Programming Abstractions

CS106X

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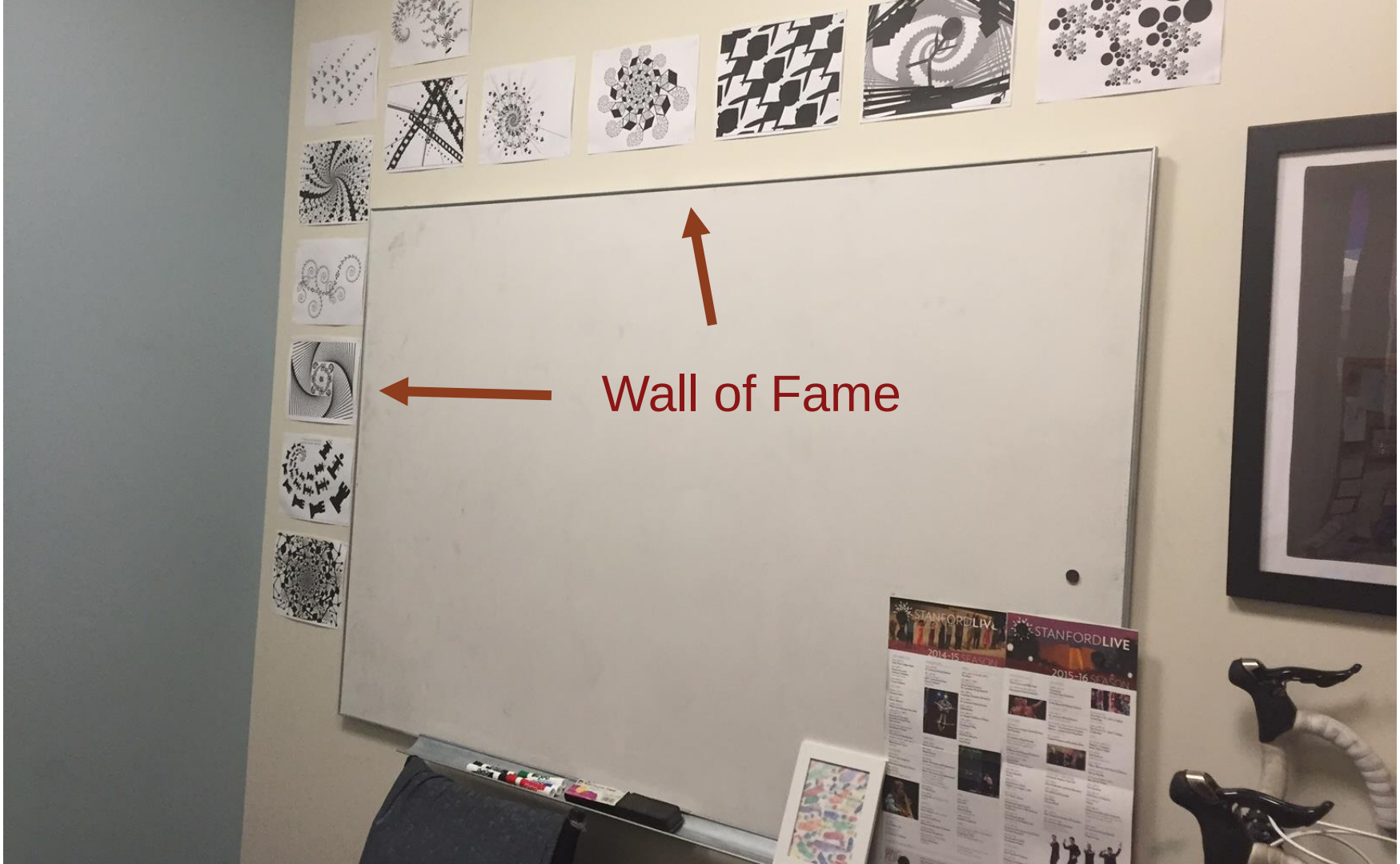
Today's topics:

- Previous lectures:
  - Introduction to recursion with Factorial
  - Mechanics of recursion: looking at the stack frames
  - Classic, widely-used CS algorithm example: Binary Search
  - Visual example: Boxy "snowflake" fractal
- Today:
  - New patterns of recursion application: adding loops
    - Loops + recursion for *generating permutations*
    - Loops + recursion for *recursive backtracking*

Announcement: Recursive art contest!

