

Name: \_\_\_\_\_

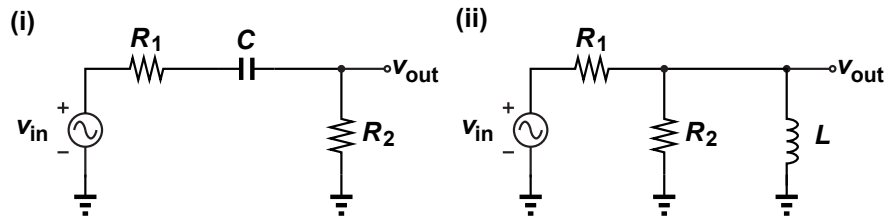
Lab section/TA: \_\_\_\_\_

## ENGR 40M Problem Set 5

Due 1:30pm, August 14, 2017

### Problem 1: Passive filters

(10 points) Please answer the follow questions based on the figure below.



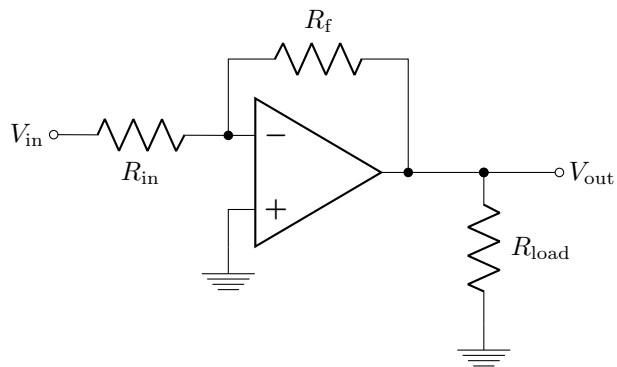
(a) For the circuit in (i) please derive its transfer function, i.e.,  $\frac{V_{out}}{V_{in}}$  with respect to frequency,  $f$ .

(b) What kind of circuit is it? (*Hint: low-pass, high-pass, band-pass, or band-stop.*)

(c) If the circuit in (ii) has the same transfer function, i.e., the same  $\frac{V_{out}}{V_{in}}$  as that of the circuit in (i), what are the conditions that  $L$ ,  $R_1$  and  $R_2$  need to satisfy?

## Problem 2: Inverting amplifier

(15 points) Consider the inverting amplifier shown below, with  $R_f = 10\text{ k}\Omega$  and  $R_{\text{in}} = 1\text{ k}\Omega$ .



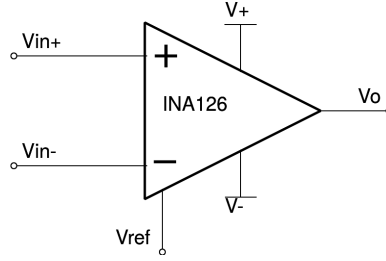
(a) For  $R_{\text{load}} = \infty$ , find the gain of the circuit,  $V_{\text{out}}/V_{\text{in}}$ .

(b) For  $R_{\text{load}} = 200\ \Omega$ , find the gain of the circuit,  $V_{\text{out}}/V_{\text{in}}$ .

(c) For  $R_{\text{load}} = 200\,\Omega$ ,  $V_{\text{in}} = 250\,\text{mV}$ , find the power dissipated by  $R_{\text{load}}$ .

### Problem 3: Instrumentation Amplifier (INA126P)

(15 points)

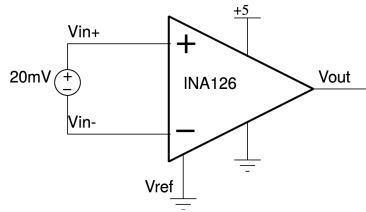


For this problem we consider a INA126P instrumentation amplifier (IA), which you will be using in lab 4. While similar to opamps, IAs do not follow the “golden rules”. Instead, the behavior of the IA can be described by the following equation:

$$V_o = G \cdot (V_{in}^+ - V_{in}^-) + V_{ref},$$

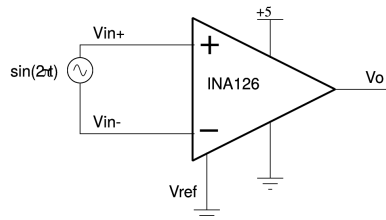
where  $G$  is the gain of the IA,  $V_{in}^+$  and  $V_{in}^-$  are the input terminals,  $V_{ref}$  is called the “reference voltage”, and  $V_+$ ,  $V_-$  are used to supply power to the amplifier.

