CS 107 Lecture 2: Integer Representations and Bits / Bytes

Wednesday, January 10, 2024

Computer Systems Winter 2024 Stanford University Computer Science Department

Reading: Reader: Bits and Bytes, Textbook: Chapter 2.2

Lecturer: Chris Gregg









Logistics

- Assign0 Due Monday
- Labs start next week
- Lab preferences: please re-do if you put in preferences on Tuesday (sorry!)
- Office hours will start this week
- Reading: Reader: Bits and Bytes, Textbook: Chapter 2.2 (very mathy...) •
- Integer Representations
 - Unsigned numbers
 - Signed numbers
 - two's complement
 - Signed vs Unsigned numbers •
 - Casting in C
 - Signed and unsigned comparisons
 - The sizeof operator
 - Min and Max integer values
 - Truncating integers
 - two's complement overflow

Today's Topics







A bit on bits

- As we briefly discussed in lecture 1, a "bit" is either a 0 or a 1
- Here is how we count in binary:

Binary	Decimal
0	0
1	1
10	2
11	3
100	4
101	5
110	6
111	7
1000	8
e	tc.

- Notice that you can represent two • numbers with 1 binary digit, four numbers with two binary digits, eight numbers with three binary digits.
- The number of integers you can represent is:

2 number of bits

- So, an "eight bit" number can represent 2⁸ numbers, which is 256.
- A 32-bit number can represent 2³² numbers





In C, everything can be thought of as a block of 8 bits





In C, everything can be thought of as a block of 8 bits called a "byte"





Information Storage

to consider an individual bit on its own.

familiar, from CS106B?)

values (ints):	7	2	8	3	14	99	-6	3	45	11
address (decimal):	200d	204d	208d	212d	216d	220d	224d	228d	232d	236d
address (hex):	0xc8	0xcc	0xd0	0xd4	0xd8	0xdc	0xe0	0xe4	0xe8	0xec

Each address (a pointer!) represents the next byte in memory.

E.g., address 0 is a byte, then address 1 is the next full byte, etc.

Again: you can't address a bit. You must address at the byte level.

- We will discuss manipulating bytes on a bit-by-bit level, but we won't be able
- In a computer, the memory system is simply a large array of bytes (sound





follows:

00000000 to 1111111

This range is 0 to 255 in decimal.

But, neither binary nor decimal is particularly convenient to write out bytes (binary is too long, and decimal isn't numerically friendly for byte representation)

So, we use "hexadecimal," (base 16).

Because a byte is made up of 8 bits, we can represent the range of a byte as







Hexadecimal has 16 digits, so we augment our normal 0-9 digits with six more digits: A, B, C, D, E, and F.

Figure 2.2 in the textbook shows the hex digits and their binary and decimal values:

Hex digit	0	1	2	3	4	5	6	7
Decimal value	0	1	2	3	4	5	6	7
Binary value	0000	0001	0010	0011	0100	0101	0110	0111
Hex digit	8	9	A	В	C	D	E	F
Decimal value	8	9	10	11	12	13	14	15
Binary value	1000	1001	1010	1011	1100	1101	1110	1111

Hex digit	0	1	2	3	4	5	6	7
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Decimal value	8	9	10	11	12	13	14	15
Binary value	1000	1001	1010	1011	1100	1101	1110	1111



Hexadecimal

- such as 0xfa1d37b, which means that it is a hex number.
- easy to figure out.
- Let's practice some hex to binary and binary to hex conversions:

Convert: 0x173A4C to binary.

Hexadecimal	1	7	3	А	4	С
Binary	0001	0111	0011	1010	0100	1100

0x173A4C is binary 0b00101110011101001001100

• In C, we write a hexadecimal with a starting 0x. So, you will see numbers • You should memorize the binary representations for each hex digit. One trick is to memorize A (1010), C (1100), and F (1111), and the others are

Hex digit	0	1	2	3	4	5	6	7
Decimal value	0	1	2	3	4	5	6	7
Binary value	0000	0001	0010	0011	0100	0101	0110	0111
Hex digit	8	9	A	В	С	D	E	F
Decimal value	8	9	10	11	12	13	14	15
Binary value	1000	1001	1010	1011	1100	1101	1110	1111







Convert: 0b1111001010110110110011 to hexadecimal.

