CS107 Lecture 2 Bits and Bytes; Integer Representations

reading:

Bryant & O'Hallaron, Ch. 2.2-2.3

CS107 Topic 1: How can a computer represent integer numbers?

Demo: Unexpected Behavior



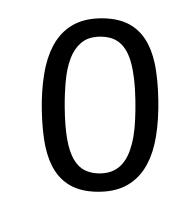
Lecture Plan

• Bits and Bytes	
Hexadecimal	33
• Integer Representations	41
Unsigned Integers	47
• Signed Integers	52
• Overflow	77
Casting and Combining Types	90

• Live Session

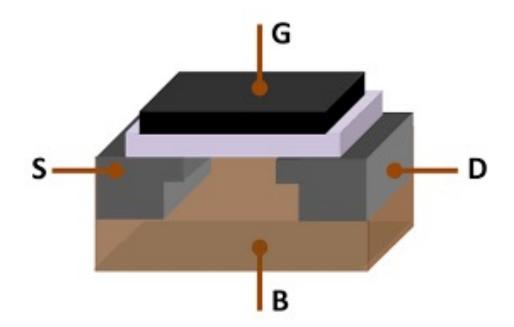
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Bits

• Computers are built around the idea of two states: "on" and "off". Transistors represent this in hardware, and bits represent this in software!



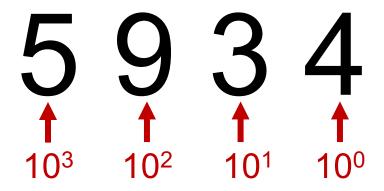
One Bit At A Time

- We can combine bits, like with base-10 numbers, to represent more data.
 bits = 1 byte.
- Computer memory is just a large array of bytes! It is byte-addressable; you can't address (store location of) a bit; only a byte.
- Computers still fundamentally operate on bits; we have just gotten more creative about how to represent different data as bits!
 - Images
 - Audio
 - Video
 - Text
 - And more...

5934

Digits 0-9 (0 to base-1)

$$= 5*1000 + 9*100 + 3*10 + 4*1$$



5 9 3 4 3 2 1 0

10^X:

2X:

Digits 0-1 (0 to base-1)





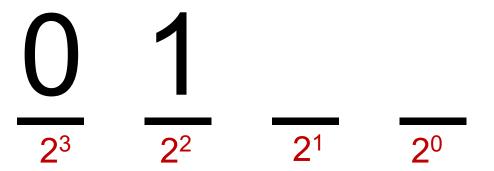
$$= 1*8 + 0*4 + 1*2 + 1*1 = 11_{10}$$

- Strategy:
 - What is the largest power of 2 ≤ 6?

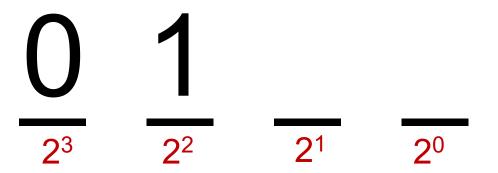
Question: What is 6 in base 2?

• Strategy:

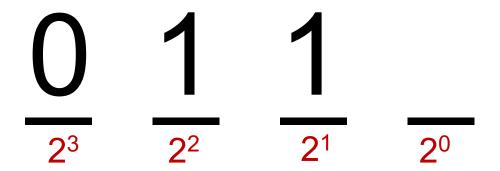
• What is the largest power of $2 \le 6$? $2^2=4$



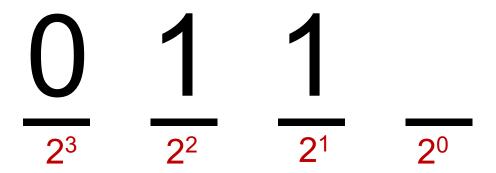
- Strategy:
 - What is the largest power of $2 \le 6$? $2^2=4$
 - Now, what is the largest power of $2 \le 6 2^2$?



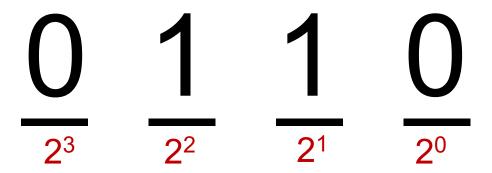
- Strategy:
 - What is the largest power of $2 \le 6$? $2^2=4$
 - Now, what is the largest power of $2 \le 6 2^2$? **2**¹=**2**



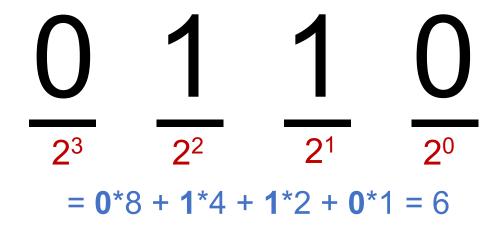
- Strategy:
 - What is the largest power of $2 \le 6$? $2^2=4$
 - Now, what is the largest power of $2 \le 6 2^2$? $2^1 = 2$
 - $6-2^2-2^1=0!$



- Strategy:
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 - $6-2^2-2^1=0!$



Practice: Base 2 to Base 10

What is the base-2 value 1010 in base-10?

- a) 20
- b) 101
- c) 10
- d) 5
- e) Other

Practice: Base 10 to Base 2

What is the base-10 value 14 in base 2?

- a) 1111
- b) 1110
- c) 1010
- d) Other

• What is the minimum and maximum base-10 value a single byte (8 bits) can store?

• What is the minimum and maximum base-10 value a single byte (8 bits) can store? **minimum = 0 maximum = ?**

What is the minimum and maximum base-10 value a single byte (8 bits) can store?
 minimum = 0
 maximum = ?



2^x:

What is the minimum and maximum base-10 value a single byte (8 bits) can store?
 minimum = 0
 maximum = ?

• Strategy 1: $1*2^7 + 1*2^6 + 1*2^5 + 1*2^4 + 1*2^3 + 1*2^2 + 1*2^1 + 1*2^0 = 255$

2^x:

What is the minimum and maximum base-10 value a single byte (8 bits) can store?
 minimum = 0
 maximum = 255

- Strategy 1: $1*2^7 + 1*2^6 + 1*2^5 + 1*2^4 + 1*2^3 + 1*2^2 + 1*2^1 + 1*2^0 = 255$
- Strategy 2: $2^8 1 = 255$

2^x:

Multiplying by Base

$$1450 \times 10 = 1450$$

 $1100_2 \times 2 = 1100$

Key Idea: inserting 0 at the end multiplies by the base!

Dividing by Base

$$1450 / 10 = 145$$
 $1100_2 / 2 = 110$

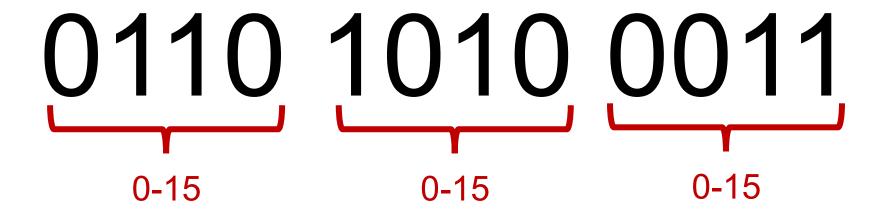
Key Idea: removing 0 at the end divides by the base!

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Hexadecimal

- When working with bits, oftentimes we have large numbers with 32 or 64 bits.
- Instead, we'll represent bits in base-16 instead; this is called hexadecimal.



Hexadecimal

- When working with bits, oftentimes we have large numbers with 32 or 64 bits.
- Instead, we'll represent bits in base-16 instead; this is called hexadecimal.



Each is a base-16 digit!

Hexadecimal

• Hexadecimal is *base-16*, so we need digits for 1-15. How do we do this?

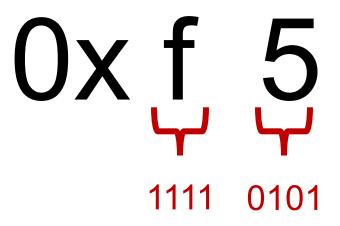
0 1 2 3 4 5 6 7 8 9 a b c d e f

Hexadecimal

Hex digit	0	1	2	3	4	5	6	7
Decimal value	0	1	2	3	4	5	6	7
Binary value	0000	0001	0010	0011	0100	0101	0110	0111
Hex digit	8	9	Α	В	C	D	E	F
Decimal value	8	9	10	11	12	13	14	15
Binary value	1000	1001	1010	1011	1100	1101	1110	1111

Hexadecimal

- We distinguish hexadecimal numbers by prefixing them with **0x**, and binary numbers with **0b**.
- E.g. **0xf5** is **0b11110101**



Practice: Hexadecimal to Binary

What is **0x173A** in binary?

