CS107 Lecture 2 Bits and Bytes; Integer Representations

reading: Bryant & O'Hallaron, Ch. 2.2-2.3

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<u>CS107 Topic 1</u>: How can a computer represent integer numbers?

Demo: Unexpected Behavior



cp -r /afs/ir/class/cs107/lecture-code/lect2 .

Lecture Plan

- Bits and Bytes
- Hexadecimal
- Integer Representations
- Unsigned Integers
- Signed Integers
- Overflow
- Casting and Combining Types

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Bits

• Computers are built around the idea of two states: "on" and "off". Transistors represent this in hardware, and bits represent this in software!



One Bit At A Time

- We can combine bits, like with base-10 numbers, to represent more data. 8
 bits = 1 byte.
- Computer memory is just a large array of bytes! It is *byte-addressable*; you can't address (store location of) a bit; only a byte.
- Computers still fundamentally operate on bits; we have just gotten more creative about how to represent different data as bits!
 - Images
 - Audio
 - Video
 - Text
 - And more...

5934

Digits 0-9 (0 to base-1)



= 5*1000 + 9*100 + 3*10 + 4*1

5 9 3 4 10^X: 3 2 1 0



1 0 1 1 2^x: 3 2 1 0

Digits 0-1 (0 to base-1)



1 0 1 1 2³ 2² 2¹ 2⁰





$$=$$
 1*8 + **0***4 + **1***2 + **1***1 = 11₁₀

- Strategy:
 - What is the largest power of $2 \le 6$?

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- Strategy:
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 - Now, what is the largest power of $2 \le 6 2^2$?



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Practice: Base 2 to Base 10

What is the base-2 value 1010 in base-10?

- a) 20
- b) 101
- c) 10
- d) 5
- e) Other

Practice: Base 10 to Base 2

What is the base-10 value 14 in base 2?

- a) 1111
- b) 1110
- c) 1010
- d) Other

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1111111 2x: 7 6 5 4 3 2 1 0

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1111111 2x: 7 6 5 4 3 2 1 0

• Strategy 1: $1^{*}2^{7} + 1^{*}2^{6} + 1^{*}2^{5} + 1^{*}2^{4} + 1^{*}2^{3} + 1^{*}2^{2} + 1^{*}2^{1} + 1^{*}2^{0} = 255$

What is the minimum and maximum base-10 value a single byte (8 bits) can store?
 minimum = 0
 maximum = 255

1111111 2x: 7 6 5 4 3 2 1 0

- Strategy 1: $1^{*}2^{7} + 1^{*}2^{6} + 1^{*}2^{5} + 1^{*}2^{4} + 1^{*}2^{3} + 1^{*}2^{2} + 1^{*}2^{1} + 1^{*}2^{0} = 255$
- **Strategy 2:** 2⁸ − 1 = 255

Multiplying by Base

$1450 \times 10 = 1450$ $1100_2 \times 2 = 1100$

Key Idea: inserting 0 at the end multiplies by the base!

Dividing by Base

1450 / 10 = 145 $1100_2 / 2 = 110$

Key Idea: removing 0 at the end divides by the base!

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Hexadecimal

- When working with bits, oftentimes we have large numbers with 32 or 64 bits.
- Instead, we'll represent bits in *base-16 instead;* this is called **hexadecimal**.



Hexadecimal

- When working with bits, oftentimes we have large numbers with 32 or 64 bits.
- Instead, we'll represent bits in *base-16 instead;* this is called **hexadecimal**.



Each is a base-16 digit!

Hexadecimal

• Hexadecimal is *base-16*, so we need digits for 1-15. How do we do this?

0 1 2 3 4 5 6 7 8 9 a b c d e f 10 11 12 13 14 15
Hexadecimal

Hex digit	0	1	2	3	4	5	6	7
Decimal value	0	1	2	3	4	5	6	7
Binary value	0000	0001	0010	0011	0100	0101	0110	0111
Hex digit	8	9	Α	В	С	D	Е	F
Decimal value	8	9	10	11	12	13	14	15
Binary value	1000	1001	1010	1011	1100	1101	1110	1111

Hexadecimal

- We distinguish hexadecimal numbers by prefixing them with **0x**, and binary numbers with **0b**.
- E.g. **0xf5** is **0b11110101**



Practice: Hexadecimal to Binary

What is **0x173A** in binary?

