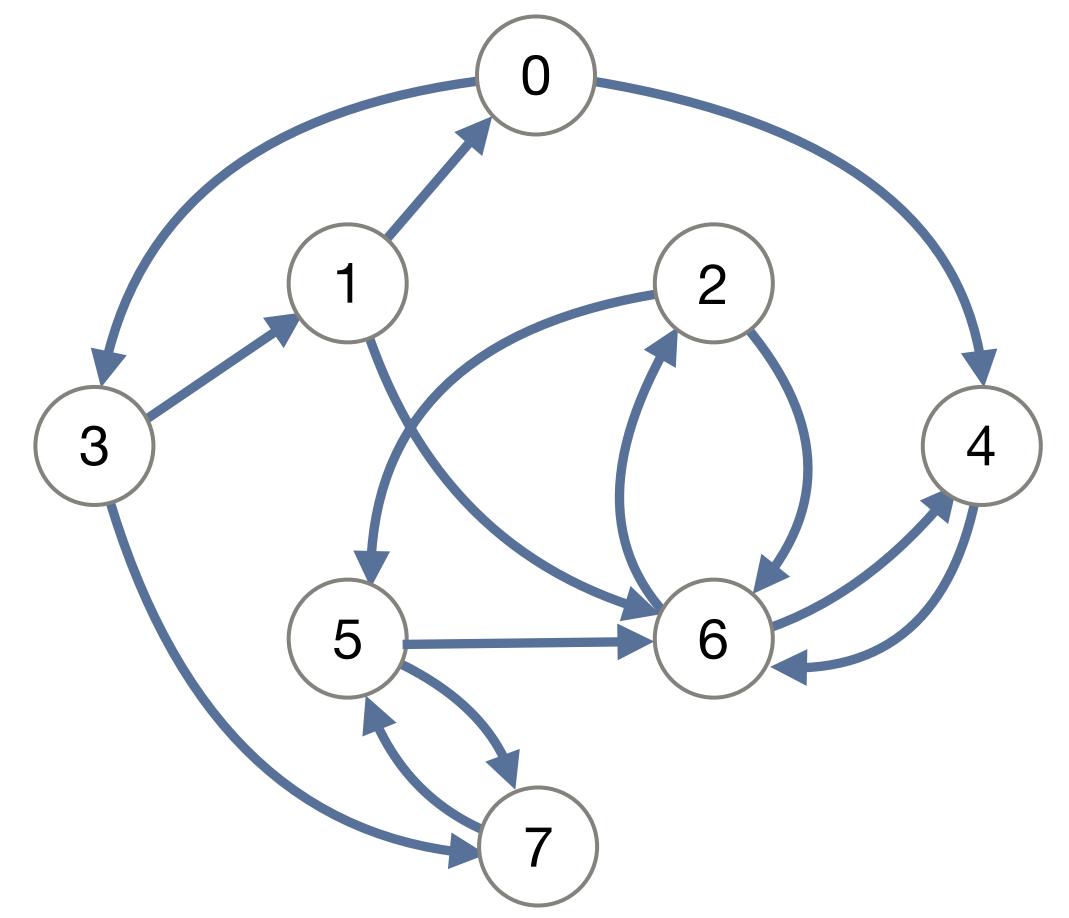
Graph Searching

3 @ 1 @ 6 @ 2 3 @ 7 @ 5 @ 6 @ 2 3@1@0@4@6@2





What paths are there from 4 to 1?



Graph Searching

None! :(



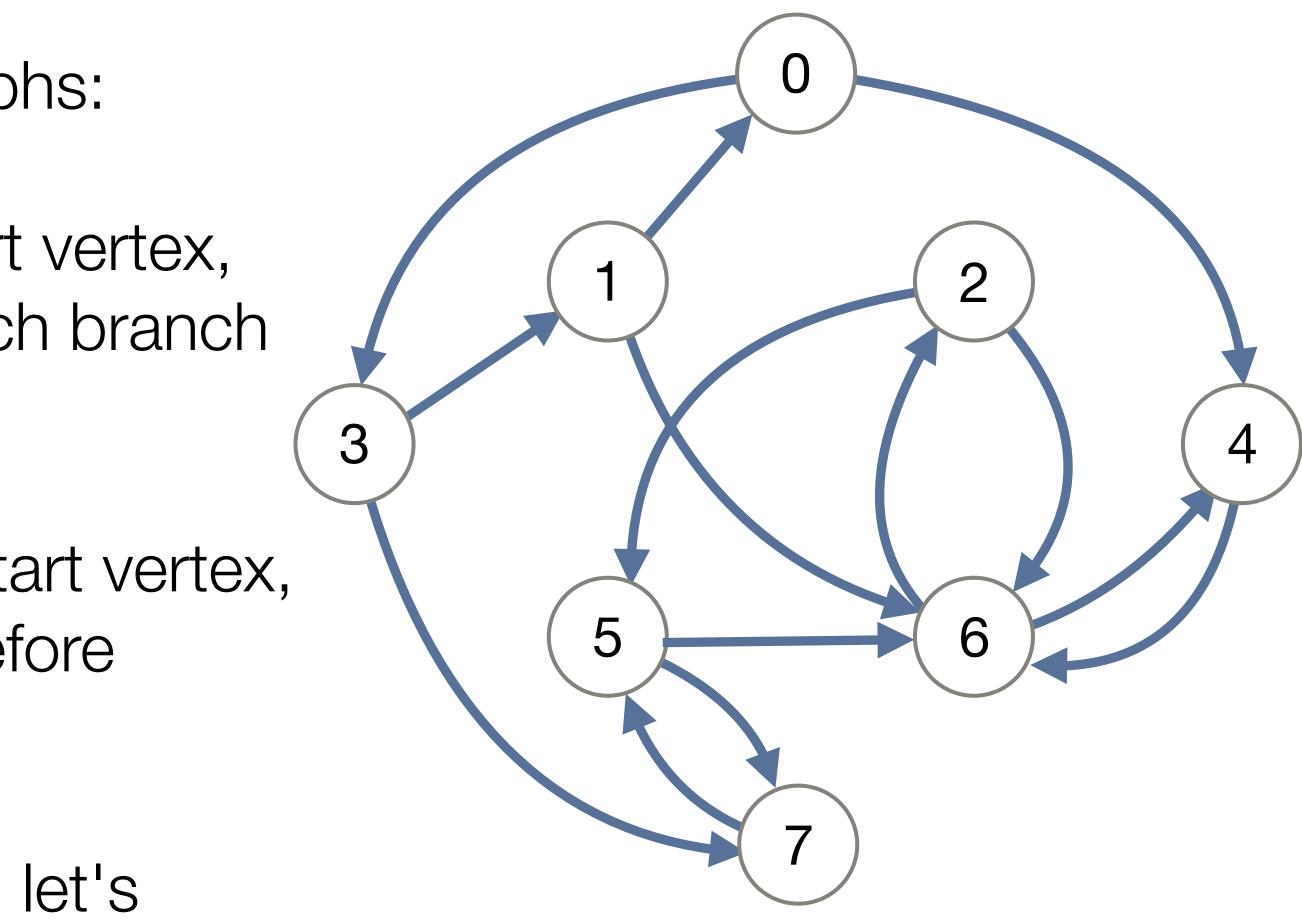


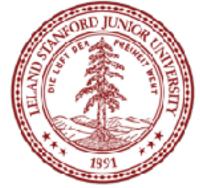
We have different ways to search graphs:

- **Depth First Search**: From the start vertex, • explore as far as possible along each branch before backtracking.
- **Breadth First Search**: From the start vertex, ulletexplore the neighbor nodes first, before moving to the next level neighbors.

Both methods have pros and cons — let's explore the algorithms.

Graph Searching





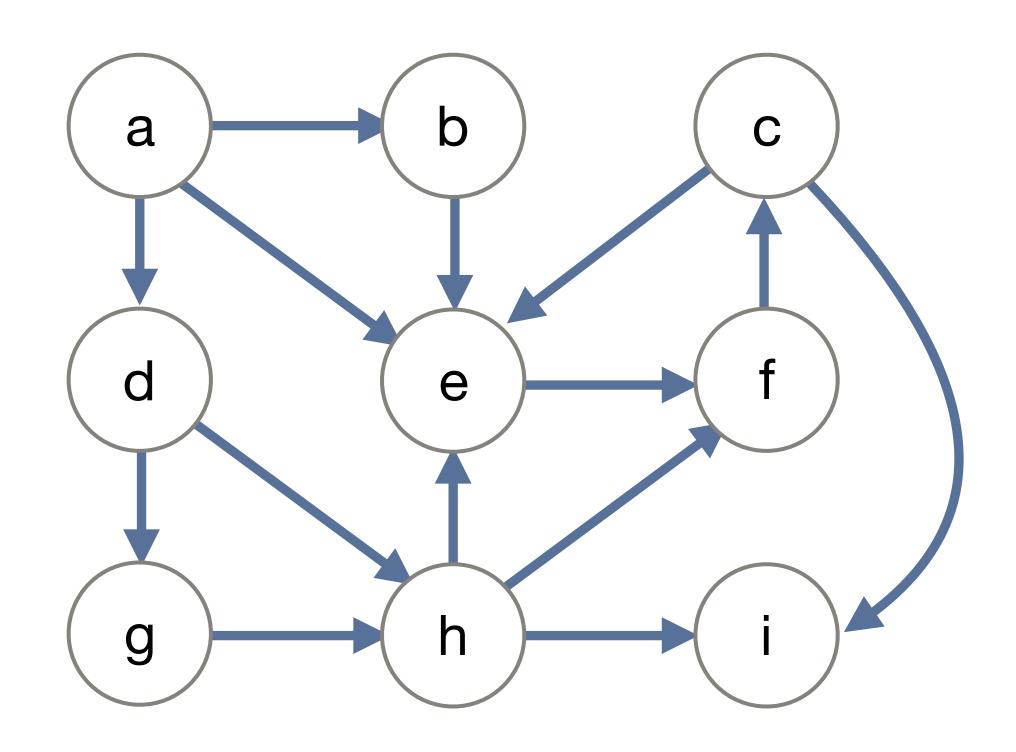
Depth First Search (DFS)

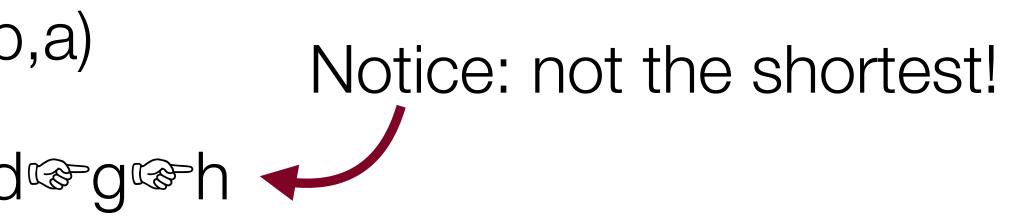
From the start vertex, explore as far as possible along each branch before backtracking.

This is often implemented recursively. For a graph, you must mark visited vertices, or you might traverse forever (e.g., c@e@f@c@e...)

DFS from a to h (assuming a-z order) visits:

ard D er i (dead end — back to c,f,e,b,a) O g path found: a cod cong conh

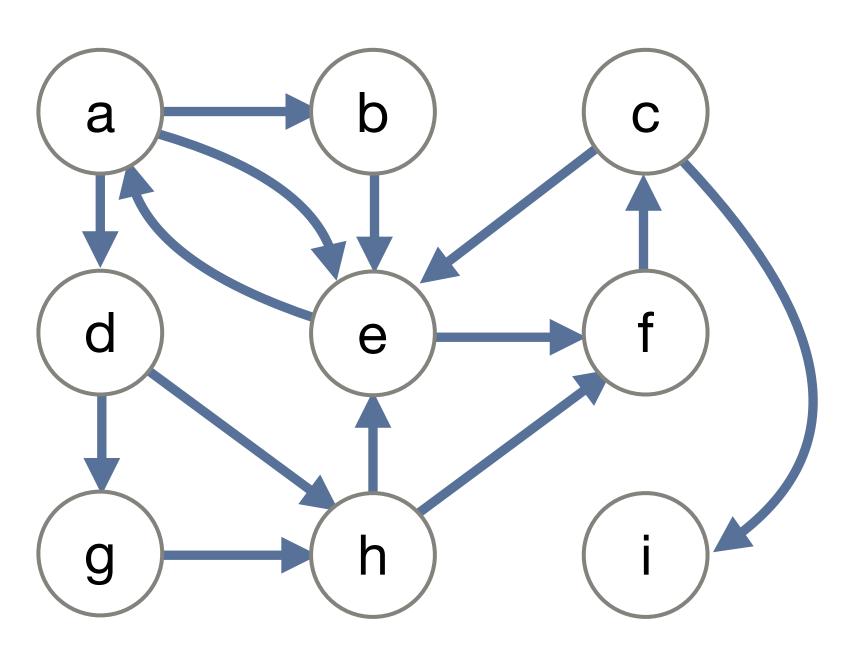






dfs from v_1 to v_2 : base case: if at v_2 , found! mark v_1 as visited. for all edges from v_1 to its neighbors: if neighbor n is unvisited, recursively call dfs(n, v2).







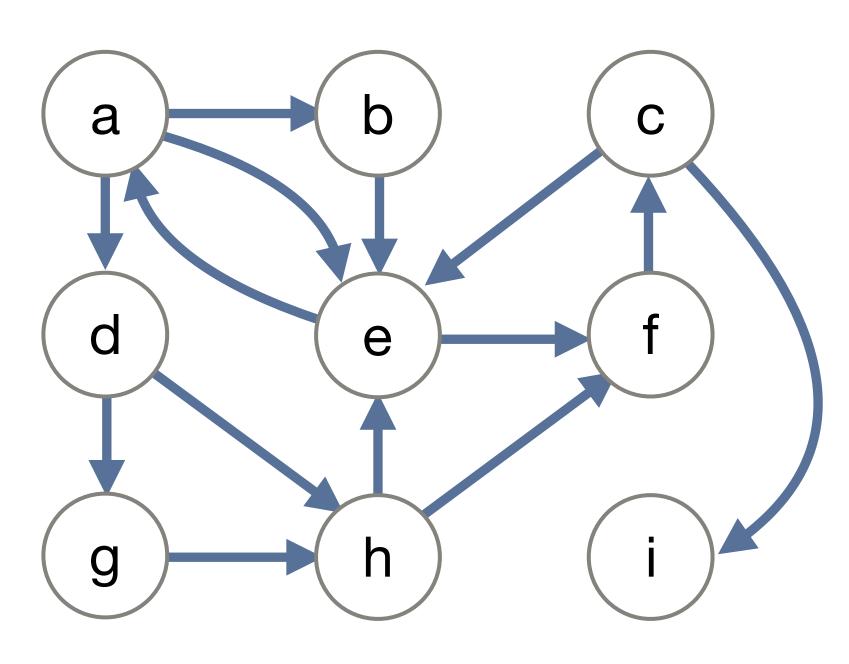


dfs from v_1 to v_2 : mark v_1 as visited. for all edges from v_1 to its neighbors: if neighbor n is unvisited, recursively call dfs(n, v_2).

Let's look at **dfs** from h to c:

| Vertex | |
|--------|--|
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| h | |
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| Visited? | |
|----------|--|
| false | |







dfs from v_1 to v_2 : mark v_1 as visited. for all edges from v_1 to its neighbors: if neighbor n is unvisited, recursively call dfs(n, v_2).