As a simple example, let us look at a DC input, assuming the IA has a gain  $G$  of 100.

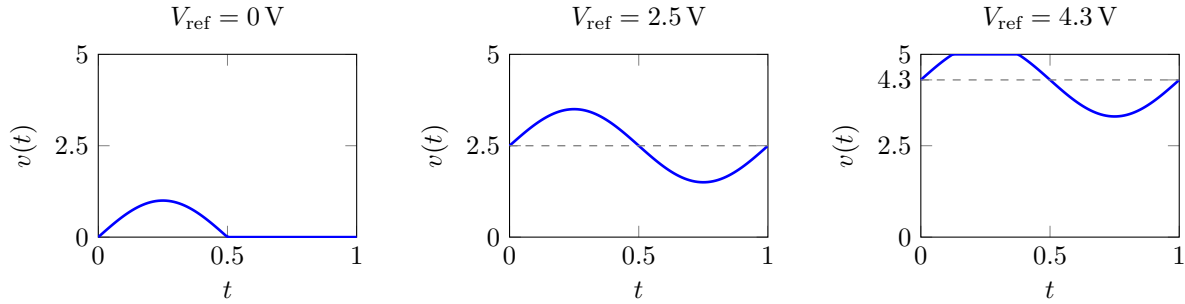


$$V_o = 100 \cdot 20 \text{ mV} + 0 \text{ V} = 2 \text{ V}.$$

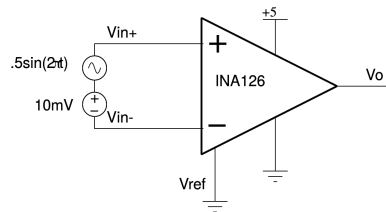
However, there is one additional consideration. The output voltage is limited by the supply voltages  $V_+$  and  $V_-$ . Instead of going above  $V_+$  or below  $V_-$ , the output signal will be cut off or ‘clipped’ so that it stays within the supply voltages. Consider the following example.



Assume that our input is a 10 mV peak-to-peak (10 mVpp) sine wave between  $V_{in}^+$  and  $V_{in}^-$  and  $V_{ref} = 0 \text{ V}$ . If  $G = 100$ , then we would ideally see a 1 Vpp sine wave at the output, centered at 0 V. However, since  $V_-$  is connected to GND, the output signal cannot be less than 0 V, and therefore, the output signal is clipped, as shown in the leftmost figure below. One solution to this problem is to change the reference voltage, which sets the “zero” reference of the output circuit. If our supply voltage range goes from 0 – 5 V, we can generate 2.5 V as the reference voltage, so we can support sine waves that go above and below the reference without going outside of our supply voltage range. With  $V_{ref} = 2.5 \text{ V}$  the 1 Vpp sine wave would 2.5 V and go from 2 – 3 V. Other reference voltages are possible, but would cause the output signal to get clipped at lower amplitudes.



Let's start off with the below configuration.  $V_{\text{ref}}$  and  $V_{\text{in}}^-$  are both connected to gnd.  $V_{\text{in}}^+$  is connected to a sine wave of amplitude 1 mVpp, centered at 10 mV (thus the max value is 10.5 mV, and the min value is 9.5 mV). Assume that  $G = 100$ .



- (a) Sketch the output waveform. Note that the gain applies to the offset voltage as well as the signal amplitude. On your output waveform, label the offset, minimum, and maximum voltages.

- (b) Now we connect the reference pin to 2.5 V instead of ground. Sketch the new output waveform. Can you still see the full sine wave?