Hexadecimal173ABinary0001011100111010

Practice: Hexadecimal to Binary

What is **0b1111001010** in hexadecimal? (*Hint: start from the right*)

Binary	11	1100	1010
Hexadecimal	3	С	Α

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Number Representations

- Unsigned Integers: positive and 0 integers. (e.g. 0, 1, 2, ... 99999...
- Signed Integers: negative, positive and 0 integers. (e.g. ...-2, -1, 0, 1,... 9999...)
- Floating Point Numbers: real numbers. (e,g. 0.1, -12.2, 1.5x10¹²)

Number Representations

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- Floating Point Numbers: real numbers. (e,g. 0.1, -12.2, 1.5x10¹²)
 Look up IEEE floating point if you're interested!

Number Representations

C Declaration	Size (Bytes)
int	4
double	8
float	4
char	1
char *	8
short	2
long	8

In The Days Of Yore...

C Declaration	Size (Bytes)
int	4
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float	4
char	1
char *	4
short	2
long	4

Transitioning To Larger Datatypes



- Early 2000s: most computers were 32-bit. This means that pointers were 4 bytes (32 bits).
- 32-bit pointers store a memory address from 0 to 2³²-1, equaling 2³² bytes of addressable memory. This equals 4 Gigabytes, meaning that 32-bit computers could have at most 4GB of memory (RAM)!
- Because of this, computers transitioned to **64-bit**. This means that datatypes were enlarged; pointers in programs were now **64 bits**.
- 64-bit pointers store a memory address from 0 to 2⁶⁴-1, equaling 2⁶⁴ bytes of addressable memory. This equals 16 Exabytes, meaning that 64-bit computers could have at most 1024*1024*1024 GB of memory (RAM)!

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Unsigned Integers

- An **unsigned** integer is 0 or a positive integer (no negatives).
- We have already discussed converting between decimal and binary, which is a nice 1:1 relationship. Examples:

0b0001 = 1

- 0b0101 = 5
- 0b1011 = 11

0b1111 = 15

The range of an unsigned number is 0 → 2^w - 1, where w is the number of bits.
 E.g. a 32-bit integer can represent 0 to 2³² - 1 (4,294,967,295).

Unsigned Integers



Let's Take A Break

To ponder during the break:

A **signed** integer is a negative, 0, or positive integer. How can we represent both negative *and* positive numbers in binary?

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Signed Integers

- A **signed** integer is a negative integer, 0, or a positive integer.
- *Problem:* How can we represent negative *and* positive numbers in binary?

Signed Integers

- A **signed** integer is a negative integer, 0, or a positive integer.
- *Problem:* How can we represent negative *and* positive numbers in binary?

Idea: let's reserve the *most* significant bit to store the sign.



0000

positive 0





- $1\ 000 = -0$ $0\ 000 = 0$
- $1\ 001 = -1$ $0\ 001 = 1$
- 1 010 = -2 0 010 = 2
- 1011 = -3 0011 = 3
- 1 100 = -4 0 100 = 4
- 1 101 = -5 0 101 = 5
- 1 110 = -6 0 110 = 6
- 1 111 = -7 0 111 = 7
- We've only represented 15 of our 16 available numbers!

- Pro: easy to represent, and easy to convert to/from decimal.
- Con: +-0 is not intuitive
- Con: we lose a bit that could be used to store more numbers
- **Con:** arithmetic is tricky: we need to find the sign, then maybe subtract (borrow and carry, etc.), then maybe change the sign. This complicates the hardware support for something as fundamental as addition.



• Ideally, binary addition would *just work* **regardless** of whether the number is positive or negative.



