

# Programming Abstractions

CS106B

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# Topics:

- **LinkedList Applications, Algorithms, and Variants**
  - › Using a linked list for a queue
  - › Tail pointers
  - › The undo-enqueue operation
  - › Doubly-linked lists
- Preview of our next topic: Binary Search Trees
  - › Starting with a dream: binary search in a linked list?
  - › How our dream provided the inspiration for the BST

Fun fact: linked list algorithms are a classic technical job interview question category!

# Queue implementation with a linked list

REAL-WORLD APPLICATION OF  
LINKED LISTS

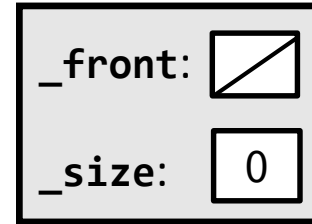


# linkedlist.h (for comparison—we will copy this design)

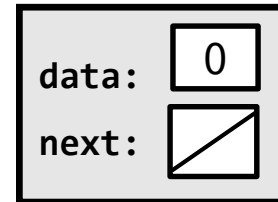
```
class LinkedList {
public:
    LinkedList();
    ~LinkedList();
    void add(int value);
    void clear();
    int get(int index) const;
    void insert(int index, int value);
    bool isEmpty() const;
    void remove(int index);
    void set(int index, int value);
    int size() const;

private:
    ListNode* _front;
    int _size;
};
```

LinkedList



struct LinkNode



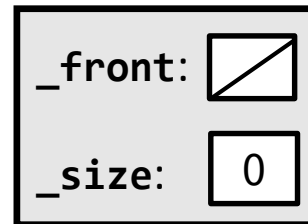
# queueLL.h [Version 1]

```
class QueueLL {  
public:  
    QueueLL();  
    ~QueueLL();  
    void enqueue(int value);  
    void clear();  
    int dequeue(int index);  
    int peek(int index) const;  
    bool isEmpty() const;  
    int size() const;  
  
private:  
    ListNode* _front;  
    int      _size;  
};
```

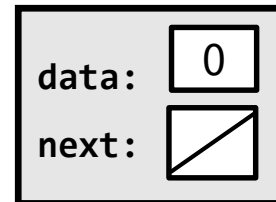
Public-facing methods are renamed and curated to provide the usual queue interface.

Internal structure is exactly the same as LinkedList class.

QueueLL

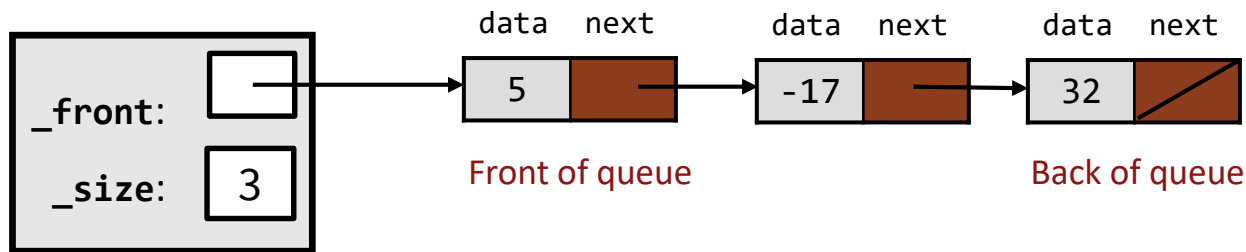


struct LinkNode



# Queue implemented with a linked list

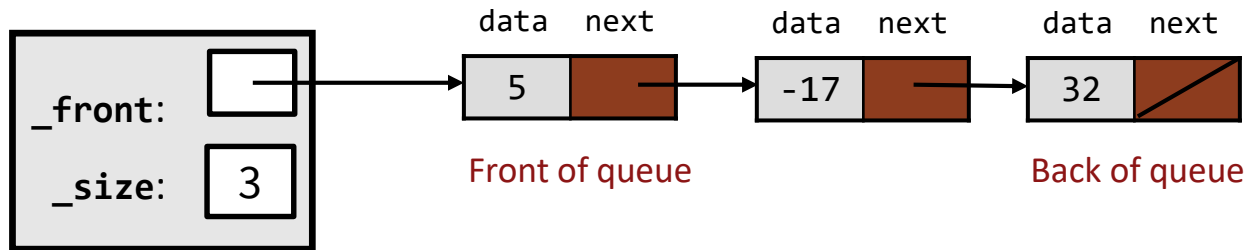
- Front of the list is the front of the queue
  - › Need to dequeue from here
  - › No problem! Unlike array  $O(N)$ , removing from the front of a linked list is just  $O(1)$
- Back of the list is the back of the queue
  - › Need to enqueue to here
  - › Hmm...not good.  $O(N)$  because we have to traverse in a loop to the end of the list