Binary	11	1100	1010	1101	1011	0011
Hexadecimal	3	\mathbf{C}	Α	D	В	3

0b1111001010110110110011 is hexadecimal 3CADB3

Hexadecimal

(start from the **right**)

Hex digit	0	1	2	3	4	5	6	7
Decimal value	0	1	2	3	4	5	6	7
Binary value	0000	0001	0010	0011	0100	0101	0110	0111
Hex digit	8	9	A	В	С	D	E	F
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Convert: 0b1111001010110110110011 to hexadecimal.

Binary	11	1100	1010	11(
Hexadecimal	3	\mathbf{C}	Α	D

0b1111001010110110110011 is hexadecimal 3CADB3

Hexadecimal

1011 0011 013 В

(start from the **right**)

Hex digit	0	1	2	3	4	5	6	7
Decimal value	0	1	2	3	4	5	6	7
Binary value	0000	0001	0010	0011	0100	0101	0110	0111
Hex digit	8	9	A	В	С	D	E	F
Decimal value	8	9	10	11	12	13	14	15
Binary value	1000	1001	1010	1011	1100	1101	1110	1111









Convert: 0b1111001010110110110011 to hexadecimal. 101011011011 0011 Binary 110011 (start from the **right**) Hexadecimal С 3 Α В 3 D

0b1111001010110110110011 is hexadecimal 3CADB3

Hexadecimal

Hex digit	0	1	2	3	4	5	6	7
Decimal value	0	1	2	3	4	5	6	7
Binary value	0000	0001	0010	0011	0100	0101	0110	0111
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Convert: 0b1111001010110110110011 to hexadecimal.

Binary	11	1100	1010	1101	1011	0011
Hexadecimal	3	\mathbf{C}	Α	D	В	3

0b1111001010110110110011 is hexadecimal 3CADB3

Hexadecimal

(start from the **right**)

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Hexadecimal

Convert: 0b1111001010110110110011 to hexadecimal.

Binary	11	1100	1010	1101	1011	0011
Hexadecimal	3	\mathbf{C}	Α	D	В	3

0b1111001010110110110011 is hexadecimal 3CADB3

(start from the **right**)

Hex digit	0	1	2	3	4	5	6	7
Decimal value	0	1	2	3	4	5	6	7
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Decimal value	8	9	10	11	12	13	14	15
Binary value	1000	1001	1010	1011	1100	1101	1110	1111





Hexadecimal

Convert: 0b1111001010110110110011 to hexadecimal. 1010Binary 1100 11011 (start from the **right**) С Hexadecimal 3 Α D

0b1111001010110110110011 is hexadecimal 3CADB3

)1	1011	0011
	В	3

Hex digit	0	1	2	3	4	5	6	7
Decimal value	0	1	2	3	4	5	6	7
Binary value	0000	0001	0010	0011	0100	0101	0110	0111
Hex digit	8	9	A	В	С	D	E	F
Decimal value	8	9	10	11	12	13	14	15
Binary value	1000	1001	1010	1011	1100	1101	1110	1111







Convert: 0b1111001010110110110011 to hexadecimal. 10101100Binary 11011 (start from the **right**) C Α Hexadecimal 3 D

0b1111001010110110110011 is hexadecimal 3CADB3

Hexadecimal

)1	1011	0011
	В	3

Hex digit	0	1	2	3	4	5	6	7
Decimal value	0	1	2	3	4	5	6	7
Binary value	0000	0001	0010	0011	0100	0101	0110	0111
Hex digit	8	9	A	В	С	D	E	F
Decimal value	8	9	10	11	12	13	14	15
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Decimal to Hexadecimal

