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# Communication and Language Emergence Among Populations and Clusters of Agents

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## Abstract

1 Algorithms and other intelligent systems are increasingly able to harness the  
2 power of language across a large number of domains. Alongside these rapid  
3 developments has come an increased interest in the mechanisms that underly the  
4 acquisition and emergence of language. Through the use of communication games,  
5 researchers have been able to investigate how pairs of agents can learn to converge  
6 to a pattern of linguistic communication. We combine the methods of multiple  
7 researchers to confirm earlier findings. Further, we extend a classic communication  
8 game to a population of more plausible communicator agents and investigate  
9 the effects population size has on the ability for agents to learn to communicate.  
10 Finally, we explore the effect of partitioning the population of agents into clusters  
11 and examine whether and how the performance of the population changes under  
12 different clustering schemes.

## 13 1 Introduction

14 Language is one of the most important aspects of human life. It allows us to communicate concepts  
15 from the simple to the extraordinary with clarity and precision. In turn, these concepts allow humans  
16 to cooperate in meaningful ways, to share knowledge among a group and to coordinate efforts among  
17 many people with different understandings and sets of knowledge. Artificially intelligent systems are  
18 increasingly able to capture the power of language, but modelling the acquisition of those linguistic  
19 skills remains difficult.

20 Most efforts to study the formation of language center on the use of “emergent communication  
21 tasks”—situations in which agents must learn to communicate linguistically (i.e. with discrete  
22 symbols) in order to jointly complete some task. Agents begin without any knowledge of the world  
23 or of the symbols they will use to communicate; everything is learned simply through interaction  
24 with other agents. While there are many differences between such a scheme and the way in which  
25 humans may learn language, these “language games” nonetheless provide a fertile ground in which to  
26 test different theories of linguistic communication.

27 While many modern approaches yield impressive results on these tasks, they tend to focus on the  
28 interaction between a single pair of agents, one that exclusively speaks and another that exclusively  
29 listens. This approach, however, misses some of the complexity of real linguistic systems. In humans,  
30 for instance, speaking and listening systems in brain are closely interconnected. It is worth exploring,  
31 then, agents who have are capable of both speaking and listening as the situation demands it.

32 Secondly, communication often occurs between entire groups of agents and not only between isolated  
33 pairs. Nevertheless, most communication games have only two players and do not examine the  
34 interaction of larger populations of agents all completing the task simultaneously. In order for artificial  
35 systems to replicate the cooperation found among groups humans, it will be important to explore how  
36 existing research can be extended to larger populations of agents.

37 Our work is motivated by these two points. We extend a classic emergent communication task, the  
38 Lewis Signalling Game (described below), to a population of agents that are each capable of both  
39 speaking and listening. We refer to the new game as the population signalling task. We are still  
40 interested in a cooperative setting (though competition between agents has proven to be an effective  
41 way to learn language as well, as demonstrated by [2]), and so examine the overall performance of  
42 the entire population.

43 Within the population signalling task, we are also interested in the effect of clustering, or partitioning  
44 a larger population of agents into smaller sub-groups. Clustering has some grounding in real  
45 communicators, as geography and other factors may cause some agents to become linguistically  
46 isolated from others. Specifically, we manipulate the "hardness" of the clustering and examine its  
47 impact on the overall performance of the population. By hardness, we mean the probability that an  
48 agent communicates within its cluster, if that probability is 1, then we say the clustering is hard. If  
49 that probability is low, so that agents communicate with all other agents at roughly the same rate,  
50 we say the clustering is soft. Again, we may ground this notion of hardness in the real world by  
51 comparing it to the physical distance between clusters (if clusters are very far apart, we would expect  
52 few instances of communication between them). We hypothesized that the relationship between the  
53 hardness of clustering and performance may be non-linear, with an optima somewhere between the  
54 softest and hardest clustering schemes.

55 Such non-linearity would indicate the complexity of the population signalling task and perhaps  
56 motivate future research into the population dynamics of artificial communicator agents.

