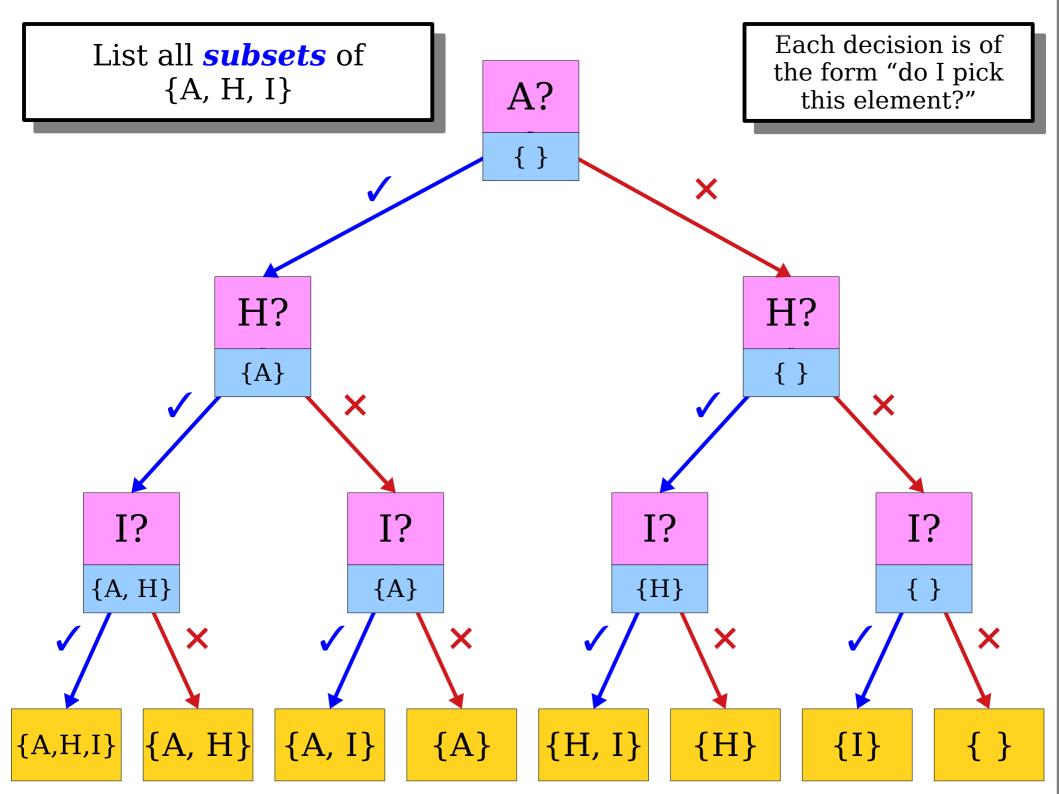
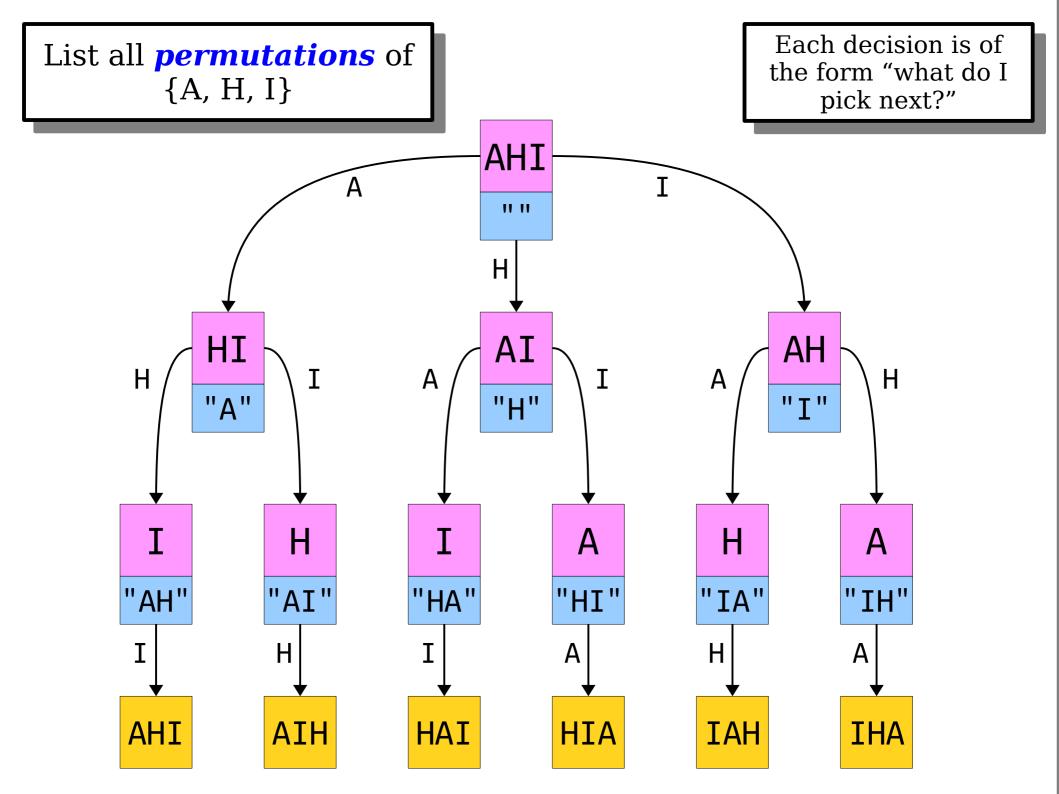
Thinking Recursively Part IV

Outline for Today

- Recap From Last Time
 - Where are we, again?
- Enumerating Combinations
 - Addressing some points from last time.
- Shrinkable Words
 - A little word puzzle!

Recap from Last Time





```
Decisions
Base Case: No
                                                      yet to be
decisions remain.
                                                       made
     void exploreRec(decisions remaining,
                      decisions already made) {
                                                     Decisions
        if (no decisions remain)
                                                       already
          process decisions made;
                                                       made
          else {
          for (each possible next choice) {
            exploreRec(all remaining decisions,
                       decisions made + that choice);
 Recursive Case:
 Try all options for
 the next decision.
```

```
void exploreAllTheThings(initial state) {
  exploreRec(initial state, no decisions made);
}
```

New Stuff!