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$\begin{array}{r} 0101 \\ +1011 \\ \hline 0000 \\ \end{array}$

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 $\begin{array}{c} 0011 \\ +1101 \\ \hline 0000 \end{array}$

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$\begin{array}{c} 0000\\ +0000\\ 0000\\ 0000\end{array}$

Decimal	Positive	Negative
0	0000	0000
1	0001	1111
2	0010	1110
3	0011	1101
4	0100	1100
5	0101	1011
6	0110	1010
7	0111	1001

Decimal	Positive	Negative
8	1000	1000
9	1001 (same as -7!)	NA
10	1010 (same as -6!)	NA
11	1011 (same as -5!)	NA
12	1100 (same as -4!)	NA
13	1101 (same as -3!)	NA
14	1110 (same as -2!)	NA
15	1111 (same as -1!)	NA

There Seems Like a Pattern Here...

$\begin{array}{ccccccc} 0101 & 0011 & 0000 \\ +1011 & +1101 & +0000 \\ \hline 0000 & 0000 & 0000 \end{array}$

• The negative number is the positive number inverted, plus one!

There Seems Like a Pattern Here...

A binary number plus its inverse is all 1s.

Add 1 to this to carry over all 1s and get 0!

 $\begin{array}{c} 0101 \\ +1010 \\ \hline 1111 \end{array}$

1111 +0001 00000

Another Trick

• To find the negative equivalent of a number, work right-to-left and write down all digits *through* when you reach a 1. Then, invert the rest of the digits.

100100 +??????? 0000000

Another Trick

• To find the negative equivalent of a number, work right-to-left and write down all digits *through* when you reach a 1. Then, invert the rest of the digits.

100100 +??100 000000

Another Trick

• To find the negative equivalent of a number, work right-to-left and write down all digits *through* when you reach a 1. Then, invert the rest of the digits.

$\begin{array}{c} 100100\\ + 011100\\ \hline 000000 \end{array}$

Two's Complement



Two's Complement

- In two's complement, we represent a positive number as itself, and its negative equivalent as the two's complement of itself.
- The **two's complement** of a number is the binary digits inverted, plus 1.
- This works to convert from positive to negative, and back from negative to positive!



Two's Complement

- Con: more difficult to represent, and difficult to convert to/from decimal and between positive and negative.
- **Pro:** only 1 representation for 0!
- **Pro:** all bits are used to represent as many numbers as possible
- **Pro:** the most significant bit still indicates the sign of a number.
- Pro: addition works for any combination of positive and negative!


Two's Complement

• Adding two numbers is just...adding! There is no special case needed for negatives. E.g. what is 2 + -5?

0010 2 +1011 -5 1101 -3

Two's Complement

 Subtracting two numbers is just performing the two's complement on one of them and then adding. E.g. 4 – 5 = -1.



Practice: Two's Complement

What are the negative or positive equivalents of the numbers below?

- a) -4 (1100)
- b) 7 (0111)
- c) 3 (0011)
- d) -8 (1000)

Practice: Two's Complement

What are the negative or positive equivalents of the numbers below?

- a) -4 (1100)
- b) 7 (0111)
- c) 3 (0011)



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Overflow

• If you exceed the **maximum** value of your bit representation, you wrap around or overflow back to the **smallest** bit representation.

0b1111 + 0b1 = 0b0000

• If you go below the **minimum** value of your bit representation, you *wrap* around or overflow back to the **largest** bit representation.

0b0000 - 0b1 = 0b1111

Min and Max Integer Values

Туре	Size (Bytes)	Minimum	Maximum
char	1	-128	127
unsigned char	1	0	255
short	2	-32768	32767
unsigned short	2	0	65535
int	4	-2147483648	2147483647
unsigned int	4	0	4294967295
long	8	-9223372036854775808	9223372036854775807
unsigned long	8	0	18446744073709551615

Min and Max Integer Values

INT_MIN, INT_MAX, UINT_MAX, LONG_MIN, LONG_MAX, ULONG_MAX, ...

