CS107, Lecture 17
Assembly: Arithmetic and Logic Wrap, Control Flow

Reading: B&O 3.5-3.6

Ed Discussion

Large Multiplication

- Multiplying 64-bit numbers can produce a 128-bit result. How does x86-64 support this with only 64-bit registers?
- If you specify two operands to **imul**, it multiplies them together and truncates it to fit in the second of the two 64-bit register operands.

```
imul S, D        D ← D * S
```

- If you specify one operand, it multiplies that by **%rax**, and splits the product across **2** registers. It puts the high-order 64 bits in **%rdx** and the low-order 64 bits in **%rax**.

Instruction	Effect	Description
`imulq S`	`R[%rdx]:R[%rax] ← S x R[%rax]`	Signed full multiply
`mulq S`	`R[%rdx]:R[%rax] ← S x R[%rax]`	Unsigned full multiply

Division and Remainder

Instruction	Effect	Description
`idivq S`	`R[%rdx] ← R[%rdx]:R[%rax] mod S;` `R[%rax] ← R[%rdx]:R[%rax]` ÷ `S`	Signed divide
`divq S`	`R[%rdx] ← R[%rdx]:R[%rax] mod S;` `R[%rax] ← R[%rdx]:R[%rax]` ÷ `S`	Unsigned divide

- <u>Terminology:</u> **dividend / divisor = quotient with remainder**
- **x86-64** supports dividing up to a 128-bit value by a 64-bit value.
- The high-order 64 bits of the dividend need to be prepared and stored in **%rdx**, the low-order 64 bits in **%rax**. The divisor is the only listed operand.
- The quotient is stored in **%rax**, and the remainder in **%rdx**.

Division and Remainder

Instruction	Effect	Description
`idivq S`	`R[%rdx] ← R[%rdx]:R[%rax] mod S;` `R[%rax] ← R[%rdx]:R[%rax]` ÷ `S`	Signed divide
`divq S`	`R[%rdx] ← R[%rdx]:R[%rax] mod S;` `R[%rax] ← R[%rdx]:R[%rax]` ÷ `S`	Unsigned divide
`cqto`	`R[%rdx]:R[%rax] ← SignExtend(R[%rax])`	Convert to oct word

- Terminology: **dividend / divisor = quotient with remainder**
- The high-order 64 bits of the dividend need to be prepared and stored in %rdx, the low-order 64 bits in %rax. The divisor is the only listed operand.
- Most division uses only 64-bit dividends. The **cqto** instruction sign-extends the 64-bit value in **%rax** into **%rdx** to fill both registers with the dividend, as the division instruction expects.

Compiler Explorer Demo

https://godbolt.org/z/4cT75M4nd

Code Reference: `full_divide`

```
// Returns x/y, stores remainder in location stored in remainder_ptr
long full_divide(long x, long y, long *remainder_ptr) {
    long quotient = x / y;
    long remainder = x % y;
    *remainder_ptr = remainder;
    return quotient;
}

-------

full_divide:
  movq %rdi, %rax
  movq %rdx, %rcx
  cqto
  idivq %rsi
  movq %rdx, (%rcx)
  ret
```

Assembly Exercise 1

```
0000000000040116e <sum_example1>:
  40116e: 8d 04 37          lea  (%rdi,%rsi,1),%eax
  401171: c3                retq
```

Which of the following is most likely to have generated the above assembly?

```
// A)
void sum_example1() {
    int x;
    int y;
    int sum = x + y;
}
```

```
// B)
int sum_example1(int x, int y) {
    return x + y;
}
```

```
// C)
void sum_example1(int x, int y) {
    int sum = x + y;
}
```

Assembly Exercise 2

```
0000000000401172 <sum_example2>:
      401172: 8b 47 0c        mov   0xc(%rdi),%eax
      401175: 03 07           add   (%rdi),%eax
      401177: 2b 47 18        sub   0x18(%rdi),%eax
      40117a: c3              retq
```

```
int sum_example2(int arr[]) {
    int sum = 0;
    sum += arr[0];
    sum += arr[3];
    sum -= arr[6];
    return sum;
}
```

What location or value in the assembly above represents the C code's **sum** variable?