## 57 **2 Related Work**

58 Our work combines the methods and approaches of many previous scholars. The Lewis Signalling  
59 Game and its variants are well studied in [4], [3], [5], [1], and [6]. Many of these studies involve  
60 image processing, in which agents are given raw pixel data and must, in addition to learning how  
61 to communicate, learn how to extract valuable information from an image. Our work hews more  
62 closely to the original signalling game and the work presented in [4], focusing instead on symbolic  
63 representations of concepts encoded as vectors of attributes.

64 Most research into the emergence of linguistic communication uses reinforcement learning techniques.  
65 This is reasonable, as the signalling game has a clearly defined reward structure and involves a  
66 sequence of discrete decisions. Our work, however, draws more inspiration from the work of [3], who  
67 have developed a strategy for using standard neural network techniques to optimize the signalling  
68 task. Their methods are described in more detail below.

69 Finally, it is important to acknowledge the work of [6], who have also studied the emergence of  
70 linguistic communication in populations of agents capable of both speaking and listening. They  
71 use a novel communication game in which agents must guide each other towards landmarks in a  
72 two-dimensional environment. They frame their task as a partially observable Markov game and  
73 are able to achieve noteworthy results (including the possibility for non-verbal communication  
74 resulting from agents' ability to view each other moving in the environment). Additionally, instead  
75 of communicating in discrete messages, agents emit continuous streams of symbols. While their  
76 approach differs somewhat from our own, their research similarly extends classic signalling games to  
77 populations of agents.

## 78 **3 Approach**

### 79 **3.1 Problem Description**

80 Our agents are designed to complete a specific emergent communication task called a "referential  
81 game" based on the Lewis Signaling Game. Two agents, a speaker and a listener, must cooperate in  
82 order to complete the game successfully. In the game, a "speaker" agent receives a target item, which  
83 has some discrete characteristics. The speaker then produces a "message" consisting of items chosen  
84 from some "alphabet." A second agent, referred to as the "listener," receives the message from the  
85 speaker and then must choose the target object from a set of distractor objects (also referred to as  
86 candidate objects). Performance in the game is often measured by "communicative success," or the

87 proportion of the time that the listener correctly identifies the target item. Many variants of this game  
88 exist in the literature, though most share these basic features.

89 Additionally, we extend the Lewis Signalling Game to a population of agents, with the following  
90 important distinction: in the standard signalling game, the speaker and listener are separate agents,  
91 whereas in the population version, a single agent consists of a paired speaker and listener, allowing  
92 each agent to participate in bi-lateral communication with other agents. We divide our  $n$  agents into  $k$   
93 distinct clusters (though  $k$  may equal 1). At each step, we select a random agent to be the "speaker."  
94 We then select the listener agent from within the speaker's cluster with probability  $p$ , or from outside  
95 the cluster with probability  $1 - p$ . By modifying  $p$  we are able to manipulate the "hardness" of  
96 the clustering. Setting  $p = 1.0$  corresponds to the "hardest" clustering, as agents communicate  
97 exclusively within their clusters, while setting  $p = \frac{1}{k}$  corresponds to the "softest" clustering, as agents  
98 are equally likely to communicate with any other agent.

99 The goal of the population is to achieve the highest possible mean communication success across all  
100 possible pair-wise communications. In this way, the task is still cooperative, as agents are encouraged  
101 to globally converge on a single language in order to maximize the total communication success.

102 Importantly, we note that agents are not given any identifiers of the other agents, such as a token  
103 representing their index within the population. This means that agents cannot learn to speak distinct  
104 languages with specific other agents, must instead attempt to learn one unified language. While  
105 poly-lingualism is obviously well motivated in the real world, it is beyond the scope of this project.