Hexadecimal	1	7	3	A
Binary	0001	0111	0011	1010

Practice: Hexadecimal to Binary

What is **0b1111001010** in hexadecimal? (Hint: start from the right)

Binary	11	1100	1010
Hexadecimal	3	C	A

Lecture Plan

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Number Representations

- Unsigned Integers: positive and 0 integers. (e.g. 0, 1, 2, ... 99999...
- **Signed Integers:** negative, positive and 0 integers. (e.g. ...-2, -1, 0, 1,... 9999...)

• Floating Point Numbers: real numbers. (e,g. 0.1, -12.2, 1.5x10¹²)

Number Representations

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- Floating Point Numbers: real numbers. (e,g. 0.1, -12.2, 1.5x10¹²)
 - **→** Look up IEEE floating point if you're interested!

Number Representations

C Declaration	Size (Bytes)
int	4
double	8
float	4
char	1
char *	8
short	2
long	8

In The Days Of Yore...

C Declaration	Size (Bytes)
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Transitioning To Larger Datatypes



- Early 2000s: most computers were 32-bit. This means that pointers were 4 bytes (32 bits).
- 32-bit pointers store a memory address from 0 to 2³²-1, equaling **2³² bytes of addressable memory**. This equals **4 Gigabytes**, meaning that 32-bit computers could have at most **4GB** of memory (RAM)!
- Because of this, computers transitioned to **64-bit**. This means that datatypes were enlarged; pointers in programs were now **64 bits**.
- 64-bit pointers store a memory address from 0 to 2⁶⁴-1, equaling **2⁶⁴ bytes of addressable memory.** This equals **16 Exabytes**, meaning that 64-bit computers could have at most **1024*1024*1024*16 GB** of memory (RAM)!

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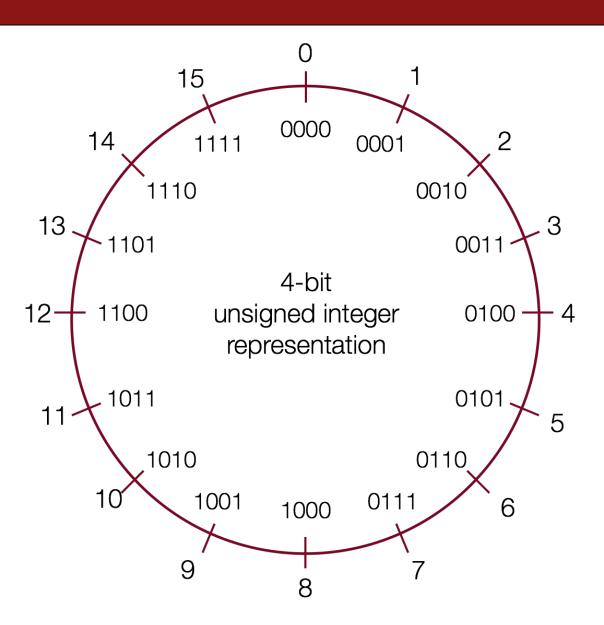
Unsigned Integers

- An **unsigned** integer is 0 or a positive integer (no negatives).
- We have already discussed converting between decimal and binary, which is a nice 1:1 relationship. Examples:

```
0b0001 = 1
0b0101 = 5
0b1011 = 11
0b1111 = 15
```

• The range of an unsigned number is $0 \rightarrow 2^w - 1$, where w is the number of bits. E.g. a 32-bit integer can represent 0 to $2^{32} - 1$ (4,294,967,295).

Unsigned Integers



Let's Take A Break

To ponder during the break:

A **signed** integer is a negative, 0, or positive integer. How can we represent both negative and positive numbers in binary?

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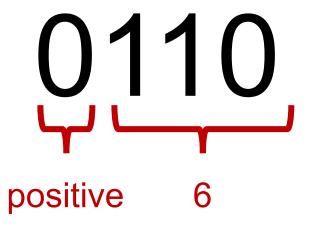
Signed Integers

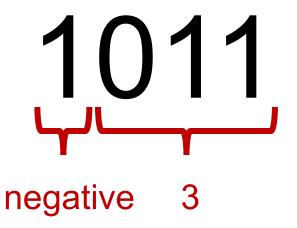
- A **signed** integer is a negative integer, 0, or a positive integer.
- *Problem:* How can we represent negative *and* positive numbers in binary?

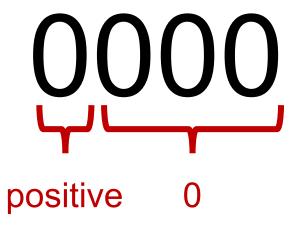
Signed Integers

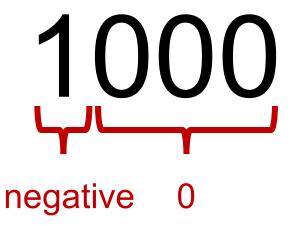
- A **signed** integer is a negative integer, 0, or a positive integer.
- *Problem:* How can we represent negative *and* positive numbers in binary?

Idea: let's reserve the *most* significant bit to store the sign.









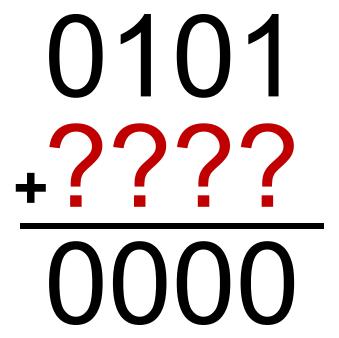


```
1\ 000 = -0 0\ 0000 = 0
1\ 001 = -1 0\ 001 = 1
1\ 010 = -2 0\ 010 = 2
1\ 011 = -3 0\ 011 = 3
1\ 100 = -4 0\ 100 = 4
1\ 101 = -5 0\ 101 = 5
1\ 110 = -6 0\ 110 = 6
1\ 111 = -7 0\ 111 = 7
```

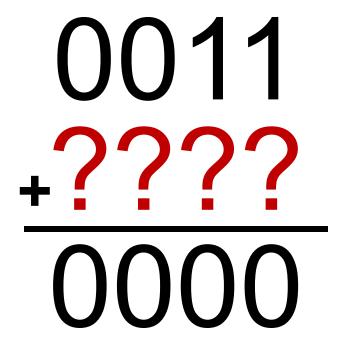
We've only represented 15 of our 16 available numbers!

- **Pro:** easy to represent, and easy to convert to/from decimal.
- Con: +-0 is not intuitive
- Con: we lose a bit that could be used to store more numbers
- **Con:** arithmetic is tricky: we need to find the sign, then maybe subtract (borrow and carry, etc.), then maybe change the sign. This complicates the hardware support for something as fundamental as addition.

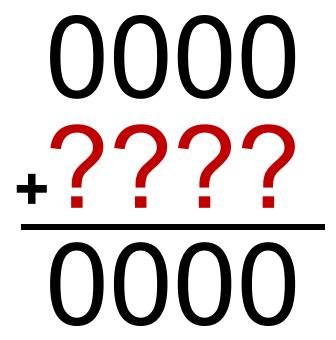
Can we do better?