- Go to http://recursivedrawing.com/
- Make recursive art
  - Win prizes!
- Come to my office hours and see my Wall of Fame of past recursive art submissions!
- Submission deadline:
  - Wednesday of Week 4 (October 14)
- Submission procedure:
  - Email me: cbl@stanford.edu


Wall of Fame
STANFORDLIVE
2014-15 SEASON
STANFORDLIVE
2015-16 SEASON

Backtracking

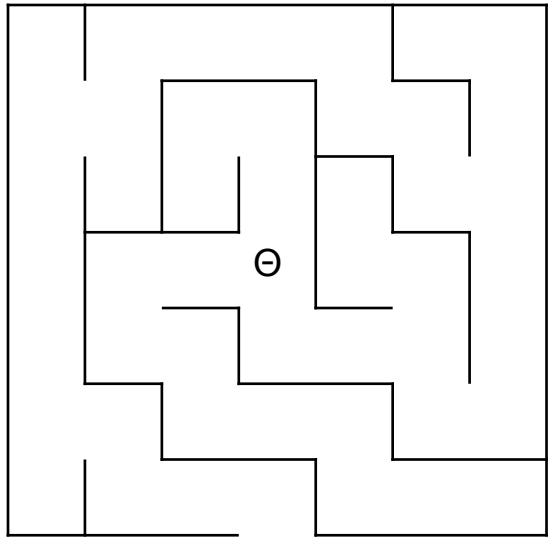
Maze solving

Backtracking

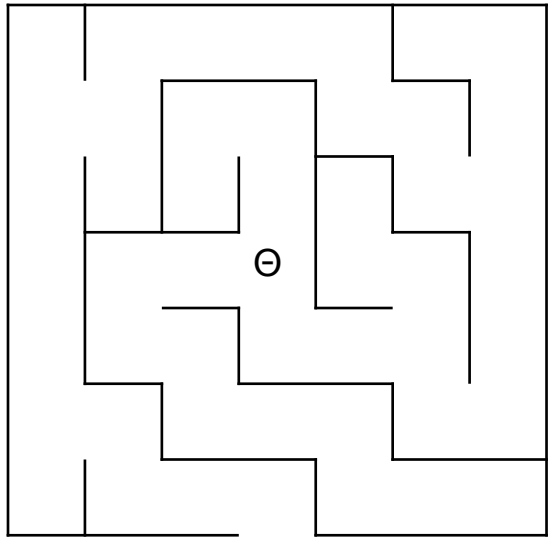
A particular behavior in recursive code where you tentatively explore many options, and recover to the nearest junction when you hit a “dead end”

The easiest way to understand this is probably to see literal exploration and dead ends

Maze-solving



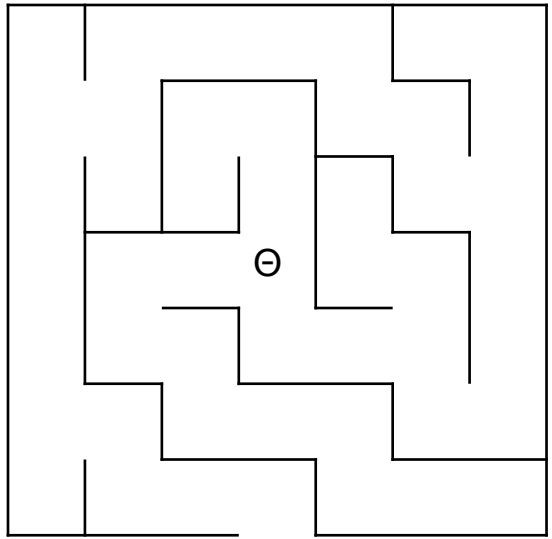
Maze-solving



Thinking through the pseudo-code:

- From position Θ, what does it mean for a step North to be a good idea?

Maze-solving



Thinking through the pseudo-code:

- From position Θ, what does it mean for a step South to be a good idea?
- It means that from position one-step-South-of-Θ, there exists some step that is a good idea…
- …Recursion!