Overflow



Overflow

At which points can overflow occur for signed and unsigned int? (assume binary values shown are all 32 bits)

- A. Signed and unsigned can both overflow at points X and Y
- B. Signed can overflow only at X, unsigned only at Y
- C. Signed can overflow only at Y, unsigned only at X
- D. Signed can overflow at X and Y, unsigned only at X
- E. Other



Unsigned Integers



Signed Numbers



Overflow In Practice: PSY

PSY - GANGNAM STYLE (강남스타일) M/V	
officialpsy 🖾	
Subscribe 7,600,830	-2142584554
🕂 Add to < Share ••• More	8,761,309 🗭 1,139,933

YouTube: "We never thought a video would be watched in numbers greater than a 32-bit integer (=2,147,483,647 views), but that was before we met PSY. "Gangnam Style" has been viewed so many times we had to upgrade to a 64-bit integer (9,223,372,036,854,775,808)!"

Overflow In Practice: Timestamps

- Many systems store timestamps as the number of seconds since Jan. 1, 1970 in a signed 32-bit integer.
- **Problem:** the latest timestamp that can be represented this way is 3:14:07 UTC on Jan. 13 2038!

Overflow In Practice: Gandhi

- In the game "Civilization", each civilization leader had an "aggression" rating. Gandhi was meant to be peaceful, and had a score of 1.
- If you adopted "democracy", all players' aggression reduced by 2. Gandhi's went from 1 to **255**!
- Gandhi then became a big fan of nuclear weapons.



https://kotaku.com/why-gandhi-is-such-an-asshole-in-civilization-1653818245

Overflow in Practice:

- Pacman Level 256
- Make sure to reboot Boeing Dreamliners every 248 days
- Comair/Delta airline had to <u>cancel thousands of flights</u> days before Christmas
- <u>Reported vulnerability CVE-2019-3857</u> in libssh2 may allow a hacker to remotely execute code
- Donkey Kong Kill Screen

Demo Revisited: Unexpected Behavior



airline.c

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printf and Integers

- There are 3 placeholders for 32-bit integers that we can use:
 - %d: signed 32-bit int
 - %u: unsigned 32-bit int
 - %x: hex 32-bit int
- The placeholder—not the expression filling in the placeholder—dictates what gets printed!

Casting

 What happens at the byte level when we cast between variable types? The bytes remain the same! This means they may be interpreted differently depending on the type.

This prints out: "v = -12345, uv = 4294954951". Why?

Casting

 What happens at the byte level when we cast between variable types? The bytes remain the same! This means they may be interpreted differently depending on the type.

```
int v = -12345;
unsigned int uv = v;
printf("v = %d, uv = %u\n", v, uv);
```

The bit representation for -12345 is 0b**1111111111111100011111000111**.

If we treat this binary representation as a positive number, it's huge!

Casting



Expression	Туре	Evaluation	Correct?
0 == 0U			
-1 < 0			
-1 < 0U			
2147483647 > -			
2147483647 - 1			
2147483647U > -			
2147483647 - 1			
2147483647 >			
(int)2147483648U			
-1 > -2			
(unsigned) - 1 > -2			



Expression	Туре	Evaluation	Correct?
0 == 0U	Unsigned	1	yes
-1 < 0			
-1 < 0U			
2147483647 > -			
2147483647 - 1			
2147483647U > -			
2147483647 - 1			
2147483647 >			
(int)2147483648U			
-1 > -2			
(unsigned) - 1 > -2			



Expression	Туре	Evaluation	Correct?
0 == 0U	Unsigned	1	yes
-1 < 0	Signed	1	yes
-1 < OU			
2147483647 > -			
2147483647 - 1			
2147483647U > -			
2147483647 - 1			
2147483647 >			
(int)2147483648U			
-1 > -2			
(unsigned) - 1 > -2			



Expression	Туре	Evaluation	Correct?
0 == 0U	Unsigned	1	yes
-1 < 0	Signed	1	yes
-1 < 0U	Unsigned	0	No!
2147483647 > -			
2147483647 - 1			
2147483647U > -			
2147483647 - 1			
2147483647 >			
(int)2147483648U			
-1 > -2			
(unsigned) - 1 > -2			



