Using Abstractions: Breadth-First Search

What is a tradition that’s special to you? (put your answers in the chat)
Roadmap

- C++ basics
- User/client
- vectors + grids
- stacks + queues
- sets + maps
- Object-Oriented Programming
- arrays
- dynamic memory management
- linked data structures
- diagnostic
- real-world algorithms
- recursive problem-solving
- Life after CS106B!

Core Tools
- testing
- algorithmic analysis
Roadmap

C++ basics

User/client

vectors + grids
stacks + queues
sets + maps

Core Tools

testing
algorithmic analysis

Object-Oriented Programming

arrays
dynamic memory management
linked data structures

Implementation

real-world algorithms
recursive problem-solving

Life after CS106B!
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dynamic memory management

linked data structures

Core Tools

algorithmic analysis

recursive problem-solving

testing
Today’s question

How can we use the unique properties of different abstractions to solve problems?
Today’s topics

1. Review
2. Implementing Counting Sort
3. Implementing Breadth-First Search
Breadth-First Search Algorithm
Review

sets and maps
What is a set?

- A set is a collection of elements with no duplicates.
- Sets are faster than ordered data structures like vectors – since there are no duplicates, it’s faster for them to find things.
  - (Later in the quarter we’ll learn about the details of the underlying implementation that makes this abstraction efficient.)
  - We’ll formally define “faster” on Thursday.
- Sets don’t have indices!
What is a map?

- A map is a collection of key/value pairs, and the key is used to quickly find the value.

- A map is an alternative to an ordered data structure, where the “indices” no longer need to be integers.
Ordered ADTs

Elements accessible by indices:

- Vectors (1D)
- Grids (2D)

Elements not accessible by indices:

- Queues (FIFO)
- Stacks (LIFO)

Unordered ADTs

- Sets (elements unique)
- Keys (keys unique)

Useful when numerical ordering of data isn’t optimal
Activity: Counting Sort
Counting Sort

- Sorting is a fundamental topic in computer science and one that we will revisit in more depth later this quarter
Counting Sort

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- For now, let's consider this question: how would you efficiently sort all the letters in a word in alphabetical order?
  - How can we take advantage of some of the data structures we've recently learned about to meaningfully structure the data that we want to sort?
Counting Sort

- Sorting is a fundamental topic in computer science and one that we will revisit in more depth later this quarter.

- For now, let's consider this question: how would you efficiently sort all the letters in a word in alphabetical order?
  - How can we take advantage of some of the data structures we've recently learned about to meaningfully structure the data that we want to sort?

- Idea: If we can tally up how many times each of the letters from 'a' to 'z' shows up, we can then build a new string composed of the correct number of 'a's, followed by the correct number of 'b's, ... etc.
Counting Sort Example
Counting Sort Example

banana
Counting Sort Example

\[ \text{letterFreq} \]

Example and slides taken from a slide deck by Keith Schwarz
Counting Sort Example

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Counting Sort Example

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Counting Sort Example

\[ \text{banana} \]

\[ \begin{array}{c|c}
 a & 1 \\
 b & 1 \\
\end{array} \]

\text{letterFreq}
Counting Sort Example

Example and slides taken from a slide deck by Keith Schwarz
Counting Sort Example

![Diagram showing the concept of Counting Sort with the word "banana" and a frequency table for its letters.]

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Counting Sort Example

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banana

letterFreq

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banana

letterFreq

Example and slides taken from a slide deck by Keith Schwarz
Counting Sort Example

banana

letterFreq

a 3
b 1
n 2

Example and slides taken from a slide deck by Keith Schwarz
Counting Sort Example

Example and slides taken from a slide deck by Keith Schwarz
Counting Sort Example

banana

letterFreq

a 3
b 1
n 2

aaab
Counting Sort Example

banana

| a | 3 |
| b | 1 |
| n | 2 |

letterFreq

aabbb
Counting Sort Example

banana

letterFreq

a 3
b 1
n 2

aaabbbnnn
Counting Sort Example

banana

letterFreq

3
1
2

aaabnnn

Mission Accomplished!
Counting Sort Pseudocode

- Loop over the word and build a frequency map of all letters that appear in the original string
- Loop through all letters from 'a' to 'z' and build up a new string with the right amount of each letter
- Return the newly generated string
pseudocode before implementing the algorithm
Counting Sort Pseudocode