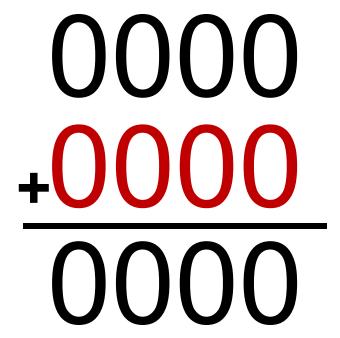


$$0101 \\ +1011 \\ \hline 0000$$



$$0011 \\ +1101 \\ \hline 0000$$

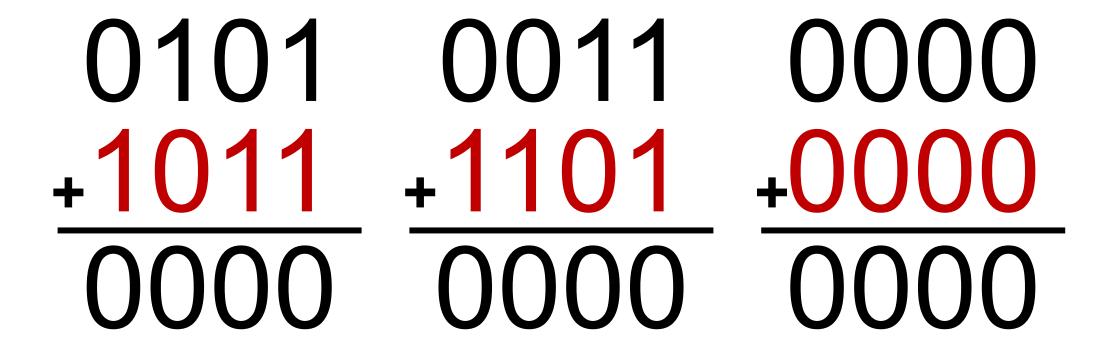




Decimal	Positive	Negative
0	0000	0000
1	0001	1111
2	0010	1110
3	0011	1101
4	0100	1100
5	0101	1011
6	0110	1010
7	0111	1001

Decimal	Positive	Negative
8	1000	1000
9	1001 (same as -7!)	NA
10	1010 (same as -6!)	NA
11	1011 (same as -5!)	NA
12	1100 (same as -4!)	NA
13	1101 (same as -3!)	NA
14	1110 (same as -2!)	NA
15	1111 (same as -1!)	NA

There Seems Like a Pattern Here...



The negative number is the positive number inverted, plus one!

There Seems Like a Pattern Here...

A binary number plus its inverse is all 1s.

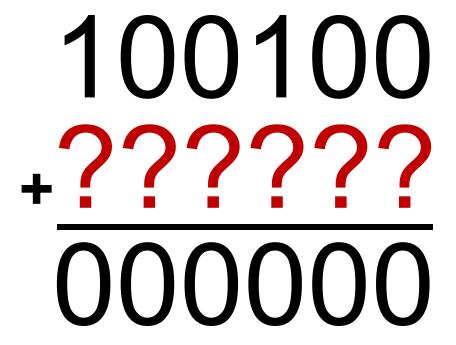
Add 1 to this to carry over all 1s and get 0!

0101
+1010
1111

1111 +001 0000

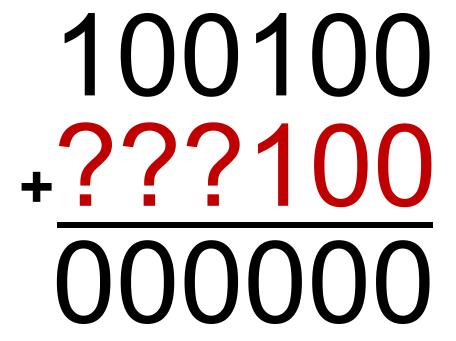
Another Trick

• To find the negative equivalent of a number, work right-to-left and write down all digits through when you reach a 1. Then, invert the rest of the digits.



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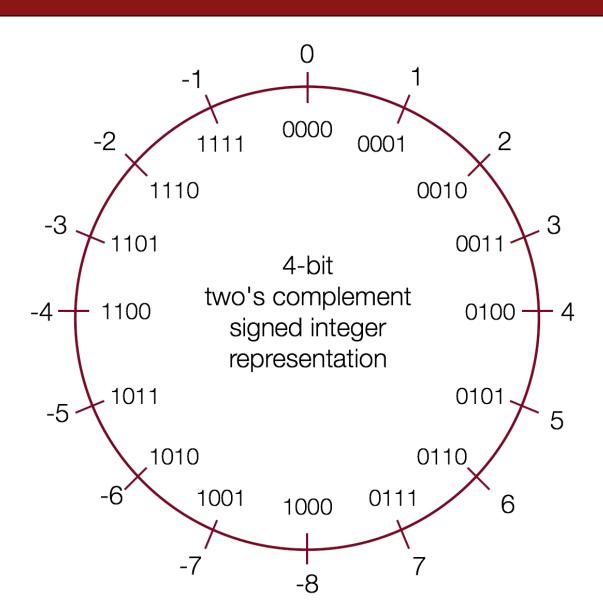


Another Trick

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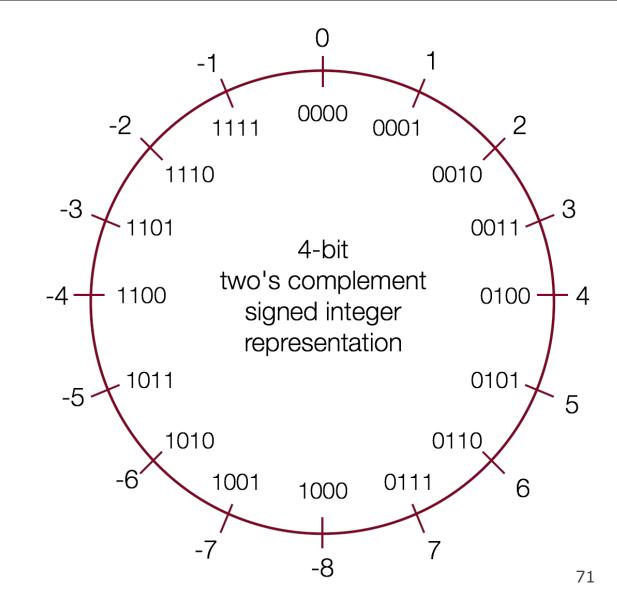
$$100100 \\ + 01100 \\ \hline 00000$$

Two's Complement



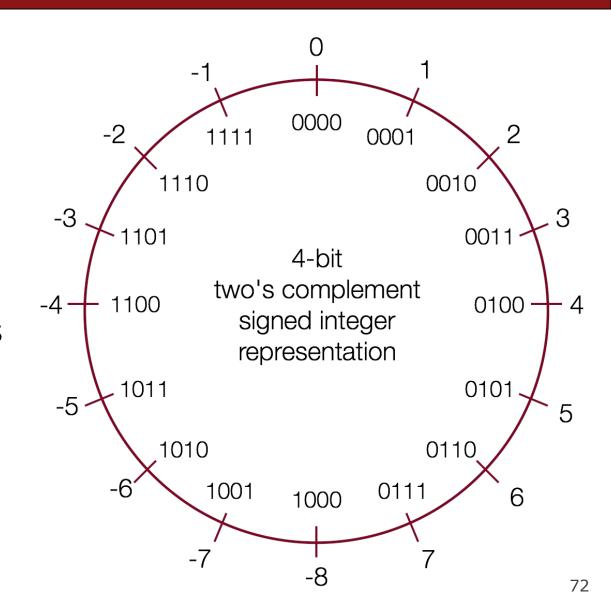
Two's Complement

- In two's complement, we represent a positive number as itself, and its negative equivalent as the two's complement of itself.
- The **two's complement** of a number is the binary digits inverted, plus 1.
- This works to convert from positive to negative, and back from negative to positive!



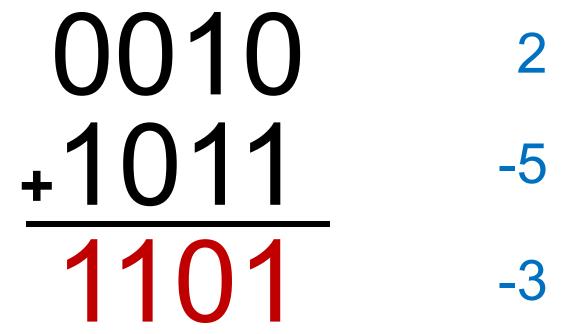
Two's Complement

- **Con:** more difficult to represent, and difficult to convert to/from decimal and between positive and negative.
- **Pro:** only 1 representation for 0!
- **Pro:** all bits are used to represent as many numbers as possible
- **Pro:** the most significant bit still indicates the sign of a number.
- **Pro:** addition works for any combination of positive and negative!