## 106 3.2 Agent Architecture

107 The speaker and listener agents both use an encoder network and a decoder network. The speaker  
108 first uses the encoder, a single affine transformation, to produce a representation of the target object.  
109 Then, the speaker uses its decoder, a single-layer LSTM, to produce the message from the target  
110 object's representation. The speaker feeds the representation of the target object as the initial hidden  
111 state of the LSTM, and uses the zero-vector as the initial input. At each step, the speaker generates  
112 the next hidden state of the LSTM and projects that hidden state into a distribution over words in  
113 the vocabulary using another affine transformation. A symbol is selected from the vocabulary using  
114 the Gumbel Softmax distribution to approximate sampling from a categorical distribution (see below  
115 for more detail on Gumbel Softmax). The generated symbol is used as the input for the next step.  
116 This process continues until a special STOP symbol is generated or the message reaches a maximum  
117 length.

118 At this point, the listener receives the message. The listener uses its decoder, which is also a single-  
119 layer LSTM, to walk through the message one symbol at a time. The final hidden state of the  
120 listener's decoder is passed through the listener's encoder, an affine transformation, and used as the  
121 "interpretation" of the message. All of the preceding architecture was implemented from scratch,  
122 though the techniques are described in [4] and [3].

123 Once again, we note the distinction between "agents" in the standard signalling game and those  
124 in the population signalling game. An agent in the population contains both of the above speaker  
125 and listener systems. Each system is optimized independently (though see notes on "self-listening"  
126 below).

## 127 3.3 Baselines

128 The most intuitive baseline for the referential game task is the random policy, where the listener  
129 simply selects from the distractor set randomly, effectively ignoring the message. We also compare  
130 the performance of the complete model to the model with the speaker parameters frozen and to the  
131 model with the listener parameters frozen, to see if both parts of the model are necessary for good  
132 performance.

## 133 3.4 Loss

134 After obtaining the message interpretation, the agents are able to compute the following loss function:

$$\mathcal{L}_{\phi, \theta}(t) = \mathbb{E}_{m_t \sim p_{\phi}(\cdot|t)} \left[ \sum_{k=1}^K \max[0, 1 - f(t)^T g(h_i^T) + f(d_k)^T g(h_i^T)] \right]$$

135 Here,  $f(t)$  is the encoding of the target object’s features.  $g(\cdot)$  is the listener’s encoder, being applied  
 136 to  $h_i^T$ , the final hidden state of the listener’s decoder LSTM. The  $d_i$ ’s are the encoding of the objects  
 137 in the distractor set (including the target).

138 Normally, it would be impossible to backpropagate this loss directly through both the listener and  
 139 speaker parameters, as generating the message involves sampling from a categorical distribution,  
 140 a non-differentiable operation. However, the Gumbel Softmax trick allows us to approximate this  
 141 sampling with a differentiable function, allowing the loss to be backpropagated normally. However,  
 142 using the output of the Gumbel Softmax directly would result in a significantly easier problem, as  
 143 the message would consist of real-valued vectors instead of one-hot symbols. So, in order to keep  
 144 the task realistic, we employ the Straight-Through Gumbel-Softmax trick (ST-GS). With ST-GS, we  
 145 convert the Gumbel Softmax output to a one-hot vector in the forward pass, and use the real-valued  
 146 vector in the backwards pass. This technique is described in [3]. The implementation of ST-GS is  
 147 from [7]. With all this in place, we are able to directly update our parameters to minimize the loss  
 148 using the Adam optimizer.

### 149 3.5 Communication Success

150 While our optimization objective is to minimize the above loss function, we are also interested in the  
 151 more interpretable measure of communication success. We define communication success as follows.  
 152 We use the following function to determine a distribution over each object  $v$  in the distractor set:

$$E(v, m_t) = -f(v)^T g(h_i^T(m_t))$$

153 We say that the agents have achieved communication success if the highest probability in the  
 154 distribution corresponds to the target object, as described in [3]. We use communication success as  
 155 our measure of a model’s performance in the following experiments.