%eax

Assembly Exercise 3

```
0000000000401172 <sum_example2>:
      401172: 8b 47 0c          mov   0xc(%rdi),%eax
      401175: 03 07             add   (%rdi),%eax
      401177: 2b 47 18          sub   0x18(%rdi),%eax
      40117a: c3                retq
```

```c
int sum_example2(int arr[]) {
    int sum = 0;
    sum += arr[0];
    sum += arr[3];
    sum -= arr[6];
    return sum;
}
```

What location or value in the assembly code above represents the C code's **6** (as in **arr[6]**)?

0x18

Reverse Engineering 1

```
int add_to(int x, int arr[], int i) {
    int sum = ___?___;
    sum += arr[___?___];
    return ___?___;
}

----------
// x in %edi, arr in %rsi, i in %edx
add_to:
  movslq %edx, %rdx
  movl %edi, %eax
  addl (%rsi,%rdx,4), %eax
  ret
```

Reverse Engineering 1

```
int add_to(int x, int arr[], int i) {
    int sum = ___?___;
    sum += arr[___?___];
    return ___?___;
}

----------
// x in %edi, arr in %rsi, i in %edx
add_to:
  movslq %edx, %rdx            // sign-extend i into full register
  movl %edi, %eax              // copy x into %eax
  addl (%rsi,%rdx,4), %eax     // add arr[i] to %eax
  ret
```

Reverse Engineering 1

```
int add_to(int x, int arr[], int i) {
    int sum = x;
    sum += arr[i];
    return sum;
}

----------
// x in %edi, arr in %rsi, i in %edx
add_to:
  movslq %edx, %rdx            // sign-extend i into full register
  movl %edi, %eax              // copy x into %eax
  addl (%rsi,%rdx,4), %eax     // add arr[i] to %eax
  ret
```

Reverse Engineering 2

```
int elem_arithmetic(int nums[], int y) {
    int z = nums[___?___] * ___?___;
    z -= ___?___;
    z >>= ___?___;
    return ___?___;
}
----------
// nums in %rdi, y in %esi
elem_arithmetic:
  movl %esi, %eax
  imull (%rdi), %eax
  subl 4(%rdi), %eax
  sarl $2, %eax
  addl $2, %eax
  ret
```

Reverse Engineering 2

```
int elem_arithmetic(int nums[], int y) {
    int z = nums[___?___] * ___?___;
    z -= ___?___;
    z >>= ___?___;
    return ___?___;
}
----------
// nums in %rdi, y in %esi
elem_arithmetic:
  movl %esi, %eax          // copy y into %eax
  imull (%rdi), %eax       // multiply %eax by nums[0]
  subl 4(%rdi), %eax       // subtract nums[1] from %eax
  sarl $2, %eax            // shift %eax right by 2
  addl $2, %eax            // add 2 to %eax
  ret
```

Reverse Engineering 2

```
int elem_arithmetic(int nums[], int y) {
    int z = nums[0] * y;
    z -= nums[1];
    z >>= 2;
    return z + 2;
}
----------
// nums in %rdi, y in %esi
elem_arithmetic:
  movl %esi, %eax          // copy y into %eax
  imull (%rdi), %eax       // multiply %eax by nums[0]
  subl 4(%rdi), %eax       // subtract nums[1] from %eax
  sarl $2, %eax            // shift %eax right by 2
  addl $2, %eax            // add 2 to %eax
  ret
```

Our First Assembly

```
int sum_array(int arr[], int nelems) {
    int sum = 0;
    for (int i = 0; i < nelems; i++) {
        sum += arr[i];
    }
    return sum;
}
```