# Queue implemented with a linked list

- Front of the list is the front of the queue
  - › Need to dequeue from here
  - › No problem! Unlike array  $O(N)$ , removing from list is just  $O(1)$
- Back of the list is the back of the queue
  - › Need to enqueue to here
  - › Hmm...not good.  $O(N)$  because we have to traverse in a loop to the end of the list

**Key insight:** actual add is  $O(1)$ , it's just getting there that takes a long time.



## Tail Pointers

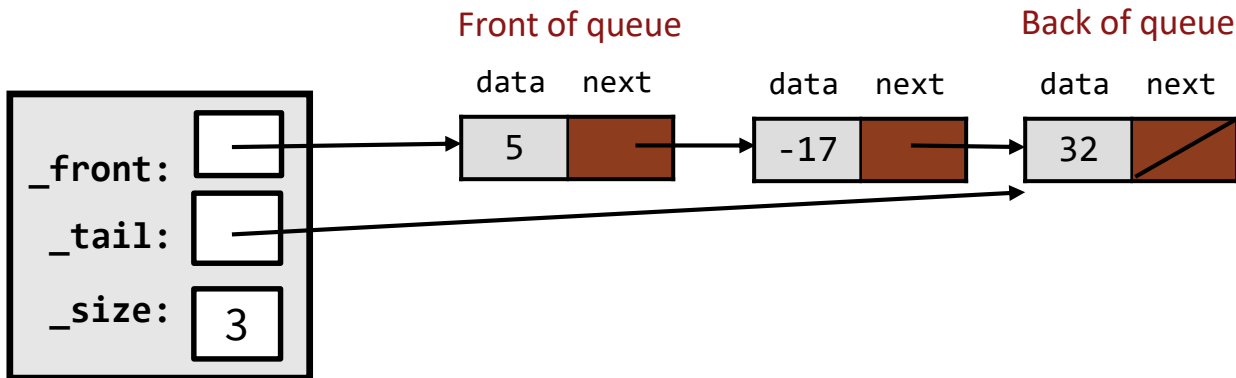
BONUS FEATURE TO IMPROVE  
LINKED LIST PERFORMANCE  
FOR APPLICATIONS LIKE  
QUEUE





## Queue implemented with a linked list with Tail Pointer

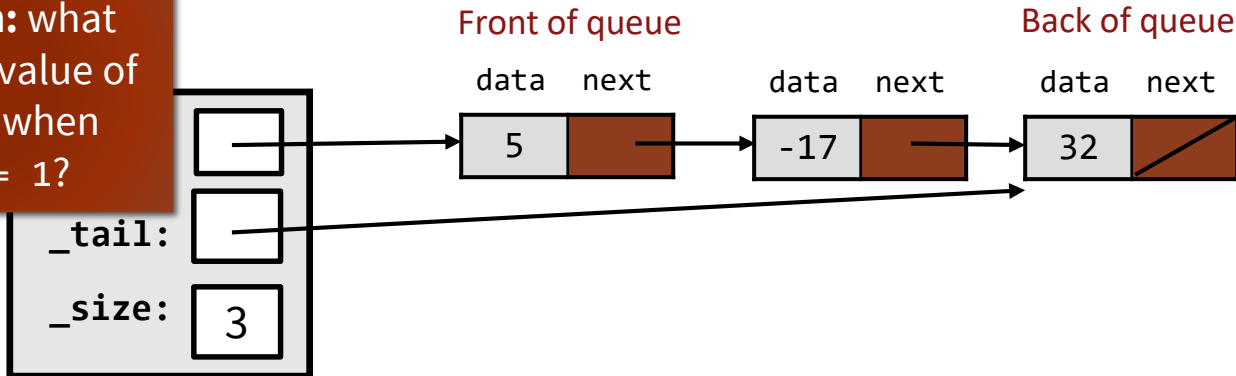
- We add a third private member variable to our LinkedList class
  - › `_front` enables dequeue in  $O(1)$
  - › `_tail` enables enqueue in  $O(1)$
  - › (`_size` stays the same)
  - › When `_size = 0`, `_front` and `_tail` will be both be `nullptr`



# Queue implemented with a linked list with Tail Pointer

- We add a third private member variable to our LinkedList class
  - › `_front` enables dequeue in  $O(1)$
  - › `_tail` enables enqueue in  $O(1)$
  - › (`_size` stays the same)
  - › When `_size = 0`, `_front` and `_tail` will be both be `nullptr`