Enumerating Combinations



- Suppose that we want to find every way to choose exactly one element from a set.
- We could do something like this:

```
for (int x: mySet) {
    cout << x << endl;
}</pre>
```

- Suppose that we want to find every way to choose exactly two
 elements from a set.
- We could do something like this:

```
for (int x: mySet) {
    for (int y: mySet) {
        if (x != y) {
            cout << x << ", " << y << endl;
        }
    }
}</pre>
```

- Suppose that we want to find every way to choose exactly *three* elements from a set.
- We could do something like this:

```
for (int x: mySet) {
  for (int y: mySet) {
    for (int z: mySet) {
      if (x != y && x != z && y != z) {
         cout << x << ", " << y << ", " << z << endl;
```

- If we know how many elements we want in advance, we can always just nest a whole bunch of loops.
- But what if we don't know in advance?
- Or we *do* know in advance, but it's a large number and we don't want to type until our fingers bleed?

combinationsOf(const Set<string>& elems,
 int numToPick);

What should this function's return type be?

Take thirty seconds to formulate a hypothesis, but don't post it in chat yet!

??? combinationsOf(const Set<string>& elems,
 int numToPick);

What should this function's return type be?

Okay, now type your hypothesis into the chat.

Implementing Combinations

Our Base Case

Pick 0 more Justices out of {Kagan, Breyer}

Chosen so far: {Alito, Roberts, Gorsuch, Thomas, Sotomayor}

There's no need to keep looking.

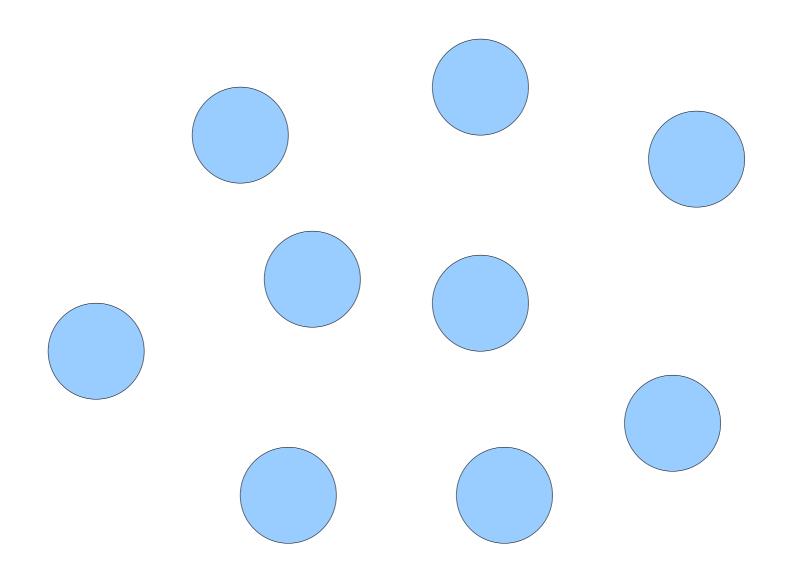
What should we return in this case?

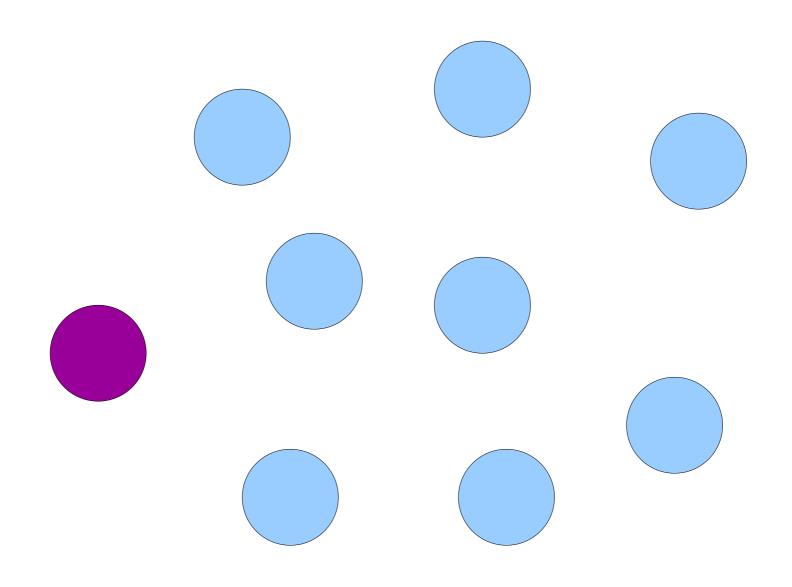
Our Base Case, Part II

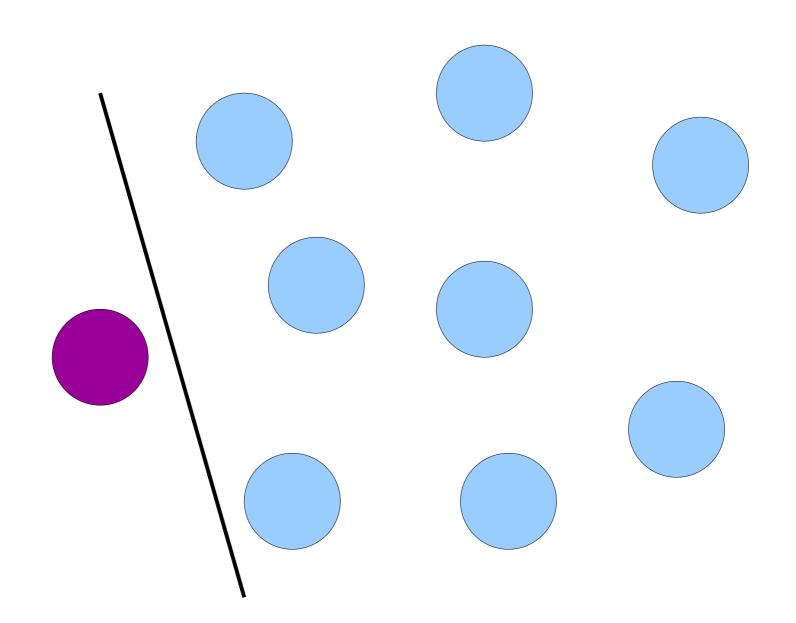
```
Pick 5 more Justices out of
  {Sotomayor, Thomas}
Chosen so far: { }
```

