# CS 106B Lecture 19: Trees

Monday, May 14, 2018

Programming Abstractions
Spring 2018
Stanford University
Computer Science Department

Lecturer: Chris Gregg

reading:

Programming Abstractions in C++, Section 16.1





#### Today's Topics

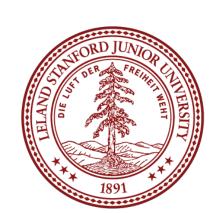
- Logistics
- •See Piazza <u>@661</u> for information about using a stringstream to utilize the << from a PatientNode.
- How do you clear a Vector? (or a heap?)
- Introduction to Trees



## Today's Topics

•How do you clear a Vector? Let's find out...





### Today's Topics

How do you clear a Vector? Let's find out...

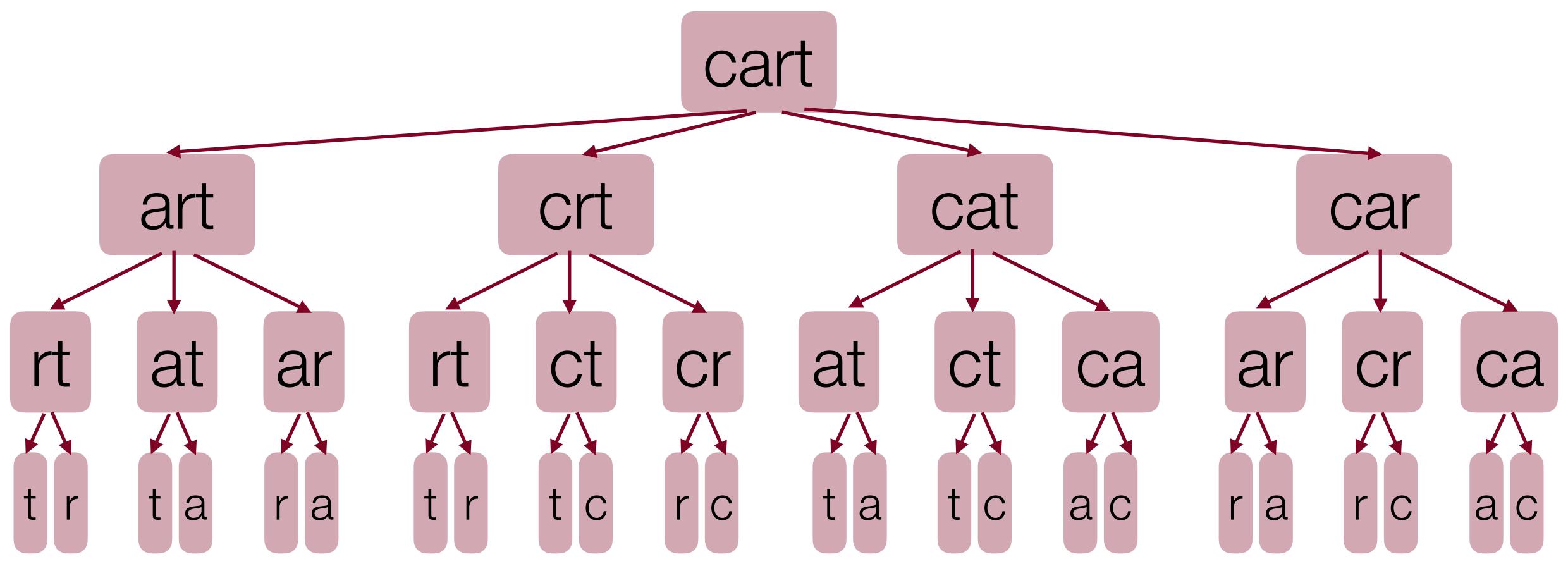


•Because the **count** is what keeps track of the number of elements in our vector, we can simply set that variable to 0, and we now have an empty vector. Yes, the capacity is the same, and yes, the old elements are still there, but they will get overwritten upon further **adds** or **inserts**.



#### Trees

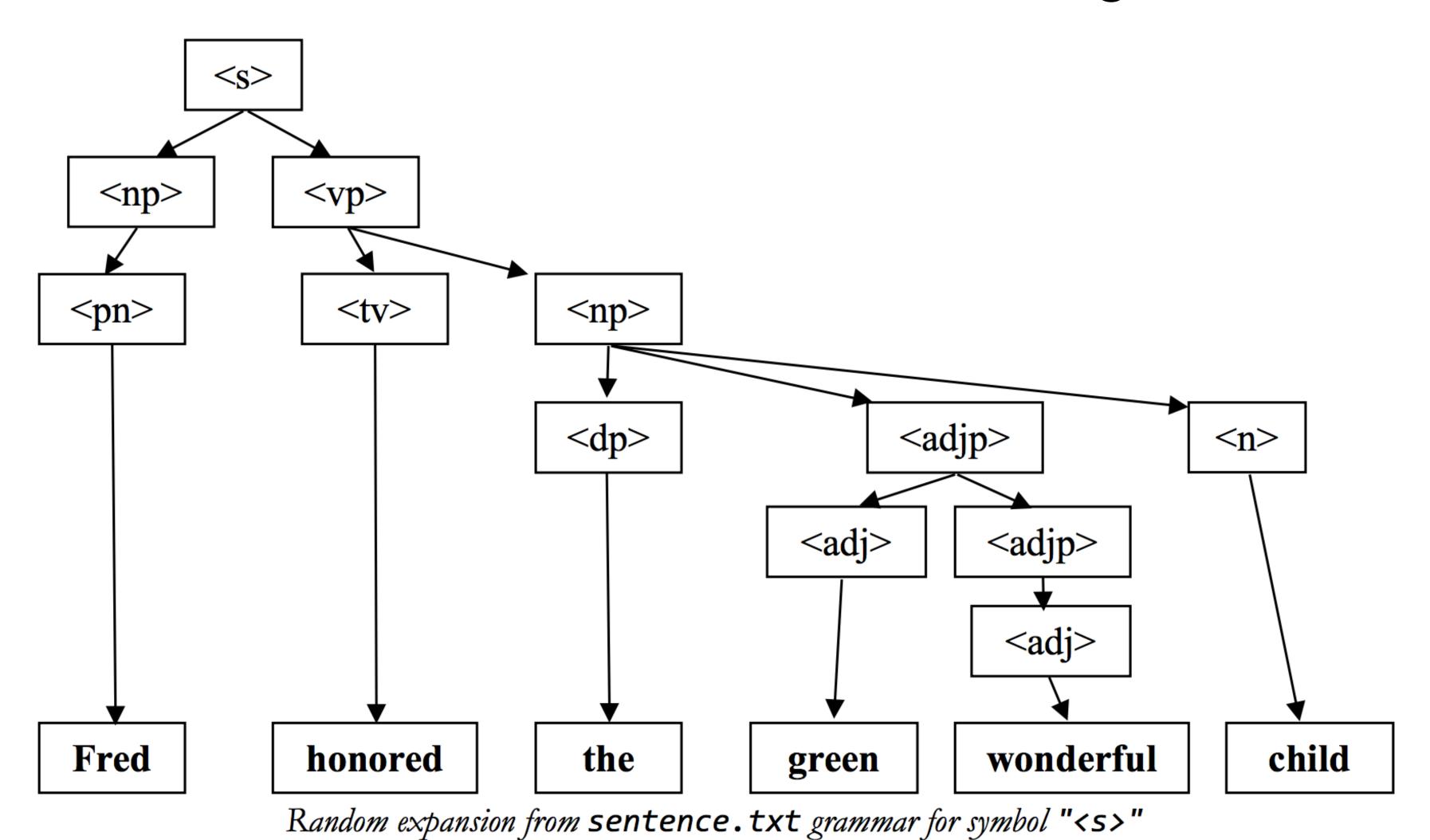
We have already seen trees in the class in the form of decision trees!

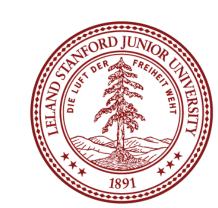




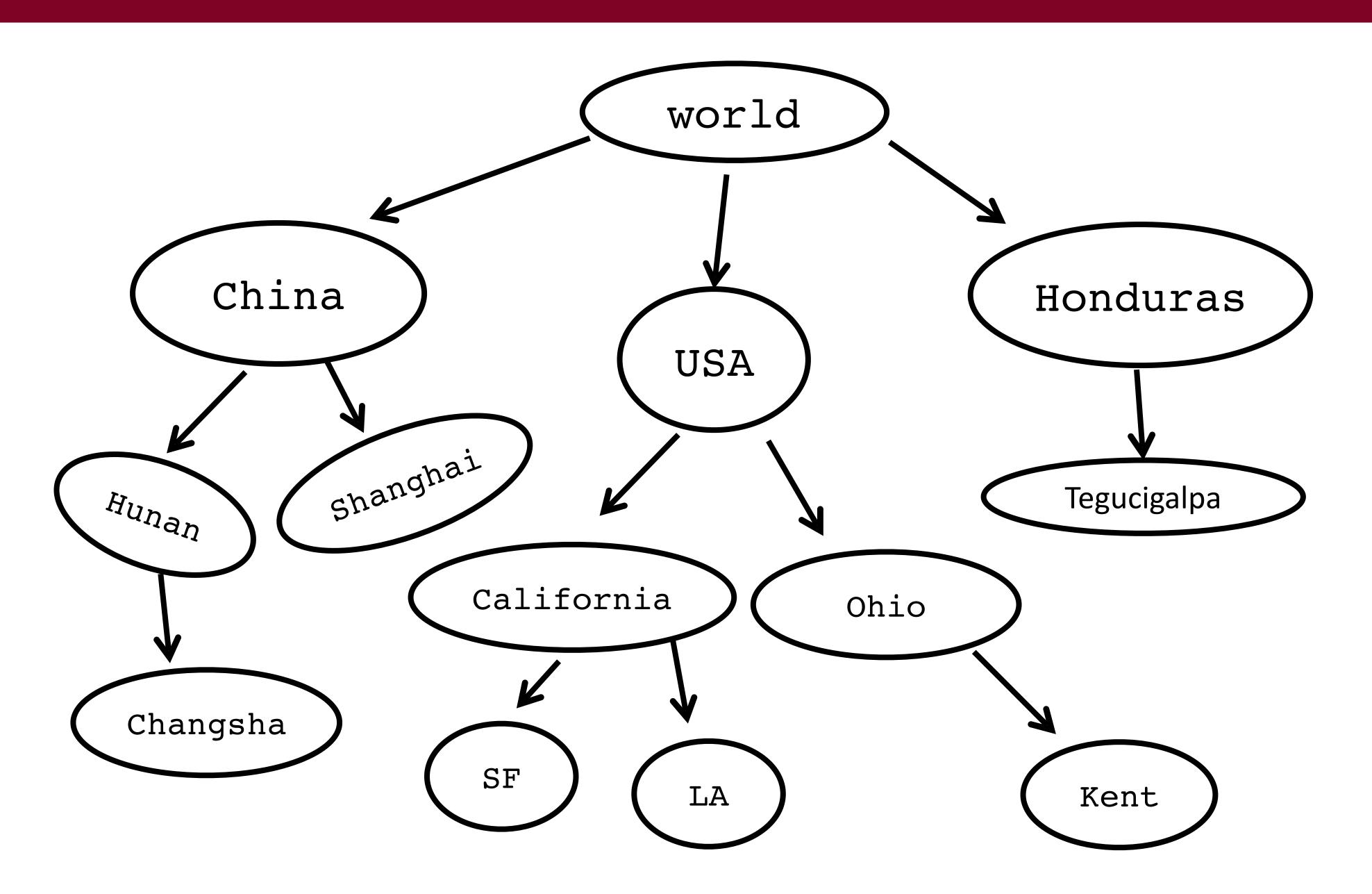
#### Trees

You've coded trees for recursive assignments!