**Your Turn:** what should the value of `_tail` be when `_size = 1`?

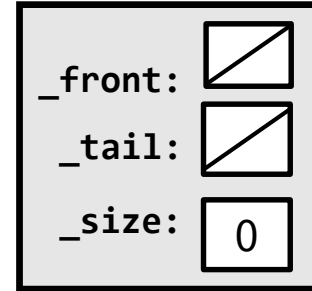


# queueLL.h [Version 2]

```
class QueueLL {  
public:  
    QueueLL();  
    ~QueueLL();  
    void enqueue(int value);  
    void clear();  
    int dequeue(int index);  
    int peek(int index) const;  
    bool isEmpty() const;  
    int size() const;  
  
private:  
    ListNode* _front;  
    ListNode* _tail;  
    int _size;  
};
```

New tail pointer member variable.

QueueLL



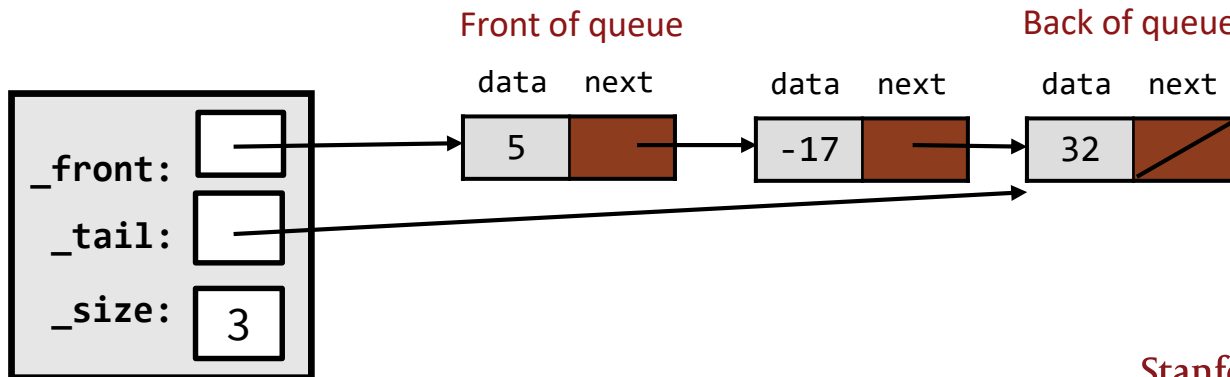
struct LinkNode



# Implementing enqueue

```
// Appends the given value to the end of the list.  
void QueueLL::enqueue(int value) {  
    ...  
}
```

- What pointer(s) must be changed to add a node to the **end** of a list?
- What different cases must we consider?



## Code for list add() compared to code for enqueue()

```
// (in linkedlist.cpp)
void LinkedList::add(int value)
{
    if (_front == nullptr) {
        // adding to an empty list
        _front = new ListNode(value);
    } else {
        // adding to the end of an existing list
        ListNode* current = _front;
        while (current->next != nullptr) {
            current = current->next;
        }
        current->next = new ListNode(value);
    }
    _size++;
}
```

```
// (in queueLL.cpp)
void QueueLL::enqueue(int value)
{
    if (_front == nullptr) {
        // adding to an empty list
        _front = new ListNode(value);
        _tail = _front;
    } else {
        // adding to the end of an existing list
        _tail->next = new ListNode(value);
        _tail = _tail->next;
    }
    _size++;
}
```

## Code for list add() compared to code for enqueue()

```
// (in linkedlist.cpp)
void LinkedList::add(int value)
{
    if (_front == nullptr) {
        // adding to an empty list
        _front = new ListNode(value);
    } else {
        // adding to the end of an existing list
        ListNode* current = _front;
        while (current->next != nullptr) {
            current = current->next;
        }
        current->next = new ListNode(value);
    }
    _size++;
}
```

```
// (in queueLL.cpp)
void QueueLL::enqueue(int value)
{
    if (_front == nullptr) {
        // adding to an empty list
        _front = new ListNode(value);
        _tail = _front;
    } else {
        // adding to the end of an existing list
        _tail->next = new ListNode(value);
        _tail = _tail->next;
    }
    _size++;
}
```

Don't need the loop anymore—just go straight to using the tail pointer.