### 156 3.6 Self-Listening

157 One of the effects of independently optimizing an agent’s speaker and listener systems is the possibility  
 158 of the two systems converging to distinct languages. Using a human metaphor, this would be akin  
 159 to speaking a language you don’t understand or understanding a language you can’t speak. While  
 160 such effects are possible among real communicators, we seek to diminish their occurrence among the  
 161 artificial agents through the use of self-listening. Simply put, whenever an agent speaks to another  
 162 agent, it also plays the reference game with itself, attempting to guess the target object with its own  
 163 listener system. Since the listener system is distinct, this is not a trivial task for an agent despite its  
 164 apparent access to the target object. The idea is that by attempting to minimize the loss between its  
 165 own internal systems at each step, agents are strongly encouraged to converge to a single language  
 166 between their speaker and listener systems.

## 167 4 Experiments

### 168 4.1 Data

169 Some previous experiments have used the Visual Attributes for Concepts (ViSA) dataset, which  
 170 consists of 500 concepts that have been annotated by humans using 636 discrete attributes (see [4]).  
 171 Since experiments on this dataset involve many parameters and are quite challenging, we have also  
 172 created a simpler, custom dataset based on ViSA. The custom dataset consists of 250 concepts with  
 173 300 attributes. Each concept is given a random number of attributes, drawn from a normal distribution  
 174 with mean 10 and standard deviation 2. While the custom dataset does not capture anything about the  
 175 real world, it still captures the difficulty of the referential game and allows fewer parameters to be  
 176 used. For this reason, the custom dataset was selected for the following experiments.

177 **4.2 Evaluation Method**

178 We use Communication Success as our evaluation method, as described above.

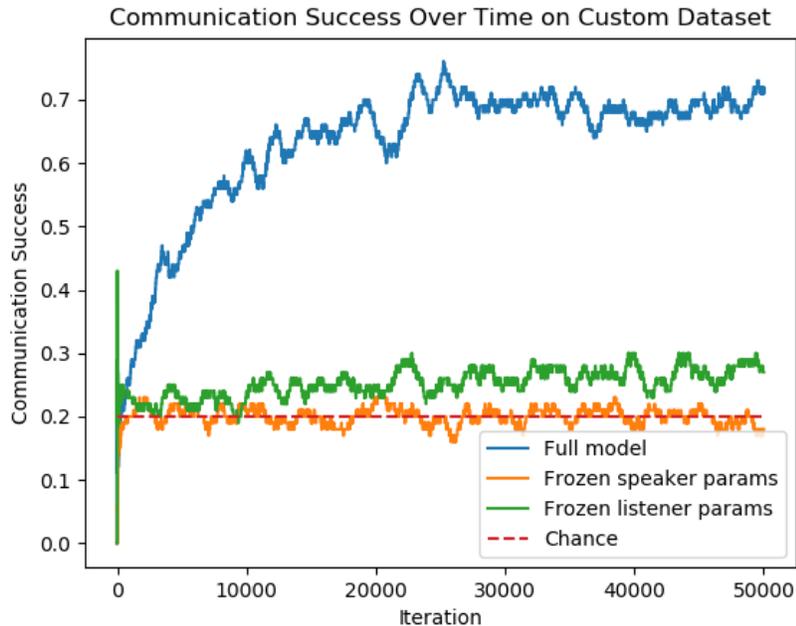
179 **4.3 Experimental Details**

180 We conduct three main experiments. The first experiment simply tests the capability of a single  
181 speaker and listener to complete the Lewis Signalling Task without any interference from other agents.  
182 For this first experiment, we use a single-layer LSTM with a hidden size of 50 for both the speaker  
183 and listener. The concept dictionary contains 250 concepts with 300 possible attributes (see above).  
184 The vocabulary has size 50. We note that it is important to have the vocabulary size be lower than  
185 the number of concepts, so that there can be no simple mapping from single symbols to concepts.  
186 The maximum sentence length is 10. We use an Adam optimizer with initial learning rate of 0.01.  
187 Training time was approximately one hour on a laptop.