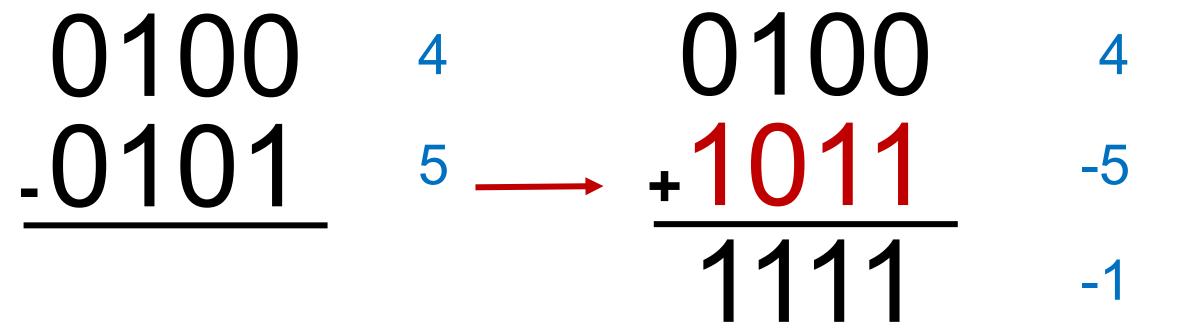
Two's Complement

• Adding two numbers is just...adding! There is no special case needed for negatives. E.g. what is 2 + -5?



Two's Complement

• Subtracting two numbers is just performing the two's complement on one of them and then adding. E.g. 4-5=-1.



Practice: Two's Complement

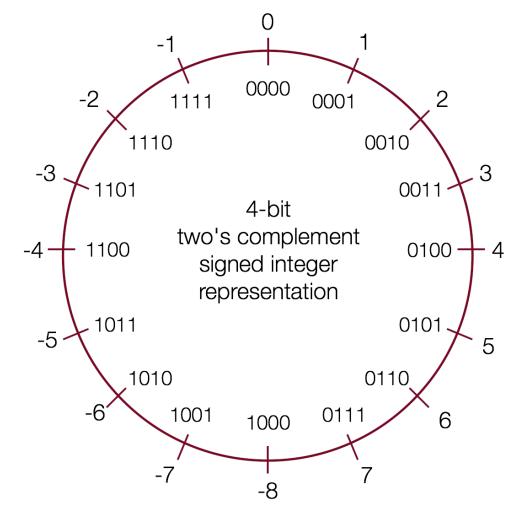
What are the negative or positive equivalents of the numbers below?

- a) -4 (1100)
- b) 7 (0111)
- c) 3 (0011)
- d) -8 (1000)

Practice: Two's Complement

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- a) -4 (1100)
- b) 7 (0111)
- c) 3 (0011)



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• Live Session

Overflow

• If you exceed the **maximum** value of your bit representation, you wrap around or overflow back to the **smallest** bit representation.

$$0b1111 + 0b1 = 0b0000$$

• If you go below the **minimum** value of your bit representation, you wrap around or overflow back to the **largest** bit representation.

$$0b0000 - 0b1 = 0b1111$$

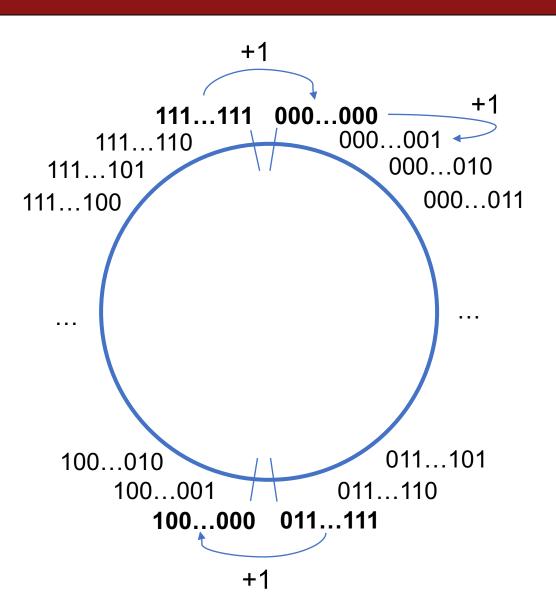
Min and Max Integer Values

Туре	Size (Bytes)	Minimum	Maximum
char	1	-128	127
unsigned char	1	0	255
short	2	-32768	32767
unsigned short	2	0	65535
int	4	-2147483648	2147483647
unsigned int	4	0	4294967295
long	8	-9223372036854775808	9223372036854775807
unsigned long	8	0	18446744073709551615
			70

Min and Max Integer Values

```
INT_MIN, INT_MAX, UINT_MAX, LONG_MIN, LONG_MAX,
ULONG_MAX, ...
```

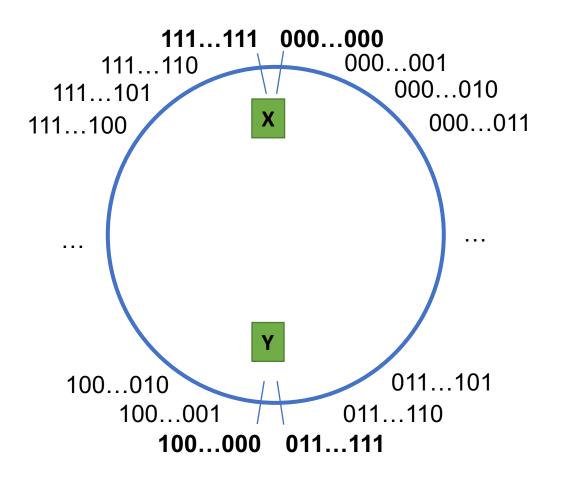
Overflow



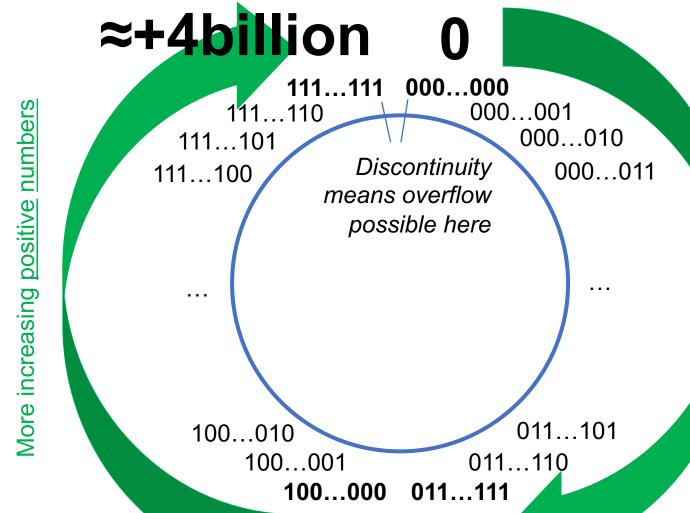
Overflow

At which points can overflow occur for signed and unsigned int? (assume binary values shown are all 32 bits)

- A. Signed and unsigned can both overflow at points X and Y
- B. Signed can overflow only at X, unsigned only at Y
- C. Signed can overflow only at Y, unsigned only at X
- D. Signed can overflow at X and Y, unsigned only at X
- E. Other