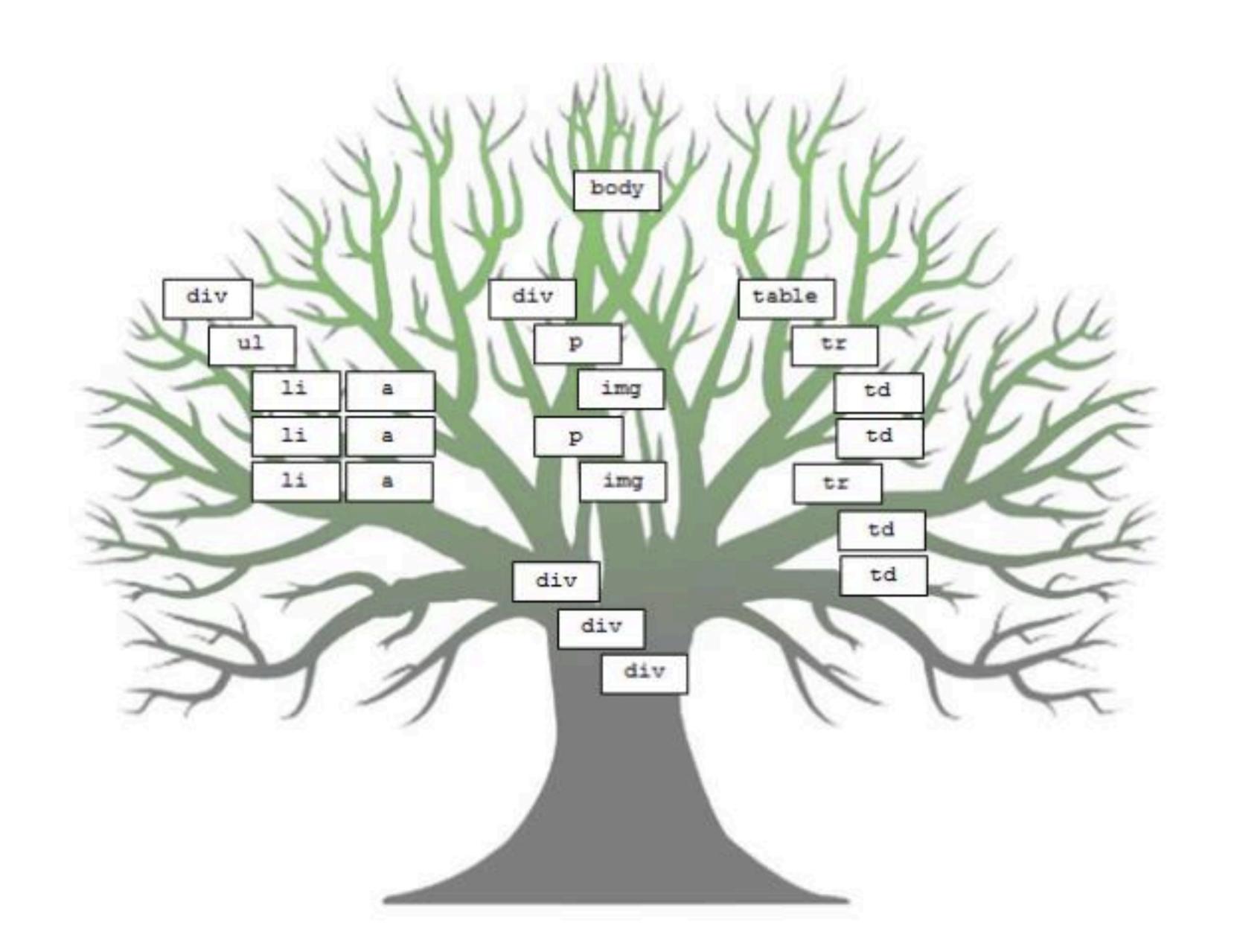


#### Trees Can Describe Hierarchies





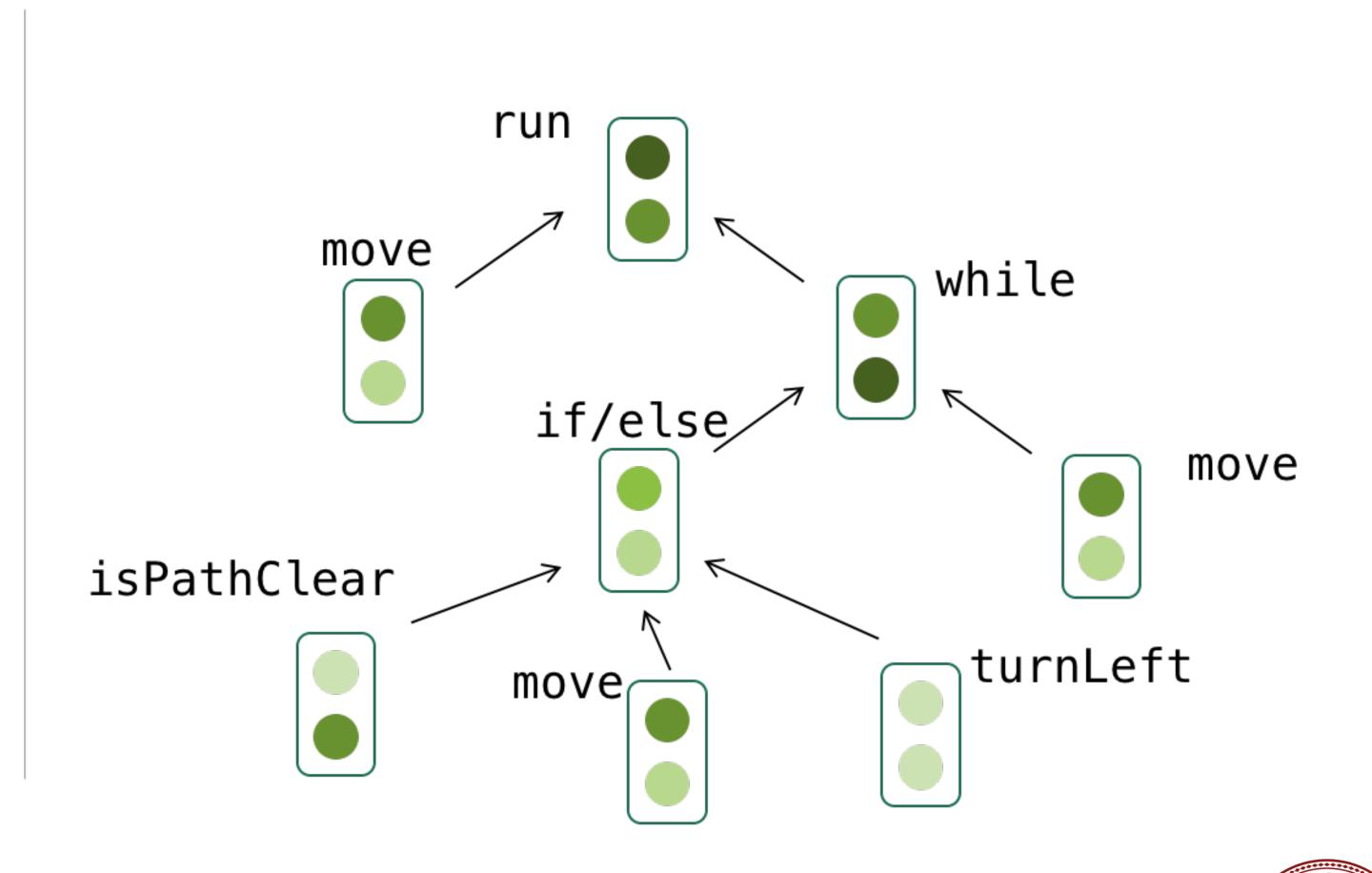
### Trees Can Describe Websites (HTML)





#### Trees Can Describe Programs

```
// Example student solution
function run() {
   // move then loop
   move();
   // the condition is fixed
   while (notFinished()) {
      if (isPathClear()) {
         move();
      } else {
         turnLeft();
      // redundant
      move();
```

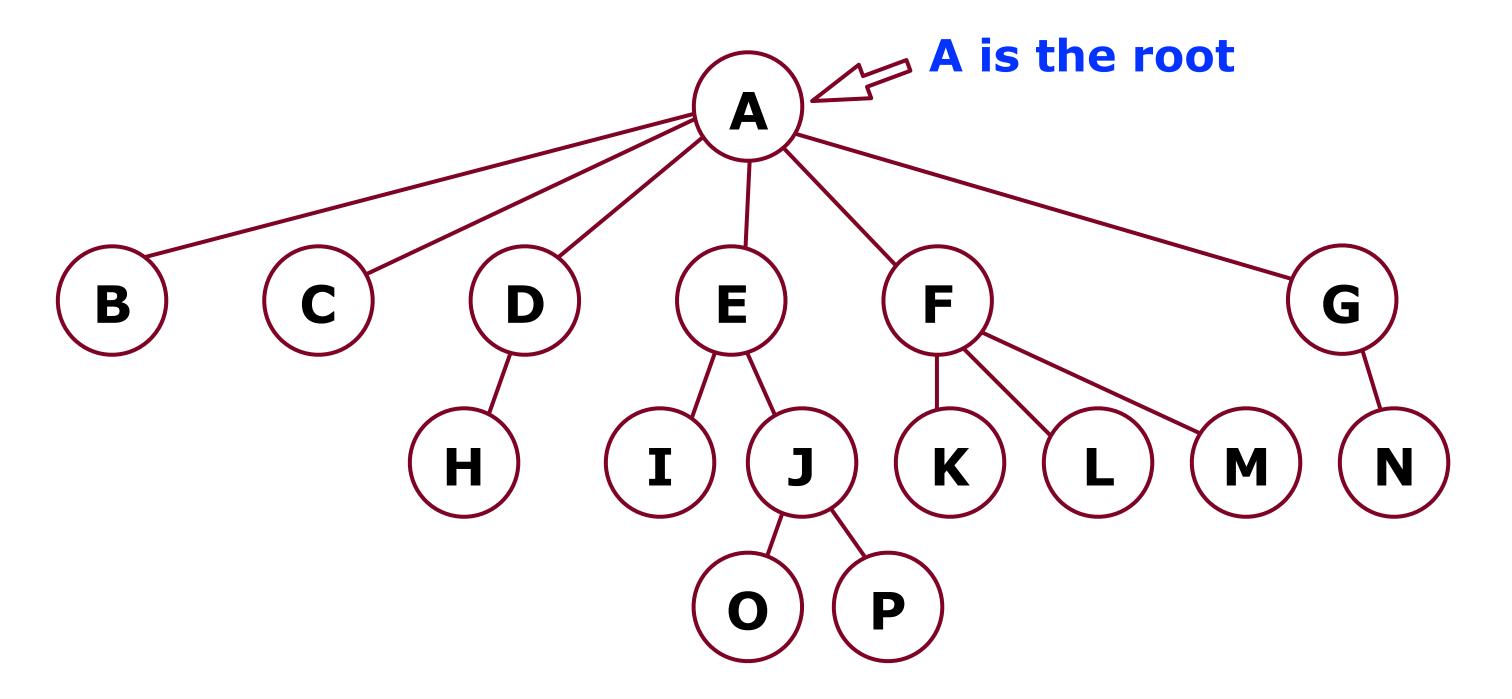


\* This is a figure in an academic paper written by a recent CS106 student!

#### Trees are inherently recursive

What is a Tree (in Computer Science)?