188 Our second experiment demonstrates the interference effect of populations of agents. One of the  
189 effects of increasing the population size is that for a fixed number of training episodes, each individual  
190 agent pair gets fewer training iterations. In order to demonstrate that the decrease in agent performance  
191 cannot solely be accounted for by this drop in training episodes, we conducted an experiment in  
192 which each increase in population was accompanied by a corresponding increase in the total number  
193 of training episodes, so that the expected number of training episodes for each speaker/listener pair  
194 remained constant. Each agent used the same parameters as above. We compare populations of size  
195 1, 2, 4, and 8 trained for 1562, 6250, 25000, and 100000 iterations respectively (we note that in each  
196 case the expected number of training episodes for each possible pair of agents is 1562). In each case,  
197 there were no clusters within the population, so all agents communicate with all other agents with  
198 equal probability.

199 Our third experiment explores the effect of the probability of training within the cluster,  $p$ , on the  
200 overall performance of a population of agents. Agents use the same architecture and hyper-parameters  
201 described above for their speaker and listener systems. The population size was 9, and agents were  
202 partitioned into 3 equally-sized clusters of 3 agents. We compare the results for the following values  
203 of  $p$ : 0.33 (corresponding to no clustering), 0.45, 0.66, 0.85, and 1.0 (corresponding to the hardest  
204 clustering possible).

205 **4.4 Results: Experiment One**



206

207 Above, we present a plot of the communication success of a single speaker and listener pair after a  
208 number of iterations.

209 As we can see, the model is able to achieve fairly impressive success on the task, reaching a  
210 communication success of around 0.7 after 50000 iterations, significantly outperforming chance.  
211 More importantly, we note that freezing the parameters of either the speaker or listener significantly  
212 lowers performance. Specifically, freezing the speaker parameters seems to result in performance no  
213 better than chance, and freezing the listener parameters results in a peak communication success of  
214 about 0.3. This indicates that the entire model is important for achieving success in the referential  
215 game. Overall, these results are somewhat expected. The referential game task is well studied,  
216 and experts are able to achieve results even superior to the ones presented here. This may simply  
217 be a matter of computational power, as it is possible that with sufficient time and resources this  
218 model would achieve comparable results to previous research. Nevertheless, this initial experiment  
219 demonstrates the capability of the model and architecture in learning to complete the standard  
220 signalling task and hence implies its potential ability to learn the population signalling task.

#### 221 4.5 Results: Experiment Two

222 Below we present a table of the overall communication success for populations of agents of various  
223 sizes with a fixed number of training iterations per pair of agents.

	Population size	Peak population performance
224	1	0.393
	2	0.370
	4	0.352
	8	0.275

225 We note a consistent decrease in performance for each increase in population size. This result  
226 indicates that the difficulty of the population signalling game does not come exclusively from the  
227 fact that each pair of agents receives fewer training iterations in expectation, but is also driven by  
228 the interference of communicating with many distinct agents. This result makes intuitive sense.  
229 As agents train, they are stochastically exposed to many other agents, each potentially speaking  
230 distinct languages. At each step, agents greedily attempt to converge to a single language with  
231 whichever agent they are currently communicating. As more agents enter the population, each agent  
232 is effectively drawn in more different directions. A potential improvement in communication success  
233 with one agent may result in a decrease in performance with another agent and be undone in the  
234 next training iteration. Smaller populations, then, seem to allow for easier learning, while larger  
235 populations must struggle to converge towards a single language.