To convert from decimal to hexadecimal, you need to repeatedly divide the number in question by 16, and the remainders make up the digits of the hex number:

314156 decimal:

19,634 / 16 = 1,227 with 2 remainder: 1,227 / 16 = 76 with 11 remainder: 76 / 16 = 4 with 12 remainder: 4 / 16 = 0 with 4 remainder:

Reading from bottom up: 0x4CB2C

314,156 / 16 = 19,634 with 12 remainder: C 2 В С 4



Hexidecimal to Decimal

To convert from hexadecimal to decimal, multiply each of the hexadecimal digits by the appropriate power of 16:

0x7AF:

 $7 * 16^2 + 10 * 16 + 15$ = 7 * 256 + 160 + 15= 1792 + 160 + 15 = 1967



Let the computer do it!

Honestly, hex to decimal and vice versa are easy to let the computer handle. You can either use a search engine (Google does this automatically), or you can use a python one-liner:



4. cgregg@myth10: ~ (ssh)



Let the computer do it!

You can also use Python to convert to and from binary:



4. cgregg@myth10: ~ (ssh)

cgregg@myth10:~\$ python -c "print(hex(0b1111001010110110110011))"

(but you should memorize this as it is easy and you will use it frequently)



Integer Representations



unsigned: can only represent non-negative numbers

signed: can represent negative, zero, and positive numbers

long)

- The C language has two different ways to represent numbers, unsigned and signed:
- We are going to talk about these representations, and also about what happens when we expand or shrink an encoded integer to fit into a different type (e.g., int to







Unsigned Integers

For positive (unsigned) integers, there is a 1-to-1 relationship between the decimal representation of a number and its binary representation. If you have a 4-bit number, there are 16 possible combinations, and the unsigned numbers go from 0 to 15:

0b0000	=	0	0b0001	=	1
0b0100	=	4	0b0101	=	5
0b1000	=	8	0b1001	=	9
0b1100	=	12	0b1101	=	13

The range of an unsigned number is $0 \rightarrow 2^{w} - 1$, where w is the number of bits in our integer. For example, a 32-bit int can represent numbers from 0 to 2^{32} - 1, or 0 to 4,294,967,295.

0b0010	=	2	0b0011	=	3
0b0110	=	6	0b0111	=	7
0b1010	=	10	0b1011	=	11
0b1110	=	14	0b1111	=	15











What if we want to represent negative numbers? We have choices!

One way we could encode a negative number is simply to designate some bit as a "sign" bit, and then interpret the rest of the number as a regular binary number and then apply the sign. For instance, for a four-bit number:

 $0\ 001 = 1$ $1\ 001 = -1$ $0\ 010 = 2$ $1\ 010 = -2$ 0.011 = 3 $1 \ 011 = -3$ $0\ 100 = 4$ $1\ 100 = -4$ $0\ 101 = 5$ $1\ 101 = -5$ $0\ 1\ 1\ 0\ =\ 6$ $1\ 110 = -6$ 0.111 = 7 $1 \ 1 \ 1 \ 1 \ -7$

This might be okay...but we've only represented 14 of our 16 available numbers...





 $0\ 001 = 1$ $0\ 010 = 2$ 0.011 = 3 $0\ 100 = 4$ 0.101 = 50.110 = 60.111 = 7

 $1\ 001 = -1$ $1\ 010 = -2$ $1\ 011 = -3$ $1\ 100 = -4$ $1\ 101 = -5$ $1\ 110 = -6$ $1 \ 1 \ 1 \ 1 \ -7$

- What about 0 000 and 1 000? What should they represent?
- Well...this is a bit tricky!