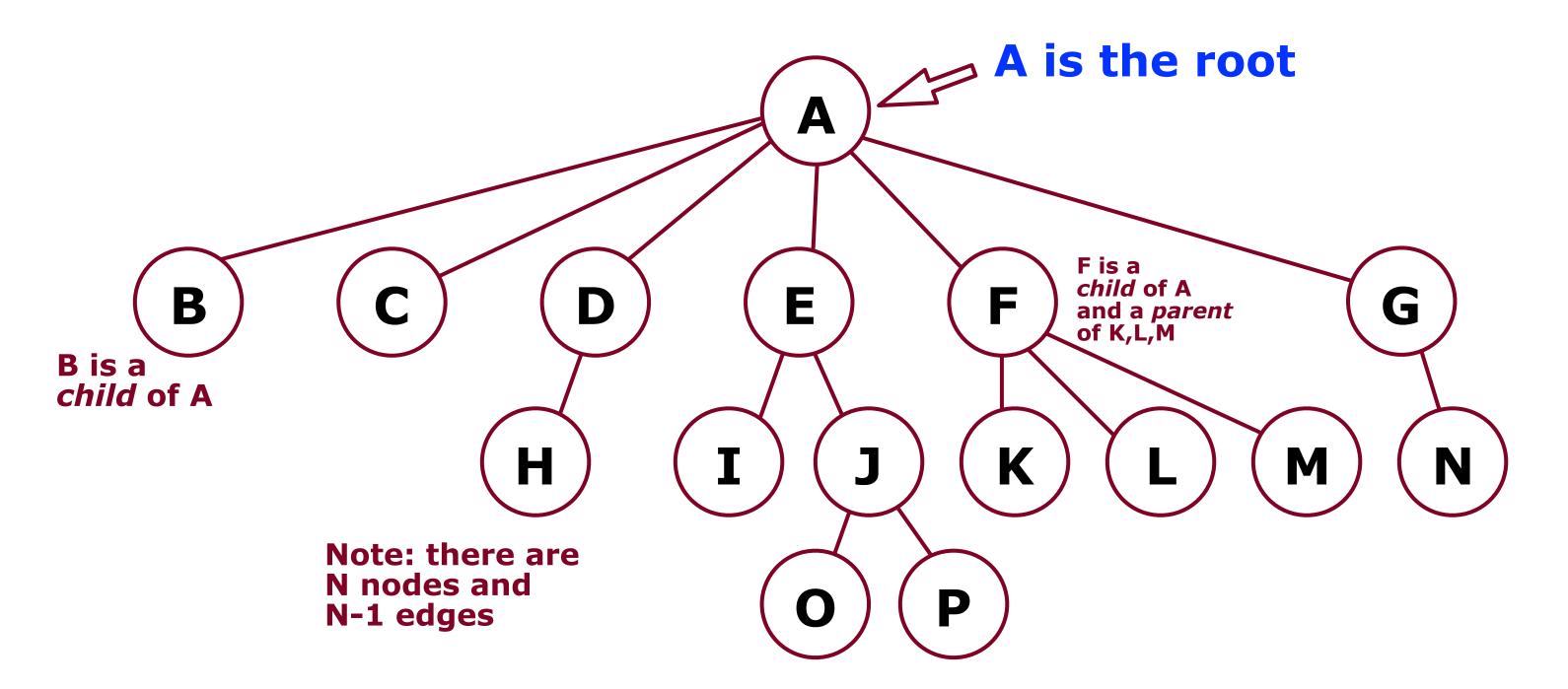
• A tree is a collection of **nodes**, which can be empty. If it is not empty, there is a "root" node, r, and  $zero\ or\ more\ non-empty\ subtrees$ ,  $T_1,\ T_2,\ \dots,\ T_k$ , whose roots are connected by a directed edge from r.

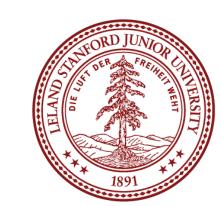




#### What is a Tree (in Computer Science)?

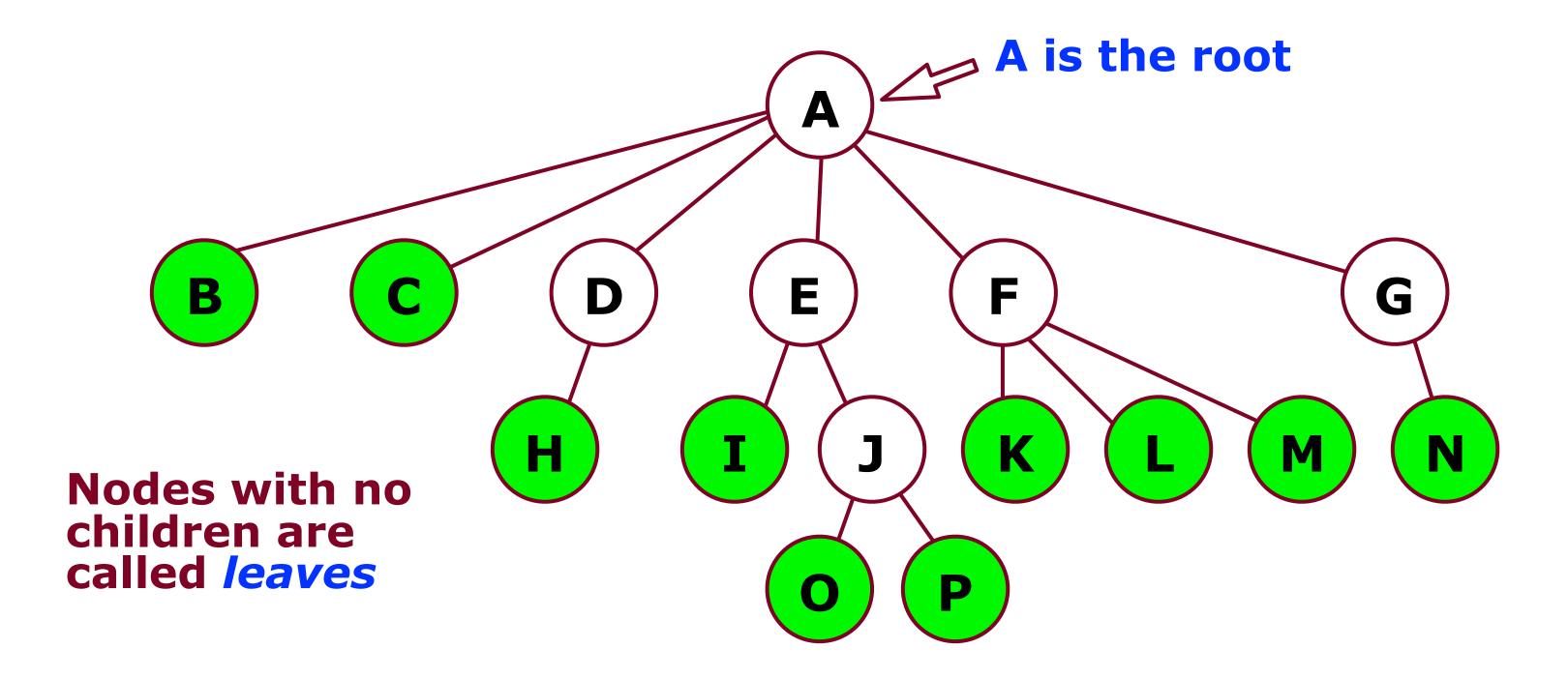
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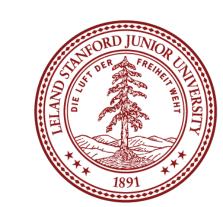




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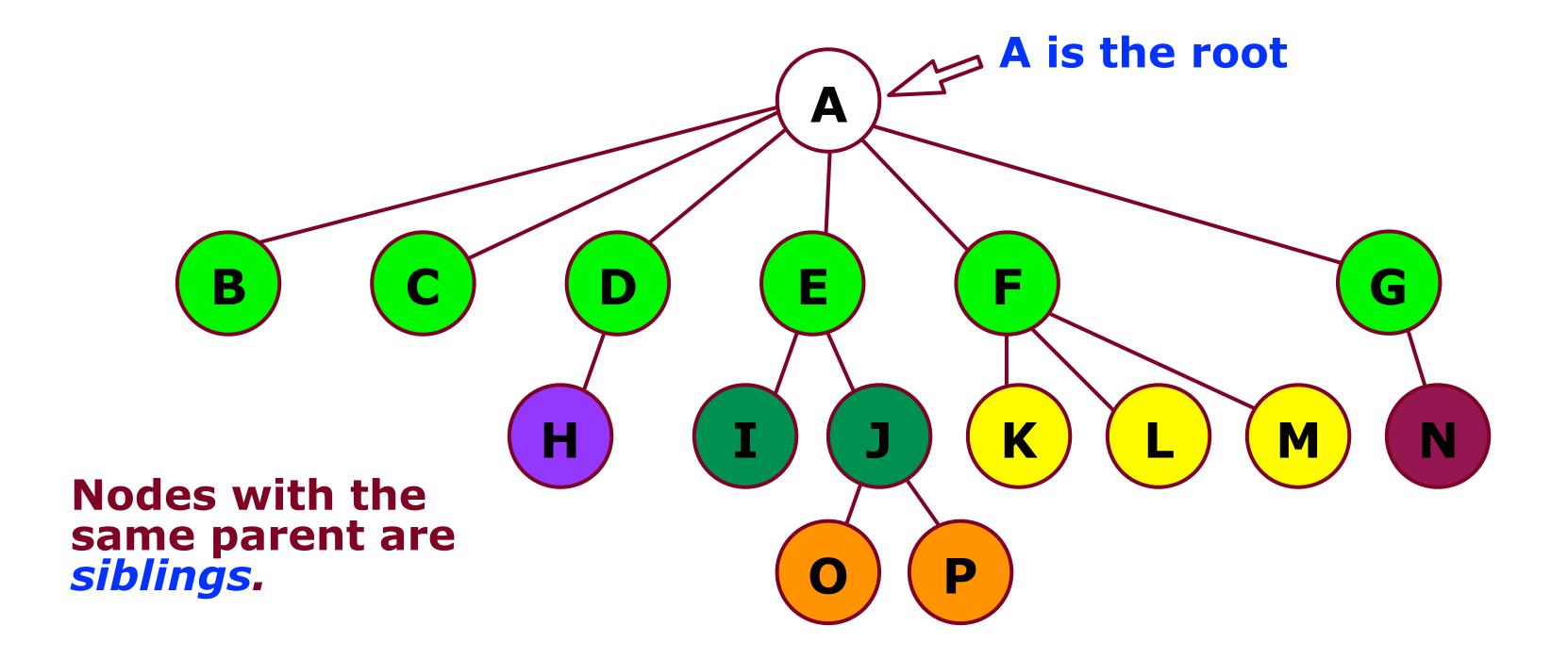
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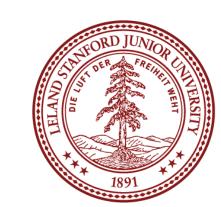


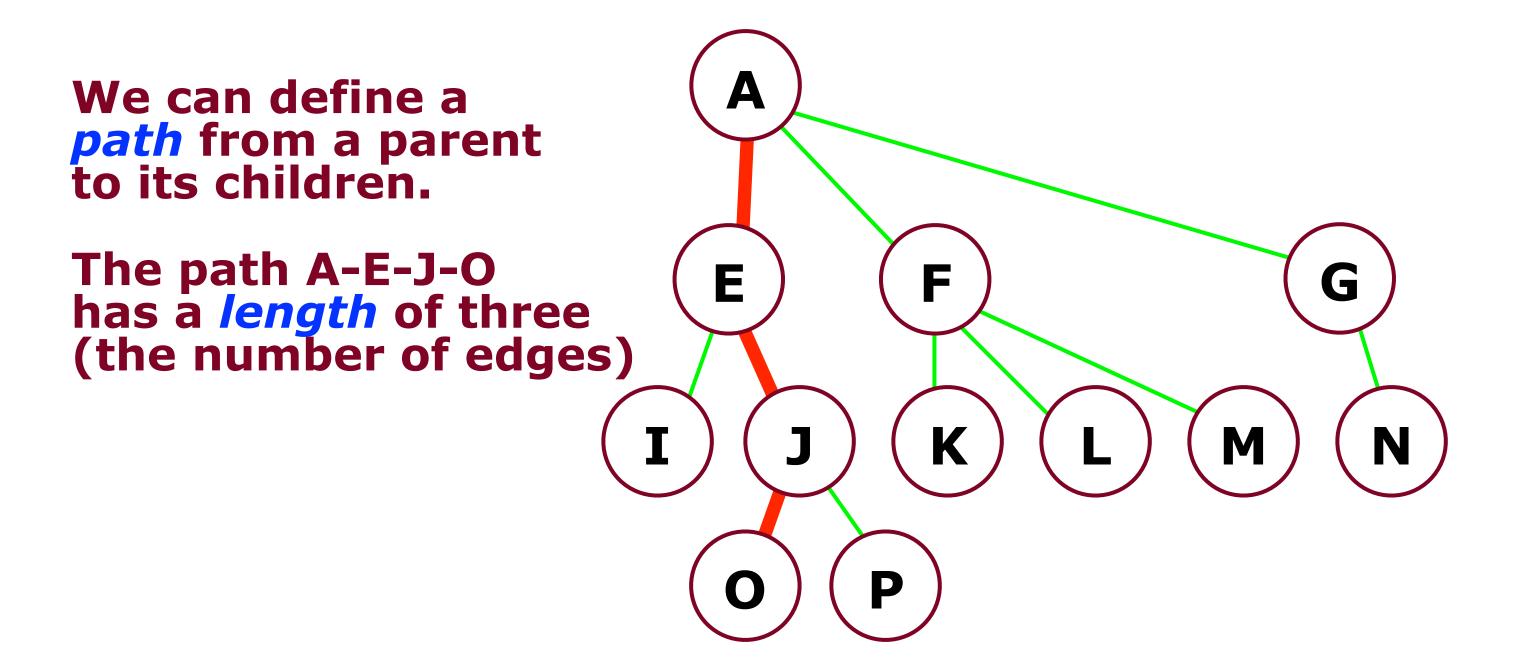


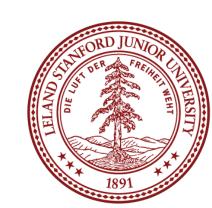
What is a Tree (in Computer Science)?