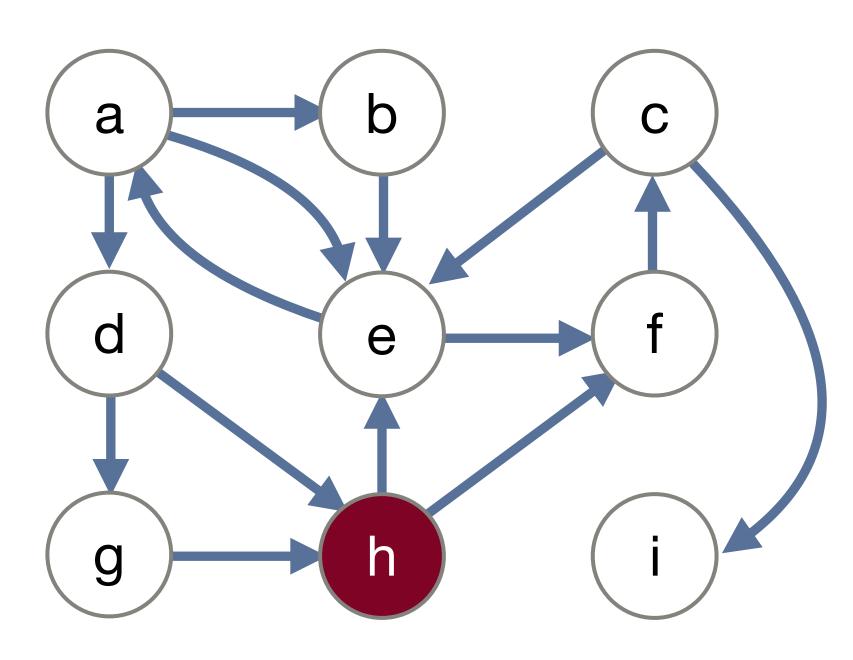
Let's look at **dfs** from h to c:

call stack:

| dfc(h c) |
|----------|
| dfs(h,c) |
| |

| Vert | ex |
|------|----|
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| Visited? |
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| false |
| true |
| false |









dfs from v_1 to v_2 : mark v_1 as visited. for all edges from v_1 to its neighbors: if neighbor n is unvisited, recursively call dfs(n, v_2).

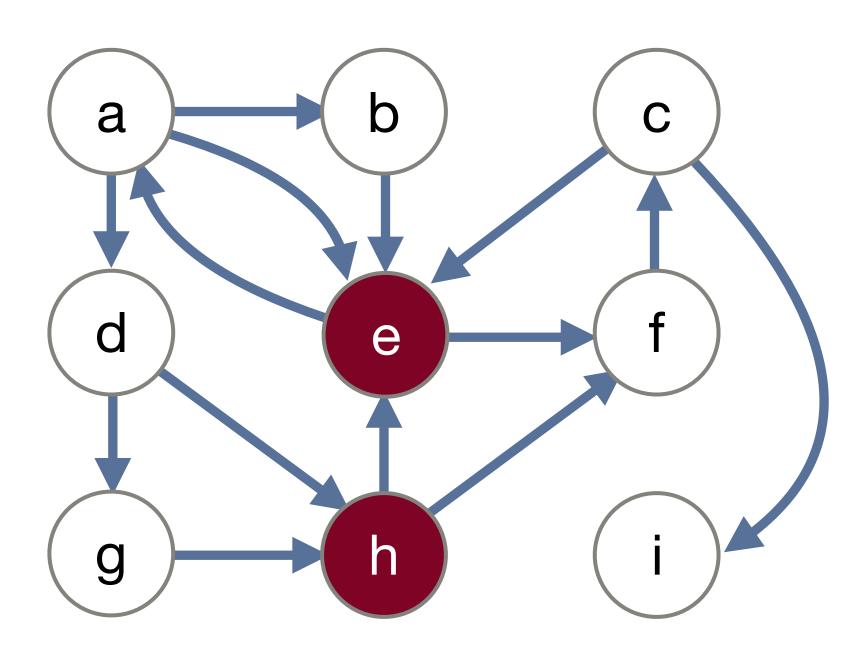
Let's look at **dfs** from h to c:

call stack:

| dfs(e,c) | |
|----------|--|
| dfs(h,c) | |

| ex |
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| /isited? | |
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| false | |
| false | |
| false | |
| true | |
| false | |
| false | |
| true | |
| false | |









dfs from v_1 to v_2 : mark v_1 as visited. for all edges from v_1 to its neighbors: if neighbor n is unvisited, recursively call dfs(n, v_2).

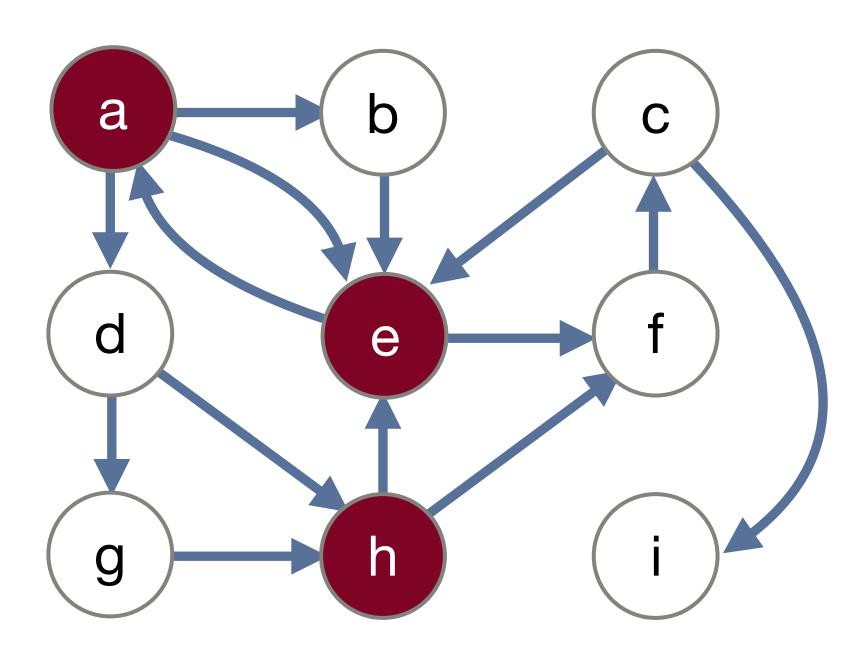
Let's look at **dfs** from h to c:

call stack:

| dfs(a,c) |
|----------|
| |
| |
| |
| |
| dfs(e,c) |
| |
| |
| |
| |
| |
| |
| dfs(h,c) |
| |

| Vert | ex |
|------|----|
| a | |
| b | |
| С | |
| d | |
| e | |
| f | |
| g | |
| h | |
| i | |

| Visited? | |
|----------|--|
| true | |
| false | |
| false | |
| false | |
| true | |
| false | |
| false | |
| true | |
| false | |









dfs from v_1 to v_2 : mark v_1 as visited. for all edges from v_1 to its neighbors: if neighbor n is unvisited, recursively call dfs(n, v_2).

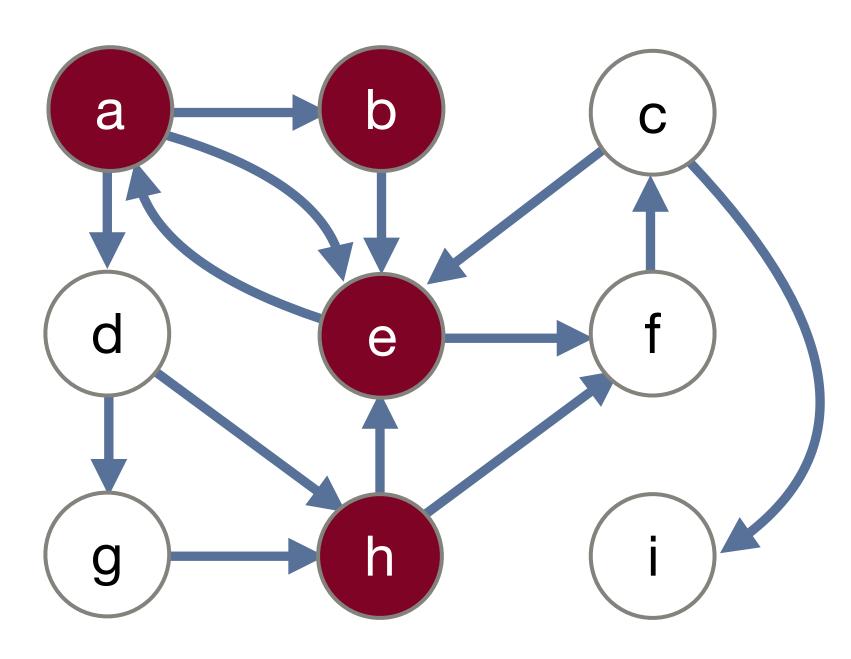
Let's look at **dfs** from h to c:

call stack:

| dfs(b,c) |
|----------|
| dfs(a,c) |
| dfs(e,c) |
| dfs(h,c) |

| Vert | ex |
|------|----|
| a | |
| b | |
| С | |
| d | |
| е | |
| f | |
| g | |
| h | |
| i | |

| /isited? | |
|----------|--|
| true | |
| true | |
| false | |
| false | |
| true | |
| false | |
| false | |
| true | |
| false | |







dfs from v_1 to v_2 : mark v_1 as visited. for all edges from v_1 to its neighbors: if neighbor n is unvisited, recursively call dfs(n, v_2).

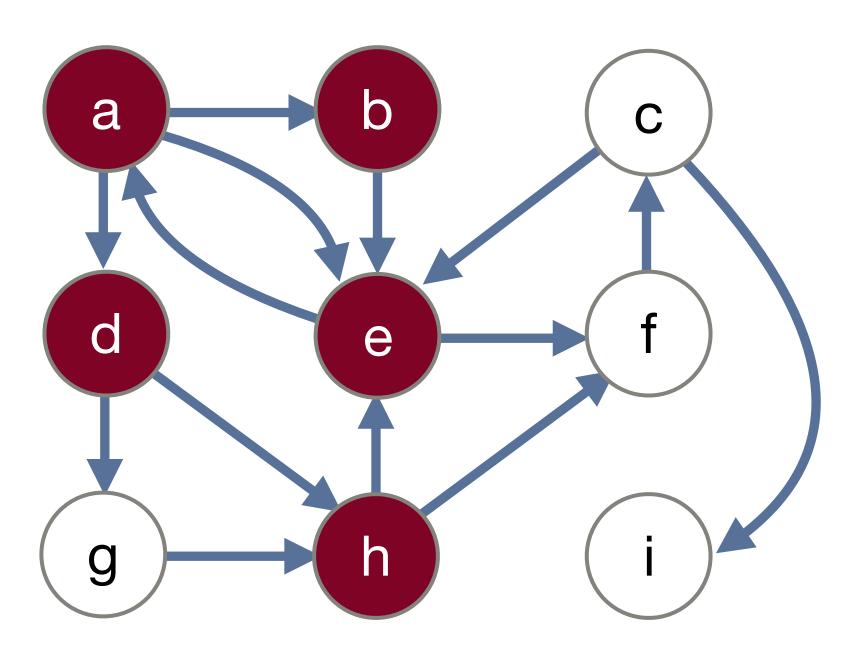
Let's look at **dfs** from h to c:

call stack:

| dfs(d,c) |
|----------|
| dfs(a,c) |
| dfs(e,c) |
| dfs(h,c) |

| Vert | ex |
|------|----|
| a | |
| b | |
| С | |
| d | |
| е | |
| f | |
| g | |
| h | |
| i | |

| Visited? | |
|----------|--|
| true | |
| true | |
| false | |
| true | |
| true | |
| false | |
| false | |
| true | |
| false | |







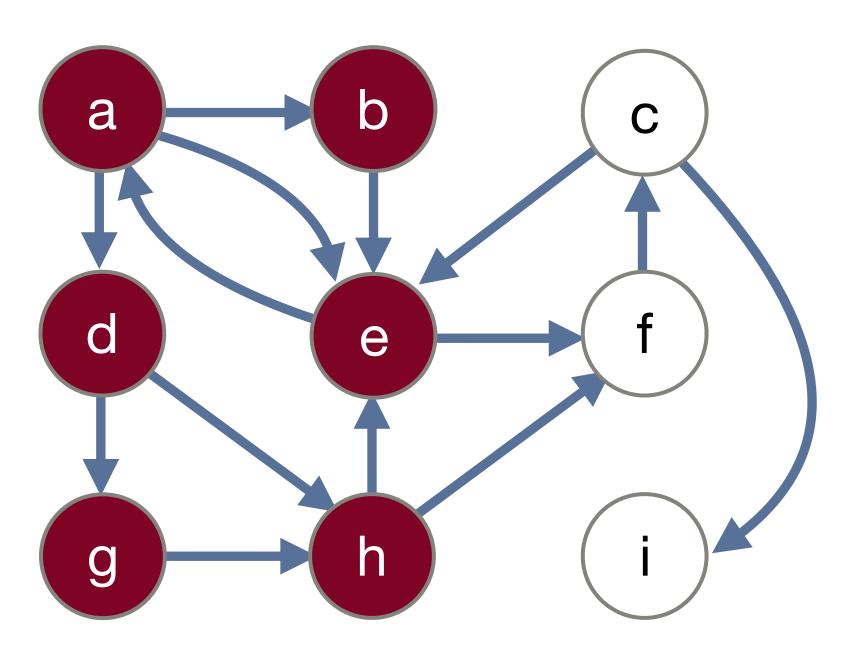
dfs from v_1 to v_2 : mark v_1 as visited. for all edges from v_1 to its neighbors: if neighbor n is unvisited, recursively call dfs(n, v_2).

Let's look at **dfs** from h to c:

| dfs(g,c) |
|----------|
| dfs(d,c) |
| dfs(a,c) |
| dfs(e,c) |
| dfs(h,c) |

| | Vertex | к Мар |
|------|--------|-------|
| Vert | ех | |
| a | | |
| b | | |
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| h | | |
| i | | |

| Visited? |
|----------|
| true |
| true |
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| false |
| true |
| true |
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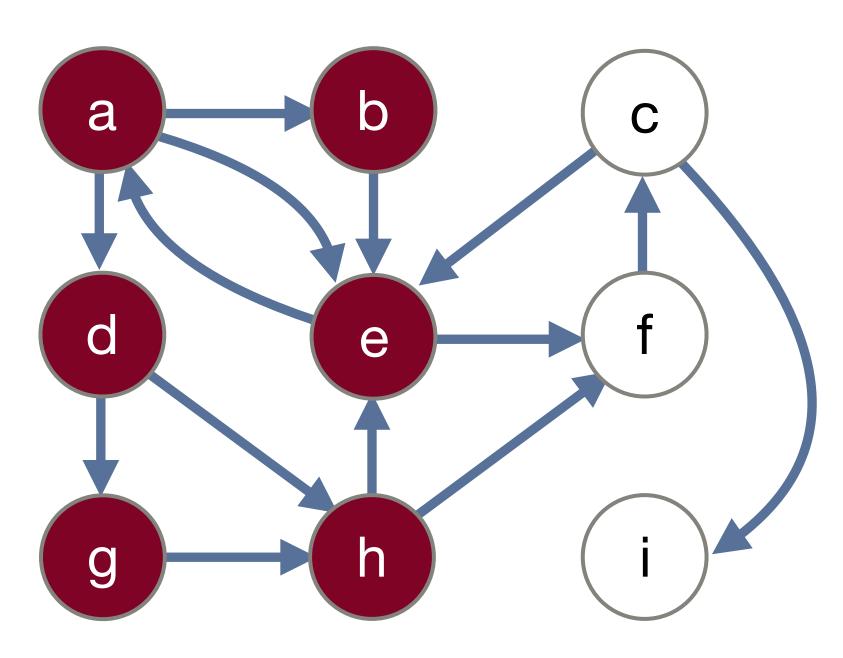
dfs from v_1 to v_2 : mark v_1 as visited. for all edges from v_1 to its neighbors: if neighbor n is unvisited, recursively call dfs(n, v_2).