## Implementing an undo-enqueue operation

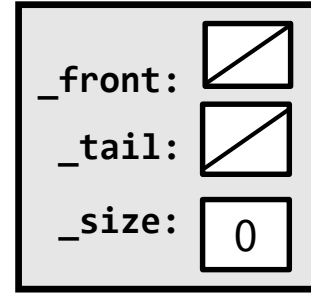
FOR THOSE “NEVERMIND,  
THIS RAMEN NAGI LINE IS TOO  
LONG, I’LL GO TO A  
DIFFERENT RESTAURANT!”  
MOMENTS



# queueLL.h [Version 3]

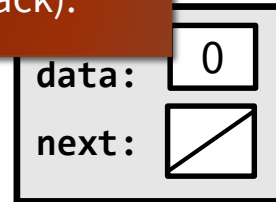
```
class QueueLL {  
public:  
    QueueLL();  
    ~QueueLL();  
    void enqueue(int value);  
    void clear();  
    int dequeue(int index);  
    int peek(int index) const;  
    bool isEmpty() const;  
    int size() const;  
    void undoEnqueue();  
  
private:  
    ListNode* _front;  
    ListNode* _tail;  
    int _size;  
};
```

QueueLL



This function would remove the most-recently-enqeued element (similar to pop in a stack).

Node

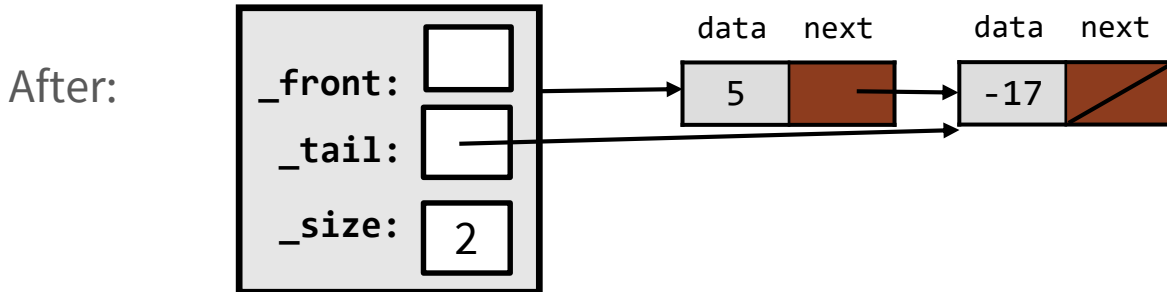
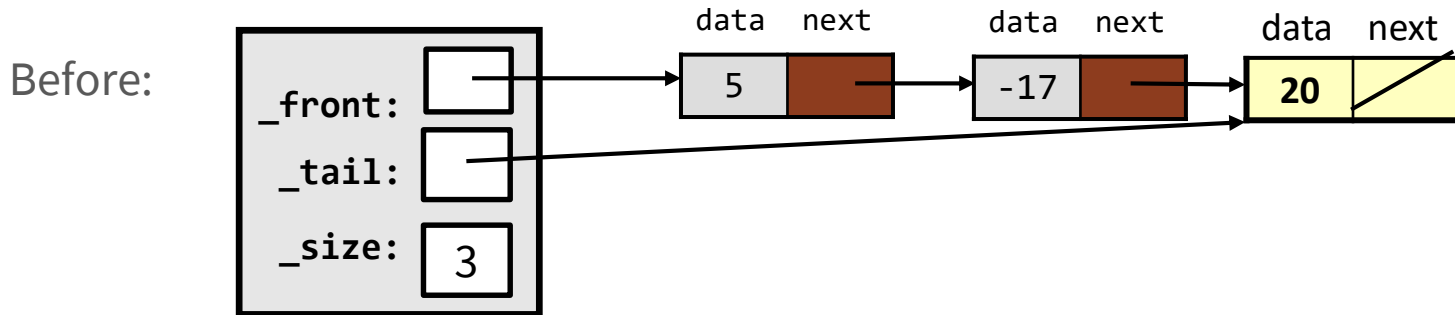




# Implementing a prepend operation

```
void QueueLL::undoEnqueue() {  
    ...  
}
```

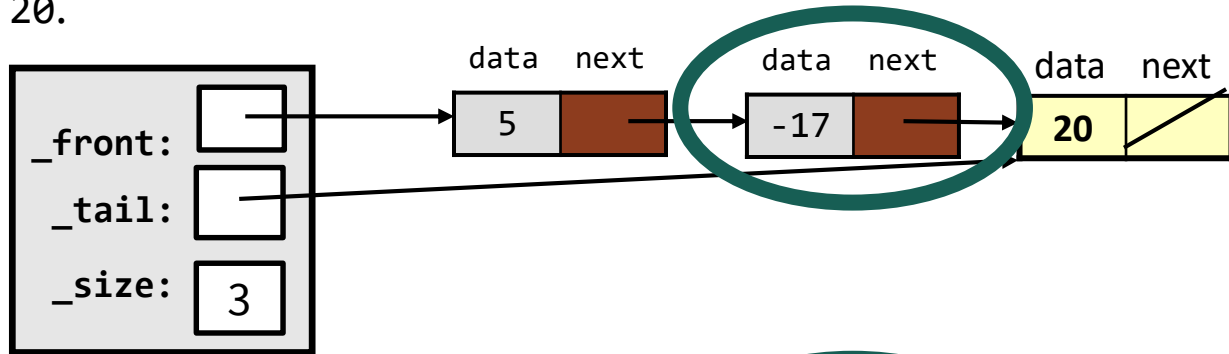
- Removes the most-recently-enqueued item.