• A tree is a collection of **nodes**, which can be empty. If it is not empty, there is a "root" node, r, and  $zero\ or\ more\ non-empty\ subtrees$ ,  $T_1,\ T_2,\ \dots,\ T_k$ , whose roots are connected by a directed edge from r.





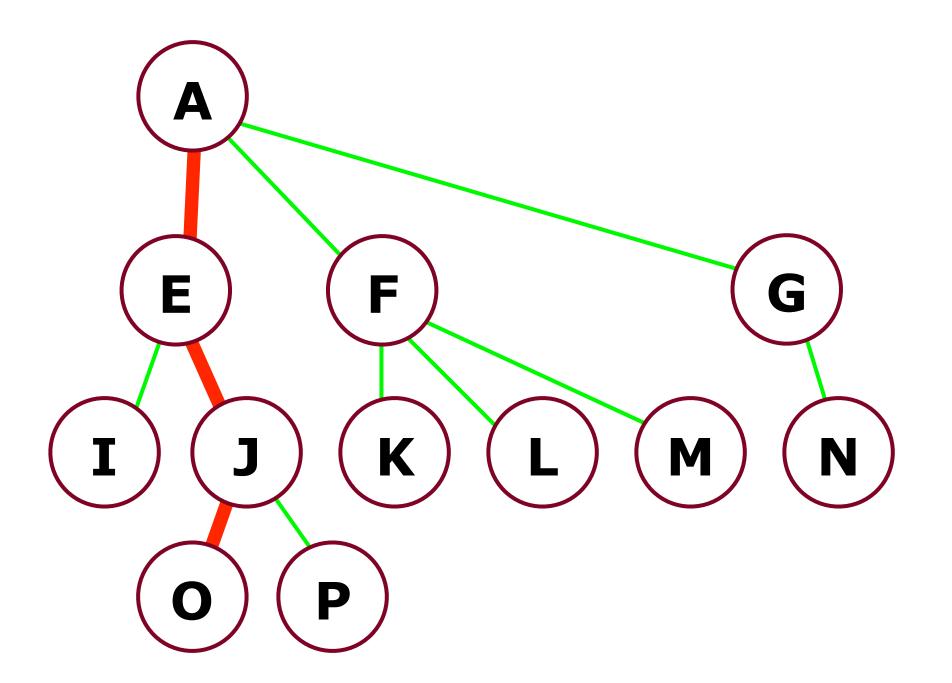






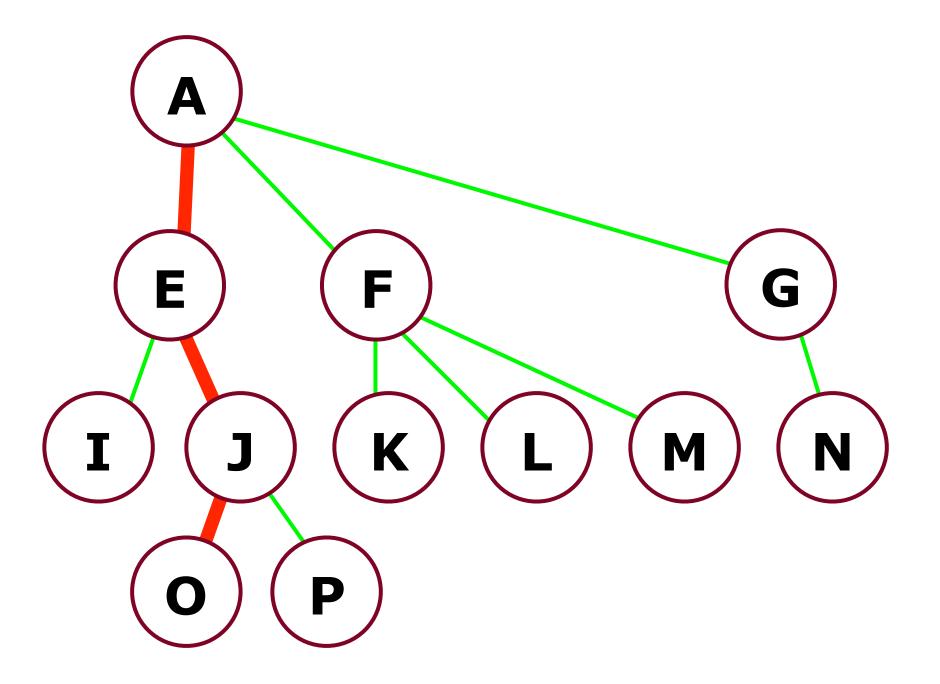
The depth of a node is the length from the root. The depth of node J is 2. The depth of the root is 0.

The *height* of a node is the longest path from the node to a leaf. The height of node F is 1. The height of all leaves is 0.





The height of a tree is the height of the root (in this case, the height of the tree is 3.





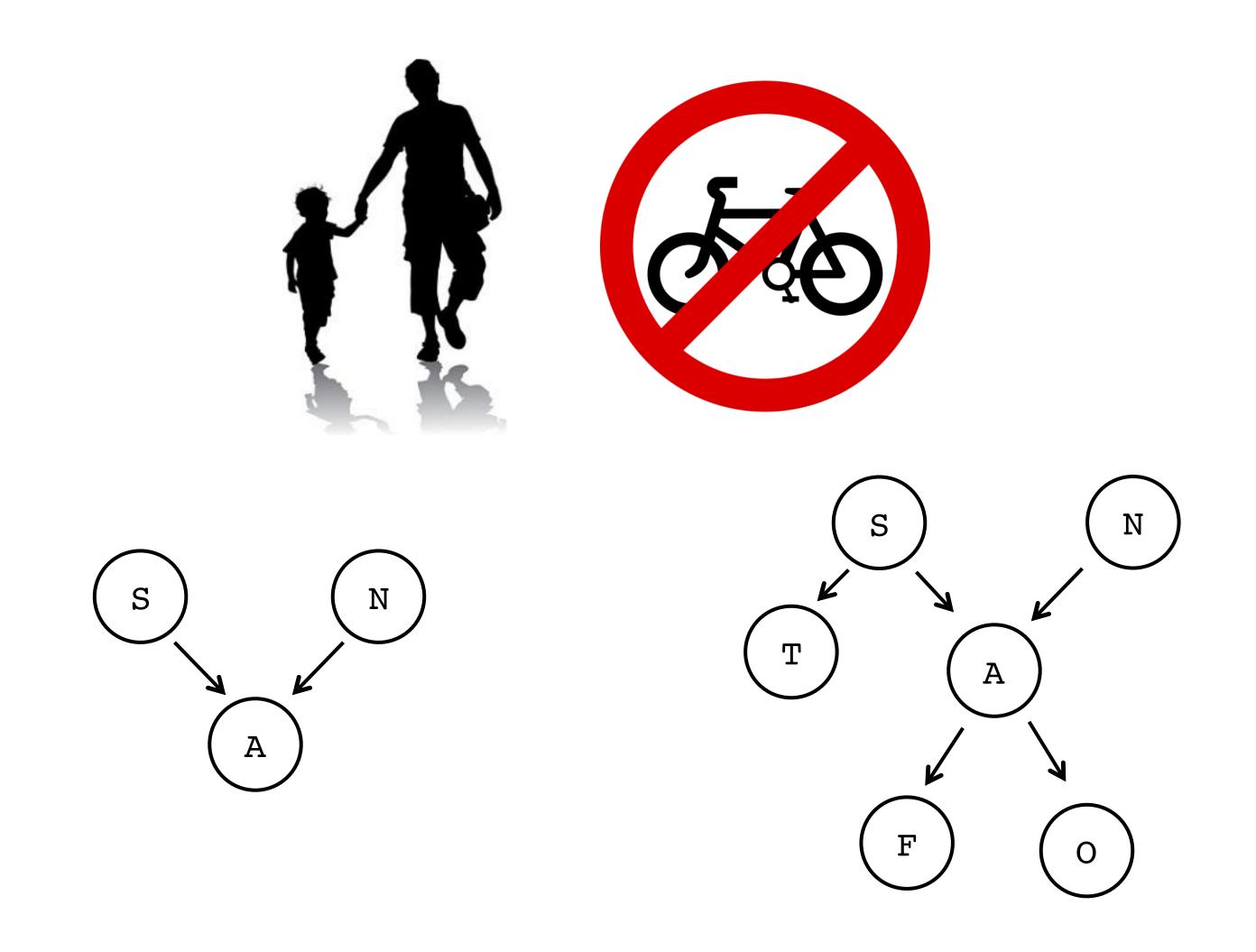
Trees can have only one parent, and cannot have cycles