Let's look at **dfs** from h to c:



| $\Pi \ IO \ C.$ | Vertex | k Map |
|-----------------|--------|-------|
| Vert | ех | |
| a | | |
| b | | |
| С | | |
| d | | |
| е | | |
| f | | |
| g | | |
| h | | |
| i | | |

| Visited? |
|----------|
| true |
| true |
| false |
| true |
| false |
| |



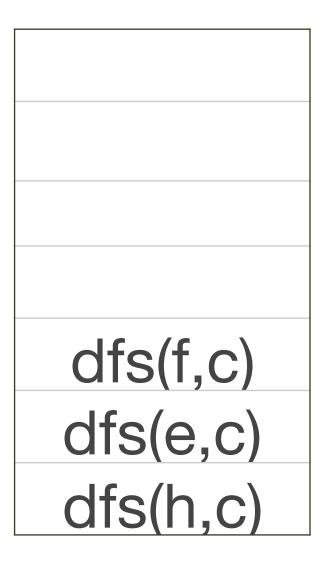






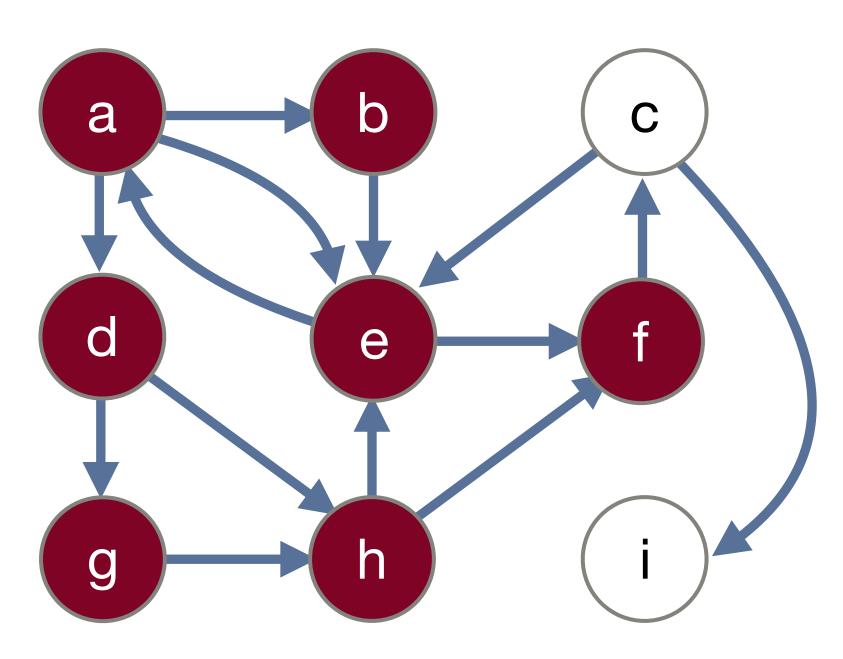
dfs from v_1 to v_2 : mark v_1 as visited. for all edges from v_1 to its neighbors: if neighbor n is unvisited, recursively call dfs(n, v_2).

Let's look at **dfs** from h to c:



| | Vertex | k Map |
|------|--------|-------|
| Vert | ех | |
| a | | |
| b | | |
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| h | | |
| i | | |

| Visited? |
|----------|
| true |
| true |
| false |
| true |
| false |
| |



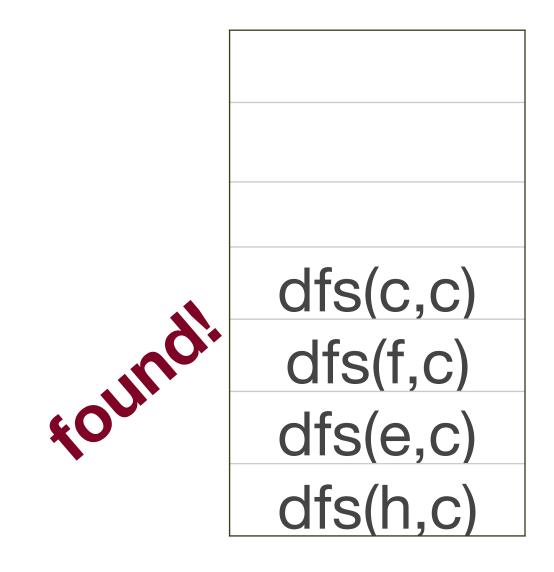






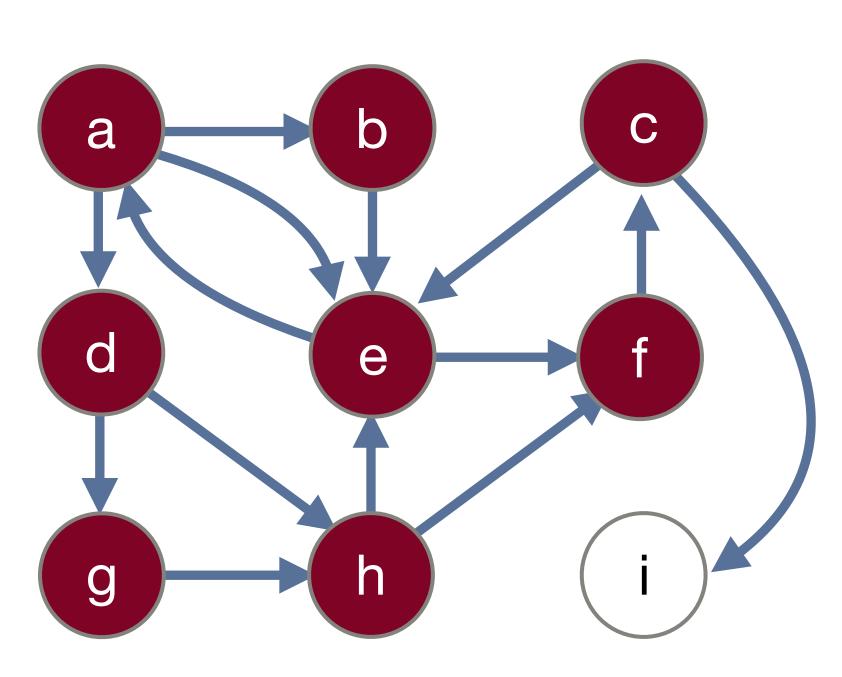
dfs from v_1 to v_2 : mark v_1 as visited. for all edges from v_1 to its neighbors: if neighbor n is unvisited, recursively call dfs(n, v_2).

Let's look at **dfs** from h to c:



| | Vertex | k Map |
|------|--------|-------|
| Vert | ех | |
| a | | |
| b | | |
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| /isited? | |
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| true | |
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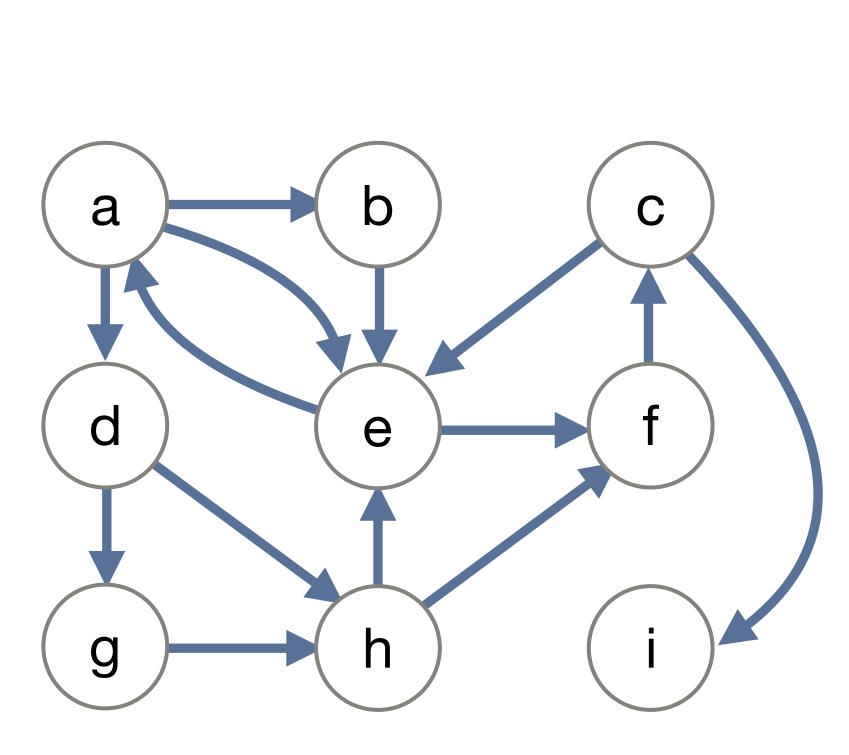




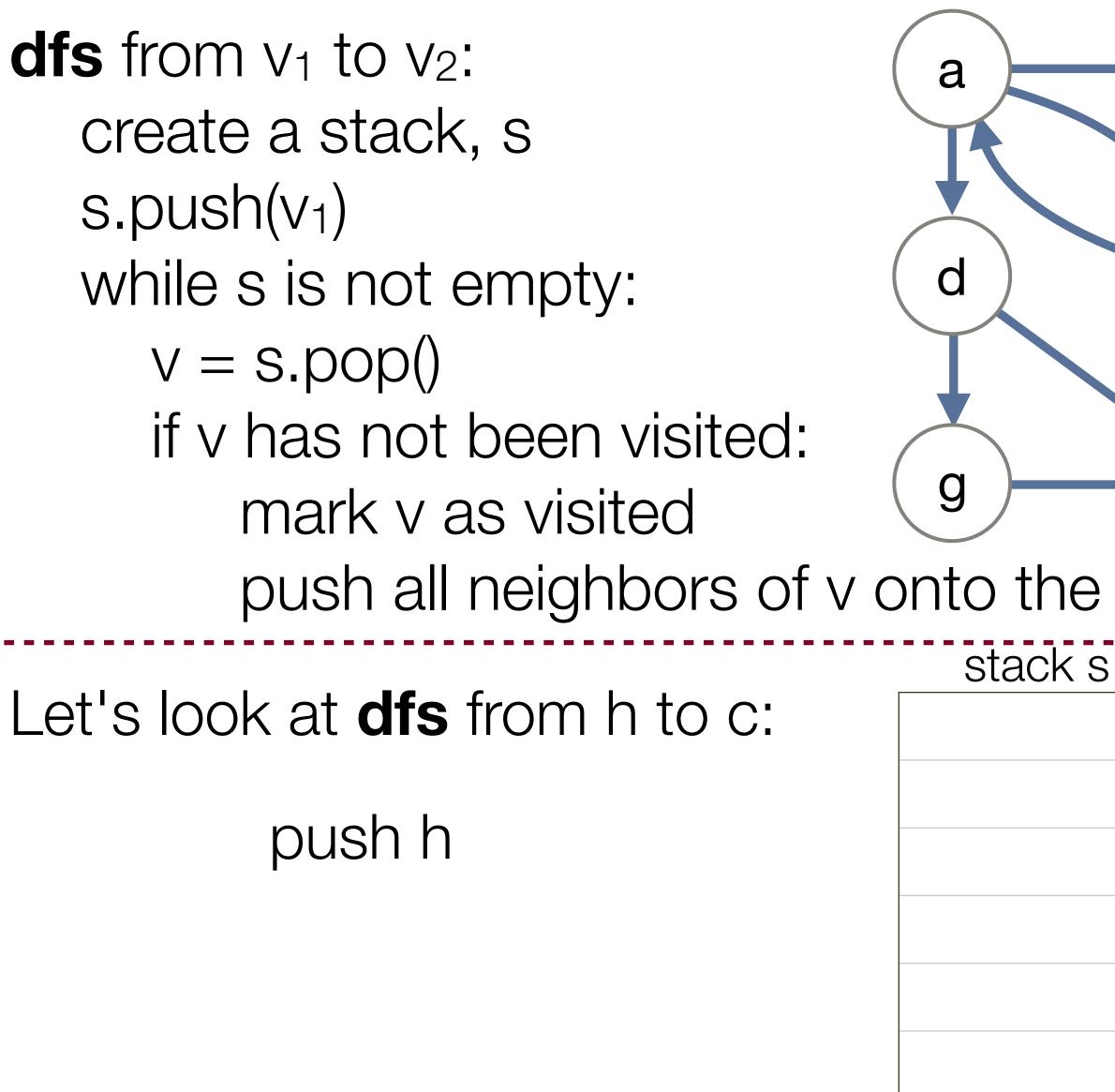


```
dfs from v_1 to v_2:
  create a stack, s
  s.push(v_1)
  while s is not empty:
     V = S.pop()
     if v has not been visited:
         mark v as visited
         push all neighbors of v onto the stack
```







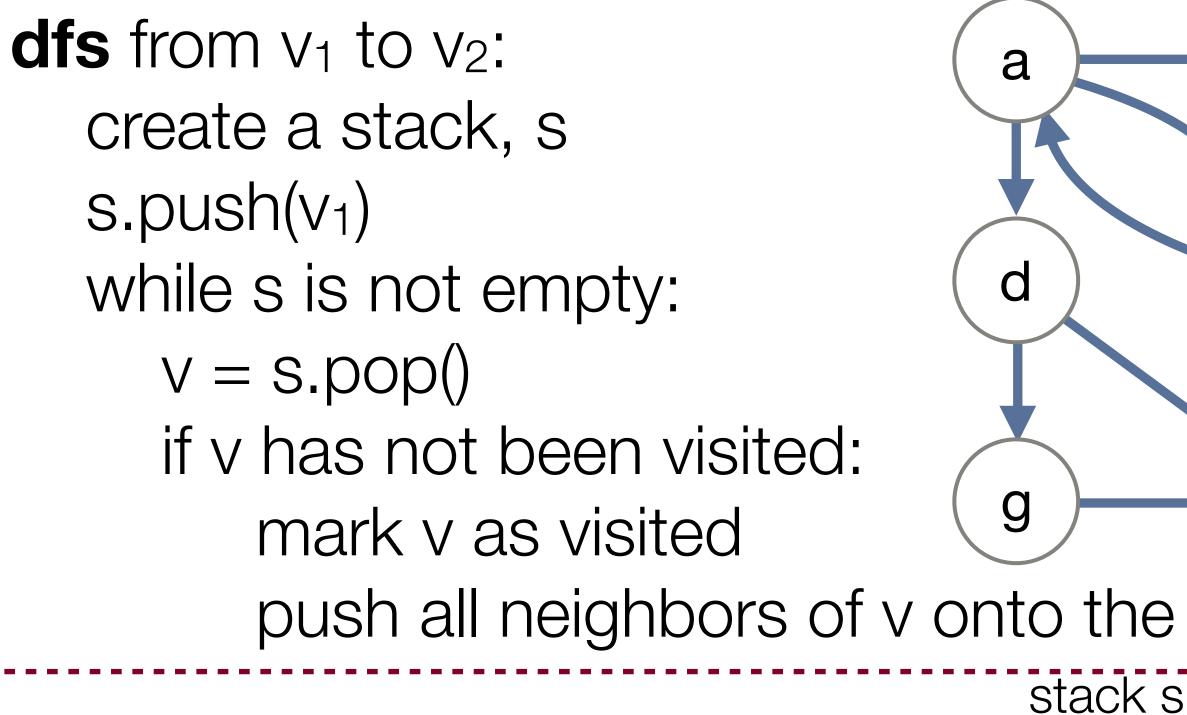


| b c e f | | |
|------------|--------|----------|
| h (i) | Verte | ex Map |
| | Vertex | Visited? |
| stack | a | false |
| | b | false |
| | С | false |
| | d | false |
| | е | false |
| | f | false |
| | g | false |
| | h | false |
| | i | false |