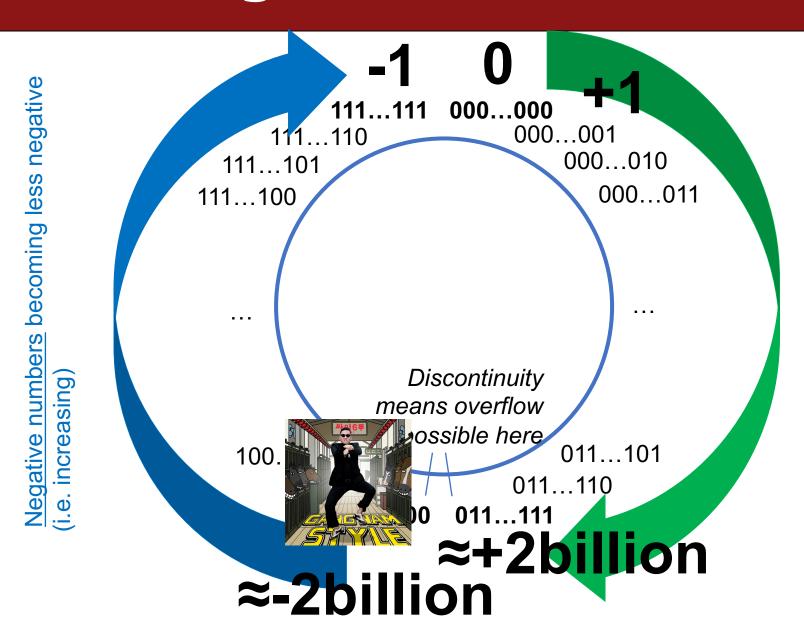


Unsigned Integers



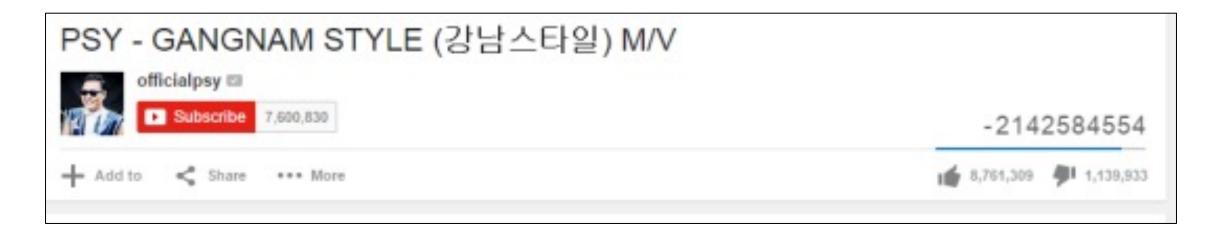
Increasing positive numbers

Signed Numbers



Increasing positive numbers

Overflow In Practice: PSY



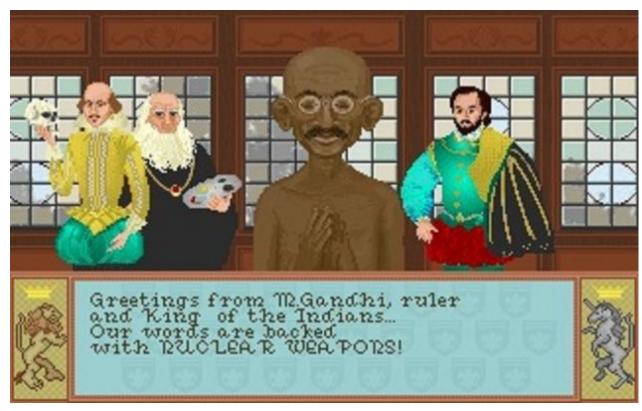
YouTube: "We never thought a video would be watched in numbers greater than a 32-bit integer (=2,147,483,647 views), but that was before we met PSY. "Gangnam Style" has been viewed so many times we had to upgrade to a 64-bit integer (9,223,372,036,854,775,808)!"

Overflow In Practice: Timestamps

- Many systems store timestamps as the number of seconds since Jan. 1, 1970 in a signed 32-bit integer.
- **Problem:** the latest timestamp that can be represented this way is 3:14:07 UTC on Jan. 13 2038!

Overflow In Practice: Gandhi

- In the game "Civilization", each civilization leader had an "aggression" rating. Gandhi was meant to be peaceful, and had a score of 1.
- If you adopted "democracy", all players' aggression reduced by 2. Gandhi's went from 1 to **255**!
- Gandhi then became a big fan of nuclear weapons.



https://kotaku.com/why-gandhi-is-such-an-asshole-in-civilization-1653818245

Overflow in Practice:

- Pacman Level 256
- Make sure to reboot Boeing Dreamliners every 248 days
- Comair/Delta airline had to <u>cancel thousands of flights</u> days before Christmas
- <u>Reported vulnerability CVE-2019-3857</u> in libssh2 may allow a hacker to remotely execute code
- Donkey Kong Kill Screen

Demo Revisited: Unexpected Behavior



airline.c

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printf and Integers

- There are 3 placeholders for 32-bit integers that we can use:
 - %d: signed 32-bit int
 - %u: unsigned 32-bit int
 - %x: hex 32-bit int
- The placeholder—not the expression filling in the placeholder—dictates what gets printed!

Casting

What happens at the byte level when we cast between variable types? The
bytes remain the same! This means they may be interpreted differently
depending on the type.

```
int v = -12345;
unsigned int uv = v;
printf("v = %d, uv = %u\n", v, uv);

This prints out: "v = -12345, uv = 4294954951". Why?
```

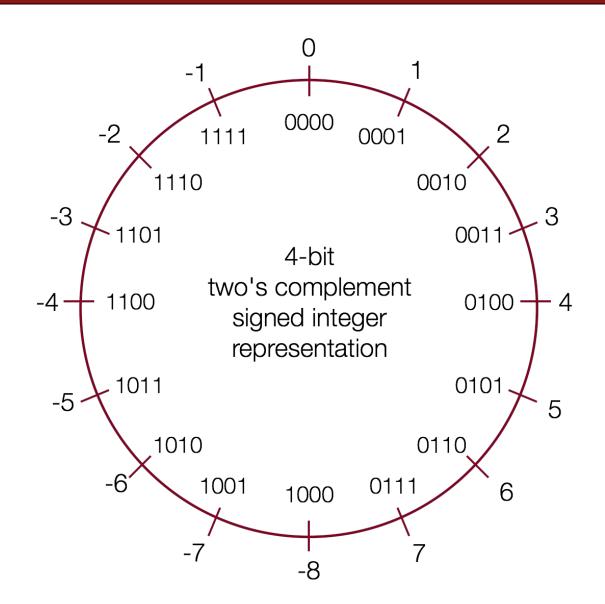
Casting

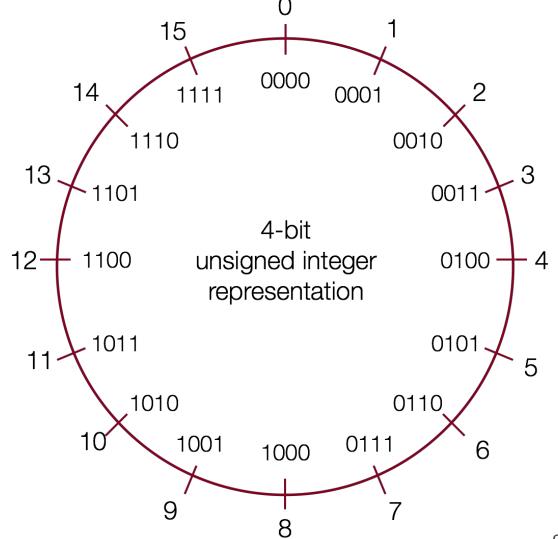
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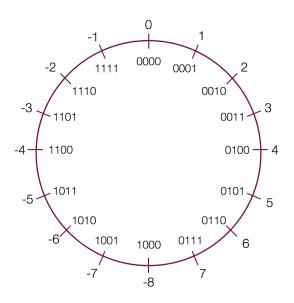
If we treat this binary representation as a positive number, it's huge!

Casting

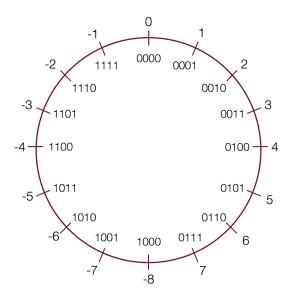




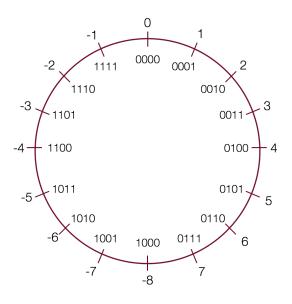
Expression	Туре	Evaluation	Correct?
0 == 0U			
-1 < 0			
-1 < 0U			
2147483647 > -			
2147483647 - 1			
2147483647U > -			
2147483647 - 1			
2147483647 >			
(int)2147483648U			
-1 > -2			
(unsigned)-1 > -2			



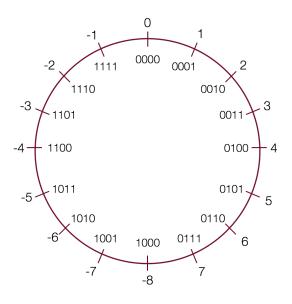
Expression	Type	Evaluation	Correct?
0 == 0U	Unsigned	1	yes
-1 < 0			
-1 < 0U			
2147483647 > -			
2147483647 - 1			
2147483647U > -			
2147483647 - 1			
2147483647 >			
(int)2147483648U			
-1 > -2			
(unsigned)-1 > -2			