- (c) In truth, signals get cut off slightly before they hit the rails. To be safe, we will try to keep our entire output signal between 1 V and 4 V. With the same setup from (b), what is the largest possible gain that would not clip your output signal?

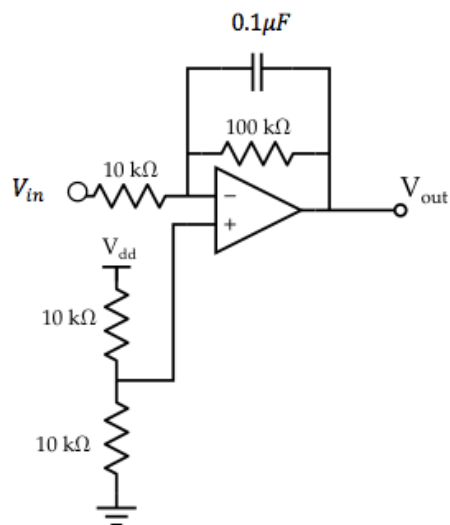
- (d) We can select the gain  $G$  of an IA using a resistor  $R_g$ . According to the datasheet for the INA126P,

$$V_o - V_{\text{ref}} = \left( 5 + \frac{80 \text{ k}\Omega}{R_g} \right) \cdot (V_{\text{in}+} - V_{\text{in}-})$$

Using this formula, what resistor value  $R_g$  will give you the gain computed in part (c)?

#### Problem 4: Operational Amplifier (LM4250CN)

(25 points) For this problem, we look at a simplified version of a subcircuit you will be using in lab 4. Assume  $V_{dd} = 5\text{ V}$ .



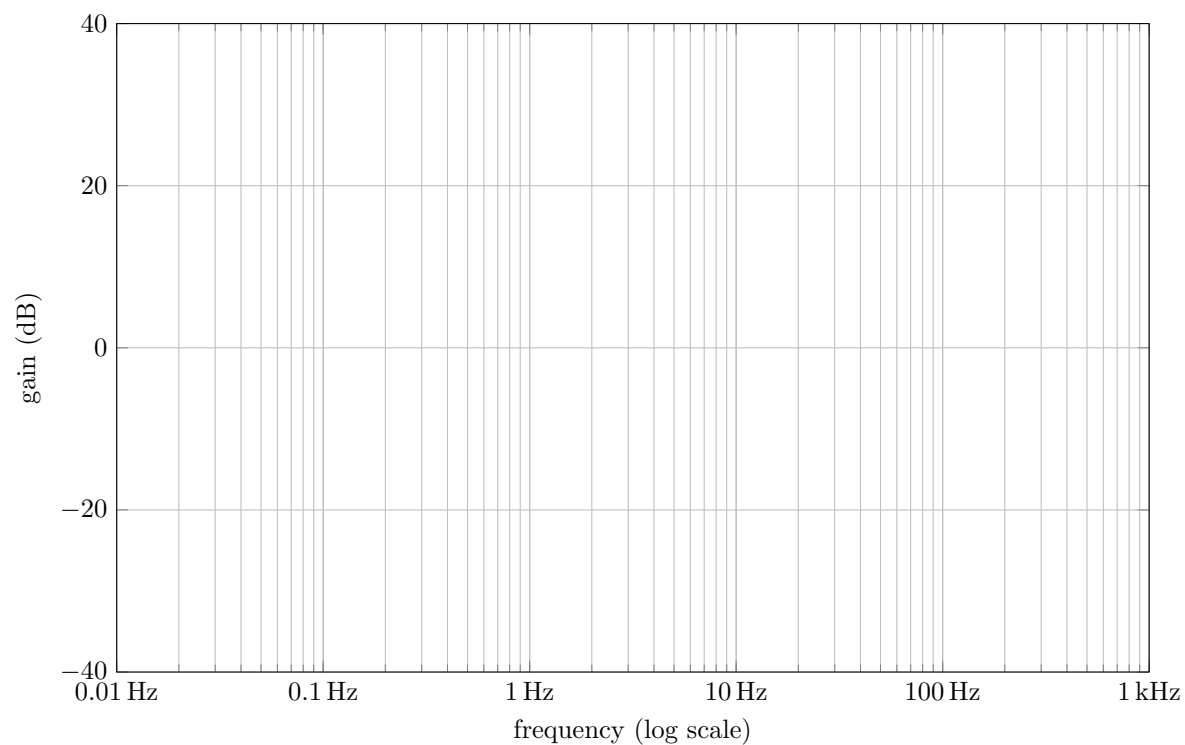
- (a) Find  $Z_p$ , the overall impedance of the parallel combination of the  $100\text{ k}\Omega$  resistor and  $0.1\mu\text{F}$  capacitor.
- (b) Using the ideal op-amp rules for current and voltage at the op-amp inputs and the impedances in this circuit, write the nodal equation for this circuit. Use your value of  $Z_p$  solved from part (a).  
*Hint: the nodal equation should be for the node at the opamp “-” input*