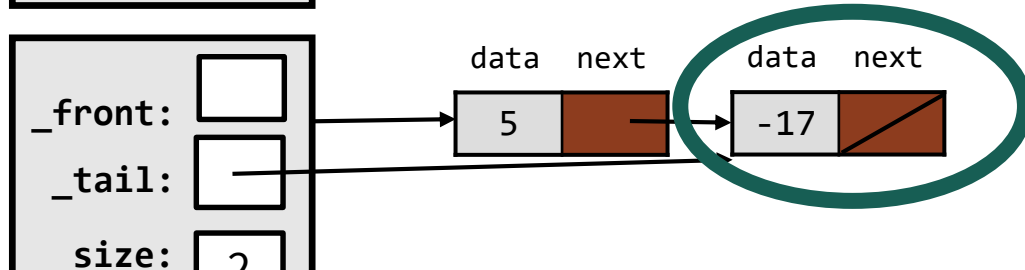
# Options for implementing a prepend operation

- Could just copy our code from `LinkedList remove(index)`, with `index` set to `size() - 1`, but this is  $O(N)$ .
  - › It's disheartening to see that our new `_tail` pointer doesn't help us. ☹️
- That's because the node whose next pointer needs to change is the one with `-17`, not `20`.

Before:



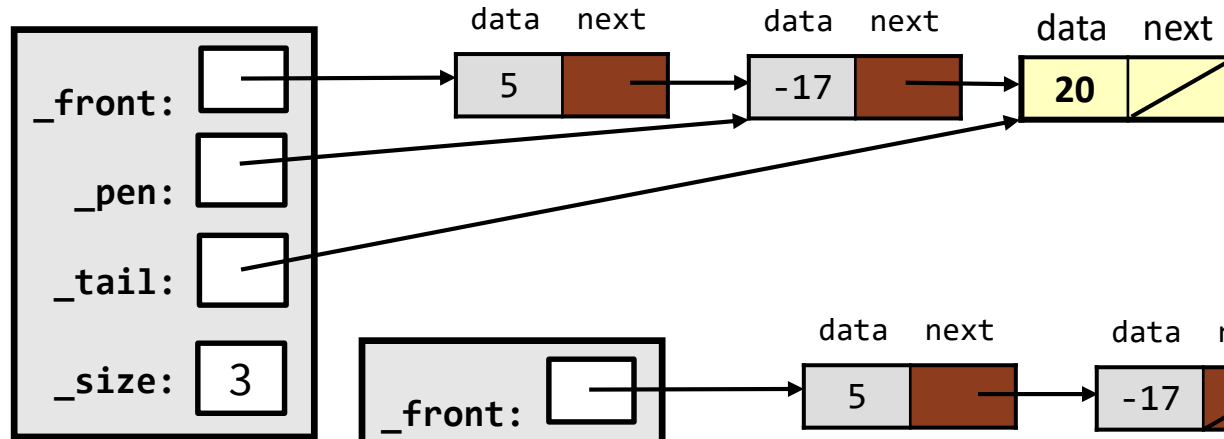
After:



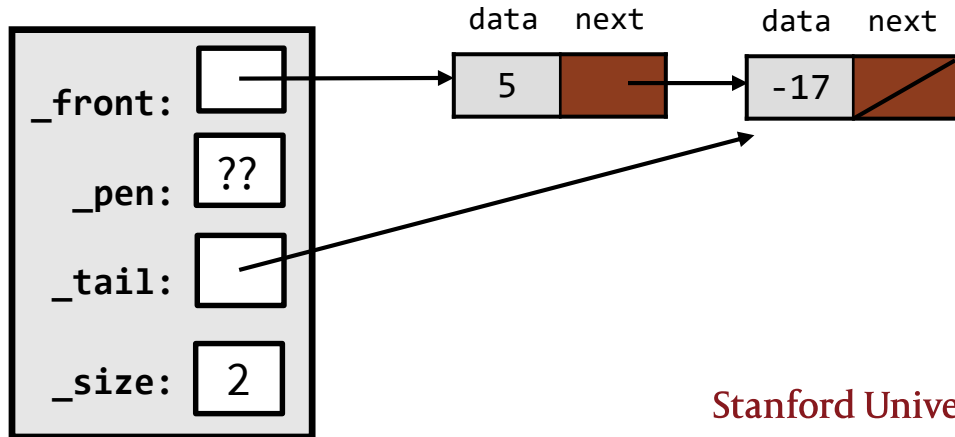
# More options for implementing a prepend operation?