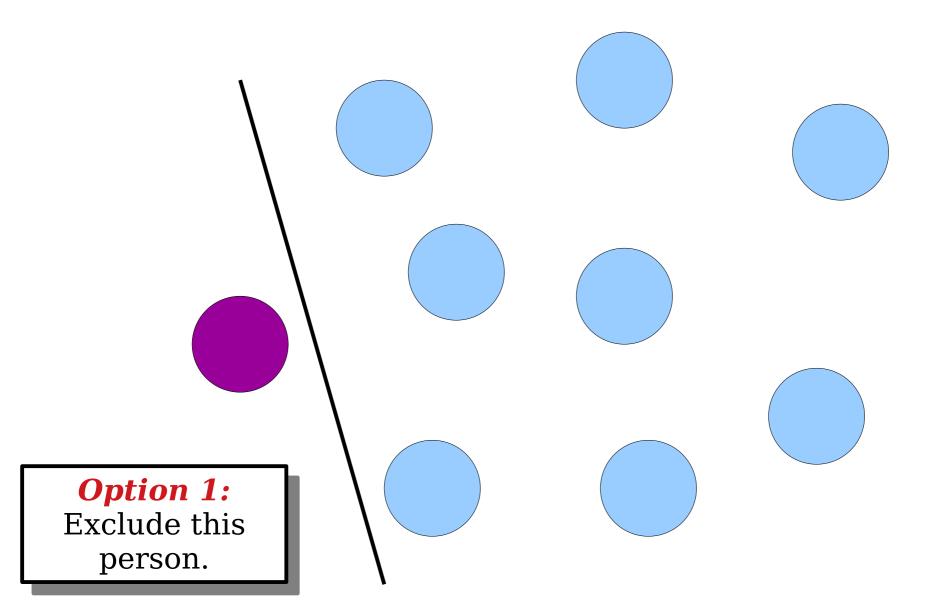
There is no way to do this!

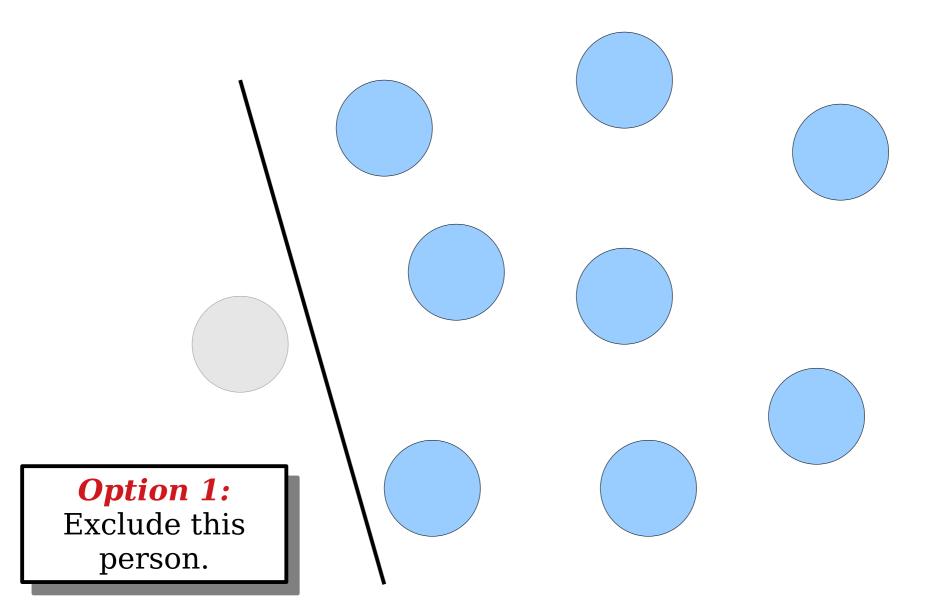
What should we return in this case?