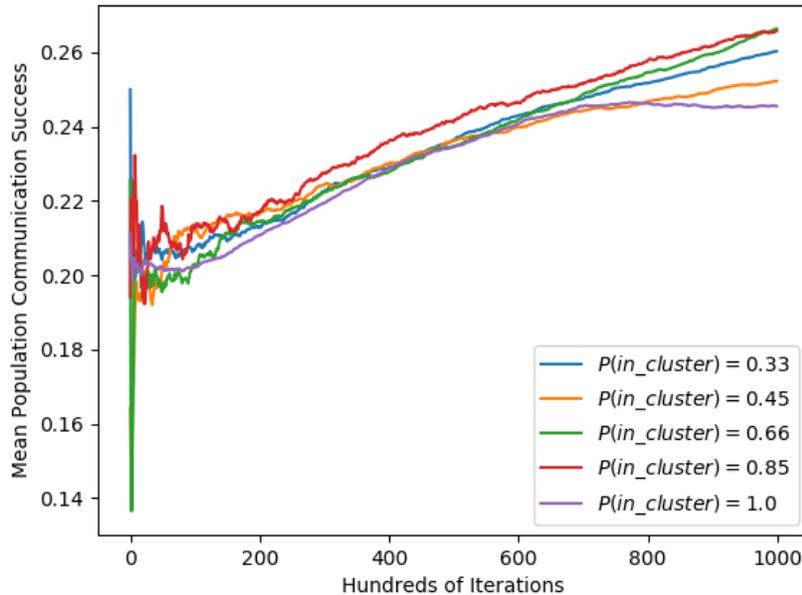
236 This result motivates our final experiment. Clusters have the potential to act as smaller sub-populations  
237 embedded within the complete population, allowing agents to rapidly converge to a language within  
238 their cluster and then using that knowledge to bootstrap convergence among the entire population.

#### 239 4.6 Results: Experiment Three

240 Below we present a plot of the overall performance of a population for distinct values of  $p$ , the  
241 probability that agents train within their clusters:

242 The plot demonstrates a slight effect of  $p$  on the overall performance of the population. Specifically,  
243 we note that the two extreme values of  $p$ , 0.33 and 1.0, do not achieve optimal results. Instead,  
244 the best performance is achieved with an intermediary value of  $p$ , such as 0.66 or 0.85. This is  
245 noteworthy, because it provides some evidence towards our hypothesis that some amount of clustering  
246 is beneficial for populations of agents in this task, but that too much or too little clustering hinders  
247 overall performance. In other words, there is some non-linearity in the interaction between clustering  
248 and overall population performance. However, it is important to note that the difference in overall  
249 performance is quite small between trials, and it is difficult to draw strong conclusions from such  
250 narrow results. The small impact of modifying  $p$  may also stem from the high difficulty of the  
251 task (see below). Since all observed populations perform relatively poorly on the task, it may be  
252 difficult to notice differences in performance. It is possible that running the experiment for a greater  
253 number of iterations or deploying other improvements to the model could result in larger performance  
254 differences.

Mean Population Performance for Different Rates of Clustering



255

256 Two further details are worth mentioning from this experiment. The first is the apparent instability at  
 257 the beginning of the trials, with some runs having early performances as low as 0.14 and as high as  
 258 0.25. This is simply the result of how performances were calculated. We averaged the communication  
 259 success (which is itself an average over multiple examples) of each possible pair-wise communication.  
 260 Early on, there are simply far fewer training examples for each pair, and hence estimates of the mean  
 261 are high variance and prone to fluctuation. We note that the performance trajectories seem to smooth  
 262 out after around 30000 iterations, as estimates become more accurate.

263 The second detail is that overall communication success is quite low. Agents begin at performances of  
 264 roughly 0.2 (chance), and after 100000 iterations reach overall performances of roughly 0.26 to 0.27.  
 265 We note that while this performance is above chance, it falls significantly below the performance of  
 266 0.7 achieved in Experiment One. Why might this be? Simply put, the population signalling game  
 267 is a very difficult task. Moving from a single speaker and listener to many brings with it a host of  
 268 difficulties. Each agent must attempt to learn a pattern of communication from the ground up with  
 269 fewer training examples, while also dealing with the interference demonstrated in Experiment Two.  
 270 Even clustering, which is designed to alleviate some of the challenges of a larger population, cannot  
 271 eliminate the underlying difficulty of the task.