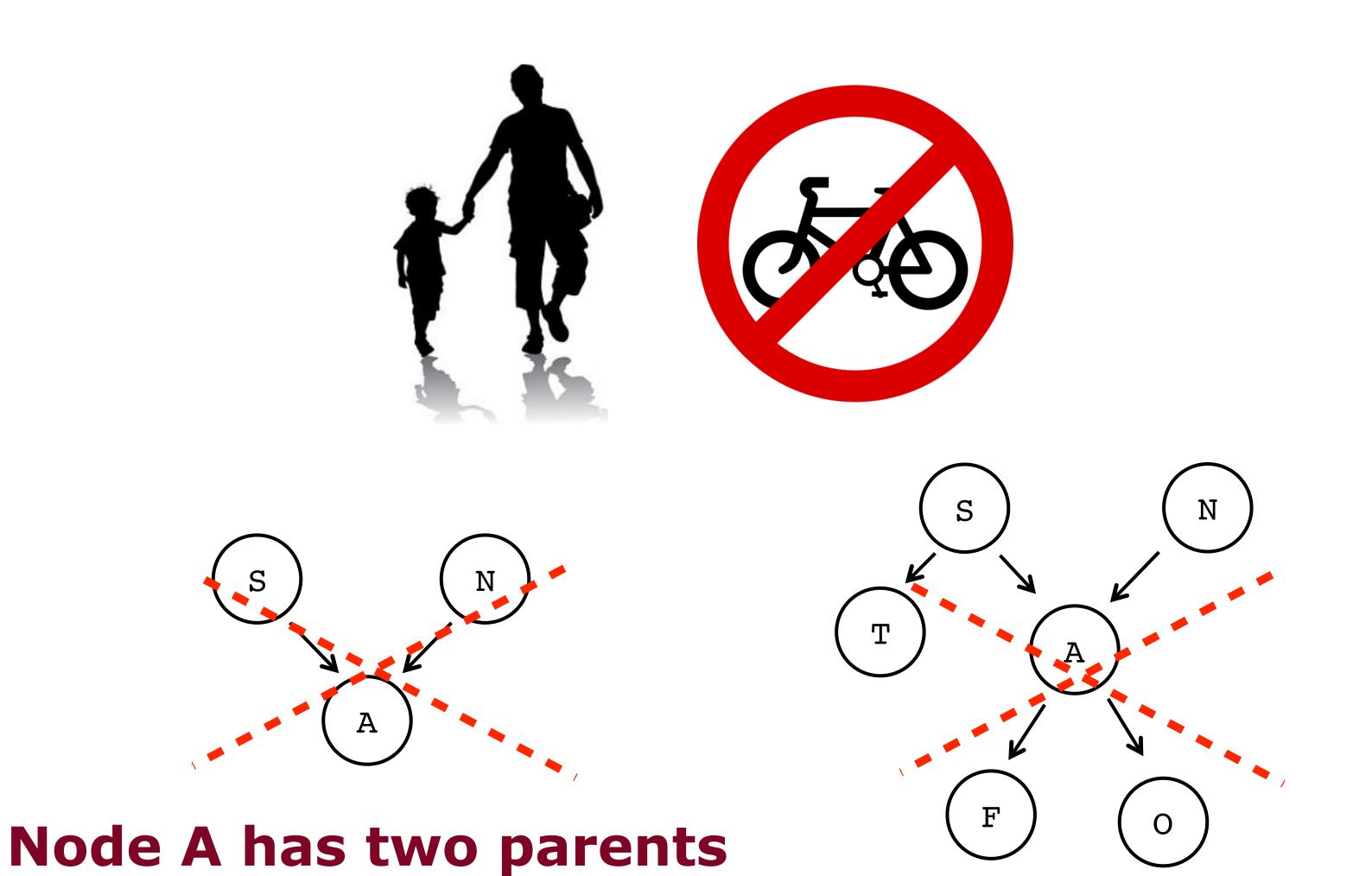


#### Trees can have only one parent, and cannot have cycles





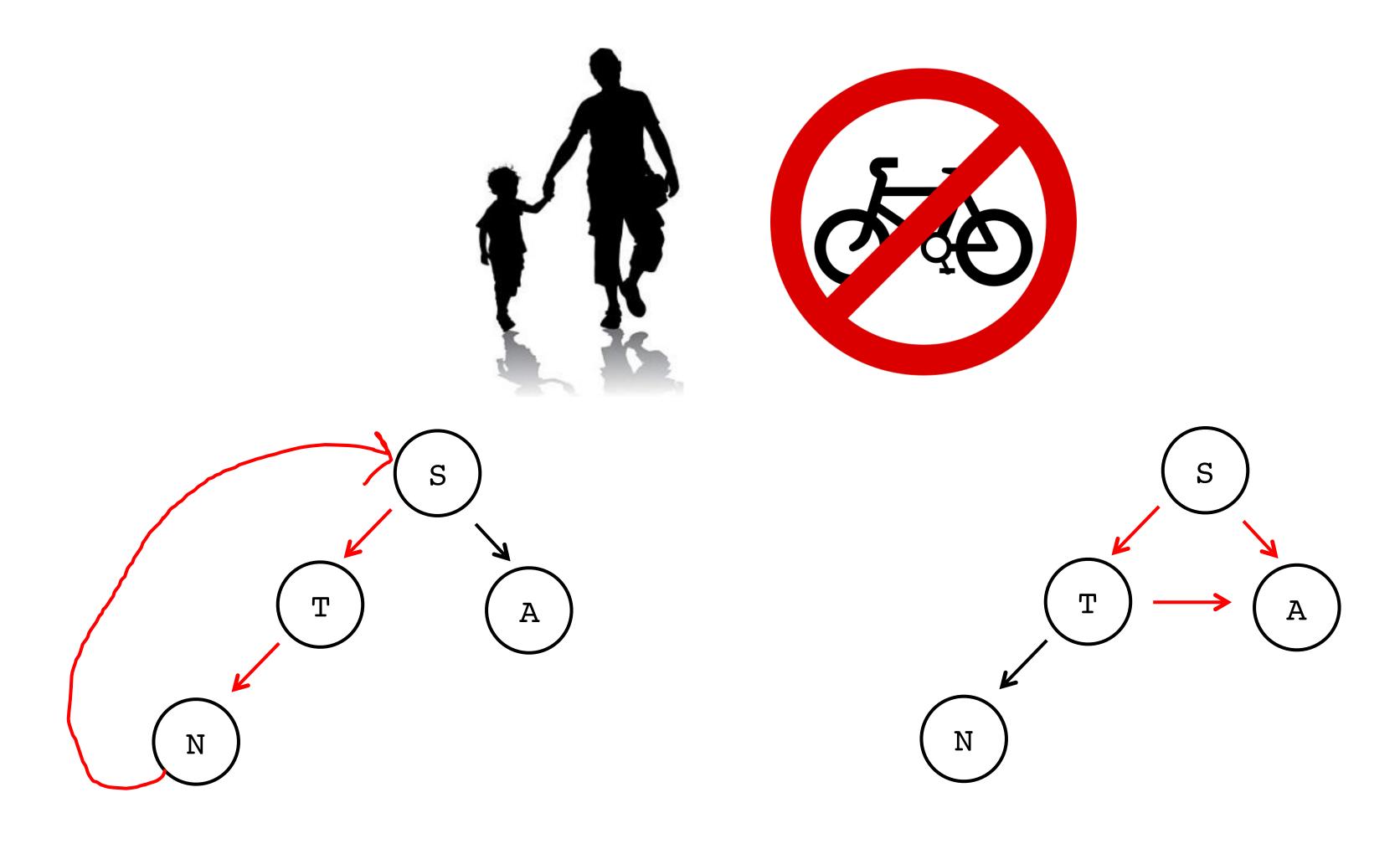
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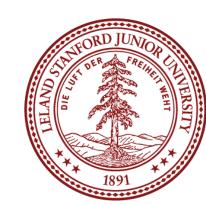


Node A has two parents

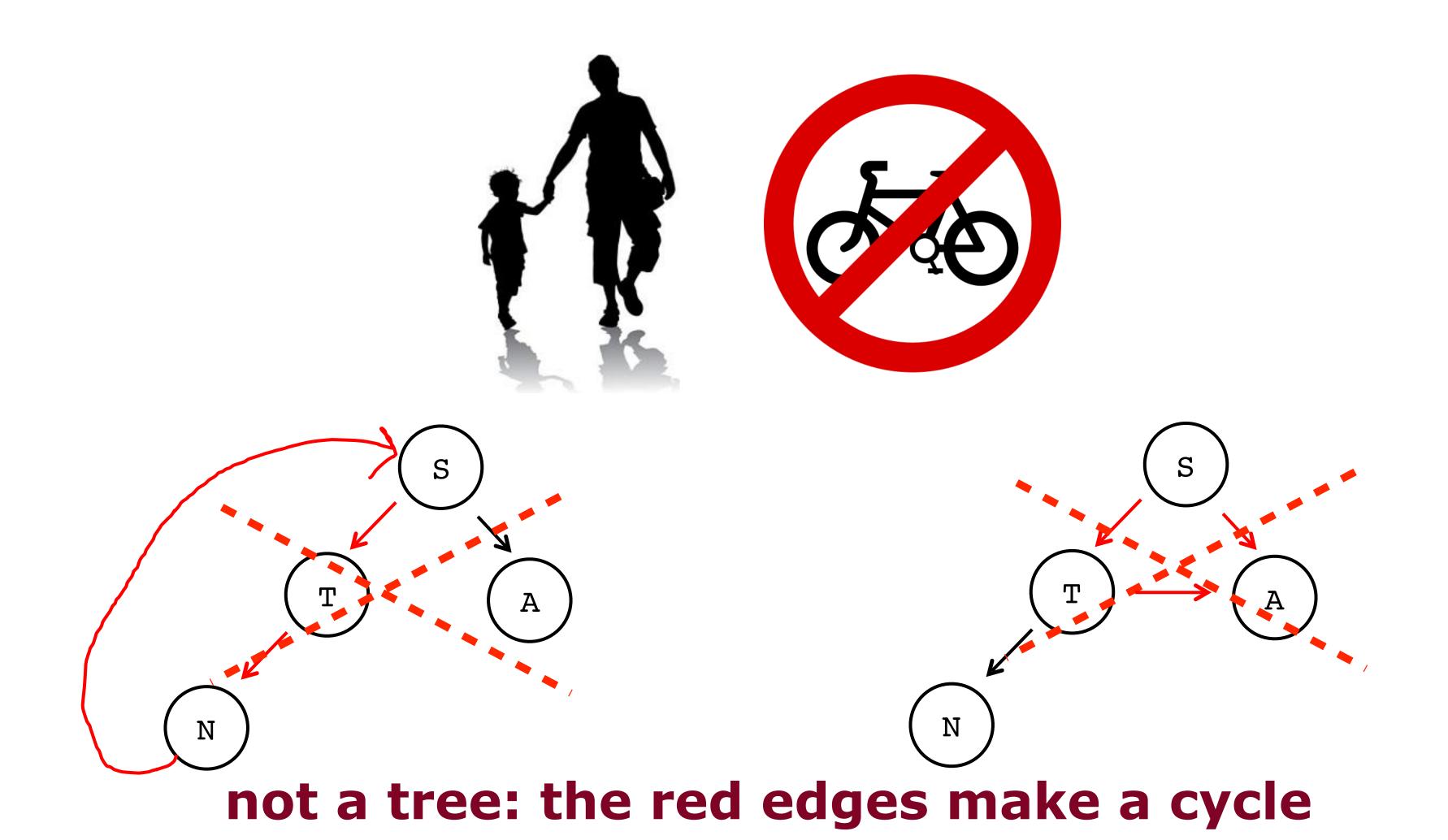


#### Trees can have only one parent, and cannot have cycles

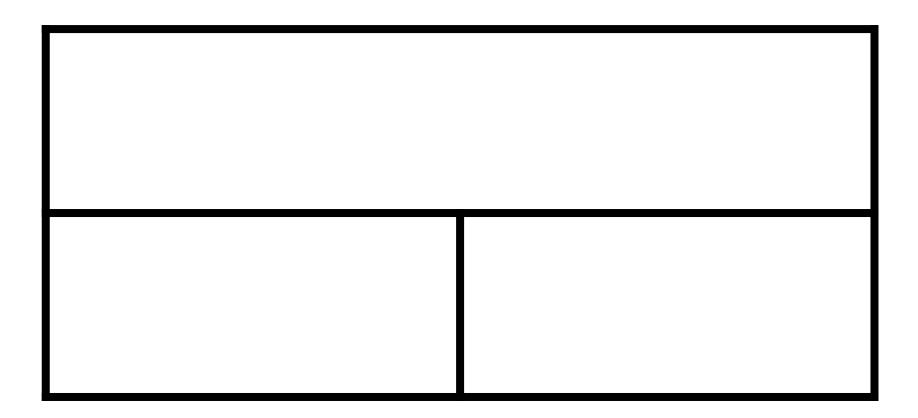




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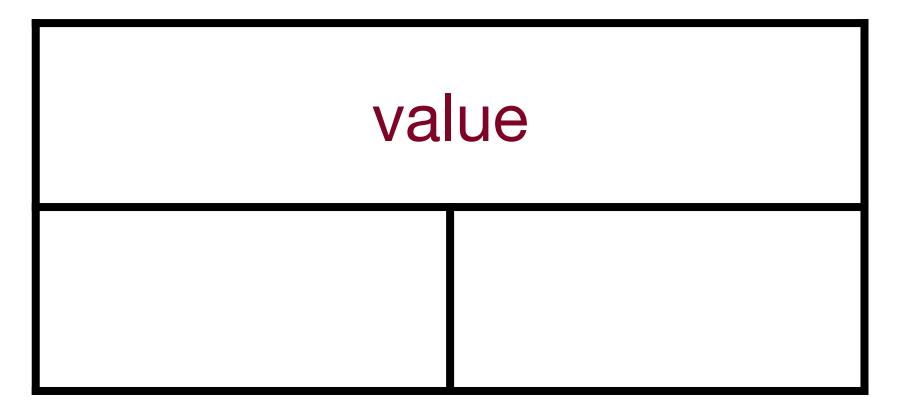