Expression	Туре	Evaluation	Correct?
0 == 0U	Unsigned	1	yes
-1 < 0	Signed	1	yes
-1 < 0U	Unsigned	0	No!
2147483647 > - 2147483647 - 1	Signed	1	yes
2147483647U > - 2147483647 - 1			
2147483647 > (int)2147483648U			
-1 > -2			
(unsigned) - 1 > -2			



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0 == 0U	Unsigned	1	yes
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2147483647 > (int)2147483648U			
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(unsigned) - 1 > -2			



Expression	Туре	Evaluation	Correct?
0 == 0U	Unsigned	1	yes
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-1 < 0U	Unsigned	0	No!
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2147483647U > - 2147483647 - 1	Unsigned	0	No!
2147483647 > (int)2147483648U	Signed	1	No!
-1 > -2			
(unsigned) - 1 > -2			



Expression	Туре	Evaluation	Correct?
0 == 0U	Unsigned	1	yes
-1 < 0	Signed	1	yes
-1 < 0U	Unsigned	0	No!
2147483647 > - 2147483647 - 1	Signed	1	yes
2147483647U > - 2147483647 - 1	Unsigned	0	No!
2147483647 > (int)2147483648U	Signed	1	No!
-1 > -2	Signed	1	yes
(unsigned) - 1 > -2			



Туре	Evaluation	Correct?
Unsigned	1	yes
Signed	1	yes
Unsigned	0	No!
Signed	1	yes
Unsigned	0	No!
Signed	1	No!
Signed	1	yes
Unsigned	1	yes
	Type Unsigned Signed Unsigned Signed Signed Signed Unsigned	TypeEvaluationUnsigned1Signed1Unsigned0Signed1Unsigned0Signed1Unsigned1Signed1Signed1Unsigned1



- s3 > u3
- u2 > u4
- s2 > s4
- s1 > s2
- u1 > u2
- s1 > u3



- s3 > u3 true
- u2 > u4
- s2 > s4
- s1 > s2
- u1 > u2
- s1 > u3



- s3 > u3 true
- u2 > u4 true
- s2 > s4
- s1 > s2
- u1 > u2
- s1 > u3



- s3 > u3 true
- u2 > u4 true
- s2 > s4 false
- s1 > s2
- u1 > u2
- s1 > u3



- s3 > u3 true
- u2 > u4 true
- s2 > s4 false
- s1 > s2 true
- u1 > u2
- s1 > u3


Comparisons Between Different Types

Which many of the following statements are true? (assume that variables are set to values that place them in the spots shown)

- s3 > u3 true
- u2 > u4 true
- s2 > s4 false
- s1 > s2 true
- u1 > u2 true
- s1 > u3



Comparisons Between Different Types

Which many of the following statements are true? (assume that variables are set to values that place them in the spots shown)

- s3 > u3 true
- u2 > u4 true
- s2 > s4 false
- s1 > s2 true
- u1 > u2 true
- **s1 > u3 true**



Expanding Bit Representations

- Sometimes, we want to convert between two integers of different sizes (e.g. short to int, or int to long).
- We might not be able to convert from a bigger data type to a smaller data type, but we do want to always be able to convert from a **smaller** data type to a **bigger** data type.
- For unsigned values, we can add *leading zeros* to the representation ("zero extension")
- For signed values, we can repeat the sign of the value for new digits ("sign extension"
- Note: when doing <, >, <=, >= comparison between different size types, it will
 promote to the larger type.

Expanding Bit Representation

unsigned short s = 4;

```
// short is a 16-bit format, so
```

s = 0000 0000 0000 0100b

unsigned int i = s;

Expanding Bit Representation

short s = 4;

```
// short is a 16-bit format, so
```

 $s = 0000 \ 0000 \ 0000 \ 0100b$

int i = s;

— or —

Truncating Bit Representation

If we want to **reduce** the bit size of a number, C *truncates* the representation and discards the *more significant bits*.

```
int x = 53191;
short sx = x;
int y = sx;
```

What happens here? Let's look at the bits in x (a 32-bit int), 53191:

0000 0000 0000 0000 1100 1111 1100 0111

When we cast x to a short, it only has 16-bits, and C truncates the number:

1100 1111 1100 0111

This is -12345! And when we cast sx back an int, we sign-extend the number.