Let's look at **dfs** from h to c:

in while loop: V = S.pop()

v: h

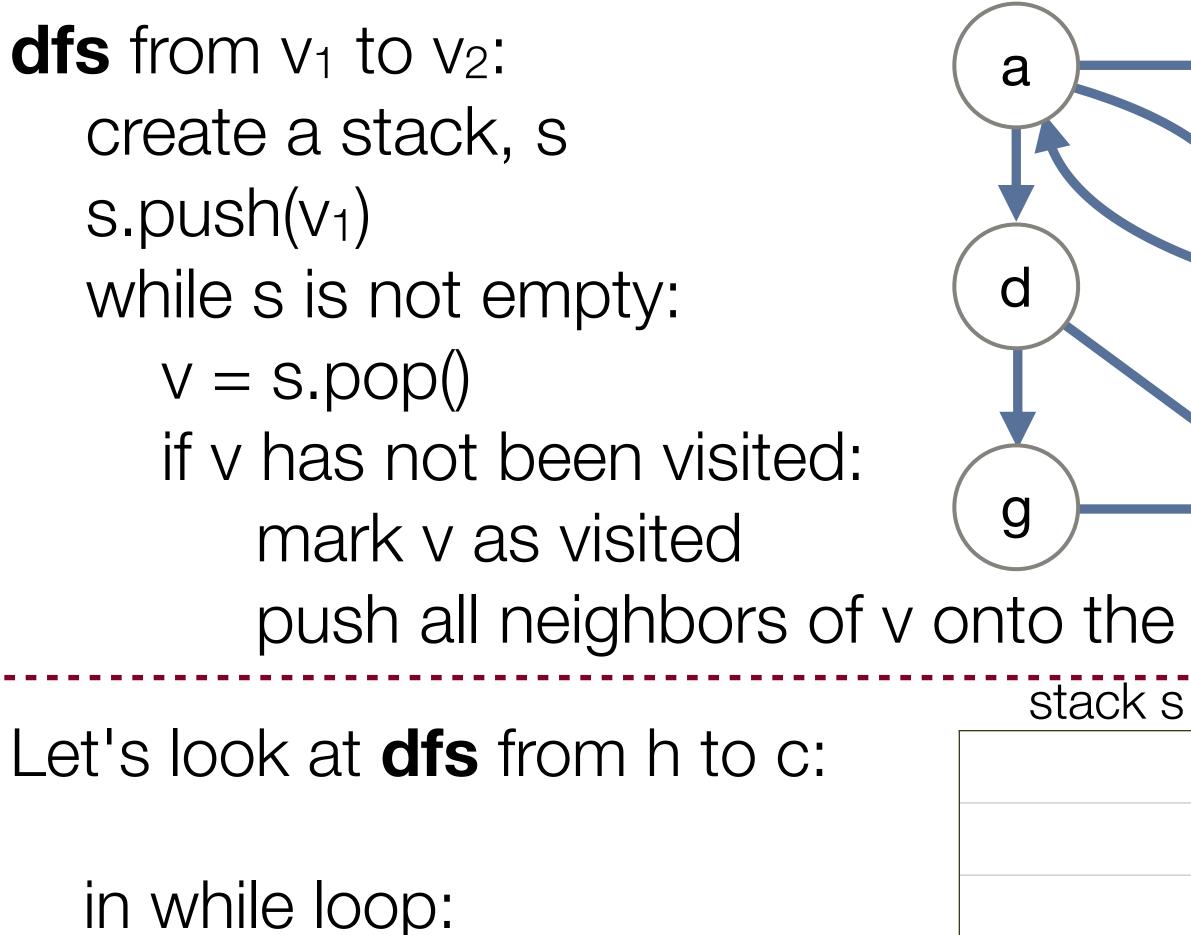
| b c e f | | |
|------------------|--------|----------|
| -h (i) | Verte | ex Map |
| | Vertex | Visited? |
| stack | a | false |
| 5 | b | false |
| | С | false |
| | d | false |
| | е | false |
| | f | false |
| | g | false |
| | h | true |
| | i | false |







e



push all neighbors of h

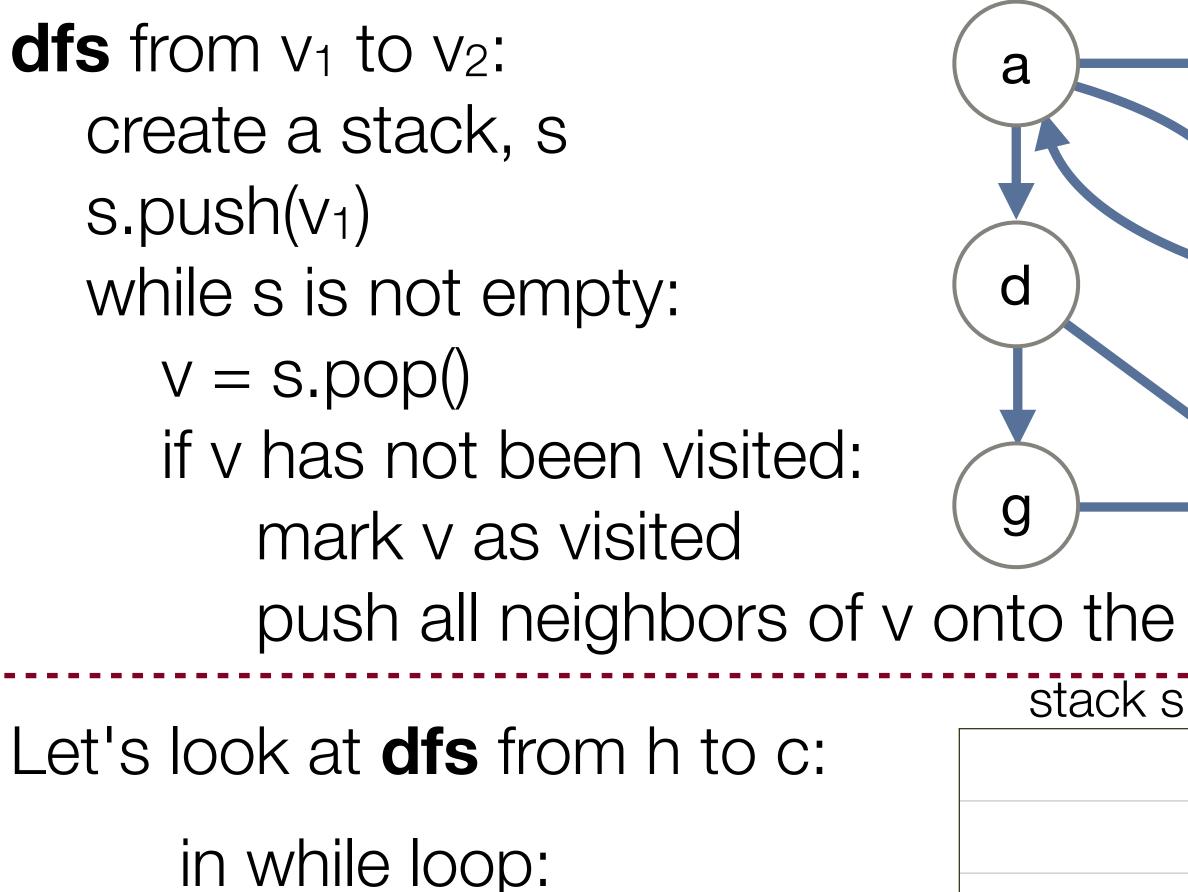
| b c e f | | |
|------------------|--------|----------|
| -h (i) | Verte | ex Map |
| | Vertex | Visited? |
| stack | a | false |
| 5 | b | false |
| | С | false |
| | d | false |
| | е | false |
| | f | false |
| | g | false |
| | h | true |
| | i | false |







e



V = S.pop()

V: f

| b c e f | | |
|------------|--------|----------|
| -h (i) | Verte | ex Map |
| | Vertex | Visited? |
| stack | a | false |
| | b | false |
| | С | false |
| | d | false |
| | е | false |
| | f | true |
| | g | false |
| | h | true |
| | i | false |

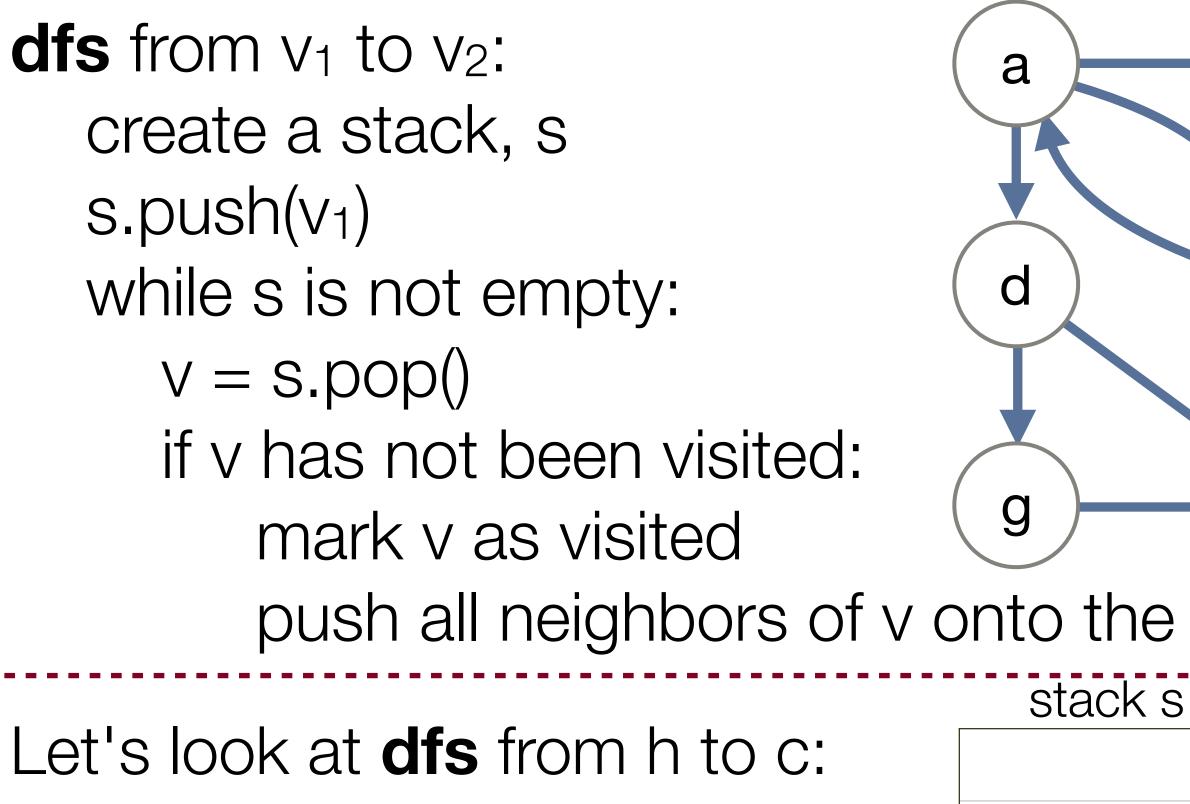






С

e



in while loop: push all neighbors of f

| b c e f | | |
|------------|--------|----------|
| -h (i) | Verte | ex Map |
| | Vertex | Visited? |
| stack | a | false |
| | b | false |
| | С | false |
| | d | false |
| | е | false |
| | f | true |
| | g | false |
| | h | true |
| | i | false |

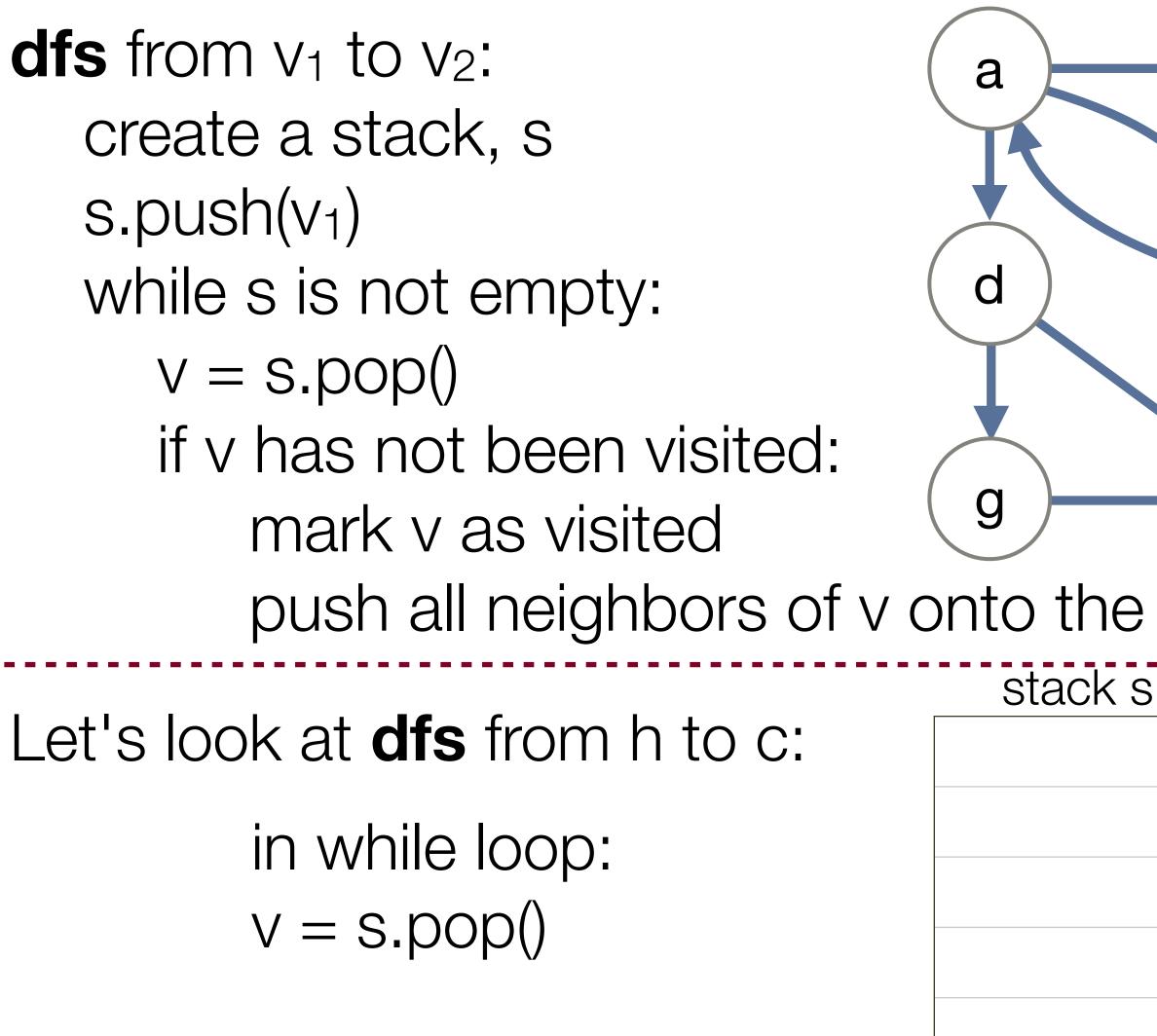






С

e



V: C found — stop!

| b c e f | | |
|------------------|--------|----------|
| | Verte | ex Map |
| | Vertex | Visited? |
| stack | a | false |
| 5 | b | false |
| | С | false |
| | d | false |
| | е | false |
| | f | true |
| | g | false |
| | h | true |
| | | false |





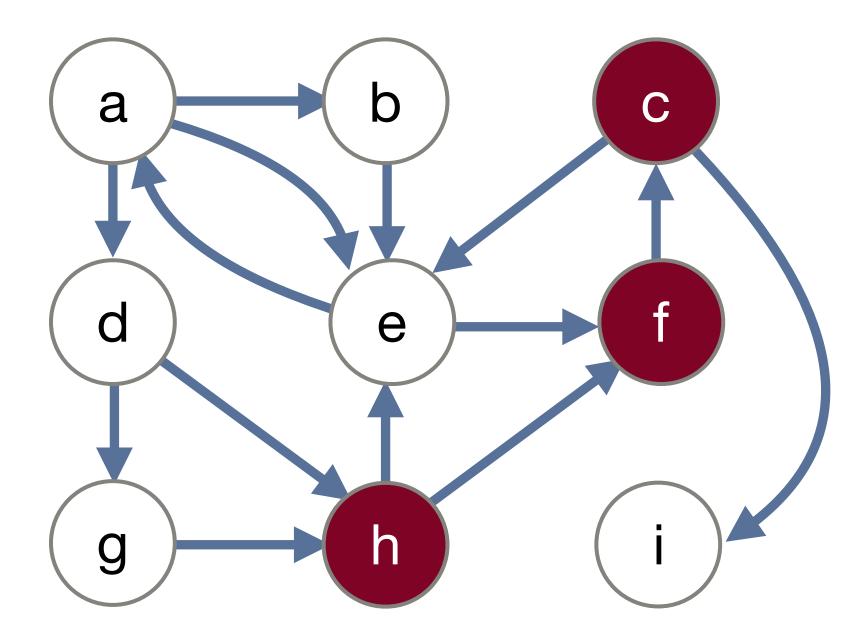


Depth First Search (DFS)

Both the recursive and iterative solutions to DFS were correct, but because of the subtle differences in recursion versus using a stack, they traverse the nodes in a different order.