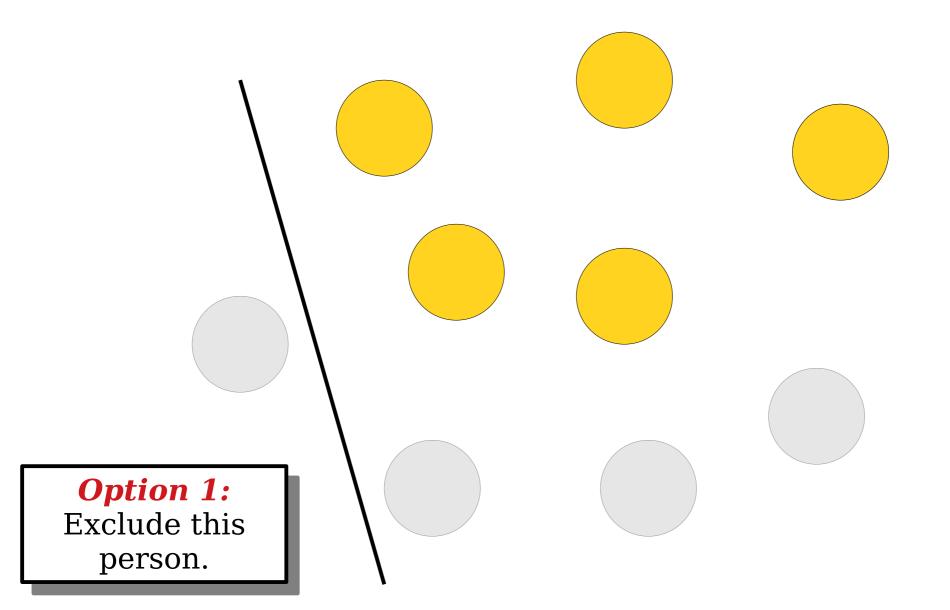


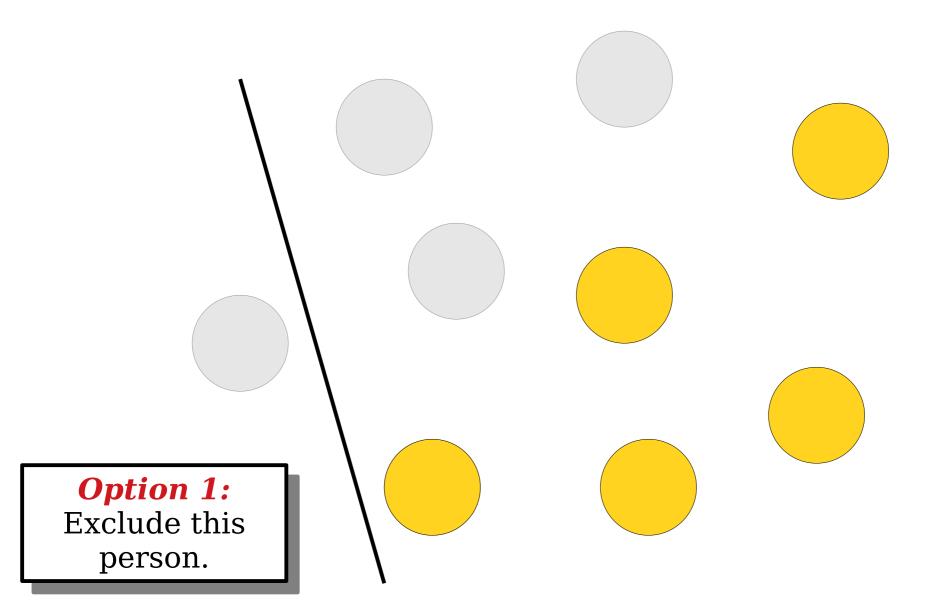


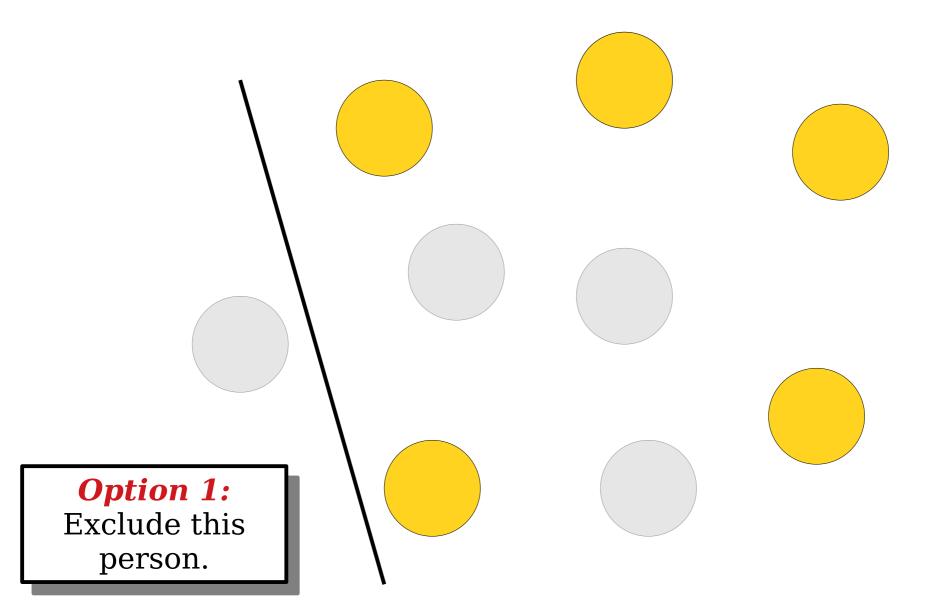


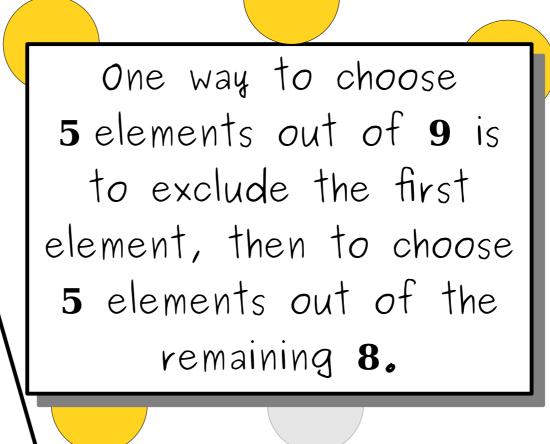