- (c) Now using this equation, find an expression for the transfer function for this circuit as a function of frequency, which should be in the form  $\frac{V_{\text{out}} - 2.5}{V_{\text{in}} - 2.5} = \frac{A}{1 + B \cdot j2\pi f}$ , where A and B depend only on the impedances in the circuit. The magnitude of the gain is the absolute value of this transfer function. Use  $V_{\text{dd}} = 5 \text{ V}$ .

- (d) What is the magnitude of this transfer function, in dB, (i) at very low frequencies and (ii) at very high frequencies? (Remember, the magnitude in dB is  $20 \log_{10}(\text{magnitude})$ .)



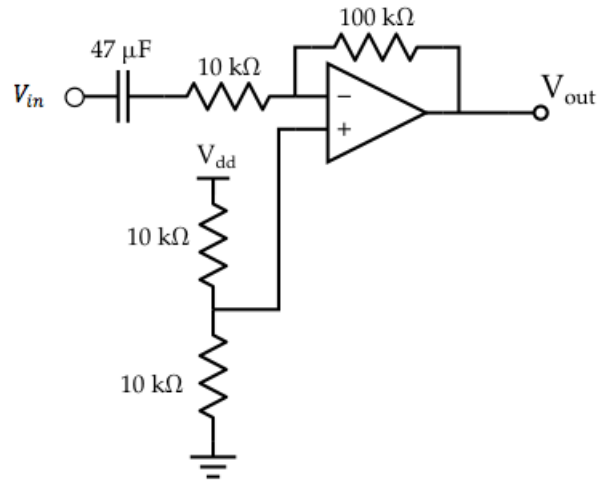
- (e) Draw the magnitude Bode plot for this circuit, labeling the important cutoff frequencies. Use the figure below for your plot.



- (f) By looking at the magnitude Bode plot, can you tell what this circuit does? (highpass, lowpass, bandpass, or bandstop?)