Binary Tree:





Binary Tree:

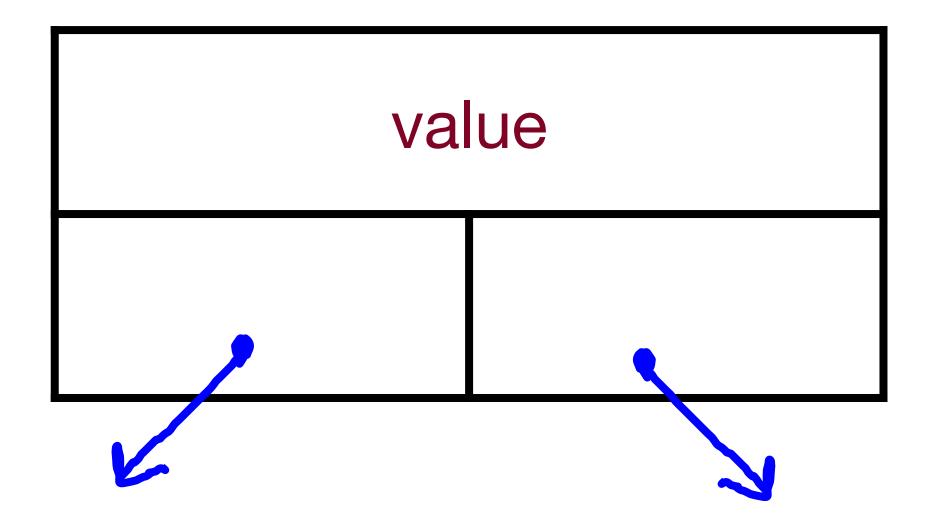
value

Linked List

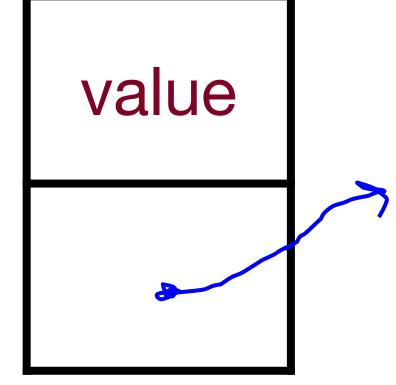
value



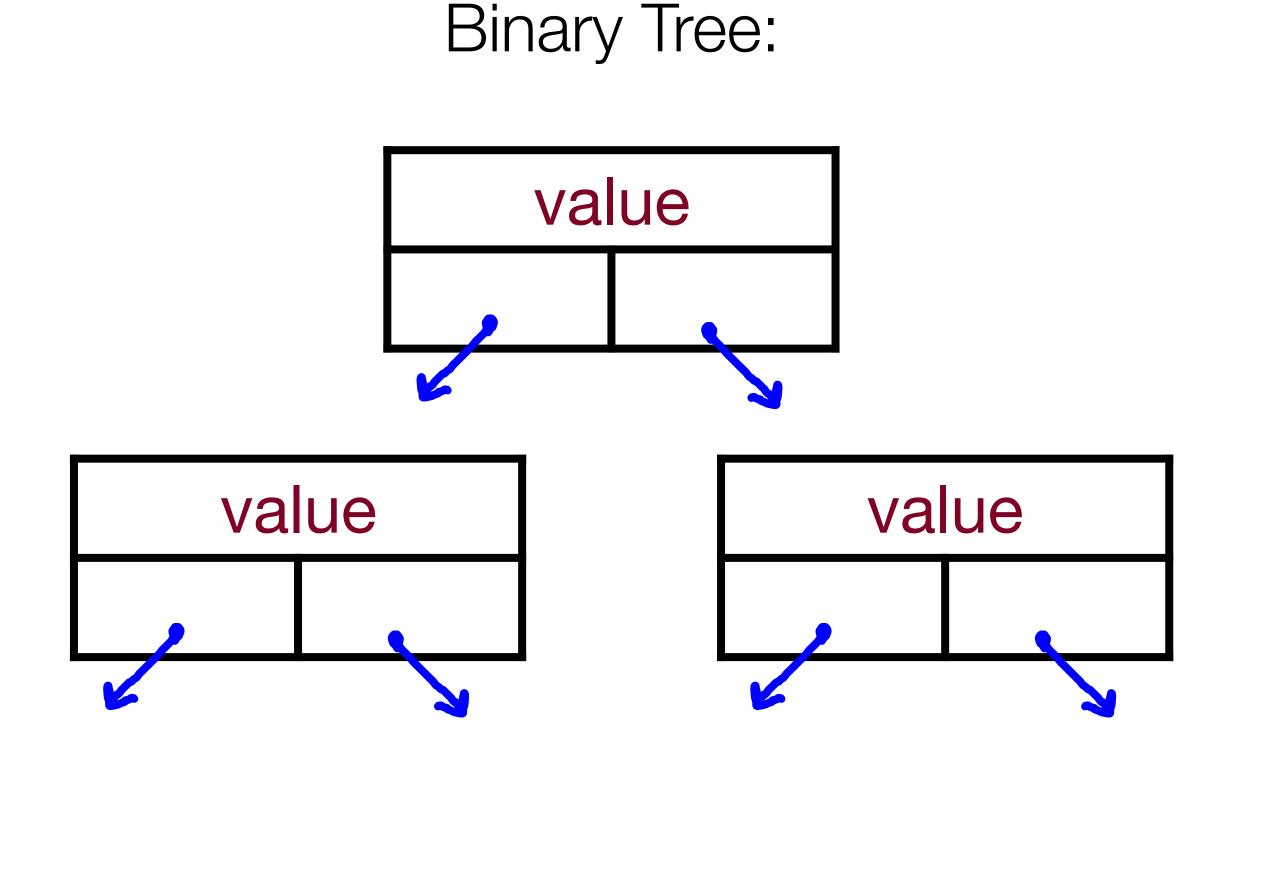
Binary Tree:



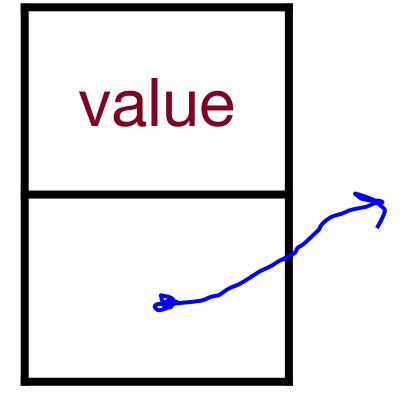
Linked List



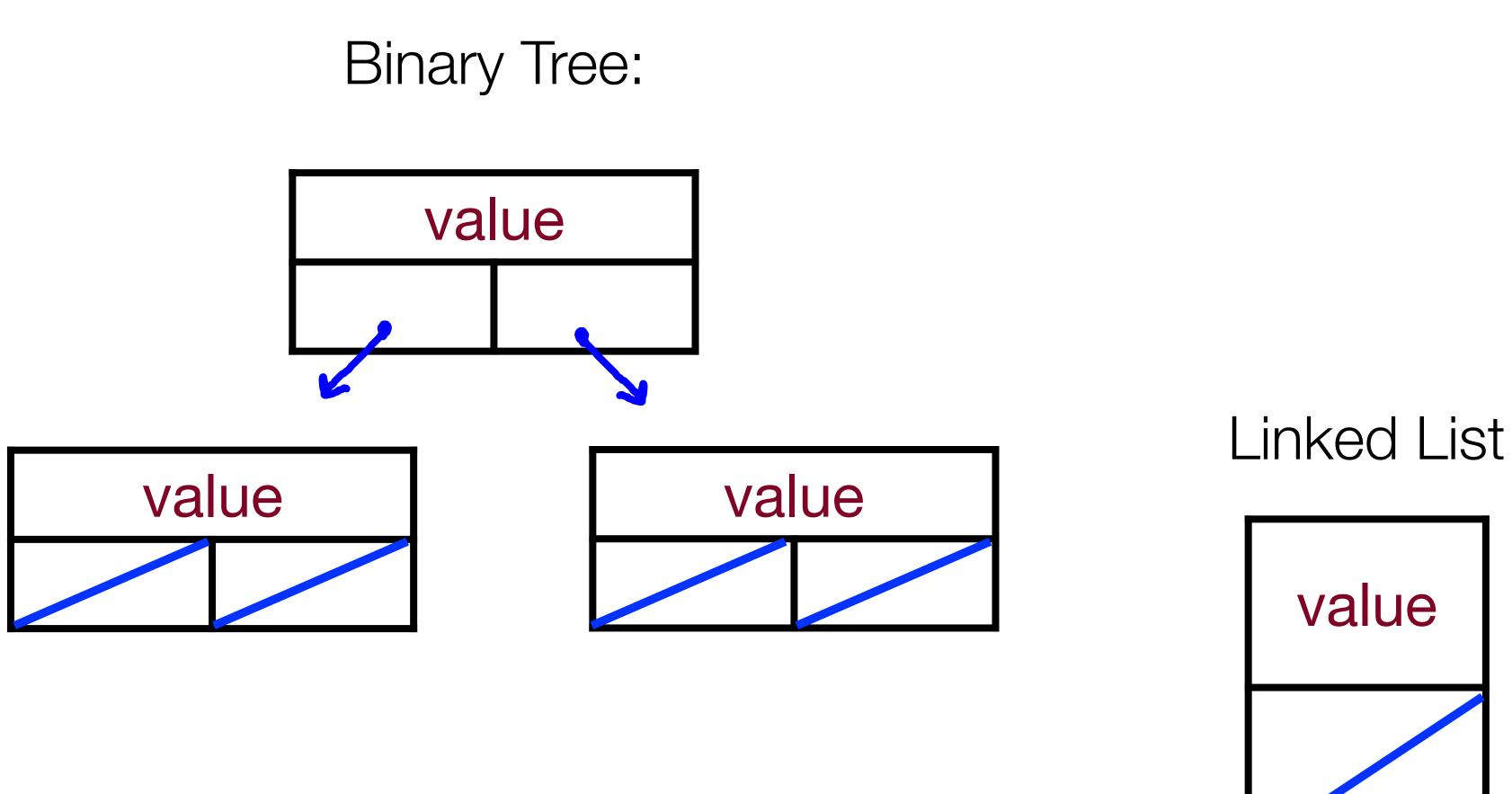


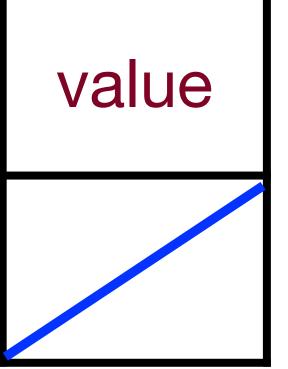


Linked List









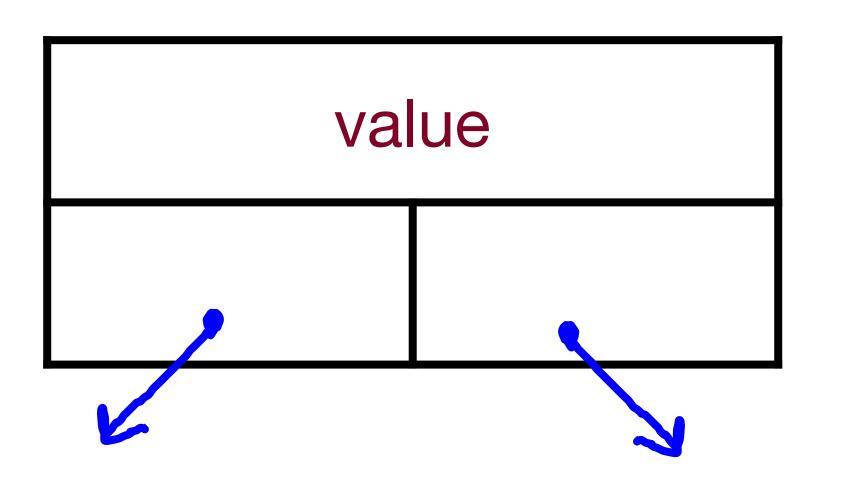


### The Most Important Slide



#### Binary Tree:

```
struct Tree {
    string value;
    Tree *left;
    Tree *right;
};
```

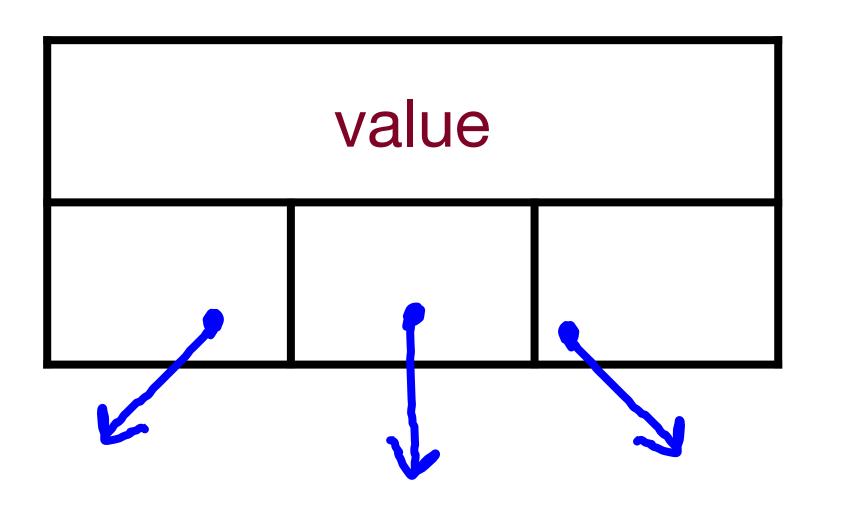




### We Can Have Ternary Trees (or any number, n)

#### Ternary Tree:

```
struct Tree {
    string value;
    Tree *left;
    Tree *middle;
    Tree *right;
};
```

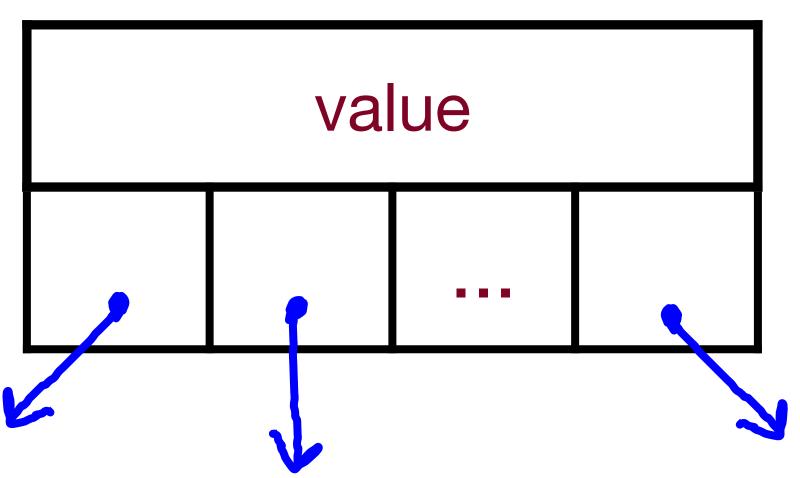




### We Can Have Ternary Trees (or any number, n)

#### N-ary Tree:

```
struct Tree {
    string value;
    Vector<Tree *> children;
};
```





#### Trees can be defined as either structs or classes

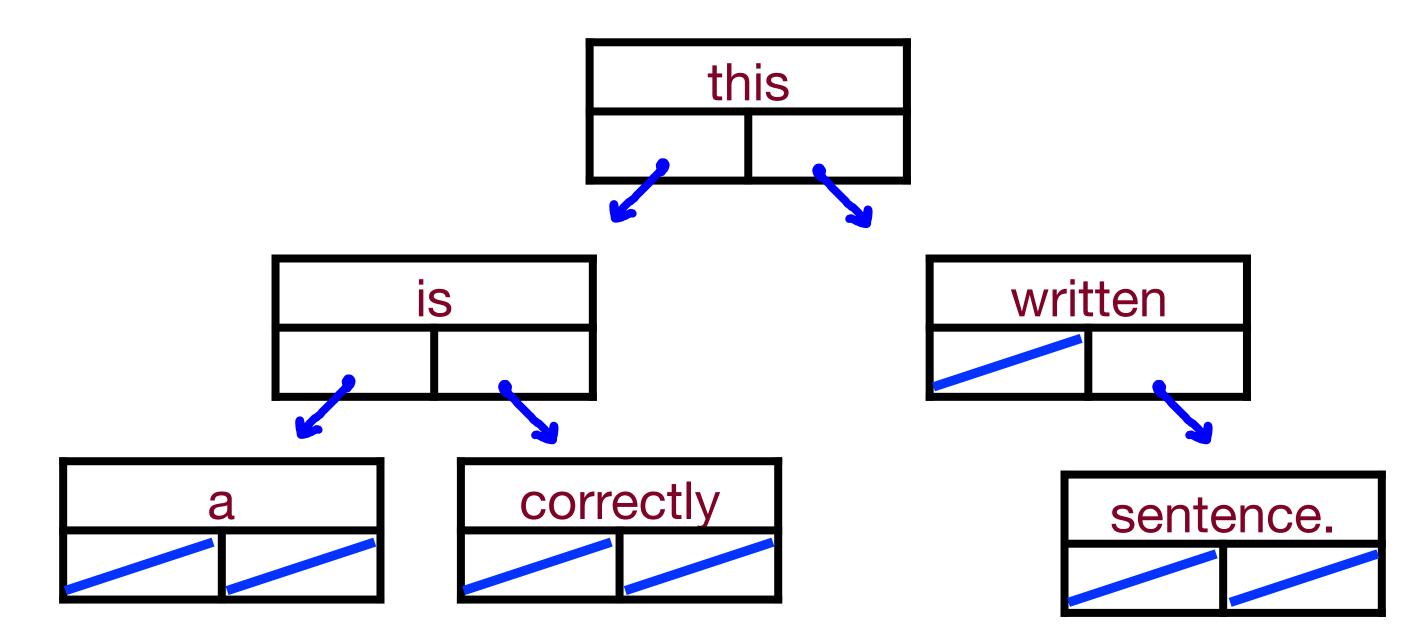
```
struct Tree {
   string value;
   Tree * left;
   Tree * right;
};
```

```
class Tree {
private:
    string value;
    Vector<Tree *> children;
};
```



```
struct Tree {
    string value;
    Tree * left;
    Tree * right;
};
```

- 1.Pre-order
- 2.In-order
- 3.Post-order
- 4.Level-order

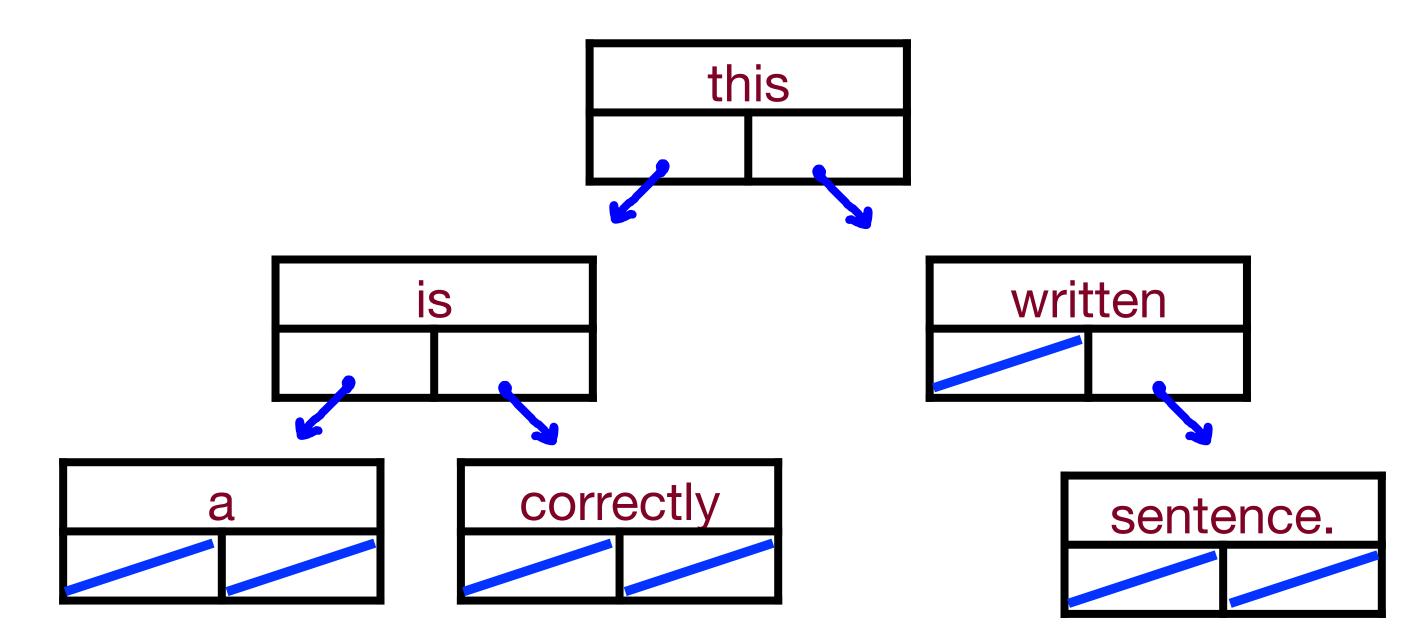




```
struct Tree {
    string value;
    Tree * left;
    Tree * right;
};
```

- 1.Pre-order
- 2.In-order
- 3.Post-order
- 4.Level-order

- 1.Do something
- 2.Go left
- 3.Go right

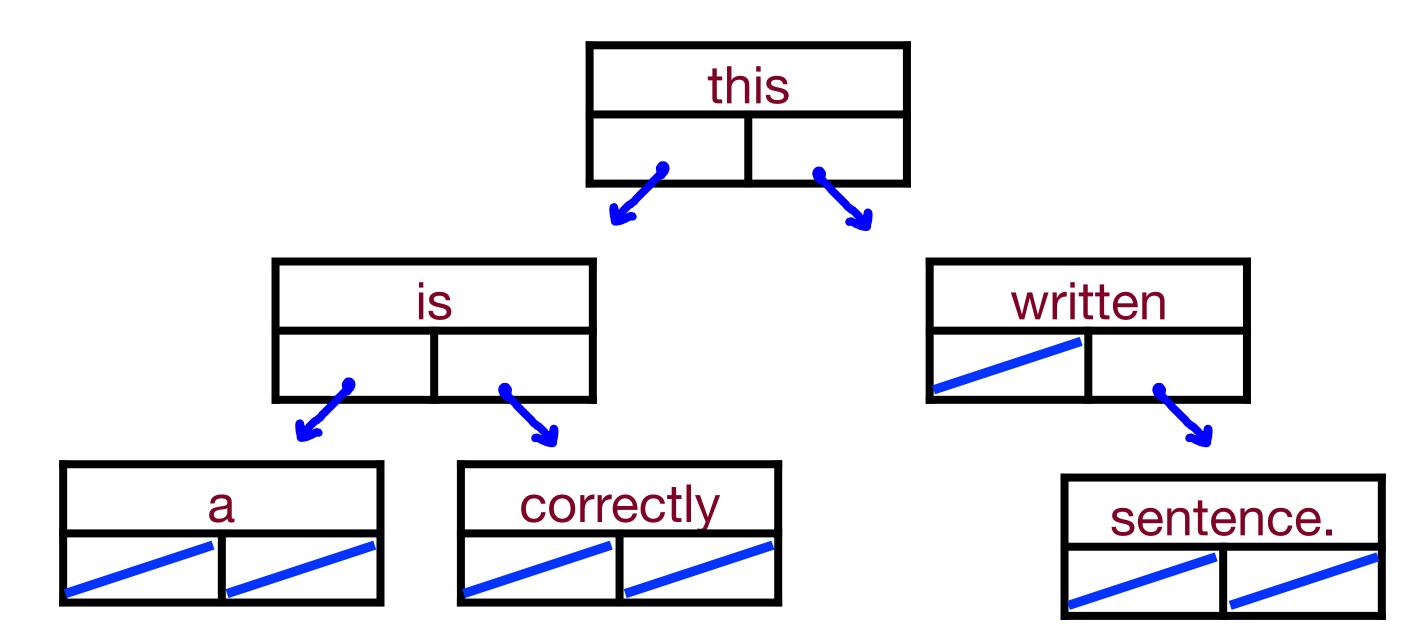




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struct Tree {
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    Tree * left;
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```