1111 1111 1111 1110 1110 1111 1100 0111 // still -12345

Truncating Bit Representation

If we want to **reduce** the bit size of a number, C *truncates* the representation and discards the *more significant bits*.

int x = -3;short sx = x;int y = sx;

What happens here? Let's look at the bits in x (a 32-bit int), -3:

1111 1111 1111 1111 1111 1111 1111 1101

When we cast x to a short, it only has 16-bits, and C truncates the number:

1111 1111 1111 1101

This is -3! If the number does fit, it will convert fine. y looks like this:

1111 1111 1111 1111 1111 1111 1101 // still -3

Truncating Bit Representation

If we want to **reduce** the bit size of a number, C *truncates* the representation and discards the *more significant bits*.

```
unsigned int x = 128000;
unsigned short sx = x;
unsigned int y = sx;
```

What happens here? Let's look at the bits in x (a 32-bit unsigned int), 128000:

0000 0000 0000 0001 1111 0100 0000 0000

When we cast x to a short, it only has 16-bits, and C truncates the number:

1111 0100 0000 0000

The sizeof Operator

long sizeof(type);

// Example
long int_size_bytes = sizeof(int); // 4
long short_size_bytes = sizeof(short); // 2
long char_size_bytes = sizeof(char); // 1

sizeof takes a variable type as a parameter and returns the size of that type, in bytes.



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Next time: How can we manipulate individual bits and bytes?



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Next time: How can we manipulate individual bits and bytes?

Additional Live Session Slides

Notes

- A literal in your C program is treated by default as a *signed int* (32 bits)
- We write hex / binary only up to the most significant 1
 - E.g. we could write a short as 0b1101 there are 12 leading zeros, but we omit them
- If we have a negative number **x** in binary, how do we find what it is in base-10?
 - 1. Find the two's complement of the number, y (y = -x)
 - 2. Figure out what **y** is in base-10
 - 3. Then we solve for \mathbf{x} : $\mathbf{x} = -\mathbf{y}$

Practice: Two's Complement

What are the negative or positive equivalents of the 8-bit numbers below?

- a) -4 (0b11111100)
- b) 24 (0b11000)
- c) 36 (0b100100)
- d) -17 (0b11101111)

Practice: Two's Complement

What are the negative or positive equivalents of the 8-bit numbers below?

- a) -4 (0b1111100) -> **0b100**
- b) 24 (0b11000) -> **0b11101000**
- c) 36 (0b100100) -> **0b11011100**
- d) -17 (0b11101111) -> **0b10001**

What are the values of cx for the passages of code below?

short x = 130; // 0b1000 0010
char cx = x;

short
$$x = -132$$
 // 0b1111 1111 0111 1100
char $cx = x;$

short x = 25; // 0b1 1001
char cx = x;

What are the values of cx for the passages of code below?

short x = 130; // 0b1000 0010char cx = x; // -126

short
$$x = -132$$
 // 0b1111 1111 0111 1100
char $cx = x$; // 124

short x = 25; // 0b1 1001char cx = x; // 25

What are the values of cx for the passages of code below?

short x = 390; // 0b1 1000 0110
char cx = x;

What are the values of cx for the passages of code below?

short x = 390; // 0b1 1000 0110char cx = x; // -122

short
$$x = -15$$
; // 0b1111 1111 1111 0001
char $cx = x$; // -15

Practice: Comparisons

What are the results of the char comparisons performed below?

- 1. -7 < 4
- 2. -7 < 4U
- (char)130 > 4 3.
- (char)-132 > 2 4.



Practice: Comparisons

What are the results of the char comparisons performed below?

- 1. -7 < 4 **true**
- 2. -7 < 4U false
- 3. (char)130 > 4 **false**
- 4. (char)-132 > 2 **true**