- What if we add a penultimate-node pointer to our member variables?
  - It will point to the second-to-last element in the list.

Before:



After: our `_pen` pointer helps us get this far...  
...but what about the update to `_pen`?



# The Doubly-Linked List structure

ANOTHER VERY COMMON  
BONUS FEATURE TO IMPROVE  
LINKED-LIST PERFORMANCE

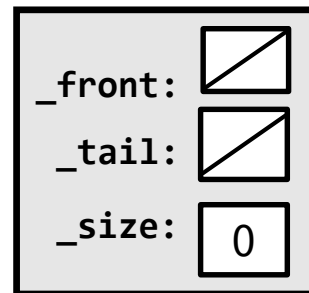


## queueLL.h [Version 3, again]

```
class QueueLL {
public:
    QueueLL();
    ~QueueLL();
    void enqueue(int value);
    void clear();
    int dequeue(int index);
    int peek(int index) const;
    bool isEmpty() const;
    int size() const;
    void undoEnqueue();

private:
    ListNode* _front;
    ListNode* _tail;
    int _size;
};
```

class QueueLL



struct LinkNode



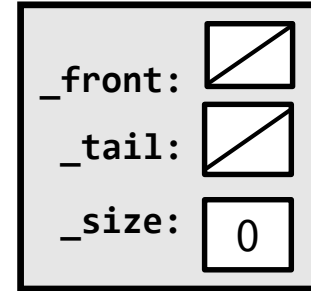
This time, instead of changing our list class, let's reconsider the node struct that we've been using all this time.

## queueLL.h [Version 4]

```
class QueueLL {
public:
    QueueLL();
    ~QueueLL();
    void enqueue(int value);
    void clear();
    int dequeue(int index);
    int peek(int index) const;
    bool isEmpty() const;
    int size() const;
    void undoEnqueue();

private:
    ListNode* _front;
    ListNode* _tail;
    int _size;
};
```

class QueueLL



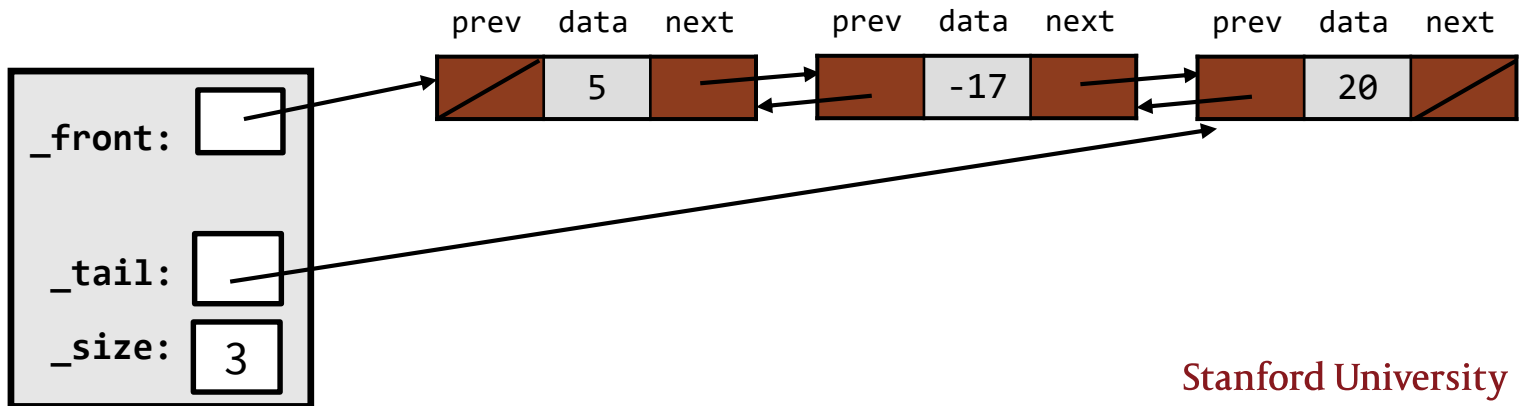
struct DoubleLinkNode



Now each node will have two pointers: a previous and a next.