What about 0 000 and 1 000? What should $1\ 001 = -1$ $0\ 001 = 1$ they represent? 0.010 = 2 $1\ 010 = -2$ 0.011 = 3 $1 \ 011 = -3$ $0\ 100 = 4$ $1\ 100 = -4$ Well...this is a bit tricky! $1\ 101 = -5$ $0\ 101 = 5$ $0\ 1\ 1\ 0\ =\ 6$ $1\ 110 = -6$ Let's look at the bit patterns: 0 0 0 0 0 $1 \ 1 \ 1 \ 1 \ -7$ 0.111 = 7

are nice.

Should we make the 0 000 just represent decimal 0? What about 1 000? We could make it 0 as well, or maybe -8, or maybe even 8, but none of the choices





What about 0 000 and 1 000? What should $1\ 001 = -1$ $0\ 001 = 1$ $0\ 010 = 2$ $1\ 010 = -2$ they represent? 0.011 = 3 $1\ 011 = -3$ Well...this is a bit tricky! $1\ 100 = -4$ $0\ 100 = 4$ $0\ 101 = 5$ $1\ 101 = -5$ $0\ 1\ 1\ 0\ =\ 6$ $1\ 110 = -6$ Let's look at the bit patterns: 0 0 0 0 0 $1 \ 1 \ 1 \ 1 \ -7$ 0.111 = 7

are nice.

Well...to add two numbers, you need to know the sign, then you might have to ugly!

- Should we make the 0 000 just represent decimal 0? What about 1 000? We could make it 0 as well, or maybe -8, or maybe even 8, but none of the choices
- Fine. Let's just make 0 000 to be equal to decimal 0. How does arithmetic work? subtract (borrow and carry, etc.), and the sign might change...this is going to get







There is a better way!





Behold: the "two's complement" circle:

In the early days of computing*, two's complement was determined to be an excellent way to store binary numbers.

In two's complement notation, positive numbers are represented as themselves (phew), and negative numbers are represented as the two's complement of themselves (definition to follow).

This leads to some amazing arithmetic properties!

*John von Neumann suggested it in 1945, for the EDVAC computer.







A two's-complement number system encodes positive and negative numbers in a binary number representation. The weight of each bit is a power of two, except for the most significant bit, whose weight is the negative of the corresponding power of two.

 $B2T_w$ means "Binary to Two's complement function"

In practice, a negative number in two's complement is obtained by inverting all the bits of its positive counterpart*, and then adding 1.

*Inverting all the bits of a number is its "one's complement"

Definition: For vector $\vec{x} = [x_{w-1}, x_{w-2}, \dots, x_0]$ of an *w*-bit integer $x_{w-1}x_{w-2}\ldots x_0$ is given by the following formula:

$$B2T_w(ec{x}) = -x_{w-1}2^{w-1} + \sum_{i=0}^{w-2} x_i 2^i.$$







In practice, a negative number in two's complement is obtained by inverting all the bits of its positive counterpart*, and then adding 1, or: x = -x + 1

Example: The number 2 is represented as normal in binary: 0010

-2 is represented by inverting the bits, and adding 1:

0010 @ 1101

1101

1110

*Inverting all the bits of a number is its "one's complement"





Trick: to convert a positive number to its negative in two's complement, start from the right of the number, and write down all the digits until you get to a 1. Then invert the rest of the digits:

Example: The number 2 is represented as normal in binary: 0010

Going from the right, write down numbers until you get to a 1: 10

Then invert the rest of the digits: 1110

*Inverting all the bits of a number is its "one's complement"





To convert a negative number to a positive number, perform the same steps!

Example: The number -5 is represented in two's complements as: 1011

5 is represented by inverting the bits, and adding 1:

```
1011 🖙 0100
```

```
0100
+ 1
```

0101

Shortcut: start from the right, and write down numbers until you get to a 1: 1 Now invert all the rest of the digits: 0101



Two's Complement: Neat Properties



There are a number of useful properties associated with two's complement numbers:

- 1. There is only one zero (yay!)
- 2. The highest order bit (left-most) is 1 for negative, 0 for positive (so it is easy to tell if a number is negative)
- 3. Adding two numbers is just...adding! Example:

2 + -5 = -3

- +1011**1** -5
 - 1101 3 decimal (wow!)