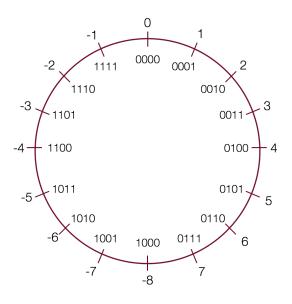
Expression	Туре	Evaluation	Correct?
0 == 0U	Unsigned	1	yes
-1 < 0	Signed	1	yes
-1 < 0U			
2147483647 > -			
2147483647 - 1			
2147483647U > -			
2147483647 - 1			
2147483647 >			
(int)2147483648U			
-1 > -2			
(unsigned)-1 > -2			



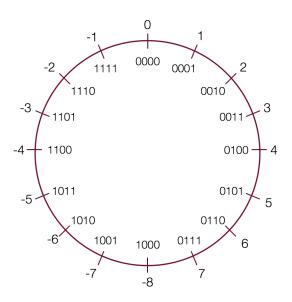
Expression	Туре	Evaluation	Correct?
0 == 0U	Unsigned	1	yes
-1 < 0	Signed	1	yes
-1 < 0U	Unsigned	0	No!
2147483647 > -			
2147483647 - 1			
2147483647U > -			
2147483647 - 1			
2147483647 >			
(int)2147483648U			
-1 > -2			
(unsigned)-1 > -2			



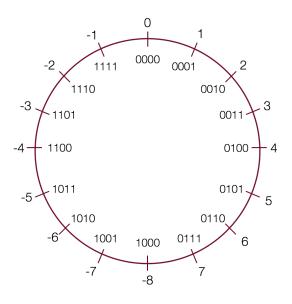
Expression	Туре	Evaluation	Correct?
0 == 0U	Unsigned	1	yes
-1 < 0	Signed	1	yes
-1 < 0U	Unsigned	0	No!
2147483647 > - 2147483647 - 1	Signed	1	yes
2147483647U > - 2147483647 - 1			
2147483647 > (int)2147483648U			
-1 > -2			
(unsigned)-1 > -2			



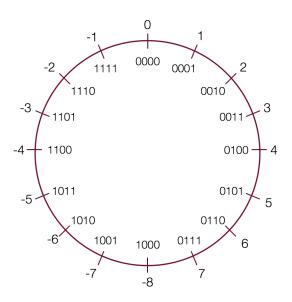
Expression	Туре	Evaluation	Correct?
0 == 0U	Unsigned	1	yes
-1 < 0	Signed	1	yes
-1 < 0U	Unsigned	0	No!
2147483647 > - 2147483647 - 1	Signed	1	yes
2147483647U > - 2147483647 - 1	Unsigned	0	No!
2147483647 > (int)2147483648U			
-1 > -2			
(unsigned)-1 > -2			



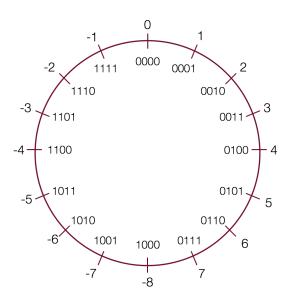
Expression	Type	Evaluation	Correct?
0 == 0U	Unsigned	1	yes
-1 < 0	Signed	1	yes
-1 < 0U	Unsigned	0	No!
2147483647 > - 2147483647 - 1	Signed	1	yes
2147483647U > - 2147483647 - 1	Unsigned	0	No!
2147483647 > (int)2147483648U	Signed	1	No!
-1 > -2			
(unsigned)-1 > -2			



Expression	Type	Evaluation	Correct?
0 == 0U	Unsigned	1	yes
-1 < 0	Signed	1	yes
-1 < 0U	Unsigned	0	No!
2147483647 > - 2147483647 - 1	Signed	1	yes
2147483647U > - 2147483647 - 1	Unsigned	0	No!
2147483647 > (int)2147483648U	Signed	1	No!
-1 > -2	Signed	1	yes
(unsigned)-1 > -2			



Expression	Туре	Evaluation	Correct?
0 == 0U	Unsigned	1	yes
-1 < 0	Signed	1	yes
-1 < 0U	Unsigned	0	No!
2147483647 > - 2147483647 - 1	Signed	1	yes
2147483647U > - 2147483647 - 1	Unsigned	0	No!
2147483647 > (int)2147483648U	Signed	1	No!
-1 > -2	Signed	1	yes
(unsigned)-1 > -2	Unsigned	1	yes



Which many of the following statements are true? (assume that variables are set to values that place them in the spots shown)

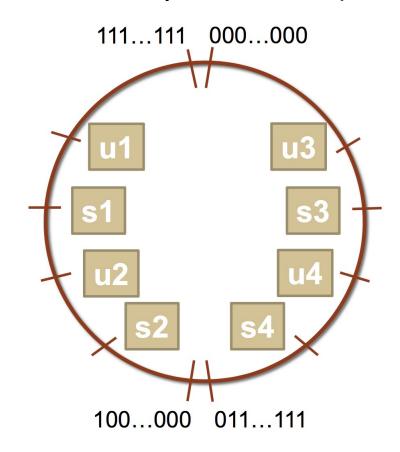
```
s3 > u3
u2 > u4
```

s2 > s4

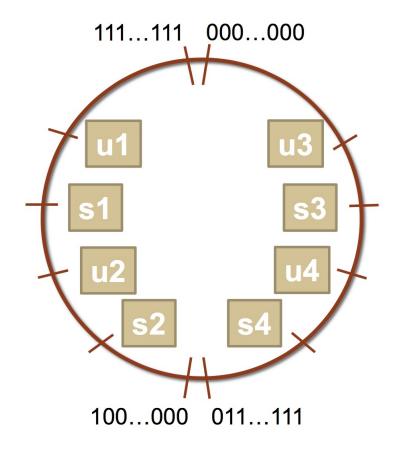
s1 > s2

u1 > u2

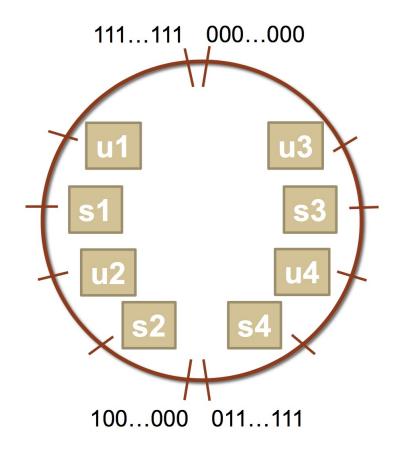
s1 > u3



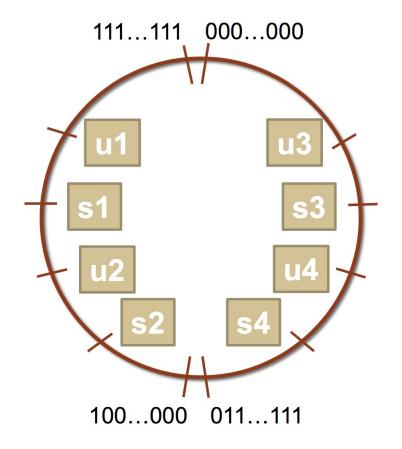
```
s3 > u3 - true
u2 > u4
s2 > s4
s1 > s2
u1 > u2
s1 > u3
```



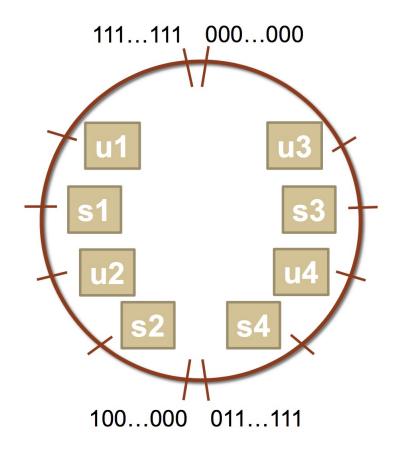
```
s3 > u3 - true
u2 > u4 - true
s2 > s4
s1 > s2
u1 > u2
s1 > u3
```



```
s3 > u3 - true
u2 > u4 - true
s2 > s4 - false
s1 > s2
u1 > u2
s1 > u3
```