For the h to c example, the iterative solution happened to be faster, but for different graphs the recursive solution may have been faster.

To retrieve the DFS path found, pass a collection parameter to each cell (if recursive) and chooseexplore-unchoose (our old friend, recursive backtracking!)

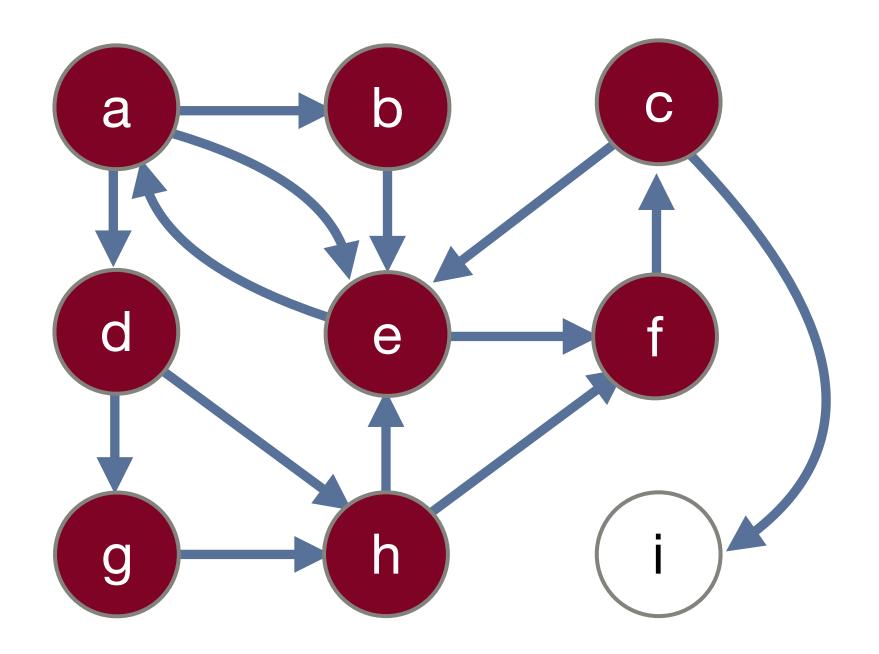


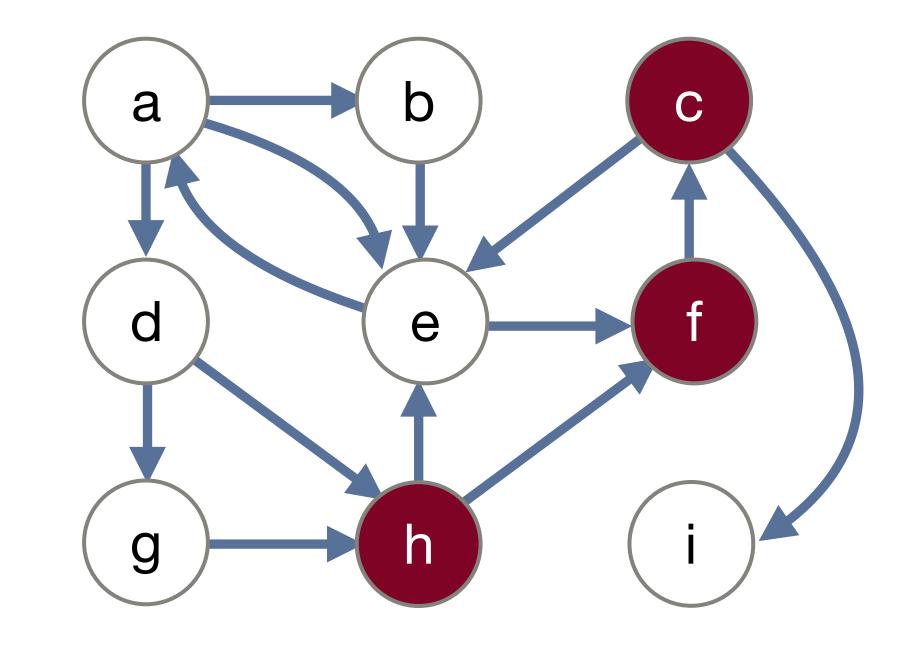


Depth First Search (DFS)

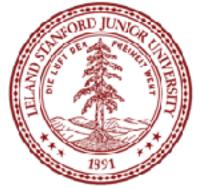
DFS is guaranteed to find a path if one exists.

It is not guaranteed to find the best or shortest path! (i.e., it is not optimal)



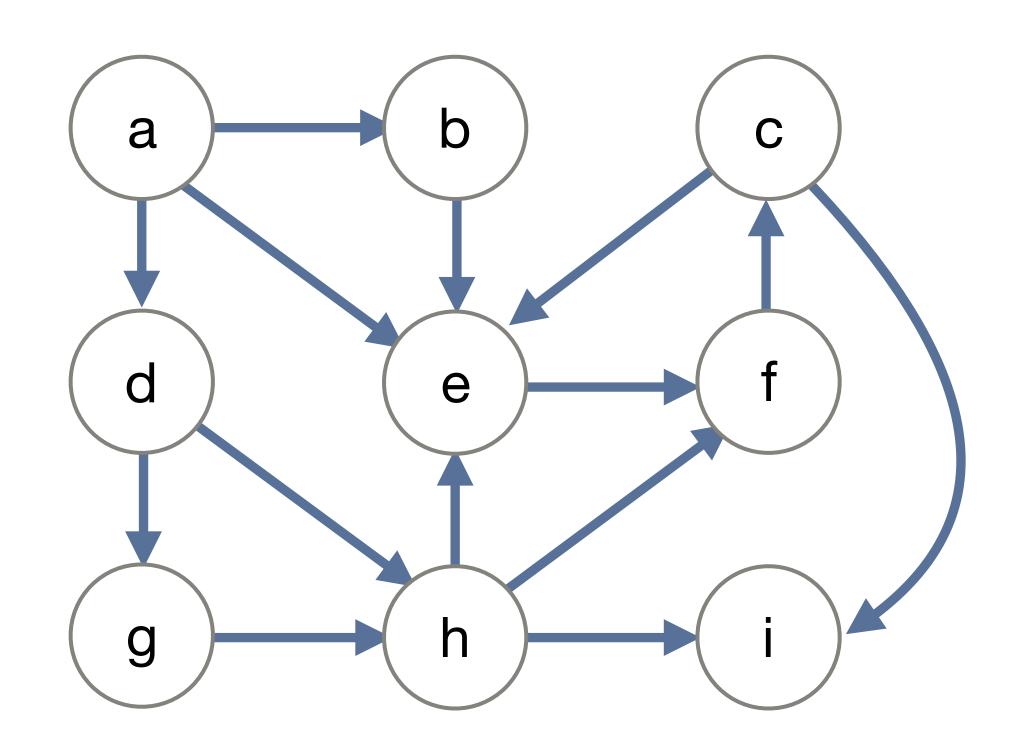


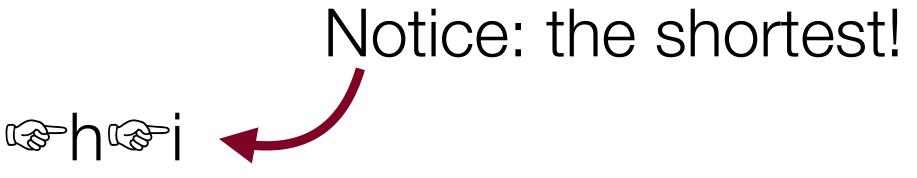




Breadth First Search (BFS)

- From the start vertex, explore the neighbor nodes first, before moving to the next level neighbors.
- This isn't easy to implement recursively. The iterative algorithm is very similar to the DFS iterative, except that we use a queue.
- BFS from a to i (assuming a-z order) visits:
- a aræb neighbors of a arsod Sr∞−6 a Cond Cond acet path: a@d@h@i aradrahra

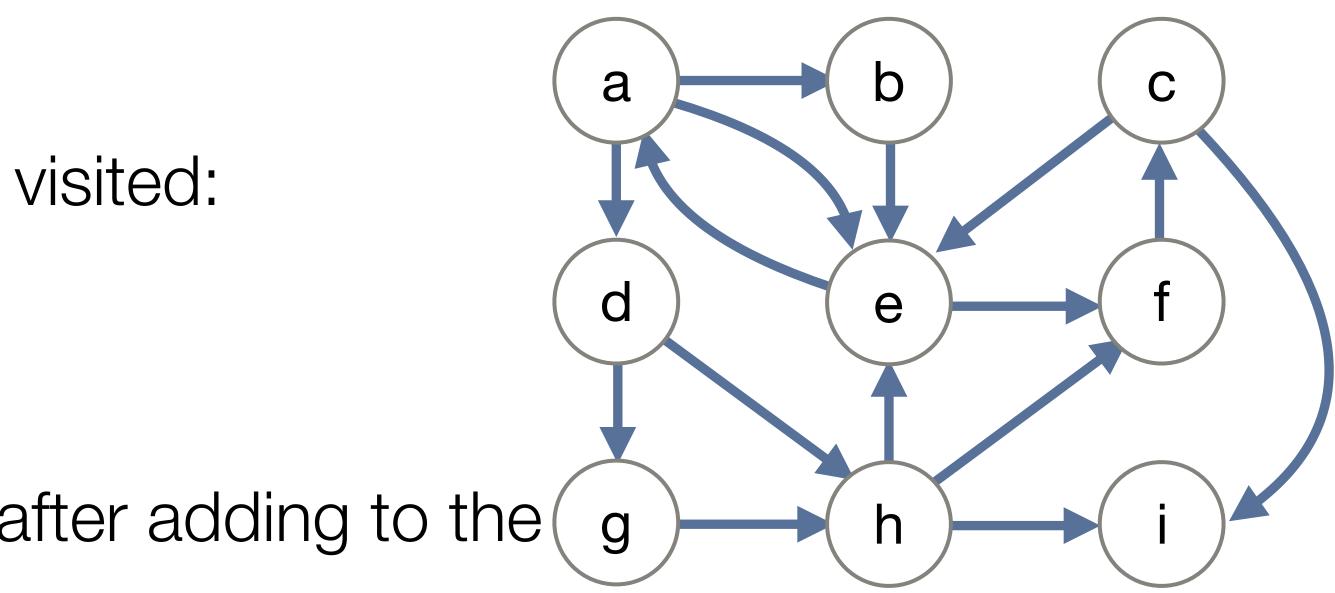






bfs from v_1 to v_2 :

- create a queue of paths (a vector), q q.enqueue(v_1 path)
- while q is not empty and v_2 is not yet visited:
 - path = q.dequeue()
 - v = last element in path
 - mark v as visited
 - if v is the end vertex, we can stop after adding to the current path.
 - for each unvisited neighbor of v: make new path with v's neighbor as last element enqueue new path onto q





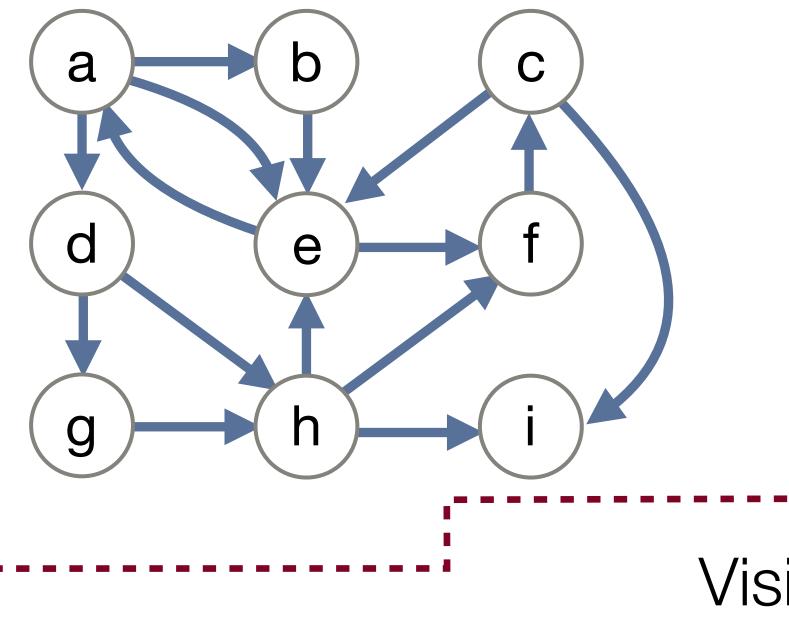


bfs from v1 to v2: create a queue of paths (a vector), q q.enqueue(v1 path) while q is not empty and v2 is not yet visited: path = q.dequeue() v = last element in path mark v as visited for each unvisited neighbor of v: make new path with v as last element enqueue new path onto q

Let's look at **bfs** from a to i:

| | | | | | front |
|--------|--|--|--|--|-------|
| queue. | | | | | а |

Vector<Vertex *> startPath startPath.add(a) q.enqueue(startPath)

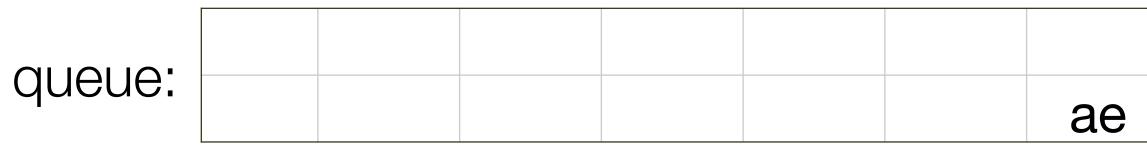


Visited Set: (empty)



bfs from v1 to v2: create a queue of paths (a vector), q q.enqueue(v1 path) while q is not empty and v2 is not yet visited: path = q.dequeue() v = last element in path mark v as visited for each unvisited neighbor of v: make new path with v's neighbor as last element enqueue new path onto q

Let's look at **bfs** from a to i:



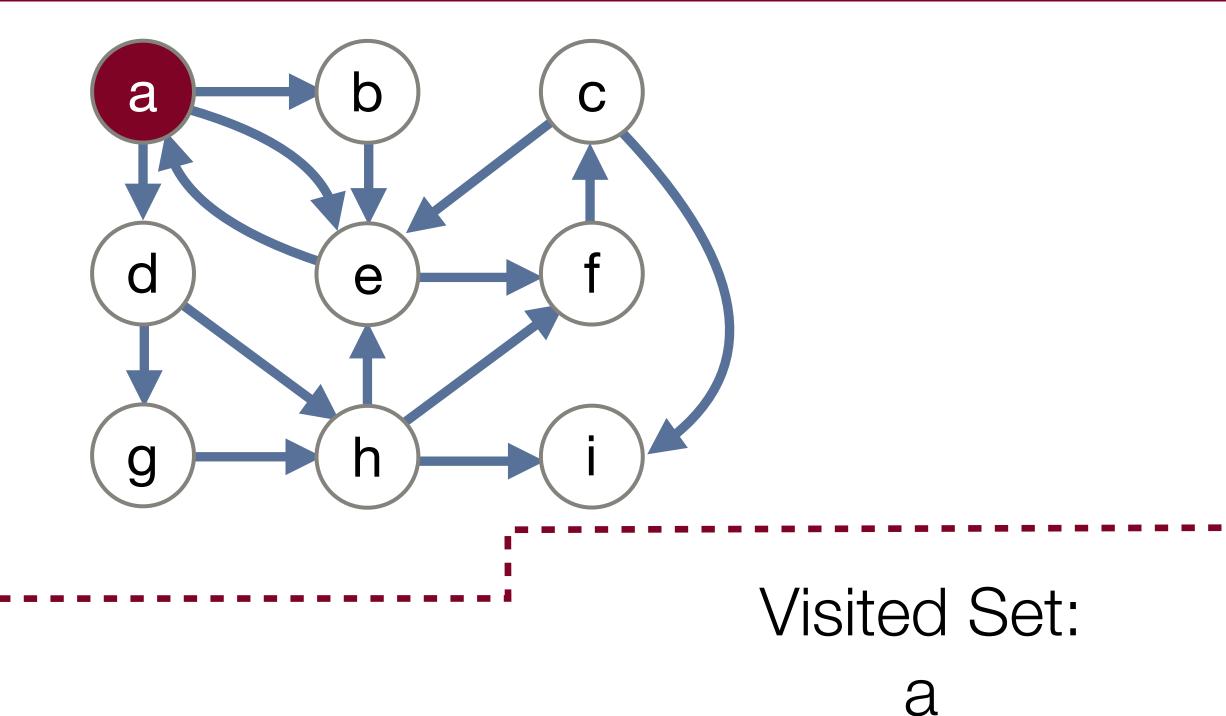
in while loop:

curPath = q.dequeue() (path is a)

v = last element in curPath (v is a)

mark v as visited

enqueue all unvisited neighbor paths onto q

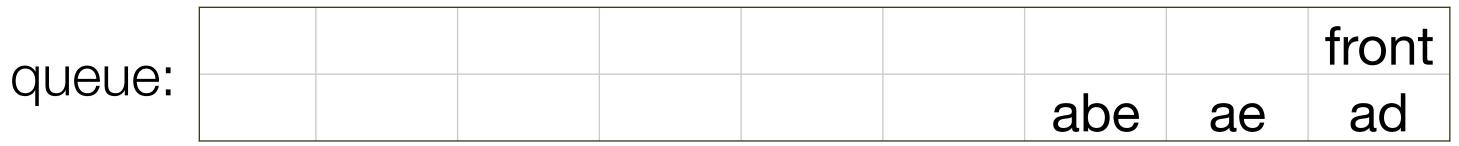


| | | front |
|---|---|-------|
| a | d | ab |



bfs from v1 to v2: create a queue of paths (a vector), q q.enqueue(v1 path) while q is not empty and v2 is not yet visited: path = q.dequeue() v = last element in path mark v as visited for each unvisited neighbor of v: make new path with v's neighbor as last element enqueue new path onto q

Let's look at **bfs** from a to i:



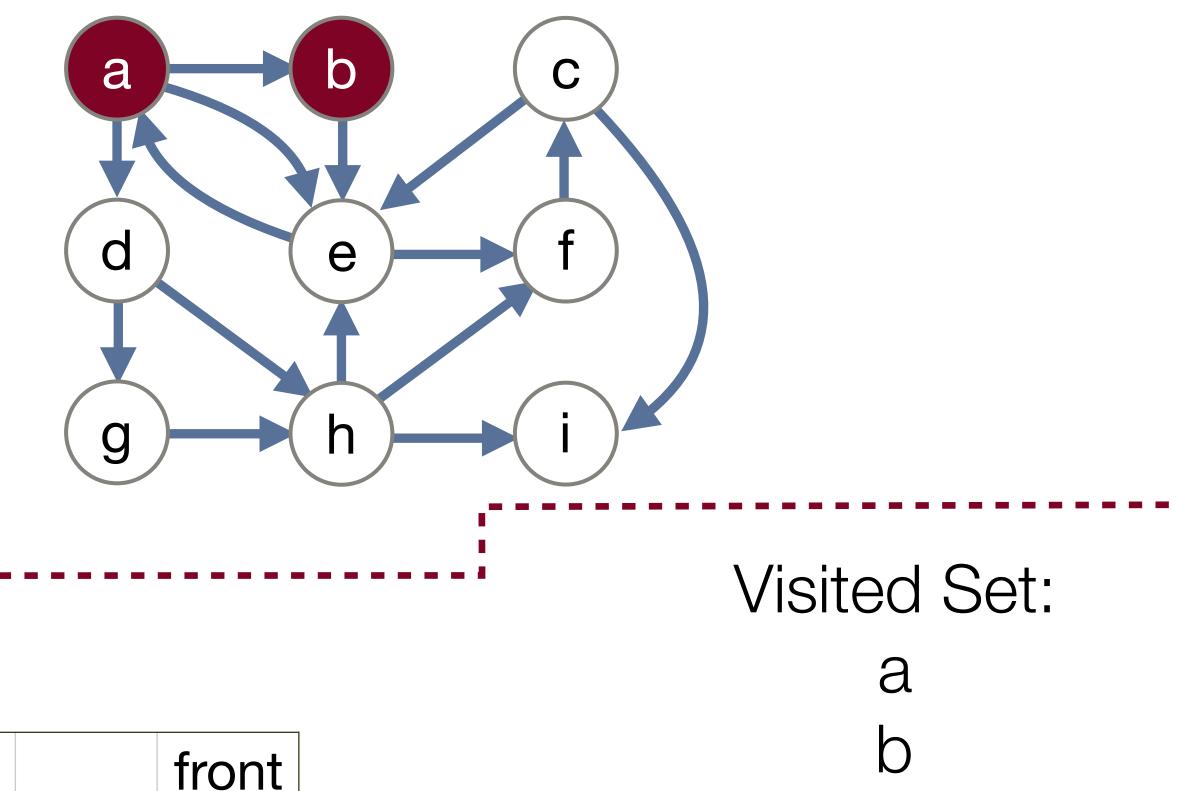
in while loop:

curPath = q.dequeue() (path is ab)

v = last element in curPath (v is b)

mark v as visited

enqueue all unvisited neighbor paths onto q





bfs from v1 to v2: create a queue of paths (a vector), q q.enqueue(v1 path) while q is not empty and v2 is not yet visited: path = q.dequeue() v = last element in path mark v as visited for each unvisited neighbor of v: make new path with v's neighbor as last element enqueue new path onto q

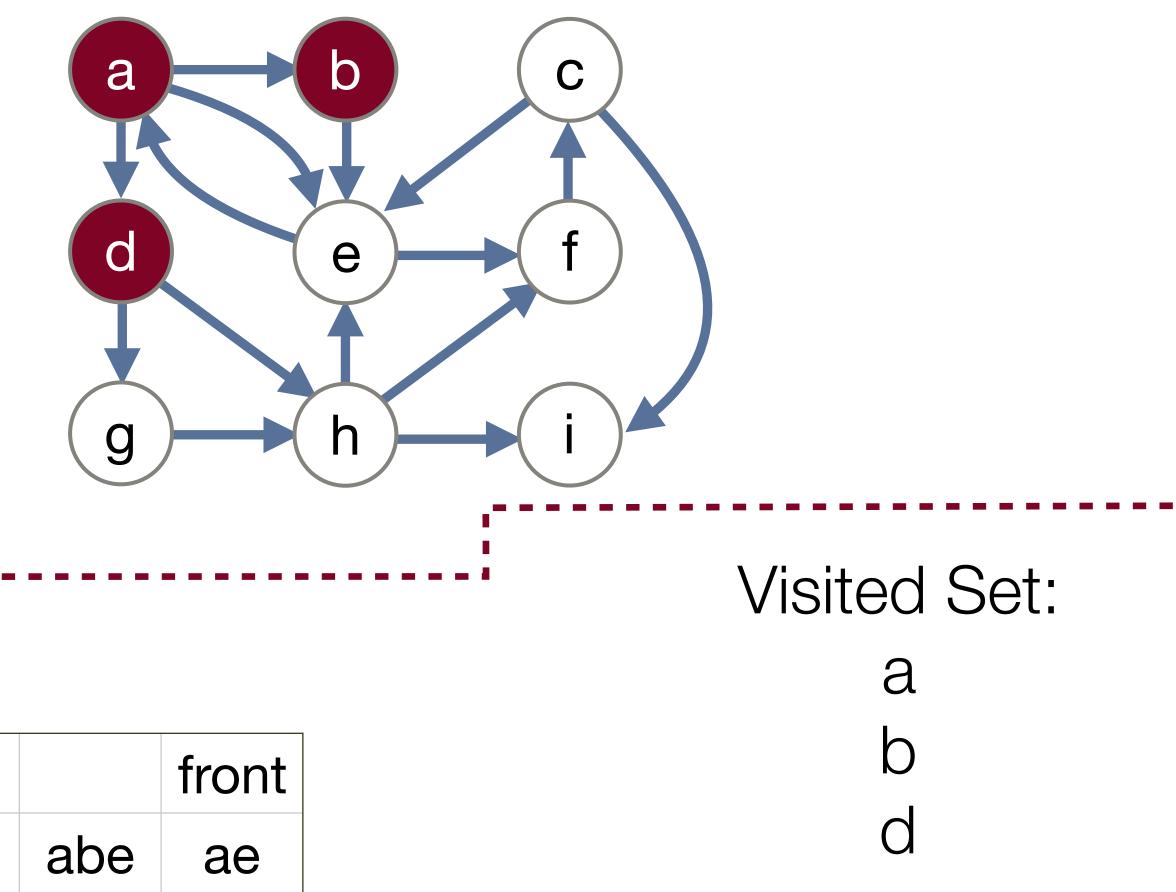
Let's look at **bfs** from a to i:

| queue: | | | adh | adg |
|--------|--|--|-----|-----|

in while loop:

curPath = q.dequeue() (path is ad)

- v = last element in curPath (v is d)
- mark v as visited
- enqueue all unvisited neighbor paths onto q





bfs from v1 to v2: create a queue of paths (a vector), q q.enqueue(v1 path) while q is not empty and v2 is not yet visited: path = q.dequeue() v = last element in path mark v as visited for each unvisited neighbor of v: make new path with v's neighbor as last element enqueue new path onto q

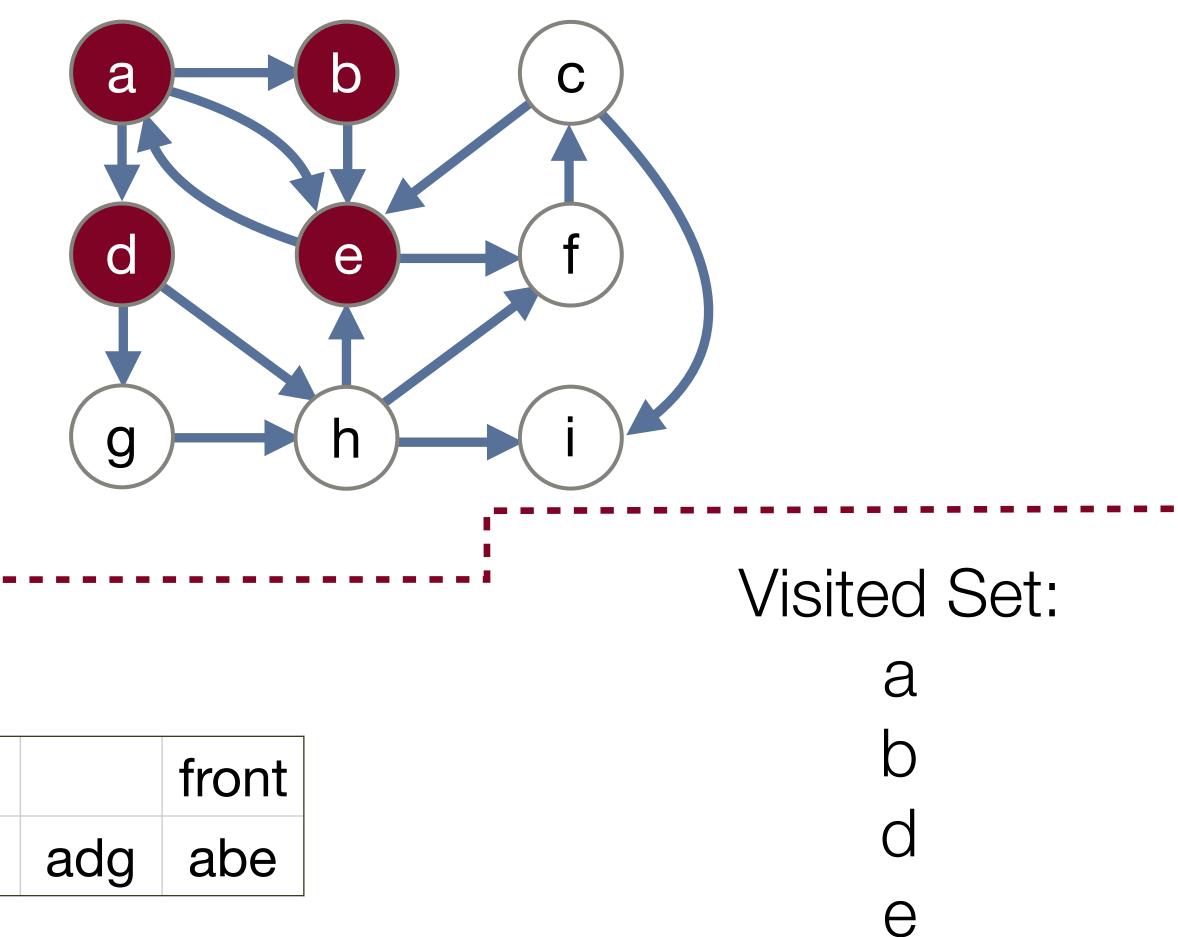
Let's look at **bfs** from a to i:

| queue: | | | aef | adh |
|--------|--|--|-----|-----|

in while loop:

curPath = q.dequeue() (path is ae)

- v = last element in curPath (v is e)
- mark v as visited
- enqueue all unvisited neighbor paths onto q