# Doubly-Linked List

- Benefits:
  - › Easy access to nodes before your node, when needed for edits
- Drawbacks:
  - › Linked list already roughly doubles amount of storage needed to hold our data (compared to array), now doubly-linked list triples it
  - › More work in every add, remove, insert, etc operation to maintain correct pointer placements



# Implementing an undo-enqueue operation (now lets do it)

FOR THOSE “NEVERMIND,  
THIS RAMEN NAGI LINE IS TOO  
LONG, I’LL GO TO A  
DIFFERENT RESTAURANT!”  
MOMENTS

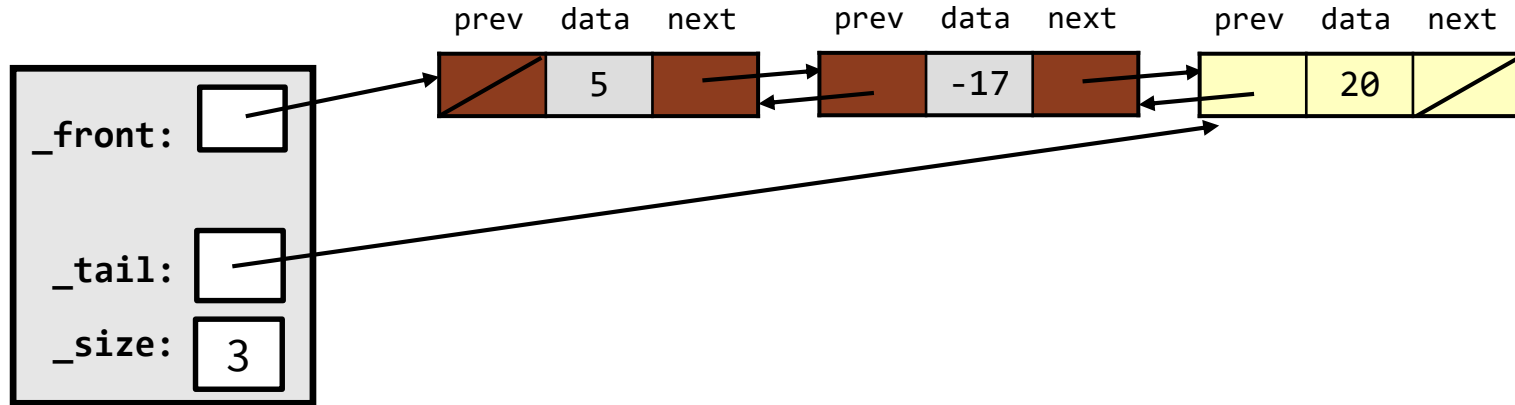




# Implementing a prepend operation

```
void QueueLL::undoEnqueue() {  
    ...  
}
```

- What pointer(s) must be changed to remove the node at the the **end** of a list?
- What different cases must we consider?



# Implementing a prepend operation

```
void QueueLL::undoEnqueue() {
    if (size() == 0) {
        error("Cannot remove from empty queue!");
    }

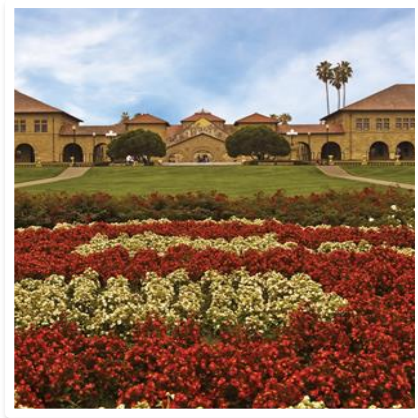
    DoubleLinkNode* trash = _tail;
    if (size() == 1) {
        _tail = _front = nullptr;
    } else {
        _tail->prev->next = nullptr;
        _tail = _tail->prev;
    }
    delete trash;
    _size--;
}
```

# SWITCHING GEARS!

Preview of our next topic: Binary Search Tree

# Binary Search in a Linked List?

EXPLORING A GOOD IDEA,  
FINDING WAY TO MAKE IT  
WORK



## Recall our beautiful algorithm: binary search!

0	1	2	3	4	5	6	7	8	9	10
2	7	8	13	25	29	33	51	89	90	95

- How long does it take us to find data in a sorted **array**?
  - › **Use binary search!**
  - ›  **$O(\log n)$** : awesome!!