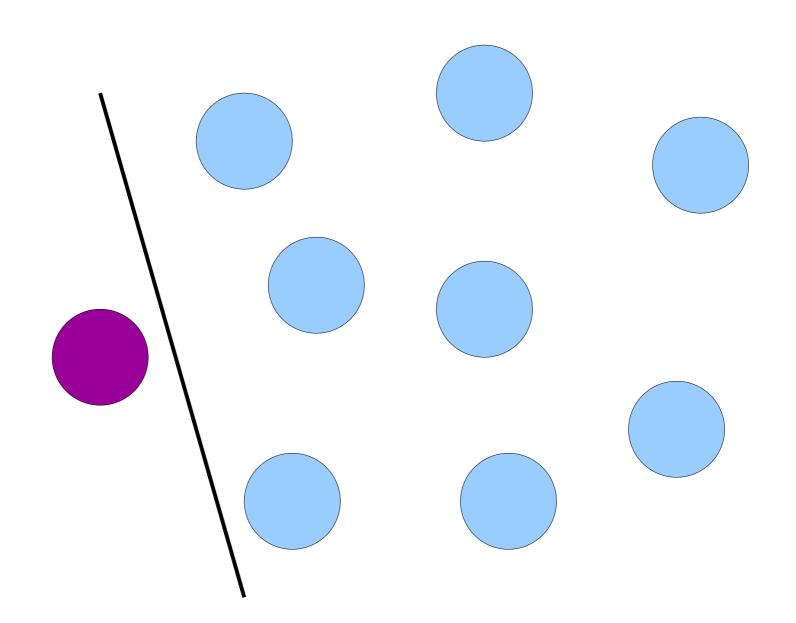


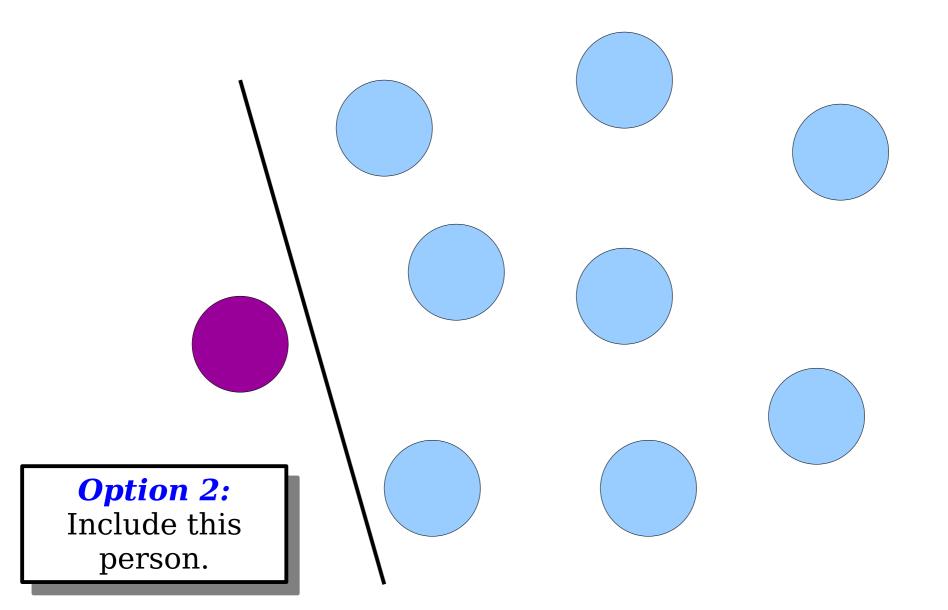


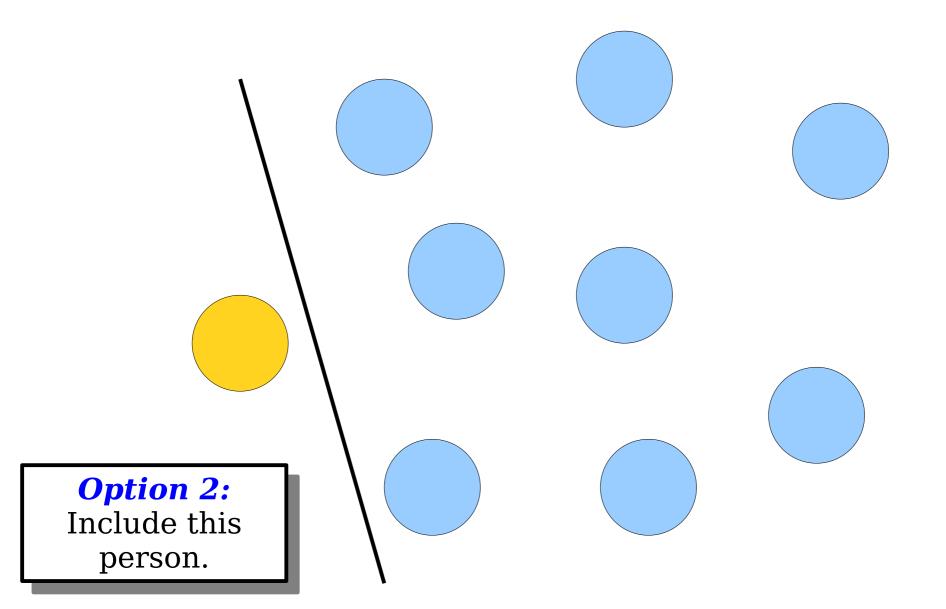


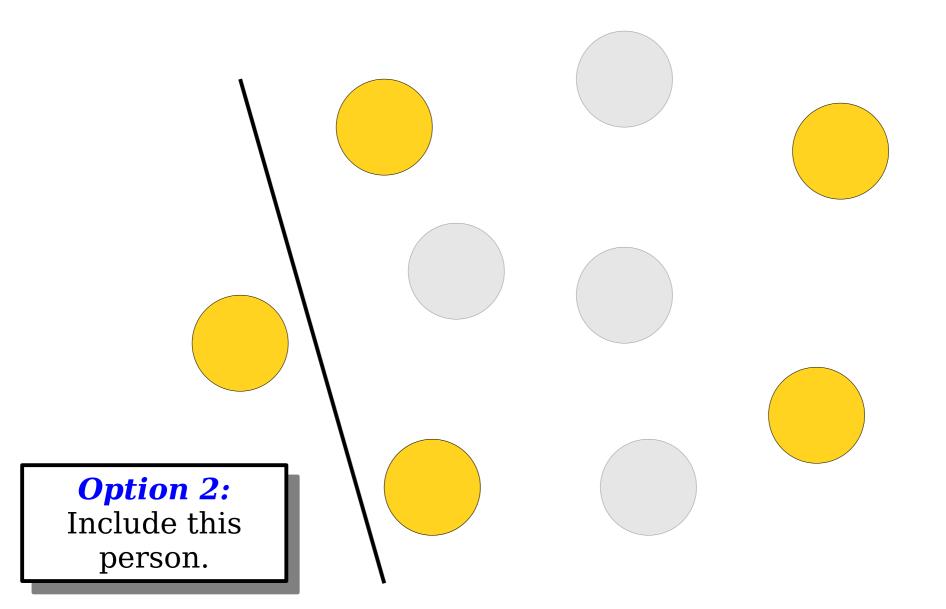
Option 1:

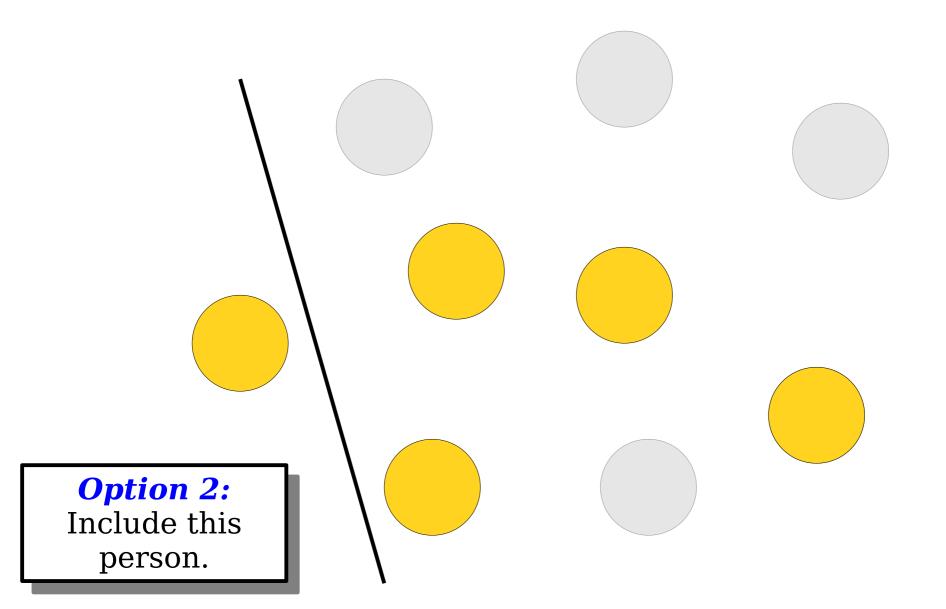
Exclude this person.



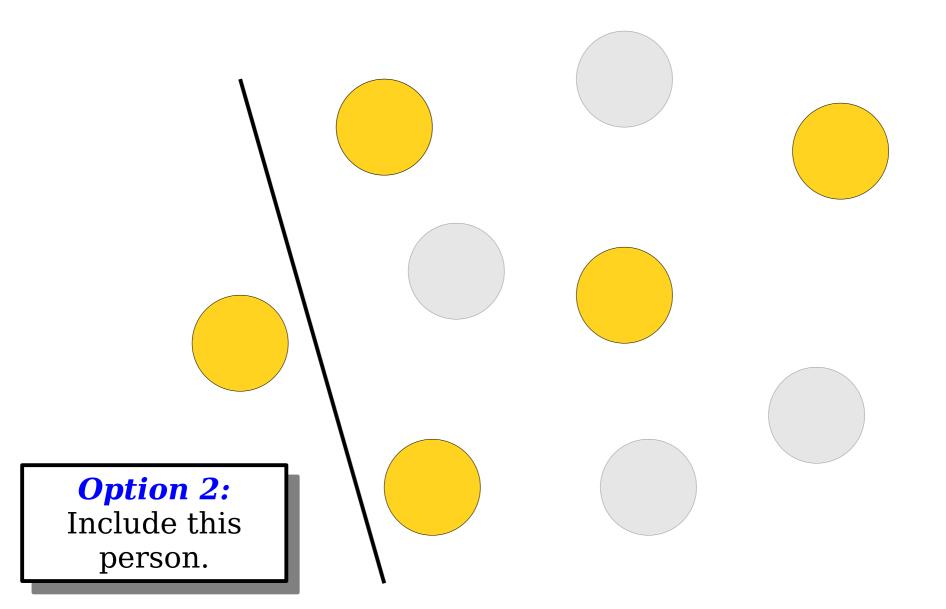




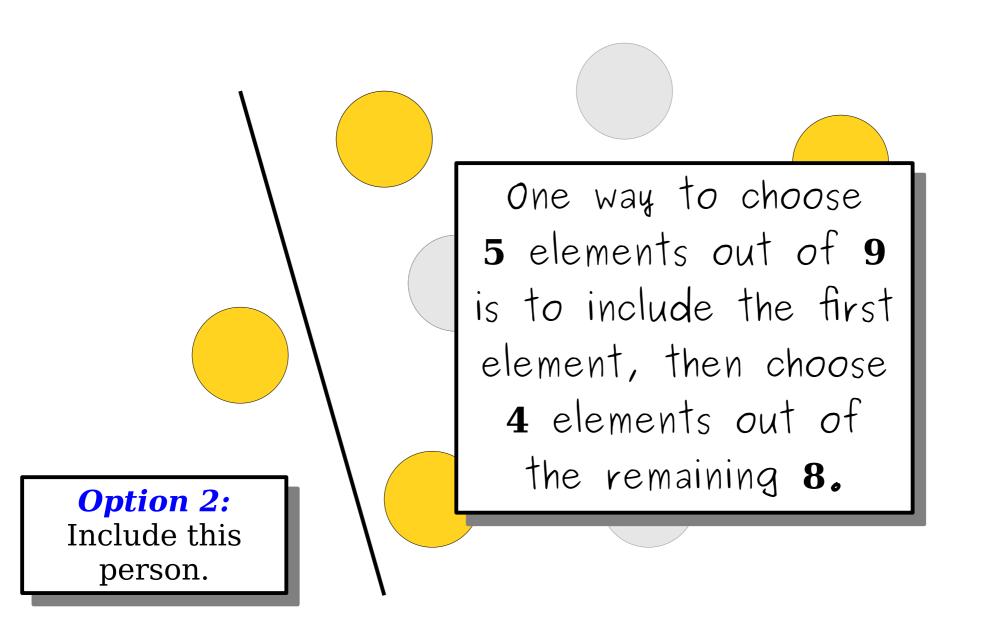




Generating Combinations



Generating Combinations



A Comment on Types

The Wonderful auto Keyword

- There are many cases in which there is exactly one possible type that a variable could have.
- In that case, rather than explicitly writing out the type, you can use the auto keyword:

auto var = expression;

 Don't go crazy with this one; use it mostly to save typing when working with container types.

Decisions Base Case: No yet to be decisions remain. made Container exploreRec(decisions remaining, decisions already made) Decisions if (no decisions remain) { already return container of decisions made made else { Container result; for (each possible next choice) { result += exploreRec(all remaining decisions, decisions made + that choice); return result; Recursive Case: Try all options for the next decision. Container exploreAllTheThings(initial state) { return exploreRec(initial state, no decisions made);

A Little Word Puzzle

"What nine-letter word can be reduced to a single-letter word one letter at a time by removing letters, leaving it a legal word at each step?"