Backtracking template

- **bool recursiveFunction(){**
  - Base case test for success: return true
  - Base case test for failure: return false
  - Loop over several options for “what to do next”:
    - Tentatively “do” one option
    - if (recursiveFunction()) return true
    - That tentative idea didn’t work, so “undo” that option
  - None of the options we tried in the loop worked, so return false

SolveMaze code

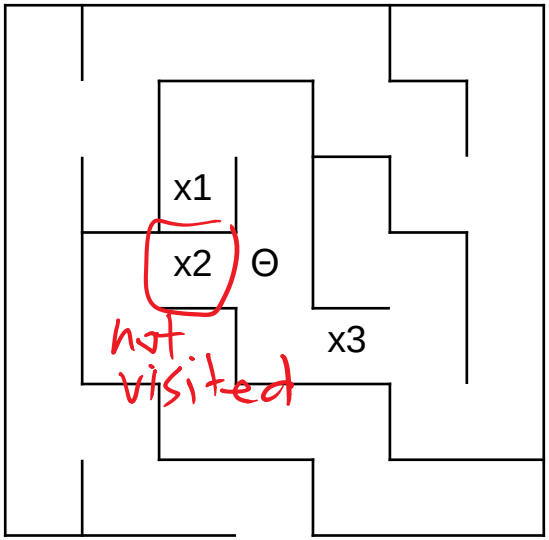
Adapted from the textbook by Eric Roberts

```
bool solveMaze(Maze & maze, Point start) {
   if (maze.isOutside(start)) return true;
   if (maze.isMarked(start)) return false;
   maze.markSquare(start);
   pause(200);
   for (Direction dir = NORTH; dir <= WEST; dir++) {
      if (!maze.wallExists(start, dir)) {
         if (solveMaze(maze, adjacentPoint(start, dir))) {
            return true;
         }
      }
   }
   maze.unmarkSquare(start);
   return false;
}
```

```
enum Direction =
{NORTH, EAST, SOUTH,
WEST};
```

```
//order of for loop:
enum Direction =
{NORTH, EAST, SOUTH, WEST};
```

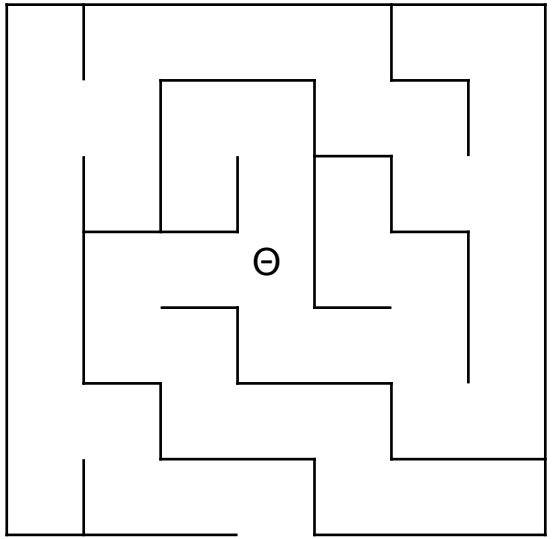
Maze-solving



In what order do we visit these spaces?

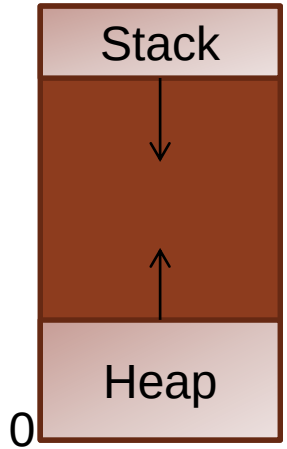
A. x1, x2, x3
B. x2, x3, x1
C. x1, x3, x2
D. We don't visit all three
E. Other/none/more

The stack



What is the deepest the Stack gets (number of stack frames) during the solving of this maze?

A. Less than 5
B. 5-10
C. 11-20
D. More than 20
E. Other/none/more



Contrast: Recursive maze-solving vs. Word ladder

- With word ladder, you did **breadth-first search**
- This problem uses **depth-first search**

- Both are possible for maze-solving!

- The contrast between these approaches is a theme that you'll see again and again in your CS career