### Problem 5: Another Op-amp Circuit

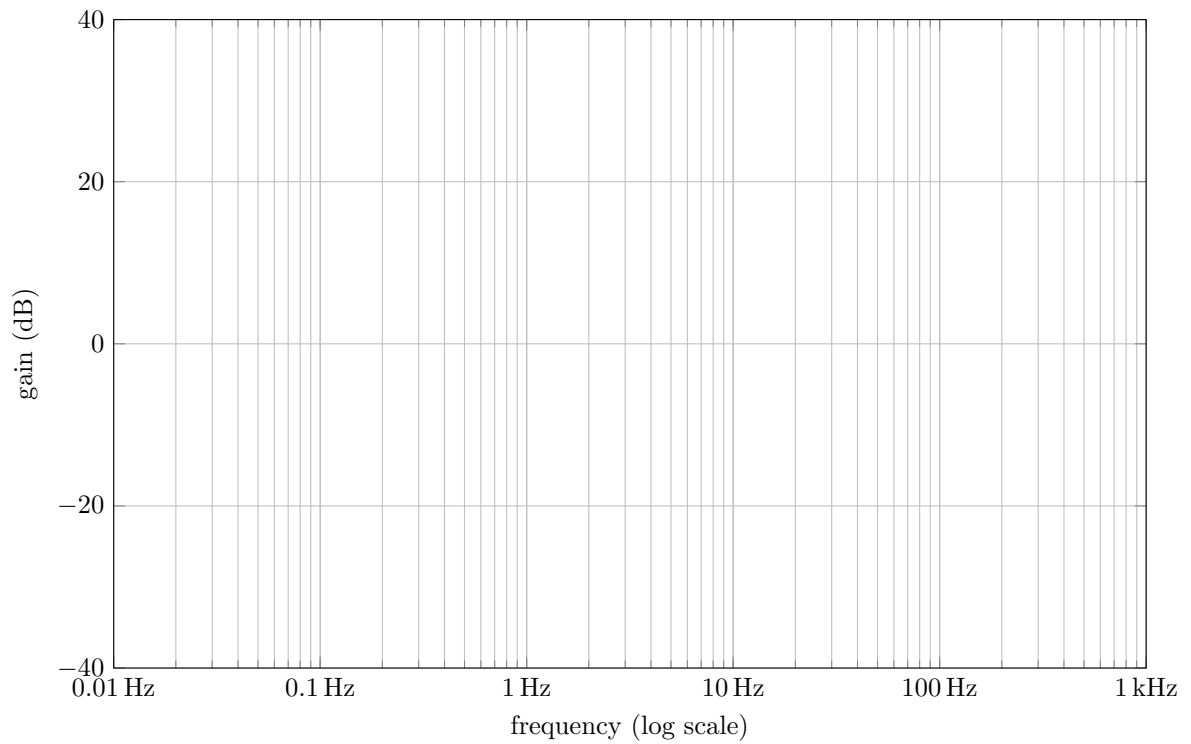
(15 points) The below circuit is a different simplification of the one you'll be making in lab 4. Assume  $V_{dd} = 5\text{ V}$ .



- (a) Using the same steps as above, find an equation for the transfer function of the circuit,  $\frac{V_{out}-2.5}{V_{in}-2.5}$ . *Hint: This transfer function will be in the form  $\frac{j2\pi f \cdot A}{1+j2\pi f \cdot B}$ .*

- (b) What is the magnitude of this transfer function, in dB, (i) at very low frequencies and (ii) at very high frequencies? (Remember, the magnitude in dB is  $20 \log_{10}(\text{magnitude})$ .)

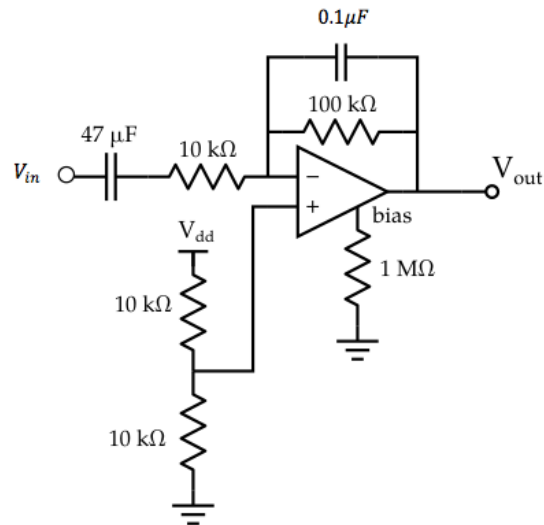
- (c) Draw the magnitude Bode plot for this circuit, labeling the important cutoff frequencies. Use the figure below for your plot.



- (d) By looking at the magnitude Bode plot, can you tell what this circuit does? (highpass, lowpass, bandpass, or bandstop?)