We’re 1/2 of the way to understanding assembly!
What looks understandable right now?

```
0000000000401136 <sum_array>:
  401136:    b8 00 00 00 00          mov    $0x0,%eax
  40113b:    ba 00 00 00 00          mov    $0x0,%edx
  401140:    39 f0                   cmp    %esi,%eax
  401142:    7d 0b                   jge    40114f <sum_array+0x19>
  401144:    48 63 c8                movslq %eax,%rcx
  401147:    03 14 8f                add    (%rdi,%rcx,4),%edx
  40114a:    83 c0 01                add    $0x1,%eax
  40114d:    eb f1                   jmp    401140 <sum_array+0xa>
  40114f:    89 d0                   mov    %edx,%eax
  401151:    c3                      retq
```

Executing Instructions

What does it mean for a program to execute?

Executing Instructions

So far:

- Program values can be stored in memory or registers.
- Assembly instructions read/write values back and forth between registers and main memory.
- Assembly instructions are **also stored in memory**.

Today:

- **Who controls the instructions**?
  How do we know what to do now or next?

Answer:

- The **program counter**, stored in %rip.

4004fd	fa
4004fc	eb
4004fb	01
4004fa	fc
4004f9	45
4004f8	83
4004f7	00
4004f6	00
4004f5	00
4004f4	00
4004f3	fc
4004f2	45
4004f1	c7
4004f0	e5
4004ef	89
4004ee	48
4004ed	55

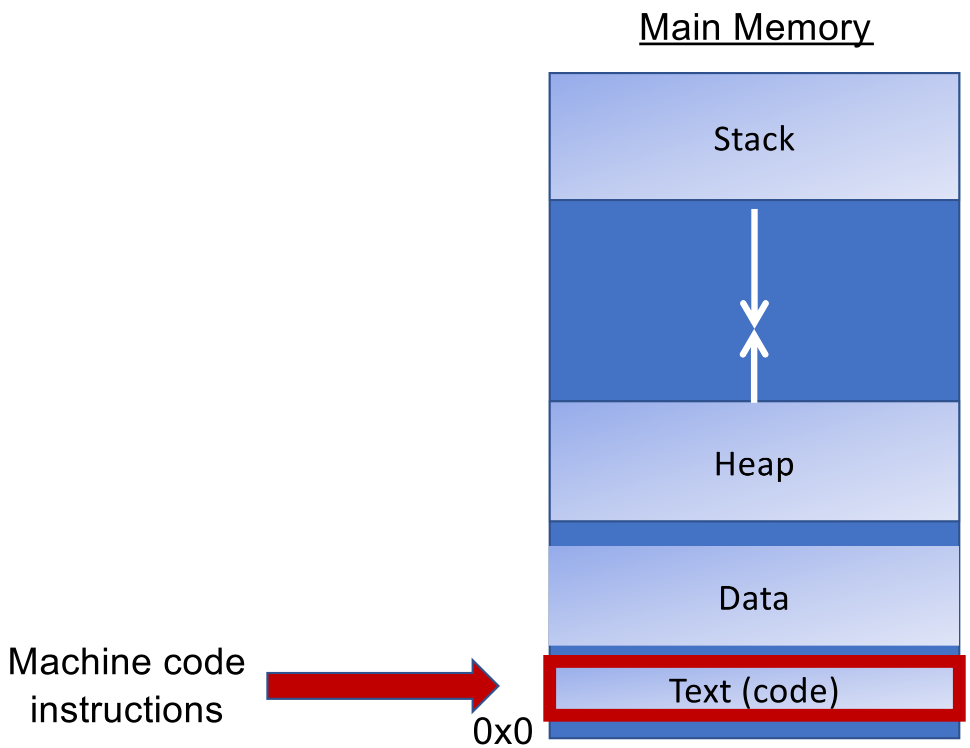
Register Responsibilities

Some registers take on special responsibilities during program execution.