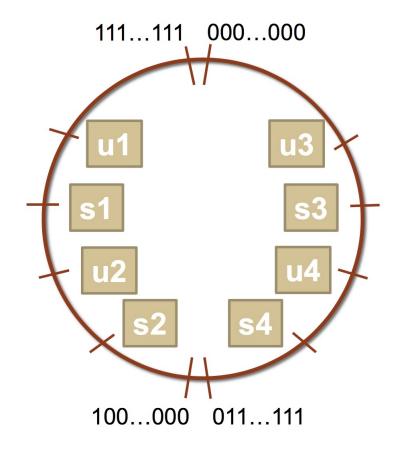
```
s3 > u3 - true
u2 > u4 - true
s2 > s4 - false
s1 > s2 - true
u1 > u2
s1 > u3
```



Comparisons Between Different Types

Which many of the following statements are true? (assume that variables are set to values that place them in the spots shown)

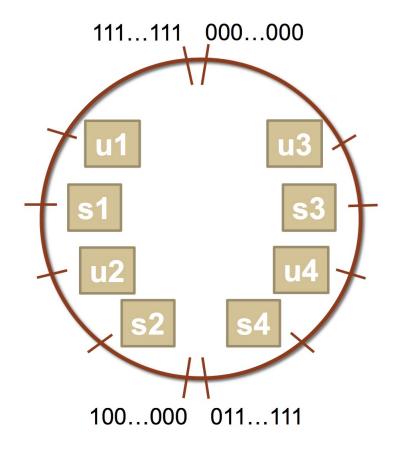
```
s3 > u3 - true
u2 > u4 - true
s2 > s4 - false
s1 > s2 - true
u1 > u2 - true
s1 > u3
```



Comparisons Between Different Types

Which many of the following statements are true? (assume that variables are set to values that place them in the spots shown)

```
s3 > u3 - true
u2 > u4 - true
s2 > s4 - false
s1 > s2 - true
u1 > u2 - true
s1 > u3 - true
```



Expanding Bit Representations

- Sometimes, we want to convert between two integers of different sizes (e.g. short to int, or int to long).
- We might not be able to convert from a bigger data type to a smaller data type, but we do want to always be able to convert from a smaller data type to a bigger data type.
- For **unsigned** values, we can add *leading zeros* to the representation ("zero extension")
- For signed values, we can repeat the sign of the value for new digits ("sign extension"
- Note: when doing <, >, <=, >= comparison between different size types, it will promote to the larger type.

Expanding Bit Representation

Expanding Bit Representation

```
short s = 4;
// short is a 16-bit format, so
                              s = 0000 \ 0000 \ 0000 \ 0100b
int i = s;
- or -
short s = -4;
                              s = 1111 \ 1111 \ 1111 \ 1100b
// short is a 16-bit format, so
int i = s;
```

Truncating Bit Representation

If we want to **reduce** the bit size of a number, C *truncates* the representation and discards the *more significant bits*.

```
int x = 53191;
short sx = x;
int y = sx;
```

What happens here? Let's look at the bits in x (a 32-bit int), 53191:

```
0000 0000 0000 0000 1100 1111 1100 0111
```

When we cast x to a short, it only has 16-bits, and C truncates the number:

```
1100 1111 1100 0111
```

This is -12345! And when we cast sx back an int, we sign-extend the number.

```
1111 1111 1111 1111 1100 1111 1100 0111 // still -12345
```

Truncating Bit Representation

If we want to **reduce** the bit size of a number, C *truncates* the representation and discards the *more significant bits*.

```
int x = -3;
short sx = x;
int y = sx;
```

What happens here? Let's look at the bits in x (a 32-bit int), -3:

```
1111 1111 1111 1111 1111 1111 1111 1101
```

When we cast x to a short, it only has 16-bits, and C truncates the number:

```
1111 1111 1111 1101
```

This is -3! If the number does fit, it will convert fine. y looks like this:

Truncating Bit Representation

If we want to **reduce** the bit size of a number, C *truncates* the representation and discards the *more significant bits*.

```
unsigned int x = 128000;
unsigned short sx = x;
unsigned int y = sx;
```

What happens here? Let's look at the bits in x (a 32-bit unsigned int), 128000:

0000 0000 0000 0001 1111 0100 0000 0000

When we cast x to a short, it only has 16-bits, and C truncates the number:

1111 0100 0000 0000

This is 62464! Unsigned numbers can lose info too. Here is what y looks like:

The size of Operator

```
long sizeof(type);

// Example
long int_size_bytes = sizeof(int); // 4
long short_size_bytes = sizeof(short); // 2
long char size bytes = sizeof(char); // 1
```

sizeof takes a variable type as a parameter and returns the size of that type, in bytes.

Recap

- Bits and Bytes
- Hexadecimal
- Integer Representations
- Unsigned Integers
- Signed Integers
- Overflow
- Casting and Combining Types

Next time: How can we manipulate individual bits and bytes?

Additional Live Session Slides

Live Session

- Optional, led by what is most helpful for us to review!
- Video and slides posted
- Post any lecture questions while watching videos in our Ed thread for lecture

Plan For Today

First 5 minutes: post questions or comments on Ed for what we should discuss!

Lecture 2 takeaway: computers represent everything in binary. We must determine how to represent our data (e.g., base-10 numbers) in a binary format so a computer can manipulate it. There may be limitations to these representations! (overflow)

Practice: Two's Complement

Fill in the below table:

3.

	char x =;		char y = -x;			
	decimal	binaı	ry	decimal	binary	
1.		0b1111	1100			
2.		0b0001	1000			

0b0010 0100

0b1101 1111

It's easier to compute base-10 for positive numbers, so use two's complement first if negative.



Practice: Two's Complement

Fill in the below table:

	char	x =	;	chai	$\mathbf{r} \mathbf{y} = -\mathbf{x}$;
	decimal	binaı	∽ y	decimal	binar	у
1.	-4	0b1111	1100	4	0b0000	0100
2.		0b0001	1000			
3.		0b0010	0100			
4.		0b1101	1111			

It's easier to compute base-10 for positive numbers, so use two's complement first if negative.



Practice: Two's Complement

Fill in the below table:

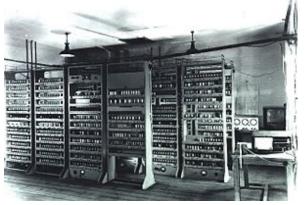
	char	x =	;	char	y = -x;	
	decimal	binary		decimal	binary	
1.	-4	0b1111	1100	4	0b0000 0100	
2.	24	0b0001	1000	-24	0b1110 1000	
3.	36	0b0010	0100	-36	0b1101 1100	
4.	-33	0b1101	1111	33	0b0010 0001	

It's easier to compute base-10 for positive numbers, so use two's complement first if negative.

History: Two's complement

- The binary representation was first proposed by John von Neumann in First Draft of a Report on the EDVAC (1945)
 - That same year, he also invented the merge sort algorithm
- Many early computers used

 sign-magnitude or one's complement
 47 0b0000 0111
 -7 0b1111 1000
 8-bit one's complement
- The System/360, developed by IBM in 1964, was widely popular (had 1024KB memory) and established two's complement as the dominant binary representation of integers



EDSAC (1949)



System/360 (1964)

Hexadecimal: It's funky but concise

• Let's take a byte (8 bits):

165

Base-10: Human-readable, but cannot easily interpret on/off bits

0b10100101

Base-2: Yes, computers use this, but not human-readable

0xa5

Base-16: Easy to convert to Base-2, More "portable" as a human-readable format (fun fact: a half-byte is called a nibble or nybble)

Hexadecimal and Truncation

For each initialization of x, what will be printed?

i.
$$x = 130$$
; $// 0x82$

```
ii. x = -132; // 0xff7c
```

```
iii. x = 25; // 0x19
```

```
short x = __;
char cx = x;
printf("%d", cx);
```



Hexadecimal and Truncation

For each initialization of x, what will be printed?