## 272 5 Analysis

273 We focus our analysis on Experiment Three. Our primary area of interest is the effect of modifying  
 274  $p$  on the performance of the entire population, and while our results indicate some non-linearity in  
 275 this interaction, performance did not vary overly much with modifications to  $p$ . Why might this have  
 276 been?

277 One possible explanation is that advantages from clustering to in-cluster performance are strongly  
 278 counterbalanced by disadvantages in out-of-cluster performance. Intuitively, clustering trades in-  
 279 creased performance with a smaller subset of agents for decreased performance against other agents  
 280 (simply in terms of number of training iterations with other agents). In the extreme case (where  
 281  $p = 1.0$ ), agents effectively forfeit their performance against out of cluster agents in order to solely  
 282 optimize their in-cluster performance. We note that in Experiment Three, each cluster consisted 3  
 283 agents, meaning 6 agents were out of cluster and hence accounted for twice as much weight in the  
 284 overall performance of the population. In order to positively affect overall performance, any increase  
 285 to in-cluster performance would need to be more than twice as large as the corresponding decrease  
 286 in performance for out-of-cluster agents. Hence, even if clustering provided some advantage, if

287 the advantage was small it would be difficult to spot using our measure of overall population  
288 performance.

289 We also note that in the population signalling game, the agents do not seem to be taking full advantage  
290 of their vocabulary. For example, we examine the messages produced by the third population in  
291 Experiment Three (the highest performing population in the experiment, with  $p = 0.66$ ).

292 For items 87, 88, 89, and 90 (a small subset of all 250 possible items), Agent 0 produces the following  
293 messages:

	Item	Message Produced by Agent 0
	87	[36, 5, 5, 5,]
294	88	[22, 5, 5, 5]
	89	[36, 5, 9, 5, 9]
	90	[36, 5, 5, 9, 5]

295 Overall, Agent 0 uses only **16** out of the possible 50 symbols in its messages, and uses the fifth symbol  
296 a staggering **60.8%** of the time. This *exact* pattern is not shared by other agents in the population  
297 (for instance, Agent 3 uses 24 of 50 symbols and favors symbol 12, using it 20.2% of the time), but  
298 there seems to be a general trend of each agent using far less than the maximum number of possible  
299 symbols in its communications.

300 As a whole, the entire population uses only 48 of the available 50 symbols in its messaging, and  
301 each agent seems to favor its own subset of symbols. This indicates that the population has not  
302 converged to a single language, and that individual speakers are either extremely efficient at encoding  
303 the concepts or are yet to fully instantiate a mapping from concepts to symbols (the latter explanation  
304 seeming more likely given the low overall performance of the population). Even within clusters  
305 there seems to be little overall cohesion. It is possible then that the listener systems are capable of  
306 mapping multiple distinct message to the same target object. Alternatively, agents may at this stage  
307 have learned only to successfully communicate about a small portion of the overall set of symbols.

## 308 **6 Conclusion**

309 Ultimately, this work should be viewed as preliminary results in the efforts of extending research of  
310 linguistic communication to populations of multiple agents. We confirm that pairs of speakers and  
311 listeners are capable of converging to a solution in the Lewis Signalling Game, analyze the interference  
312 effects of populations of agents, and begin to investigate effects of clustering in populations of agent  
313 communicators. We present some evidence that the "hardness" of the clustering has a non-linear  
314 effect on the overall performance of the population. However, the results of this final experiment are  
315 limited. The differences in population performance were quite small, and the overall performance  
316 quite low. While some of this is likely the result of the inherent difficulty of the population signalling  
317 task, more research must be done before strong conclusions can be drawn. Future work might take  
318 advantage of more computational resources and different techniques to examine larger populations  
319 of agents or existing populations for longer periods of time. Alternatively, experiments surrounding  
320 populations and clustering could be performed on other communication games.

## 321 **7 Additional Information**

322 **Mentor:** Michael Hahn

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