Two's Complement: Neat Properties



More useful properties:

Subtracting two numbers is simply performing the two's complement on one of them and then adding.
 Example:

$$4 - 5 = -1$$

0100 @ 4,0101 @ 5

Find the two's complement of 5: 1011 add:

0100 @ 4

<u>+1011</u> 🖙 -5

1111 @ -1 decimal



Two's Complement: Neat Properties



More useful properties:

5. Multiplication of two's complement works just by multiplying (throw away overflow digits).

```
Example: -2 * -3 = 6
```

```
1110 -2
               -3
    x<u>1101</u>
            F
      1110
     0000
   1110
<u>+1110</u>
<u>10110110</u> 🖙 6
```







Two's Complement: Powers of two remain!



For vector $\vec{x} = [x_{w-1}, x_{w-2}, \dots, x_0]$ of an *w*-bit integer $x_{w-1}x_{w-2}\ldots x_0$ is given by the following formula:

$$B2T_w(ec{x}) = -x_{w-1}2^{w-1} + \sum_{i=0}^{w-2} x_i 2^i.$$

From the definition of a two's complement number, we can see that we are still dealing with bits being equal to their powers-of-two place: there isn't anything magical about the placement of the bits:

 $(1 * -2^3) + (0 * 2^2) + (1 * 2^1) + (1 * 2^0)$







Practice

Convert the following 4-bit numbers from positive to negative, or from negative to positive using two's complement notation:

- -4 (1100) R a.
- G D.
- c. 3 (0011) F
- d. -8 (1000) 🖙





Practice

Convert the following 4-bit numbers from positive to negative, or from negative to positive using two's complement notation:

- -4 (1100) 0100 B a.
- 1001
- 1101 c. 3 (0011) B

d. -8 (1000) 🖙 1000 (?! If you look at the chart, +8 cannot be represented in two's complement with 4 bits!)





Practice

Convert the following 8-bit numbers from positive to negative, or from negative to positive using two's complement notation:

-4 (11111100) 🖙 00000100 a.

27 (00011011) 🖙 11100101 b.

c. −127 (1000001) 🖙 01111111

d. 1 (00000001) 🖙



Casting Between Signed and Unsigned

Converting between two numbers in C can happen explicitly (using a parenthesized cast), or implicitly (without a cast):

explicit

1 int tx, ty; 2 unsigned ux, uy; 3 ... 4 tx = (int) ux; 5 uy = (unsigned) ty;

When casting: **the underlying bits do not change**, so there isn't any conversion going on, except that the variable is treated as the type that it is. You cannot convert a signed number to its unsigned counterpart using a cast!

implicit

1 int tx, ty; 2 unsigned ux, uy; 3 ... 4 tx = ux; // cast to signed 5 uy = ty; // cast to unsigned





Casting Between Signed and Unsigned

When casting: **the underlying bits do not change**, so there isn't any conversion going on, except that the variable is treated as the type that it is. You cannot convert a signed number to its unsigned counterpart using a cast!

```
1 // test_cast.c
2 #include<stdio.h>
3 #include<stdlib.h>
4
5 int main() {
6     int v = -12345;
7     unsigned int uv = (unsigned int) v;
8
9     printf("v = %d, uv = %u\n",v,uv);
10
11     return 0;
12 }
```

\$./test_cast v = -12345, uv = 4294954951





Casting Between Signed and Unsigned

printf has three 32-bit integer representations:

- %d : signed 32-bit int
- %u : unsigned 32-bit int
- %x: hex 32-bit int

As long as the value is a 32-bit type, printf will treat it according to the formatter it is applying:

int x = -1;2 unsigned u = 300000000; // 3 billion 3 printf("x = $u = d \in x, x$); 4 5 printf("u = u = d n", u, u);

./test printf \$ x = 4294967295 = -1u = 300000000 = -1294967296





Signed vs Unsigned Number Wheels







When a C expression has combinations of signed and unsigned variables, you need to be careful!