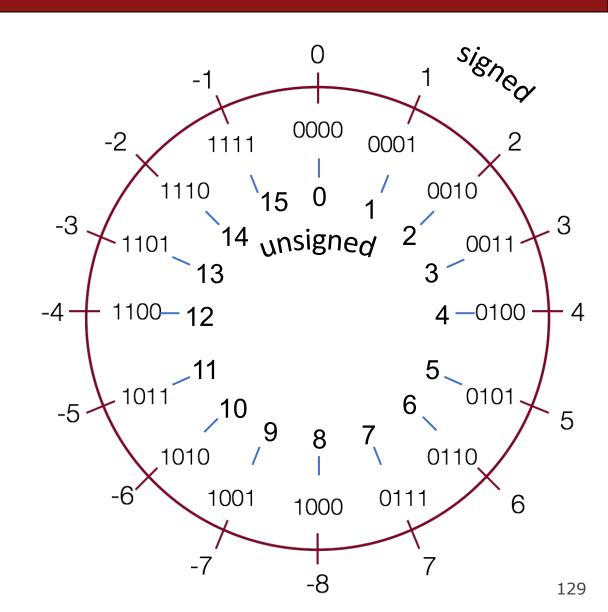
```
-126 i. x = 130; // 0x82
```

```
124 ii. x = -132; // 0xff7c
```

```
25 iii. x = 25; // 0x19
```

```
short x = __;
char cx = x;
printf("%d", cx);
```

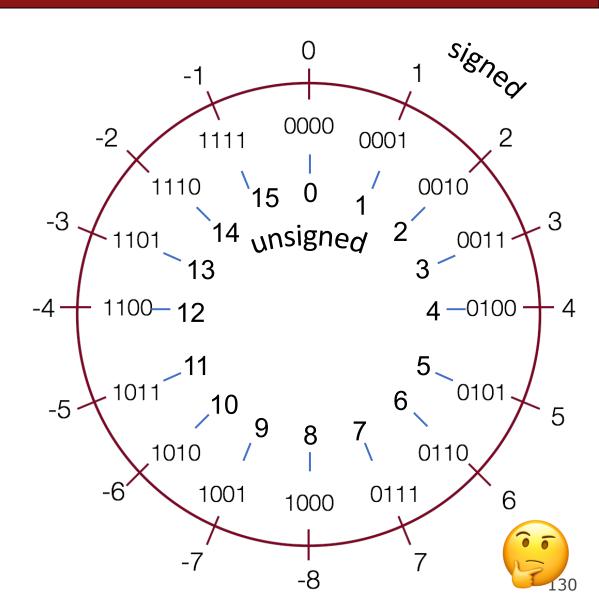
Signed vs. Unsigned Integers



Underspecified question

What is the following base-2 number in base-10?

0b1101



Underspecified question

What is the following base-2 number in base-10?

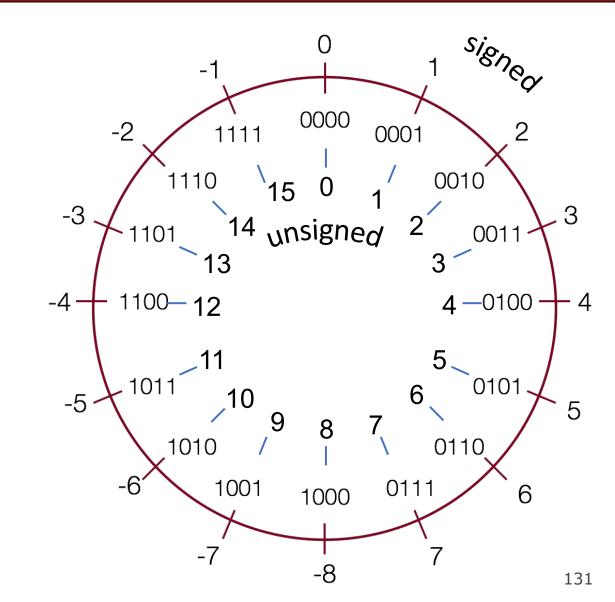
0b1101

If 4-bit signed: -3

If 4-bit unsigned: 13

If >4-bit signed or unsigned: 13

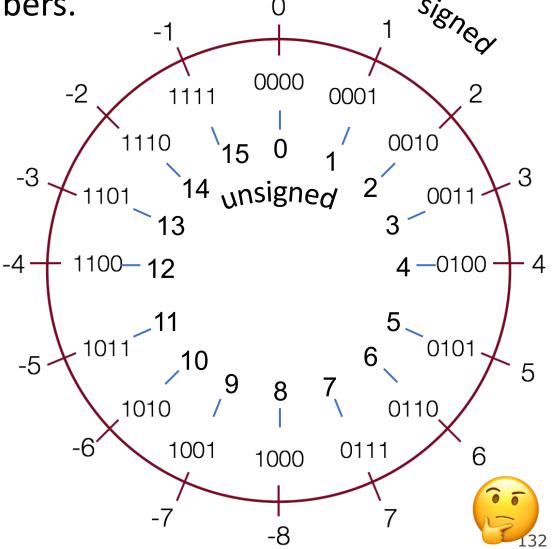
You need to know the type to determine the number! (Note by default, numeric constants in C are signed ints)



Overflow

• What is happening here? Assume 4-bit numbers.

0b1101+ 0b0100



Overflow

• What is happening here? Assume 4-bit numbers.

<u>Signed</u>

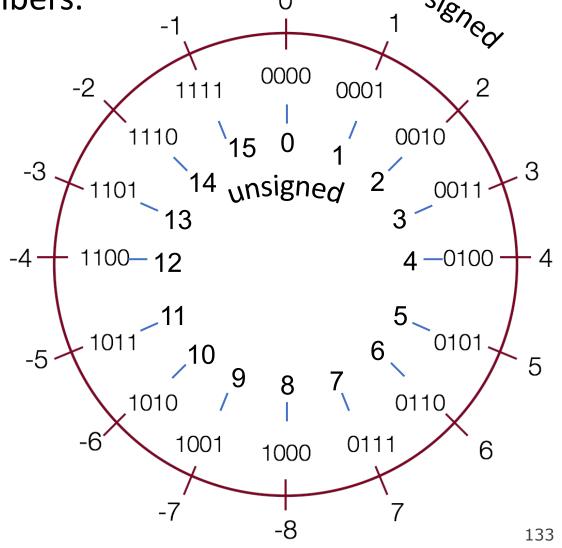
$$-3 + 4 = 1$$

No overflow

Unsigned

$$13 + 4 = 1$$

Overflow



Limits and Comparisons

1. What is the... Largest unsigned? Largest signed? Smallest signed? char

- 2. Will the following char comparisons evaluate to true or false?
 - i. -7 < 4

iii. (char)
$$130 > 4$$

iv.
$$(char) -132 > 2$$



Limits and Comparisons

1. What is the...

	Largest unsigned?	Largest signed?	Smallest signed?	
char	28 - 1 = 255	$2^7 - 1 = 127$	$-2^7 = -128$	
int	$2^{32} - 1 = 4294967296$	$2^{31} - 1 =$	$-2^{31} =$ -2147483648	
	429496/296	2147483647	-214/403040	

These are available as UCHAR_MAX, INT_MIN, INT_MAX, etc. in the imits.h> header.

Limits and Comparisons

- 2. Will the following char comparisons evaluate to true or false?
 - i. -7 < 4

true

iii. (char) 130 > 4

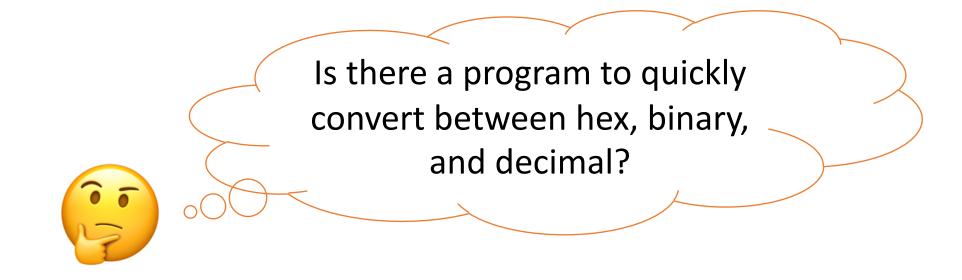
false

iv.
$$(char) -132 > 2$$

true

By default, numeric constants in C are signed ints, unless they are suffixed with u (unsigned) or L (long).

Tools: A binary/hex calculator



- Yes. Next week, we will learn more about gdb, our debugger.
- gdb can print out variables/constants in any format: hex, decimal, unsigned...
- To look ahead, check out our GDB guide and read about print format codes.
 Or watch Lecture 3!