## Q. Can we do binary search on a linked list?

A. No.

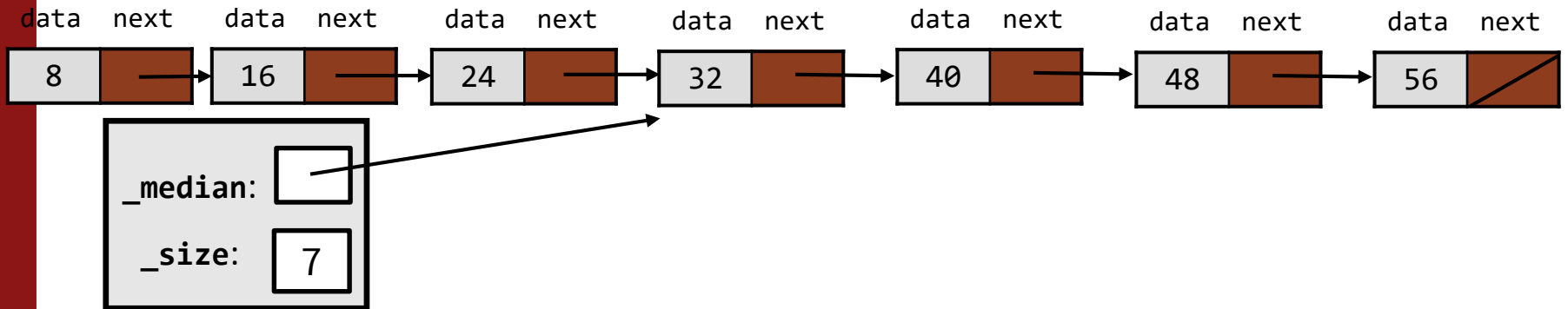
- The nodes are spread all over memory, and we must follow “next” pointers one at a time to navigate (the treasure hunt).
- **Therefore cannot jump right to the middle.**
- **Therefore cannot do binary search.**
- **Find is  $O(N)$ :** not terrible, but pretty bad compared to  $O(\log n)$  or  $O(1)$

**Let's brainstorm a wild idea and then see if we can make it work**

## “What if...?”

# The inspiration for Binary Search Trees

- What if...
- ...instead of having a `_front` pointer in our linked list, we had a pointer to the element we want to look at first in binary search: the exact median/middle element?

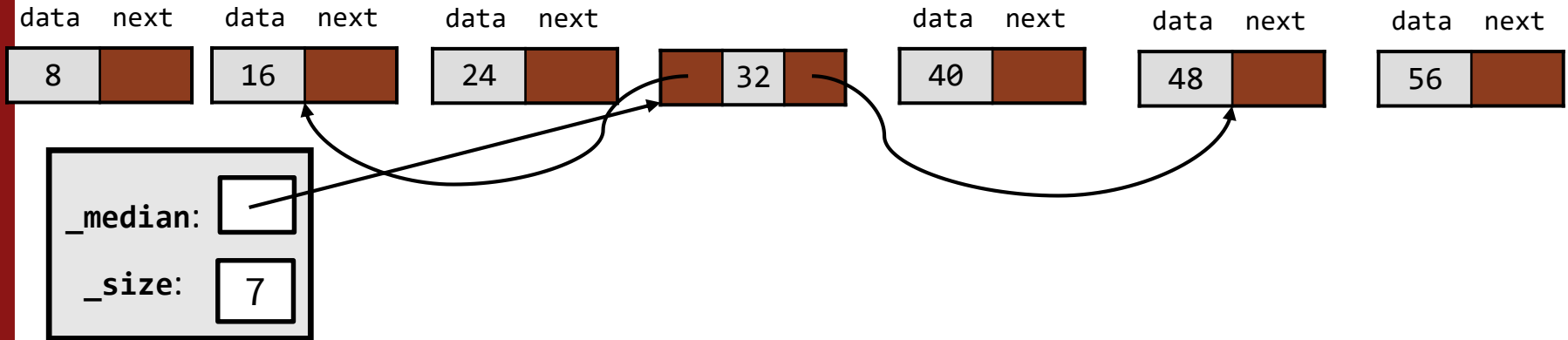


- That would make the first step of our binary search **really** fast/easy!
- What about the next step? (and the front half of our list, lol)

## “What if...?”

# The inspiration for Binary Search Trees

- What about the next step? (and the front half of our list, lol)
- Well, we could have the middle element point to the middle element of both the left half and the right half, so the 2<sup>nd</sup> step of our binary search is easy/fast too!



- Keep doing this until all elements have pointers to the middle of what remains to their left/right sides...voila!



## An Idealized Binary Search Tree

- Our class will have a pointer to the median element\*, and each element has pointers to the medians of everything to their left and right
  - \* *actually it's hard to guarantee it will be the exact middle element, more on this, and lots more about Binary Search Trees, next time!*