STARTLING

STARTING

STARING

STRING

S T I N G

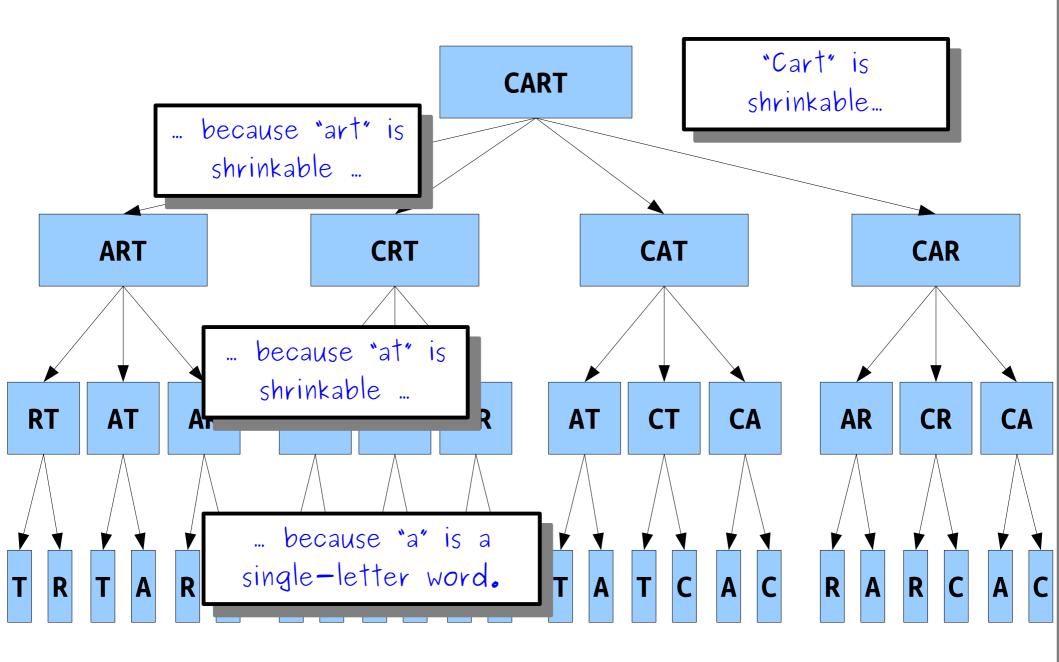
S I N G

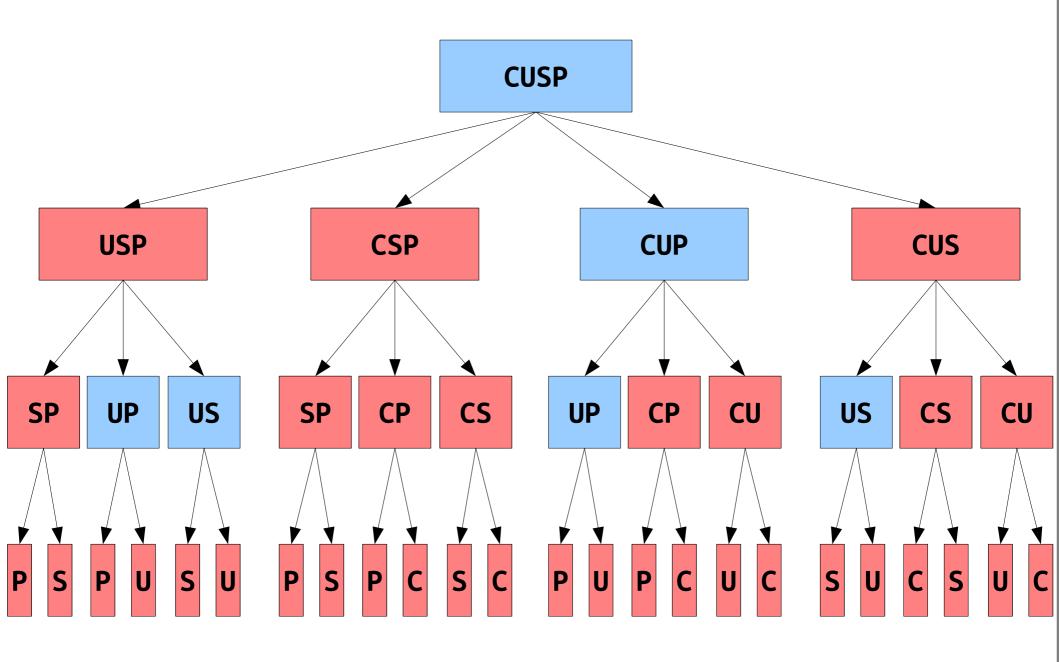
SIN

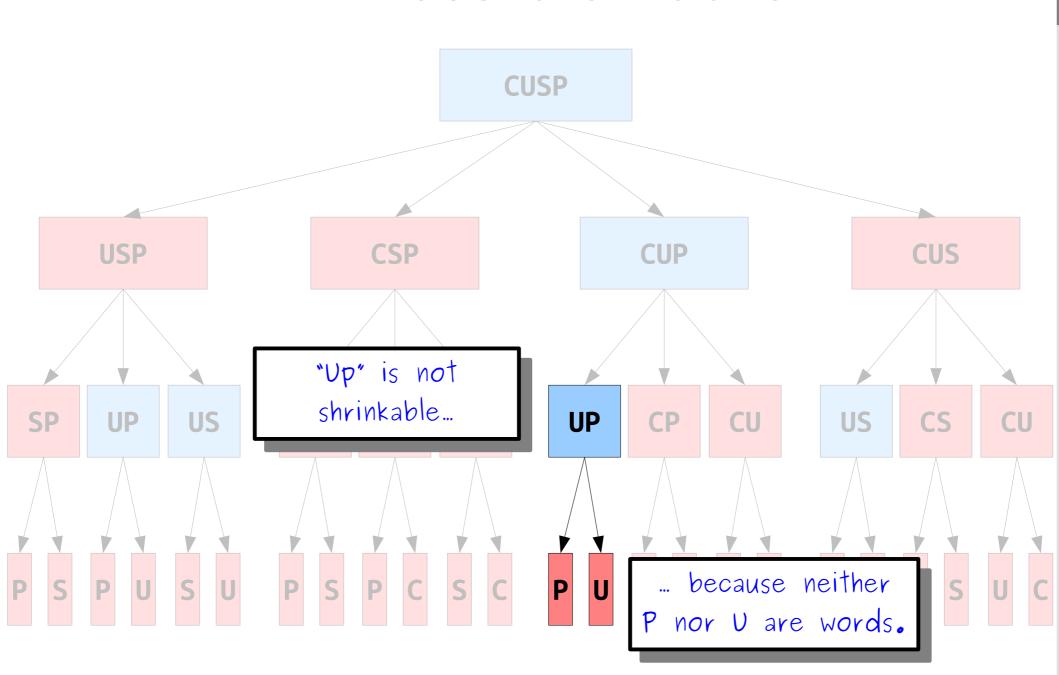
IN

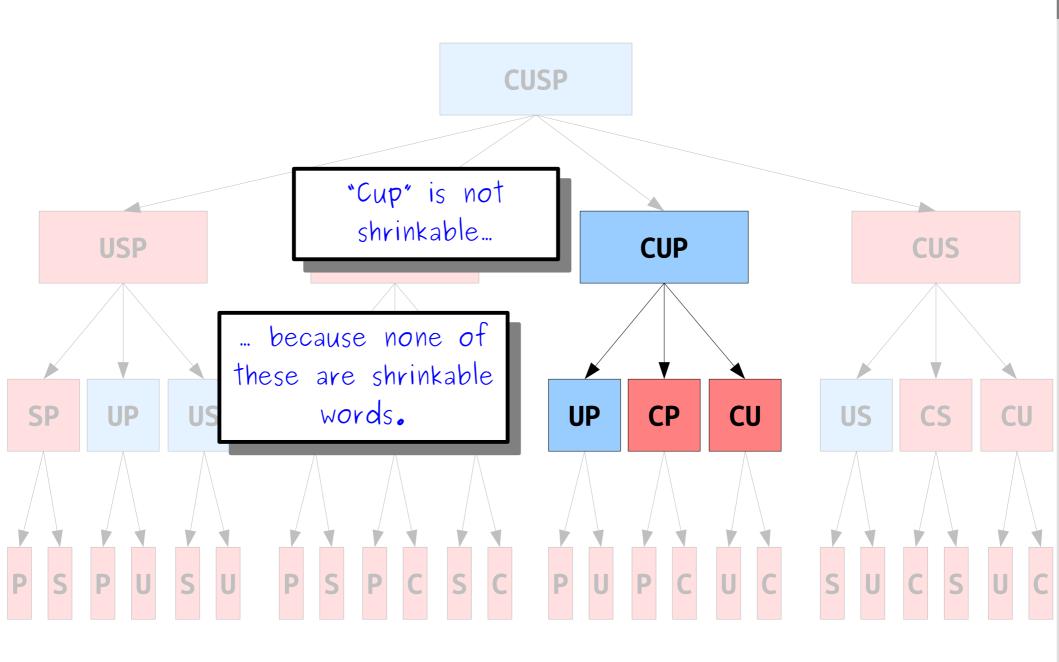
Ι

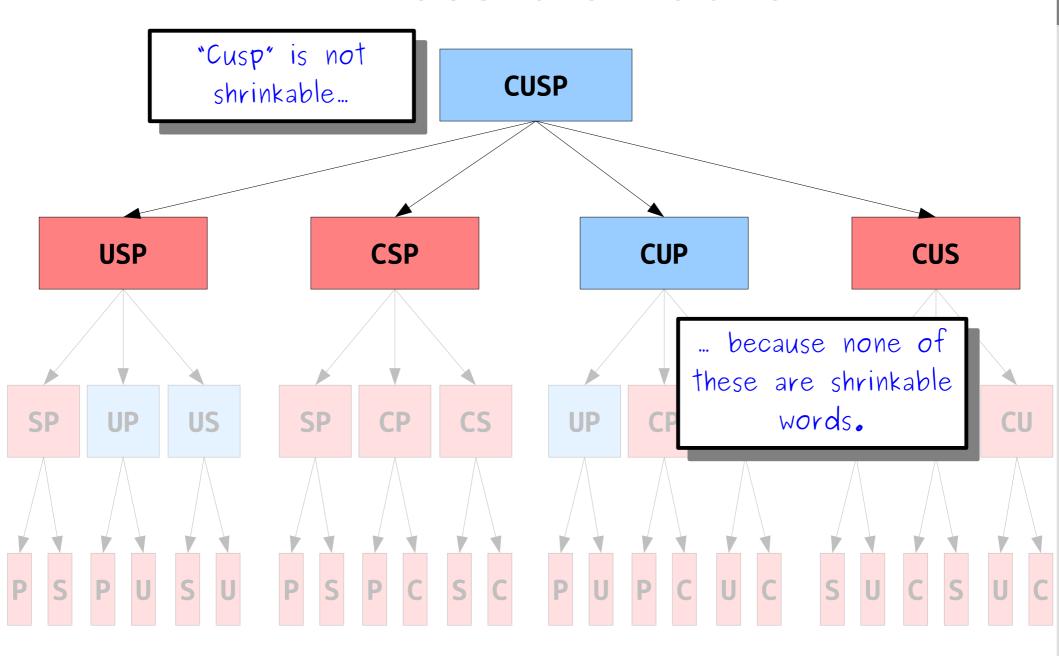
Is there *really* just one nine-letter word with this property?











Shrinkable Words

• A *shrinkable word* is a word that can be reduced down to one letter by removing one character at a time, leaving a word at each step.

• Base Cases:

- A string that is not a word is not a shrinkable word.
- Any single-letter word is shrinkable (A, I, and O).

Recursive Step:

- A multi-letter word is shrinkable if you can remove a letter to form a shrinkable word.
- A multi-letter word is not shrinkable if no matter what letter you remove, it's not shrinkable.

Your Action Items

- Read Chapter 9 of the textbook.
 - There's tons of cool backtracking examples there, and it will help you prep for Friday.
- Keep working on Assignment 3.
 - If you're following our timetable, you should be working on "What Are YOU Doing?" See if you can finish it by Wednesday and start working on Shift Scheduling.
 - Ask for help if you need it! That's what we're all here for.

Next Time

• Output Parameters

 Recovering the solution to a backtracking problem.

More Backtracking

Techniques in searching for feasibility.

Closing Thoughts on Recursion

• It'll come back, but we're going to focus on other things for a while!