If an operation is performed that has both a signed and an unsigned value, C implicitly casts the signed argument to unsigned and performs the operation assuming both numbers are non-negative. Let's take a look...





When a C expression has combinations of signed and unsigned variables, you need to be careful!

If an operation is performed that has both a signed and an unsigned value, C implicitly casts the signed argument to unsigned and performs the operation assuming both numbers are non-negative. Let's take a look...

Expression	Туре	Evaluation
0 == 0U	Unsigned	1
-1 < 0	Signed	1
-1 < 0U	Unsigned	0
2147483647 > -2147483647 - 1	Signed	1
2147483647U > -2147483647 - 1	Unsigned	0
2147483647 > (int)2147483648U	Signed	1
-1 > -2	Signed	1
(unsigned) - 1 > -2	Unsigned	1

Note: In C, 0 is false and everything else is true. When C produces a boolean value, it allways chooses 1 to represent true.





Let's try some more...a bit more abstractly.

- int s1, s2, s3, s4;
- unsigned int u1, u2, u3, u4;

Which many of the following statements are true? (assume that variables are set to values that place them in the spots shown)

- s3 > u3
- u2 > u4
- s2 > s4
- s1 > s2
- u1 > u2 s1 > u3







Let's try some more...a bit more abstractly.

- int s1, s2, s3, s4;
- unsigned int u1, u2, u3, u4;

Which many of the following statements are true? (assume that variables are set to values that place them in the spots shown)

- s3 > u3 : true
- u2 > u4 : true
- s2 > s4 : false
- s1 > s2 : true
- u1 > u2 : true
- s1 > u3 : true







The sizeof Operator

bytes each type uses:

int main() { printf("sizeof(char): %d\n", (int) sizeof(char)); printf("sizeof(short): %d\n", (int) sizeof(short)); printf("sizeof(int): %d\n", (int) sizeof(int)); printf("sizeof(unsigned int): %d\n", (int) sizeof(unsigned int)); printf("sizeof(long): %d\n", (int) sizeof(long)); printf("sizeof(long long): %d\n", (int) sizeof(long long)); printf("sizeof(size t): %d\n", (int) sizeof(size t)); printf("sizeof(void *): %d\n", (int) sizeof(void *)); return 0;

\$./sizeof sizeof(char): 1 sizeof(short): 2 sizeof(int): 4 sizeof(unsigned int): 4 sizeof(long): 8 sizeof(long long): 8 sizeof(size t): 8 sizeof(void *): 8

TY
ch
sh
in
10
vo

As we have seen, integer types are limited by the number of bits they hold. On the 64-bit myth machines, we can use the sizeof operator to find how many

pe	Width in bytes	Width in bits
ar	1	8
ort	2	16
t	4	32
ng	8	64
id *	8	64



MIN and MAX values for integers

Because we now know how bit patterns for integers works, we can figure out the maximum and minimum values, designated by INT MAX, UINT MAX, INT MIN, (etc.), which are defined in limits.h

Туре	Width (bytes)	Width (bits)	Min in hex (name)	Max in hex (name)
char	1	8	80 (CHAR_MIN)	7F (CHAR_MAX)
unsigned char	1	8	0	FF (UCHAR_MAX)
short	2	16	8000 (SHRT_MIN)	7FFF (SHRT_MAX)
unsigned short	2	16	0	FFFF (USHRT_MAX)
int	4	32	8000000 (INT_MIN)	7FFFFFFF (INT_MAX)
unsigned int	4	32	0	FFFFFFF (UINT_MAX)
long	8	64	800000000000000 (LONG_MIN)	7FFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFF
unsigned long	8	64	0	FFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFF





Expanding the bit representation of a number

Sometimes we want to convert between two integers having different sizes. E.g., a short to an int, or an int to a long.