- **%rax** stores the return value
- **%rdi** stores the first parameter to a function
- **%rsi** stores the second parameter to a function
- **%rdx** stores the third parameter to a function
- **%rip** stores the address of the next instruction to execute
- **%rsp** stores the address of the current top of the stack

See the x86-64 Guide and Reference Sheet on the Resources webpage for more!

Instructions Are Just Bytes!

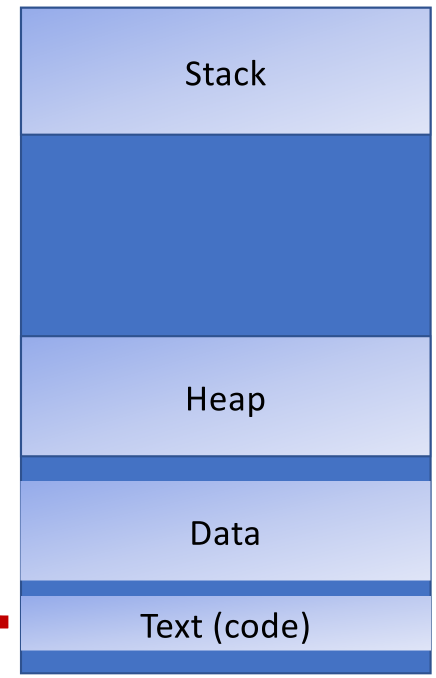


%ri

```
00000000004004ed <loop>:
4004ed: 55                      push   %rbp
4004ee: 48 89 e5                mov    %rsp,%rbp
4004f1: c7 45 fc 00 00 00 00    movl   $0x0,-0x4(%rbp)
4004f8: 83 45 fc 01             addl   $0x1,-0x4(%rbp)
4004fc: eb fa                   jmp    4004f8 <loop+0xb>
```

4004fd	fa
4004fc	eb
4004fb	01
4004fa	fc
4004f9	45
4004f8	83
4004f7	00
4004f6	00
4004f5	00
4004f4	00
4004f3	fc
4004f2	45
4004f1	c7
4004f0	e5
4004ef	89
4004ee	48
4004ed	55

Main Memory



%rip

```
0000000004004ed <loop>:
4004ed: 55                      push   %rbp
4004ee: 48 89 e5                mov    %rsp,%rbp
4004f1: c7 45 fc 00 00 00 00    movl   $0x0,-0x4(%rbp)
4004f8: 83 45 fc 01             addl   $0x1,-0x4(%rbp)
4004fc: eb fa                   jmp    4004f8 <loop+0xb>
```

The **program counter** (PC), known as %rip in x86-64, stores the address in memory of the ***next instruction*** to be executed.

`0x4004ed`

%rip

4004fd	fa
4004fc	eb
4004fb	01
4004fa	fc
4004f9	45
4004f8	83
4004f7	00
4004f6	00
4004f5	00
4004f4	00
4004f3	fc
4004f2	45
4004f1	c7
4004f0	e5
4004ef	89
4004ee	48
4004ed	55

%rip

```
00000000004004ed <loop>:
4004ed: 55                    push   %rbp
4004ee: 48 89 e5              mov    %rsp,%rbp
4004f1: c7 45 fc 00 00 00 00  movl   $0x0,-0x4(%rbp)
4004f8: 83 45 fc 01           addl   $0x1,-0x4(%rbp)
4004fc: eb fa                 jmp    4004f8 <loop+0xb>
```

4004fd	fa
4004fc	eb
4004fb	01
4004fa	fc
4004f9	45
4004f8	83
4004f7	00
4004f6	00
4004f5	00
4004f4	00
4004f3	fc
4004f2	45
4004f1	c7
4004f0	e5
4004ef	89
4004ee	48
4004ed	55

The **program counter** (PC), known as %rip in x86-64, stores the address in memory of the ***next instruction*** to be executed.