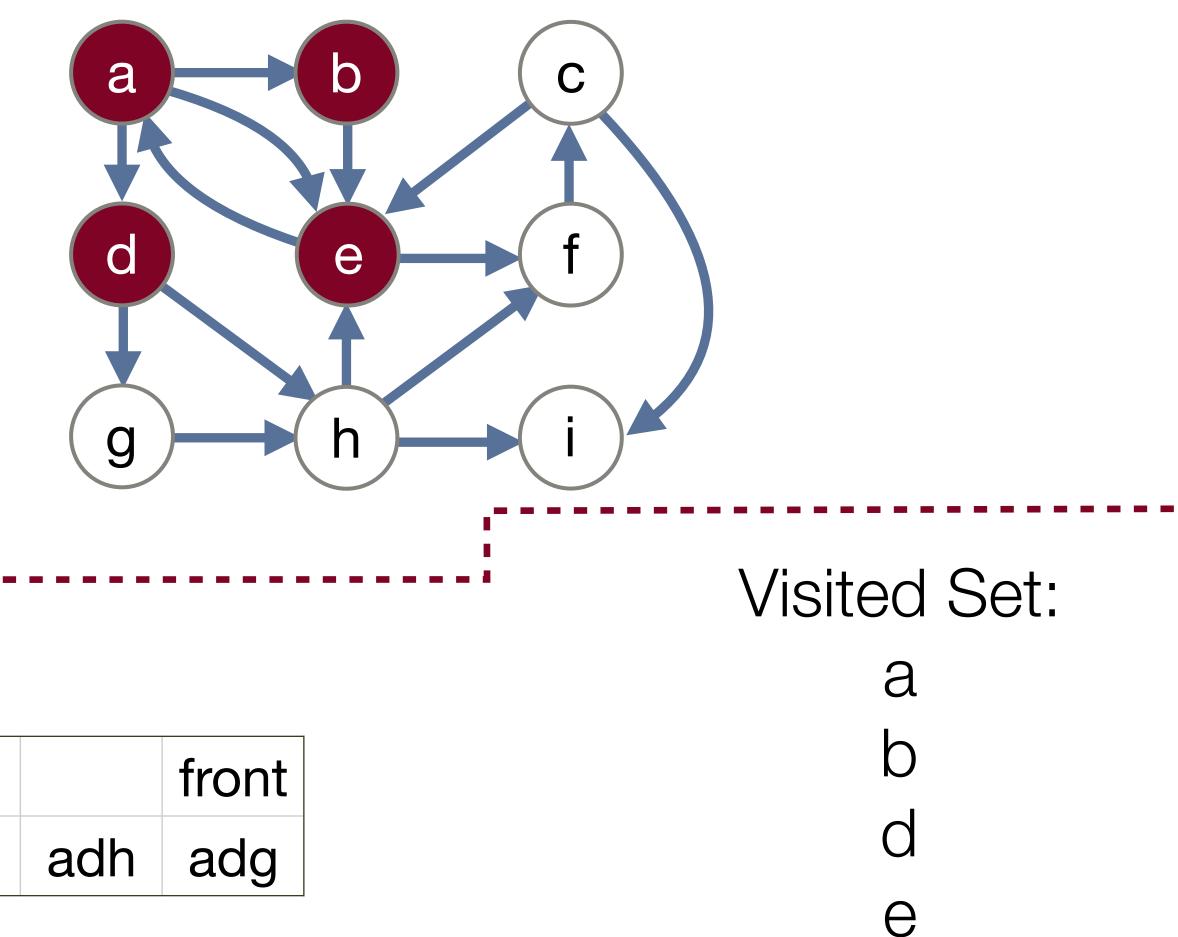
bfs from v1 to v2: create a queue of paths (a vector), q q.enqueue(v1 path) while q is not empty and v2 is not yet visited: path = q.dequeue() v = last element in path mark v as visited for each unvisited neighbor of v: make new path with v's neighbor as last element enqueue new path onto q

Let's look at **bfs** from a to i:

| queue: | | | abef | aef |
|--------|--|--|------|-----|

in while loop:

curPath = q.dequeue() (path is abe)
v = last element in curPath (v is e)
mark v as visited (already been marked)
enqueue all unvisited neighbor paths onto q





bfs from v1 to v2: create a queue of paths (a vector), q q.enqueue(v1 path) while q is not empty and v2 is not yet visited: path = q.dequeue() v = last element in path mark v as visited for each unvisited neighbor of v: make new path with v's neighbor as last element enqueue new path onto q

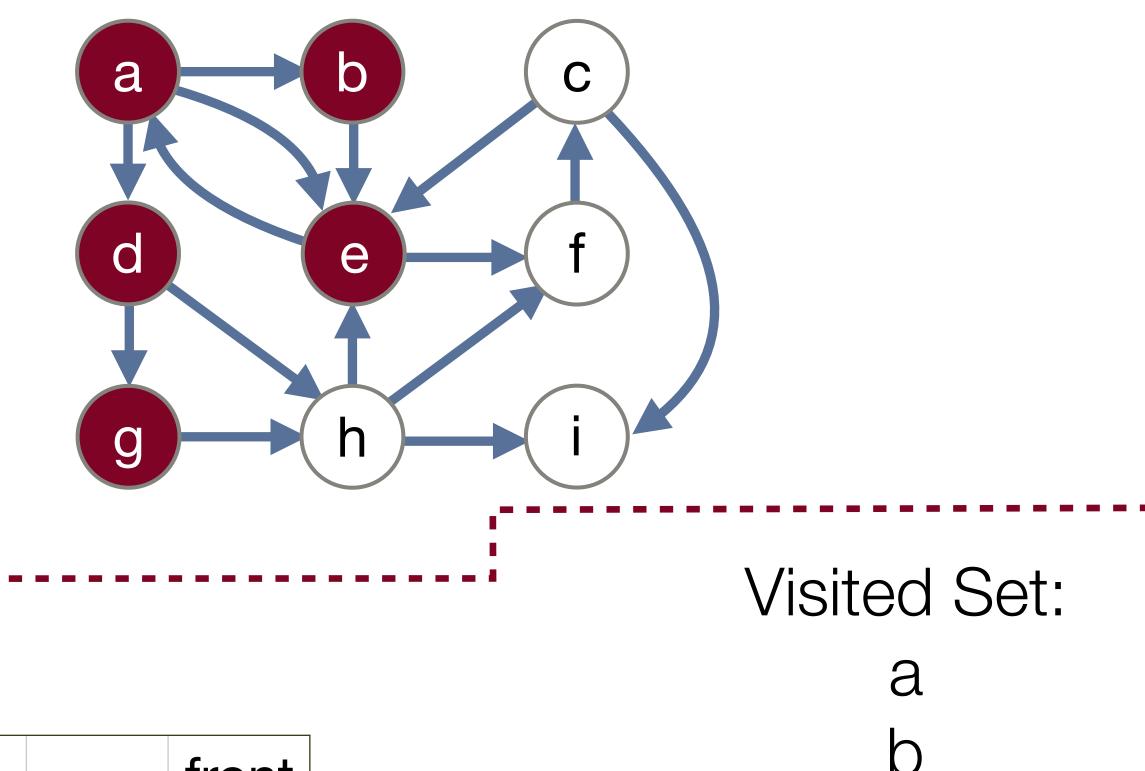
Let's look at **bfs** from a to i:

| | | | | | | front |
|--------|--|--|------|------|-----|-------|
| queue: | | | adgh | abef | aef | adh |

in while loop:

curPath = q.dequeue() (path is adg)

- v = last element in curPath (v is g)
- mark v as visited
- enqueue all unvisited neighbor paths onto q



TELAND

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bfs from v1 to v2: create a queue of paths (a vector), q q.enqueue(v1 path) while q is not empty and v2 is not yet visited: path = q.dequeue() v = last element in path mark v as visited for each unvisited neighbor of v: make new path with v's neighbor as last element enqueue new path onto q

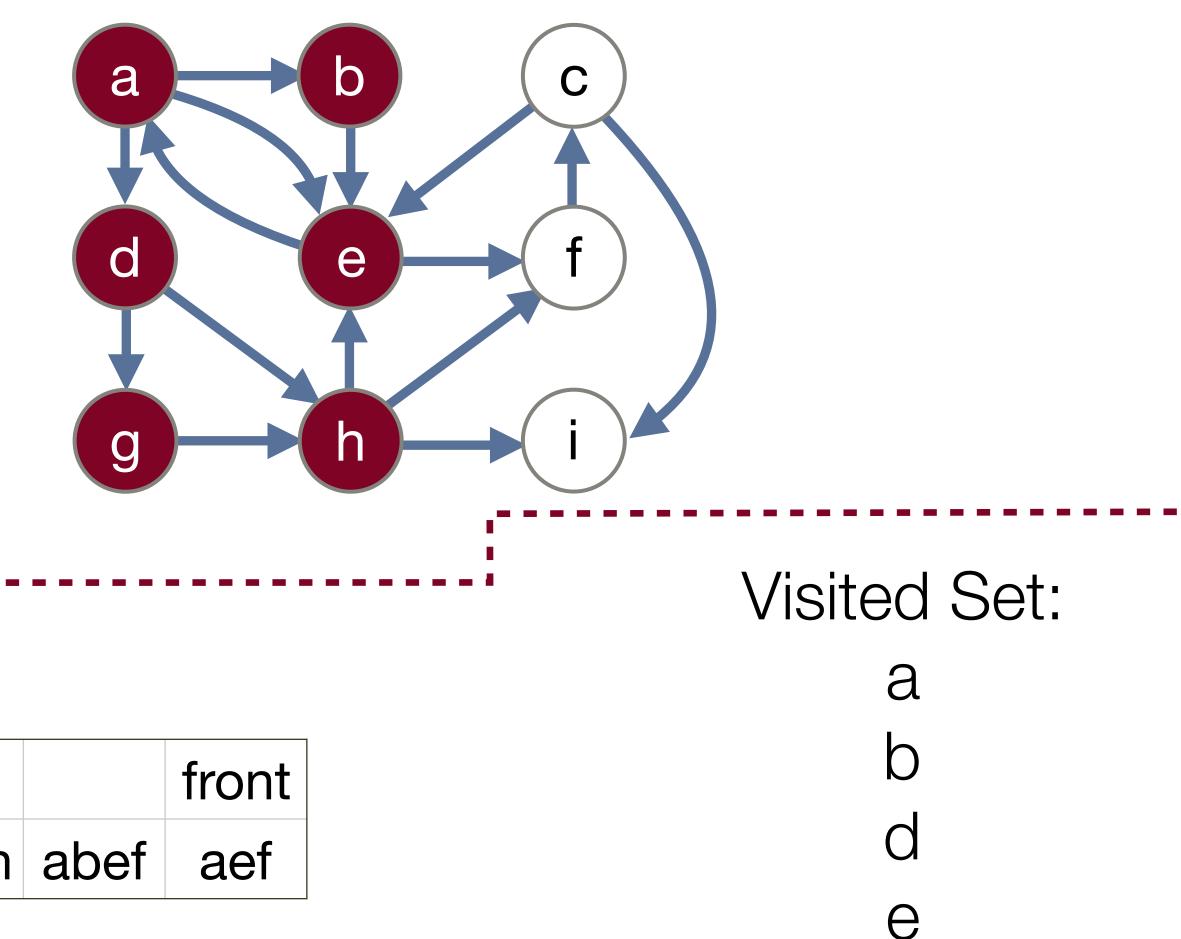
Let's look at **bfs** from a to i:

| queue: | | | adhi | adhf | adgh |
|--------|--|--|------|------|------|

in while loop:

curPath = q.dequeue() (path is adh)

- v = last element in curPath (v is h)
- mark v as visited
- enqueue all unvisited neighbor paths onto q



TELAND



bfs from v1 to v2: create a queue of paths (a vector), q q.enqueue(v1 path) while q is not empty and v2 is not yet visited: path = q.dequeue() v = last element in path mark v as visited for each unvisited neighbor of v: make new path with v's neighbor as last element enqueue new path onto q

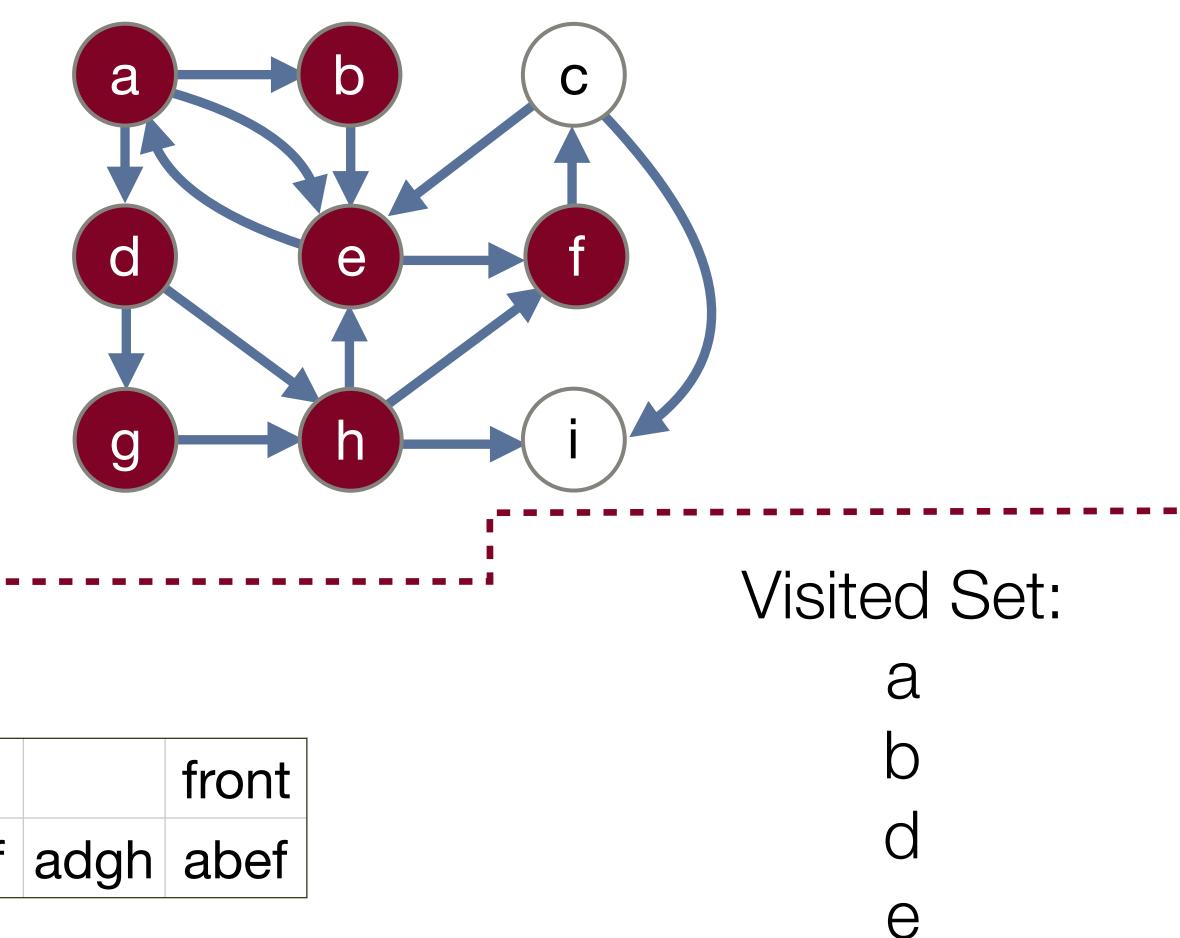
Let's look at **bfs** from a to i:

| queue: | | | aefc | adhi | adhf |
|--------|--|--|------|------|------|

in while loop:

curPath = q.dequeue() (path is aef)

- v = last element in curPath (v is f)
- mark v as visited
- enqueue all unvisited neighbor paths onto q