We might not be able to convert from a bigger data type to a smaller data type, but we do want to always be able to convert from a smaller data type to a bigger data type.

This is easy for unsigned values: simply add leading zeros to the representation (called "zero extension").

unsigned short s = 4;// short is a 16-bit format, so

unsigned int i = s;

0000 0000 0000 0100b



Expanding the bit representation of a number

For signed values, we want the number to remain the same, just with more bits. In this case, we perform a "sign extension" by repeating the sign of the value for the new digits. E.g.,

short s = 4;// short is a 16-bit format, so int i = s;

— or —

short s = -4;// short is a 16-bit format, so

int i = s;

s = 0000 0000 0000 0100b

s = 1111 1111 1111 1100b



Sign-extension Example

```
// show bytes() defined on pg. 45, Bryant and O'Halloran
int main() {
   short sx = -12345; // -12345
   unsigned short usx = sx; // 53191
   int x = sx; // -12345
   unsigned ux = usx; // 53191
   printf("sx = %d:\t", sx);
    show bytes((byte pointer) &sx, sizeof(short));
   printf("usx = %u:\t", usx);
   show bytes((byte pointer) &usx, sizeof(unsigned short));
   printf("x = d: t', x);
    show bytes((byte pointer) &x, sizeof(int));
   printf("ux = %u:\t", ux);
   show bytes((byte pointer) &ux, sizeof(unsigned));
   return 0;
```

<pre>\$./sign_extens</pre>	sio	n	
sx = -12345:	c7	cf	
usx = 53191:	c7	cf	
x = -12345:	c7	cf	ff
ux = 53191:	c 7	cf	00

(careful: this was printed on the little-endian myth *machines!*)





Truncating Numbers: Signed

What if we want to reduce the number of bits that a number holds? E.g.

- What happens here? Let's look at the bits in x (a 32-bit int), 53191:
- 0000 0000 0000 0000 1100 1111 1100 0111
- When we cast x to a short, it only has 16-bits, and C *truncates* the number:
- 1100 1111 1100 0111

What is this number in decimal? Well, it must be negative (b/c of the initial 1), and it is -12345.

int x = 53191;short sx = (short) x;int y = sx;



Truncating Numbers: Signed

What if we want to reduce the number of bits that a number holds? E.g.

This is a form of overflow! We have altered the value of the number. **Be careful!**

in the int, so the strange values occur.

What is y above? We are converting a short to an int, so we sign-extend, and we get -12345!

1100 1111 1100 0111 becomes

1111 1111 1111 1111 1100 11111 1100 0111

Play around here: <u>http://www.convertforfree.com/twos-complement-calculator/</u>

int x = 53191;// 53191 short sx = (short) x; // -12345int y = sx;

- We don't have enough bits to store the int in the short for the value we have



Truncating Numbers: Signed

If the number does fit into the smaller representation in the current form, it will convert just fine.

int sho int

1111 1111 1111 1111 1111 1111 1101 becomes X: 1111 1111 1111 11011111 SX:

x =
$$-3;$$
 // -3
ort sx = (short) $-3;$ // -3
y = sx; // -3

Play around here: <u>http://www.convertforfree.com/twos-complement-calculator/</u>



Truncating Numbers: Unsigned

We can also lose information with unsigned int x = 128000; unsigned numbers:

Bit representation for x = 128000 (32-bit unsigned int):

0000 0000 0000 0001 1111 0100 0000 0000

Truncated unsigned short sx:

which equals 62464 decimal.