`0x4004ee`

%rip

%rip

```
00000000004004ed <loop>:
4004ed: 55                     push   %rbp
4004ee: 48 89 e5               mov    %rsp,%rbp
4004f1: c7 45 fc 00 00 00 00   movl   $0x0,-0x4(%rbp)
4004f8: 83 45 fc 01            addl   $0x1,-0x4(%rbp)
4004fc: eb fa                  jmp    4004f8 <loop+0xb>
```

4004fd	fa
4004fc	eb
4004fb	01
4004fa	fc
4004f9	45
4004f8	83
4004f7	00
4004f6	00
4004f5	00
4004f4	00
4004f3	fc
4004f2	45
4004f1	c7
4004f0	e5
4004ef	89
4004ee	48
4004ed	55

The **program counter** (PC), known as %rip in x86-64, stores the address in memory of the ***next instruction*** to be executed.

0x4004f1

%rip

%rip

```
00000000004004ed <loop>:
4004ed: 55                      push   %rbp
4004ee: 48 89 e5                mov    %rsp,%rbp
4004f1: c7 45 fc 00 00 00 00    movl   $0x0,-0x4(%rbp)
4004f8: 83 45 fc 01             addl   $0x1,-0x4(%rbp)
4004fc: eb fa                   jmp    4004f8 <loop+0xb>
```

4004fd	fa
4004fc	eb
4004fb	01
4004fa	fc
4004f9	45
4004f8	83
4004f7	00
4004f6	00
4004f5	00
4004f4	00
4004f3	fc
4004f2	45
4004f1	c7
4004f0	e5
4004ef	89
4004ee	48
4004ed	55

The **program counter** (PC), known as %rip in x86-64, stores the address in memory of the ***next instruction*** to be executed.

0x4004f8

%rip

%rip

```
0000000004004ed <loop>:
4004ed: 55                      push   %rbp
4004ee: 48 89 e5                mov    %rsp,%rbp
4004f1: c7 45 fc 00 00 00 00    movl   $0x0,-0x4(%rbp)
4004f8: 83 45 fc 01             addl   $0x1,-0x4(%rbp)
4004fc: eb fa                   jmp    4004f8 <loop+0xb>
```

4004fd	fa
4004fc	eb
4004fb	01
4004fa	fc
4004f9	45
4004f8	83
4004f7	00
4004f6	00
4004f5	00
4004f4	00
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4004f1	c7
4004f0	e5
4004ef	89
4004ee	48
4004ed	55

The **program counter** (PC), known as %rip in x86-64, stores the address in memory of the ***next instruction*** to be executed.

0x4004fc

%rip

%rip

```
00000000004004ed <loop>:
4004ed: 55                    push   %rbp
4004ee: 48 89 e5              mov    %rsp,%rbp
4004f1: c7 45 fc 00 00 00 00  movl   $0x0,-0x4(%rbp)
4004f8: 83 45 fc 01           addl   $0x1,-0x4(%rbp)
4004fc: eb fa                 jmp    4004f8 <loop+0xb>
```

Special hardware sets the program counter to the next instruction:

%rip += size of bytes of current instruction

4004fd	fa
4004fc	eb
4004fb	01
4004fa	fc
4004f9	45
4004f8	83
4004f7	00
4004f6	00
4004f5	00
4004f4	00
4004f3	fc
4004f2	45
4004f1	c7
4004f0	e5
4004ef	89
4004ee	48
4004ed	55

0x4004fc

%rip

Going In Circles

- How can we use this representation of execution to represent e.g., a **loop**?
- **Key Idea:** we can override what **%rip** stores and populate it with the address of an earlier instruction.