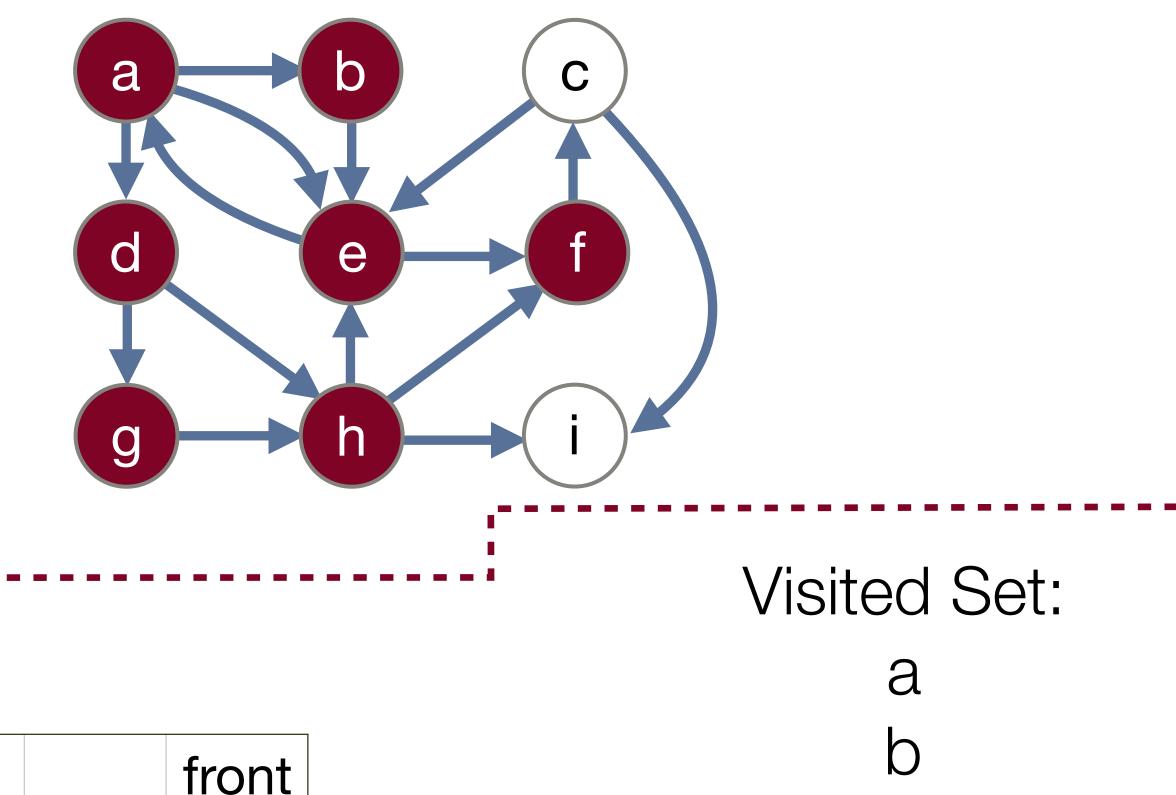
bfs from v1 to v2: create a queue of paths (a vector), q q.enqueue(v1 path) while q is not empty and v2 is not yet visited: path = q.dequeue() v = last element in path mark v as visited for each unvisited neighbor of v: make new path with v's neighbor as last element enqueue new path onto q

Let's look at **bfs** from a to i:

| | | | | | | | front |
|--------|--|--|-------|------|------|------|-------|
| queue: | | | abefc | aefc | adhi | adhf | adgh |

in while loop:

curPath = q.dequeue() (path is abef)
v = last element in curPath (v is f)
mark v as visited (already been marked)
enqueue all unvisited neighbor paths onto q



b d e f



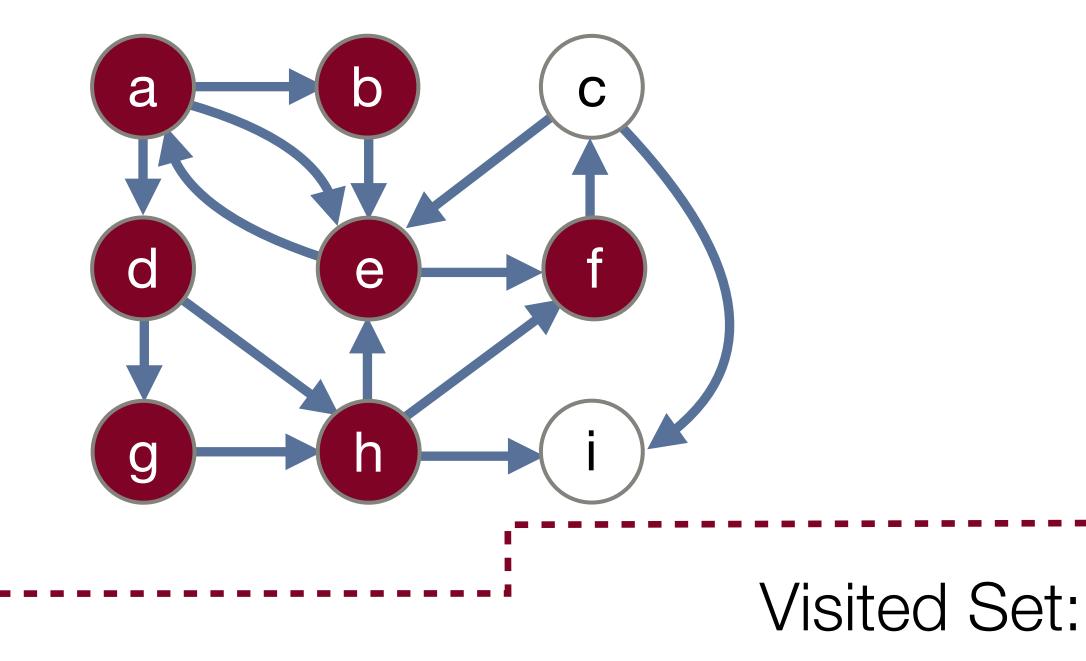
bfs from v1 to v2: create a queue of paths (a vector), q q.enqueue(v1 path) while q is not empty and v2 is not yet visited: path = q.dequeue() v = last element in path mark v as visited for each unvisited neighbor of v: make new path with v's neighbor as last element enqueue new path onto q

Let's look at **bfs** from a to i:

| | | | | | | | front |
|--------|--|--|-------|-------|------|------|-------|
| queue: | | | adghi | abefc | aefc | adhi | adhf |

in while loop:

curPath = q.dequeue() (path is adgh)
v = last element in curPath (v is h)
mark v as visited (already been marked)
enqueue all unvisited neighbor paths onto q



а

D

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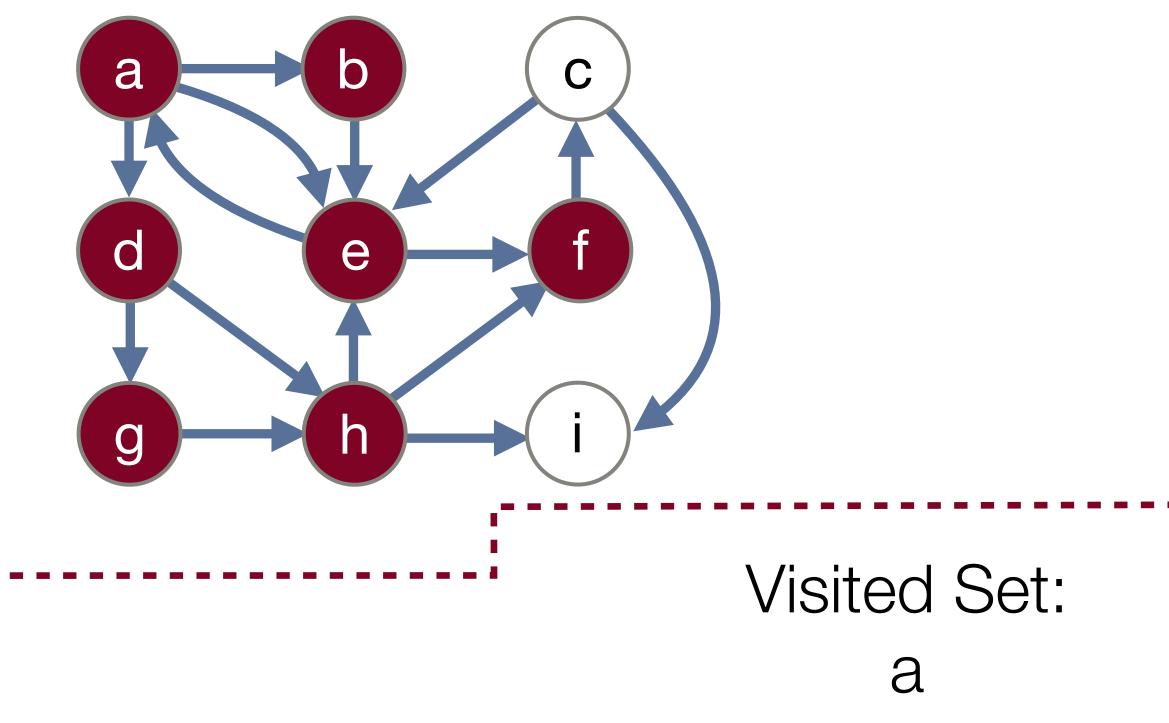
bfs from v1 to v2: create a queue of paths (a vector), q q.enqueue(v1 path) while q is not empty and v2 is not yet visited: path = q.dequeue() v = last element in path mark v as visited for each unvisited neighbor of v: make new path with v's neighbor as last element enqueue new path onto q

Let's look at **bfs** from a to i:

| | | | | | | | front |
|--------|--|--|-------|-------|-------|------|-------|
| queue: | | | adhfc | adghi | abefc | aefc | adhi |

in while loop:

curPath = q.dequeue() (path is adhf)
v = last element in curPath (v is f)
mark v as visited (already been marked)
enqueue all unvisited neighbor paths onto q



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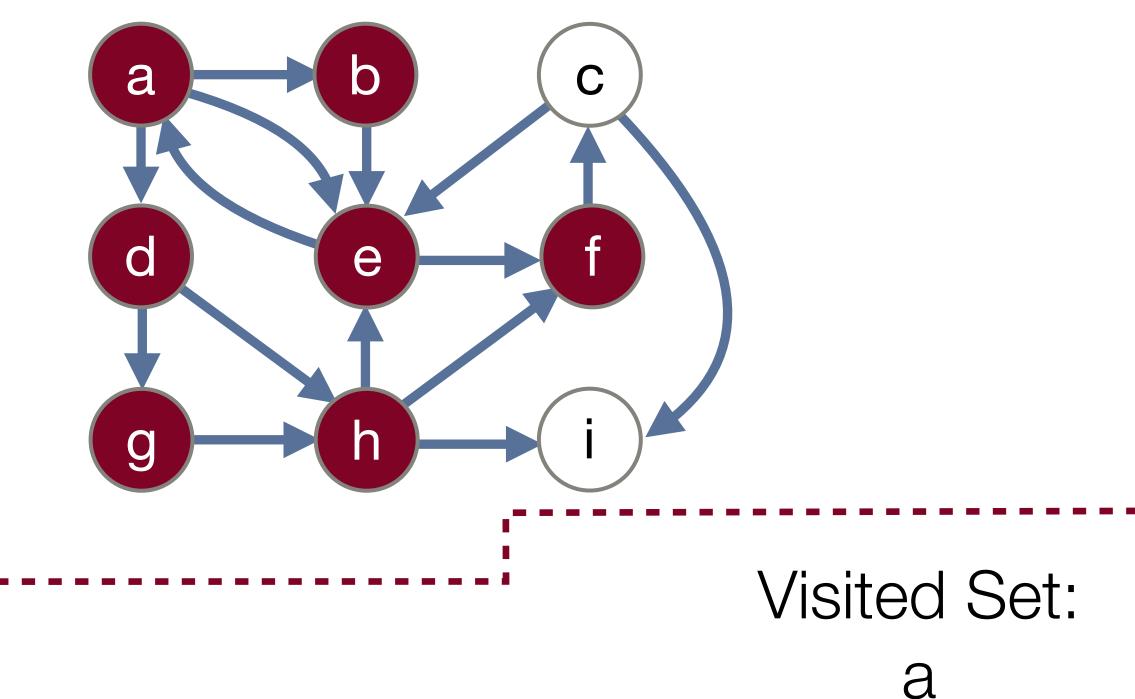


bfs from v1 to v2: create a queue of paths (a vector), q q.enqueue(v1 path) while q is not empty and v2 is not yet visited: path = q.dequeue() v = last element in path mark v as visited for each unvisited neighbor of v: make new path with v's neighbor as last element enqueue new path onto q

Let's look at **bfs** from a to i:

| | | | | | | | front |
|--------|--|--|-------|-------|-------|------|-------|
| queue: | | | adhfc | adghi | abefc | aefc | adhi |

in while loop: curPath = q.dequeue() (path is adhi) v = last element in curPath (v is i) found!



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Wikipedia: Getting to Philosophy



So I downloaded Wikipedia...

It turns out that you can download Wikipedia, but it is > 10 Terabytes (!) uncompressed. The reason Wikipedia asks you for money every so often is because they have lots of fast computers with lots of memory, and this is expensive (so donate!)

But, the Internet is just a graph...so, Wikipedia pages are just a graph...let's just do the searching by taking advantage of this: download pages as we need them.





Wikipedia: Getting to Philosophy



What kind of search is the "getting to philosophy" algorithm? "Clicking on the first lowercase link in the main text of a Wikipedia article, and then repeating the process for subsequent articles, usually eventually gets one to the Philosophy article."

This is a depth-first search! To determine if a Wikipedia article will get to Philosophy, we just select the first link each time. If we ever have to select a second link (or if a first-link refers to a visited vertex), then that article doesn't get to Philosophy.

WikipediA The Free Encyclopedia



Wikipedia: Getting to Philosophy



WIKIPEDIA The Free Encyclopedia

We can also perform a Breadth First Search, as well. How would this change our search?

A BFS would look at all links on a page, then all links for each link on the page, etc. This has the potential of taking a long time, but it will find a shortest path.





References and Advanced Reading

• References:

- •Depth First Search, Wikipedia: <u>https://en.wikipedia.org/wiki/Depth-first_search</u>
- •Breadth First Search, Wikipedia: <u>https://en.wikipedia.org/wiki/Breadth-first_search</u>

Advanced Reading:

- •Visualizations:
- <u>https://www.cs.usfca.edu/~galles/visualization/DFS.html</u>
- <u>https://www.cs.usfca.edu/~galles/visualization/BFS.html</u>

<u>dia.org/wiki/Depth-first_search</u> edia.org/wiki/Breadth-first_search

<u>'DFS.html</u> 'BFS.html



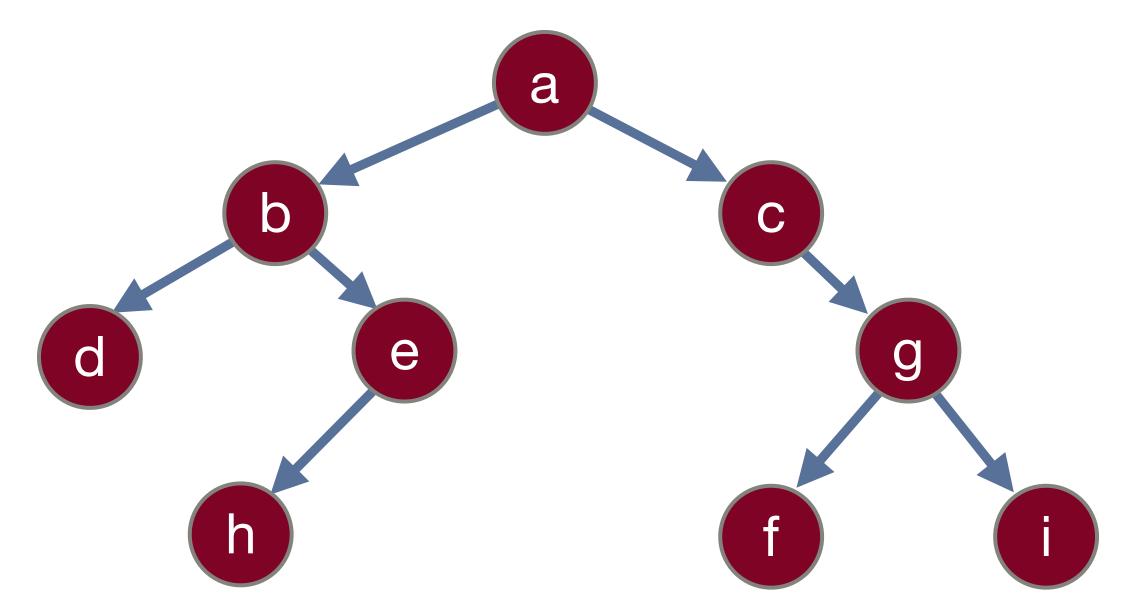


Extra Slides



Breadth First Search (BFS): Tree searching

A Breadth First Search on a tree will produce a "level order traversal":



Breadth First Search: a@b@c@d@e@g@h@f@i

This is necessary if we want to print the tree to the screen in a pretty way, such that it retains its tree-like structure.