## Problem 6: Opamps: Final Version

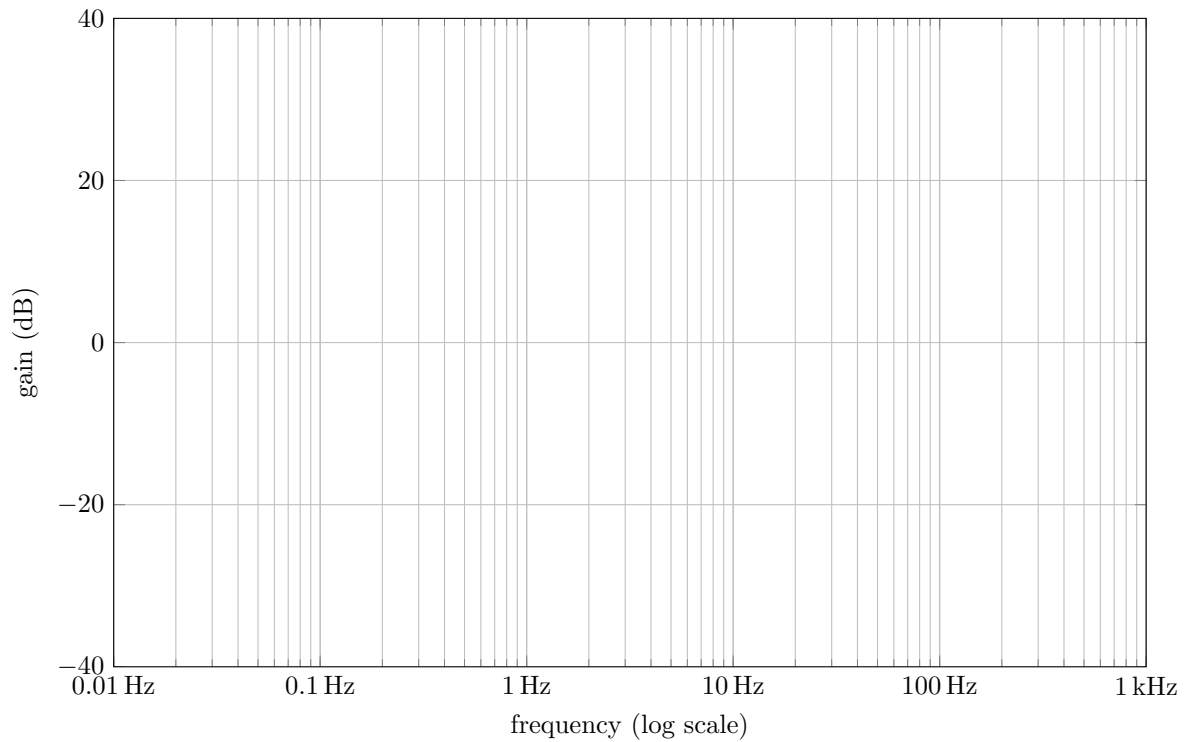
(20 points) Now, below is the circuit we are doing in lab. Notice that all the resistors are the same and we have included both of the capacitors this time.



- (a) Write the nodal equation at the negative input as function of  $Z_s$ , the impedance of the  $47\ \mu\text{F}$  capacitor and the  $10\ \text{k}\Omega$  resistor in series, and  $Z_p$ , the impedance of the  $0.1\ \mu\text{F}$  capacitor and the  $100\ \text{k}\Omega$  resistor in parallel.
  
- (b) Find an equation for the transfer function in the last circuit by rearranging your nodal equation and substituting in  $Z_p$  and  $Z_s$ . You can leave the denominator in factored form (you don't have to multiply out to find the  $(j2\pi f)^2$  term).

- (c) What is the magnitude, in dB, of this transfer function at very low frequencies? At very high frequencies? What is the magnitude between the two cutoff frequencies? *Hint: In the factored transfer function, your denominator should contain two  $(1+j2\pi f \cdot A)$  terms. Between the two cutoff frequencies,  $j2\pi f$  will dominate the first of these terms, while the 1 will still dominate the second.*

- (d) Draw the magnitude bode plot for this circuit, labeling the important cutoff frequencies. Use the figure below for your plot.



- (e) By looking at the magnitude bode plot, can you tell what this circuit does? (highpass, lowpass, bandpass, or bandstop?)

### **Problem 7: Reflection**

(2 points)

(a) How long did it take you to complete this assignment?

(b) Which problem was the most difficult, and why?