Jump!

```
00000000004004ed <loop>:
4004ed: 55                      push   %rbp
4004ee: 48 89 e5                mov    %rsp,%rbp
4004f1: c7 45 fc 00 00 00 00    movl   $0x0,-0x4(%rbp)
4004f8: 83 45 fc 01             addl   $0x1,-0x4(%rbp)
4004fc: eb fa                   jmp    4004f8 <loop+0xb>
```

4004fd	fa
4004fc	eb
4004fb	01
4004fa	fc
4004f9	45
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4004f7	00
4004f6	00
4004f5	00
4004f4	00
4004f3	fc
4004f2	45
4004f1	c7
4004f0	e5
4004ef	89
4004ee	48
4004ed	55

The **jmp** instruction is an **unconditional jump** that sets the program counter to the jump target (the operand).

0x4004fc

%rip

Jump!

```
00000000004004ed <loop>:
4004ed: 55                     push   %rbp
4004ee: 48 89 e5               mov    %rsp,%rbp
4004f1: c7 45 fc 00 00 00 00   movl   $0x0,-0x4(%rbp)
4004f8: 83 45 fc 01            addl   $0x1,-0x4(%rbp)
4004fc: eb fa                  jmp    4004f8 <loop+0xb>
```

The **jmp** instruction is an **unconditional jump** that sets the program counter to the **jump target** (the operand).

4004fd	fa
4004fc	eb
4004fb	01
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4004f9	45
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4004f7	00
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4004f5	00
4004f4	00
4004f3	fc
4004f2	45
4004f1	c7
4004f0	e5
4004ef	89
4004ee	48
4004ed	55

0x4004fc

%rip

Jump!

```
0000000004004ed <loop>:
4004ed: 55                    push   %rbp
4004ee: 48 89 e5              mov    %rsp,%rbp
4004f1: c7 45 fc 00 00 00 00  movl   $0x0,-0x4(%rbp)
4004f8: 83 45 fc 01           addl   $0x1,-0x4(%rbp)
4004fc: eb fa                 jmp    4004f8 <loop+0xb>
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4004fd	fa
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The **jmp** instruction is an **unconditional jump** that sets the program counter to the **jump target** (the operand).

0x4004fc

%rip

Jump!

```
00000000004004ed <loop>:
4004ed: 55                      push   %rbp
4004ee: 48 89 e5                mov    %rsp,%rbp
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4004fc: eb fa                   jmp    4004f8 <loop+0xb>
```

4004fd	fa
4004fc	eb
4004fb	01
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4004f9	45
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4004f0	e5
4004ef	89
4004ee	48
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The **jmp** instruction is an **unconditional jump** that sets the program counter to the **jump target** (the operand).

0x4004fc

%rip

Jump!

```
00000000004004ed <loop>:
4004ed: 55                        push   %rbp
4004ee: 48 89 e5                  mov    %rsp,%rbp
4004f1: c7 45 fc 00 00 00 00      movl   $0x0,-0x4(%rbp)
4004f8: 83 45 fc 01               addl   $0x1,-0x4(%rbp)
4004fc: eb fa                     jmp    4004f8 <loop+0xb>
```

This assembly represents an infinite loop in C!

```
while (true) {…}
```

4004fd	fa
4004fc	eb
4004fb	01
4004fa	fc
4004f9	45
4004f8	83
4004f7	00
4004f6	00
4004f5	00
4004f4	00
4004f3	fc
4004f2	45
4004f1	c7
4004f0	e5
4004ef	89
4004ee	48
4004ed	55

0x4004fc

%rip

jmp

The **jmp** instruction jumps to another instruction in the assembly code (an "unconditional jump").

```
jmp Label       (Direct Jump)
jmp *Operand    (Indirect Jump)
```

The destination can be hardcoded into the instruction (direct jump):

```
jmp 404f8 <loop+0xb>  # jump to instruction at 0x404f8
```

The destination can also be one of the usual operand forms (indirect jump):

```
jmp *%rax     # jump to instruction at address in %rax
```

"Interfering" with %rip

1. How do we repeat instructions in a loop?

   `jmp [target]`

   - A 1-step unconditional jump (always jump when we execute this instruction)

   What if we want a **conditional jump**?