Converting back to an unsigned int, y = 62464

- unsigned short sx = (short) x; unsigned int y = sx;

1111 0100 0000 0000





Overflow in Unsigned Addition

```
#include<stdio.h>
#include<stdlib.h>
#include<limits.h> // for UINT MAX
int main() {
    unsigned int a = UINT_MAX;
    unsigned int b = 1;
    unsigned int c = a + b;
    printf("a = u \in a;
    printf("b = u \in b;
    printf("a + b = u \in (n, c);
    return 0;
                                    // for a
                                   #include
                                   unsigned
                                   unsigned
                                   if (a >
```

When integer operations overflow in C, the runtime does not produce an error:

- \$./unsigned overflow
- a = 4294967295
- b = 1
- a + b = 0

Technically, unsigned integers in C don't overflow, they just wrap. You need to be aware of the size of your numbers. Here is one way to test if an addition will fail:

addition	
e <limits.< td=""><td>•h></td></limits.<>	•h>
d int a =	<something>;</something>
d int $x =$	<something>;</something>
UINT_MAX	<pre>- x) /* `a + x` would overflow */;</pre>



Overflow in Signed Addition

Signed overflow wraps around to the negative numbers:



(the first video with over INT MAX number of views) was negative.

YouTube fell into this trap — their view counter was a signed, 32-bit int. They fixed it after it was noticed, but for a while, the view count for Gangnam Style



Overflow in Signed Addition

In the news on January 5, 2022 (!):



GOOD THING ANDROID IS GREAT AT ROLLING OUT UPDATES – Google fixes nightmare Android bug that stopped user from calling 911

An integer overflow/underflow crash lets misbehaving apps lock users out of 911.

RON AMADEO - 1/5/2022, 3:09 PM

https://arstechnica.com/gadgets/2022/01/google-fixes-nightmare-android-bugthat-stopped-user-from-calling-911/

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Overflow in Signed Addition

Signed overflow wraps around to the negative numbers.

```
#include<stdio.h>
#include<stdlib.h>
#include<limits.h> // for INT MAX
int main() {
    int a = INT MAX;
    int b = 1;
    int c = a + b;
    printf("a = d \in a;
    printf("b = d \in , b);
    printf("a + b = d \in c;
    return 0;
                      // for addition
                     #include <limits.h>
                     int a = <something>;
                     int x = <something>;
```

- \$./signed overflow a = 2147483647
- b = 1
- a + b = -2147483648

Technically, signed integers in C produce undefined behavior when they overflow. On two's complement machines (virtually all machines these days), it does overflow predictably. You can test to see if your addition will be correct:







References and Advanced Reading

•References:

- Two's complement calculator: <u>http://www.convertforfree.com/twos-complement-</u> calculator/
- •Wikipedia on Two's complement: <u>https://en.wikipedia.org/wiki/</u> Two%27s complement
- •The sizeof operator: <u>http://www.geeksforgeeks.org/sizeof-operator-c/</u>

Advanced Reading:

- •Signed overflow: <u>https://stackoverflow.com/questions/16056758/c-c-unsigned-</u> integer-overflow
- Integer overflow in C: <u>https://www.gnu.org/software/autoconf/manual/</u> autoconf-2.62/html_node/Integer-Overflow.html <u>https://stackoverflow.com/questions/34885966/when-an-int-is-cast-to-a-short-and-</u> truncated-how-is-the-new-value-determined



References and Advanced Reading

•References:

- •argc and argv: <u>http://crasseux.com/books/ctutorial/argc-and-argv.html</u> •The C Language: <u>https://en.wikipedia.org/wiki/C (programming language)</u> •Kernighan and Ritchie (K&R) C: <u>https://www.youtube.com/watch?v=de2Hsvxaf8M</u> •C Standard Library: <u>http://www.cplusplus.com/reference/clibrary/</u> •<u>https://en.wikipedia.org/wiki/Bitwise_operations_in_C</u> •<u>http://en.cppreference.com/w/c/language/operator_precedence</u>

Advanced Reading:

- •After All These Years, the World is Still Powered by C Programming
- Is C Still Relevant in the 21st Century?
- Why Every Programmer Should Learn C