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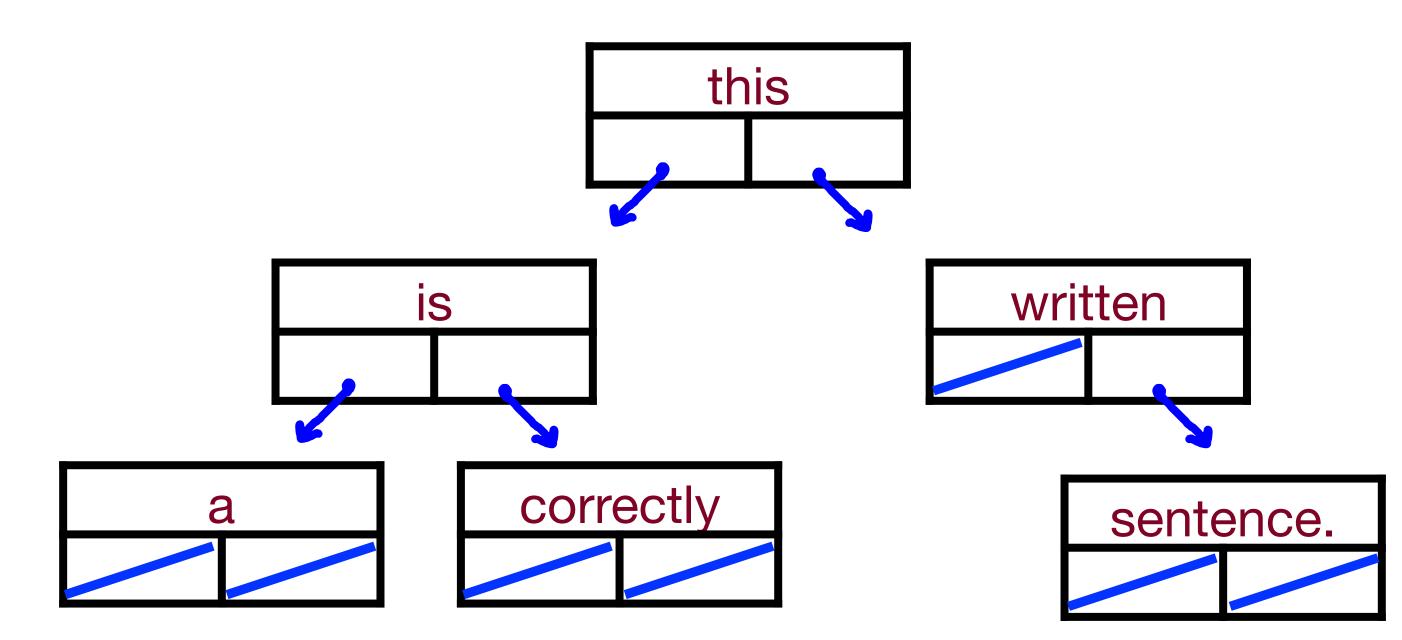




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struct Tree {
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};
```

- 1.Pre-order
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- 1.Go left
- 2.Go right
- 3.Do something

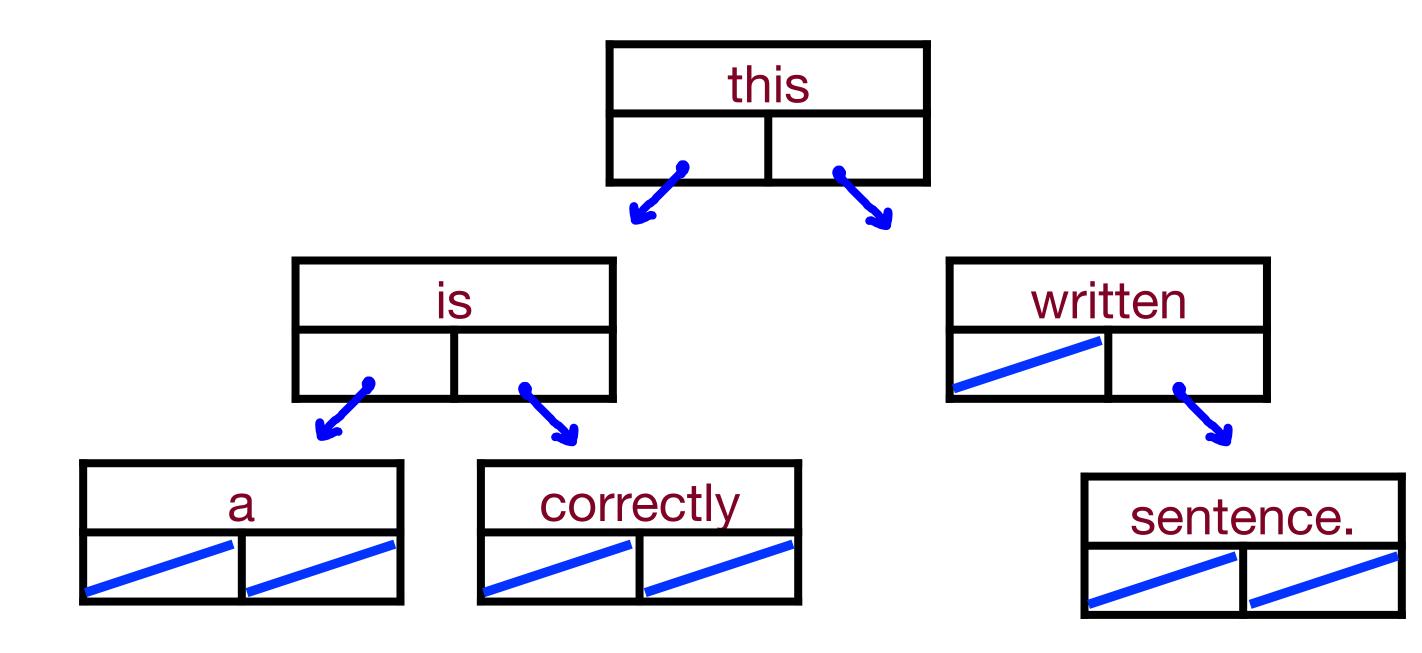




```
struct Tree {
    string value;
    Tree * left;
    Tree * right;
};
```

There are multiple ways to traverse the nodes in a binary tree:

- 1.Pre-order
- 2.In-order
- 3.Post-order
- 4.Level-order



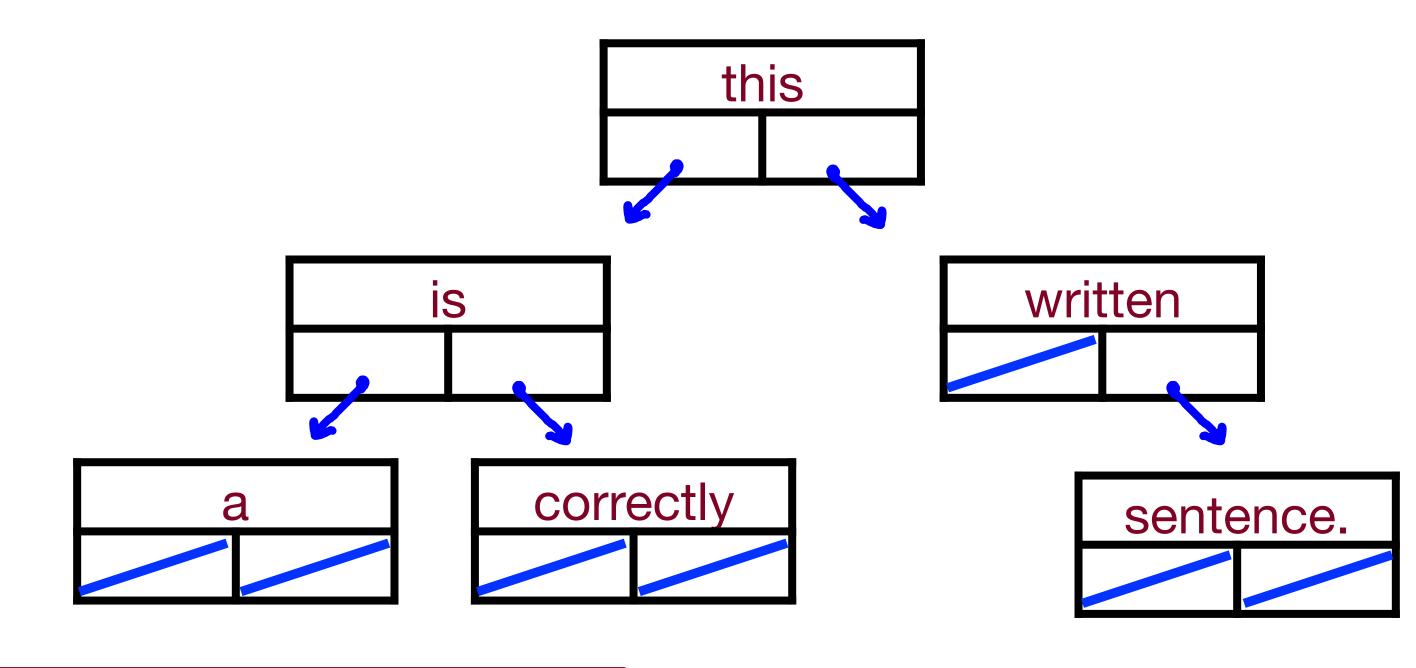
Hmm...can we do this recursively? We want to print the levels: 0, 1, 2 from left-to-right order



```
struct Tree {
    string value;
    Tree * left;
    Tree * right;
};
```

There are multiple ways to traverse the nodes in a binary tree:

- 1.Pre-order
- 2.In-order
- 3.Post-order
- 4.Level-order



Not easy recursively...let's use a queue!

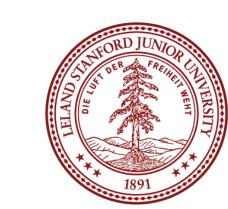
- 1. Enqueue root
- 2. While queue is not empty:
  - a. dequeue node
  - b. do something with node
  - c. enqueue left child of node if it exists
  - d. enqueue right child of node if it exists

should look familiar...word ladder?



#### Let's write some code

```
struct Tree {
   string value;
                                                                                   this
   Tree * left;
   Tree * right;
};
                                                                      İS
void preOrder(Tree * tree) {
  if(tree == nullptr) return;
  cout<< tree->value <<" ";</pre>
  preOrder(tree->left);
                                                                          correctly
  preOrder(tree->right);
void inOrder(Tree * tree) {
                                        void levelOrder(Tree *tree) {
                                            Queue<Tree *>treeQueue;
  if(tree == nullptr) return;
                                            treeQueue.enqueue(tree);
  inOrder(tree->left);
                                            while (!treeQueue.isEmpty()) {
  cout<< tree->value <<" ";</pre>
                                                Tree *node = treeQueue.dequeue();
  inOrder(tree->right);
                                                cout << node->value << " ";</pre>
                                               if (node->left != nullptr) {
                                                    treeQueue.enqueue(node->left);
void postOrder(Tree * tree) {
  if(tree == NULL) return;
                                                if (node->right != nullptr) {
  postOrder(tree->left);
                                                    treeQueue.enqueue(node->right);
  postOrder(tree->right);
  cout<< tree->value << " ";</pre>
```



written

sentence.

#### References and Advanced Reading

#### · References:

- https://en.wikipedia.org/wiki/Tree\_(data\_structure)
- http://pages.cs.wisc.edu/~vernon/cs367/notes/8.TREES.html

#### Advanced Reading:

- •http://www.cs.cmu.edu/~adamchik/15-121/lectures/Trees/trees.html
- •Great set of tree-type questions:
  - http://cslibrary.stanford.edu/110/BinaryTrees.html