- Loop over the word and build a frequency map of all letters that appear in the original string
- Loop through all letters from 'a' to 'z' and build up a new string with the right amount of each letter
- Return the newly generated string
Provided Code

```cpp
string countingSort(string s) {
    Map<char, int> freqMap;
    for (char ch: s) {
        freqMap[ch] = freqMap[ch] + 1;
    }

    string sortedString;
    for (char ch = 'a'; ch <= 'z'; ch++) {
        // Use freqMap to construct sortedString
    }
    return sortedString;
}
```
- Loop over the word and build a frequency map of all letters that appear in the original string
- Loop through all letters from 'a' to 'z' and build up a new string with the right amount of each letter

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string countingSort(string s) {
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    for (char ch: s) {
        freqMap[ch] = freqMap[ch] + 1;
    }

    string sortedString;
    for (char ch = 'a'; ch <= 'z'; ch++) {
        /* TODO: Generate pseudocode to complete the algorithm! */
    }

    return sortedString;
}
```
Loop through all letters from 'a' to 'z' and build up a new string with the right amount of each letter

```java
string countingSort(string s) {
    Map<char, int> freqMap;
    for (char ch : s) {
        freqMap[ch] = freqMap[ch] + 1;
    }

    string sortedString;
    for (char ch = 'a'; ch <= 'z'; ch++) {
        /* TODO: Generate pseudocode to complete the algorithm! */
    }
    return sortedString;
}
```
Loop through all letters from 'a' to 'z' and build up a new string with the right amount of each letter

```cpp
string countingSort(string s) {
    Map<char, int> freqMap;
    for (char ch : s) {
        freqMap[ch] = freqMap[ch] + 1;
    }

    string sortedString;
    for (char ch = 'a'; ch <= 'z'; ch++) {
        /* TODO: Generate pseudocode to complete the algorithm! */
        /* Use ch as key into the freq map & get associated value. */
    }
    return sortedString;
}
```
Loop through all letters from 'a' to 'z' and build up a new string with the right amount of each letter

```java
string countingSort(string s) {
    Map<char, int> freqMap;
    for (char ch : s) {
        freqMap[ch] = freqMap[ch] + 1;
    }

    string sortedString;
    for (char ch = 'a'; ch <= 'z'; ch++) {
        /* TODO: Generate pseudocode to complete the algorithm! */
        /* Use ch as key into the freq map & get associated value. */
        /* Add ch to sortedString as many times as that value. */
    }
    return sortedString;
}
```
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    Map<char, int> freqMap;
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        freqMap[ch] = freqMap[ch] + 1;
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    string sortedString;
    for (char ch = 'a'; ch <= 'z'; ch++) {
        /* Use ch as key into the freq map & get associated value. */
        /* Add ch to sortedString as many times as that value. */
    }
    return sortedString;
}
Counting Sort Code

```cpp
string countingSort(string s) {
    Map<char, int> freqMap;
    for (char ch : s) {
        // taking advantage of map auto-insertion!
        freqMap[ch] = freqMap[ch] + 1;
    }

    string sortedString;
    for (char ch = 'a'; ch <= 'z'; ch++) {
        /* Use ch as key into the freq map and get associated value. */
        /* Add ch to sortedString as many times as that value. */
        for (int i = 0; i < freqMap[ch]; i++) {
            sortedString += charToString(ch);
        }
    }
    return sortedString;
}
```
Counting Sort Code

```cpp
string countingSort(string s) {
    Map<char, int> freqMap;
    for (char ch: s) {
        // taking advantage of map auto-insertion!
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        }
    }
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```
Loop through all letters from 'a' to 'z' and build up a new string with the right amount of each letter.

```cpp
string countingSort(string s) {
    Map<char, int> freqMap;
    for (char ch: s) {
        freqMap[ch] = freqMap[ch] + 1;
    }

    string sortedString;
    for (char ch = 'a'; ch <= 'z'; ch++) {
        /* Check if the freq map contains the key ch */
        /* If so, get associated value for ch key from freq map. */
        /* Add ch to sortedString as many times as that value. */
    }
    return sortedString;
}
```
string countingSort(string s) {
    Map<char, int> freqMap;
    for (char ch: s) {
        // taking advantage of map auto-insertion!
        freqMap[ch] = freqMap[ch] + 1;
    }

    string sortedString;
    for (char ch = 'a'; ch <= 'z'; ch++) {
        /* Check if the freq map contains the key ch */
        if (freqMap.containsKey(ch)) {
            /* If so, get associated value for ch key from freq map. */
            /* Add ch to sortedString as many times as that value. */
            for (int i = 0; i < freqMap[ch]; i++) {
                sortedString += charToString(ch);
            }
        }
    }

    return sortedString;
}

Counting Sort Code

```cpp
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            for (int i = 0; i < freqMap[ch]; i++) {
                sortedString += charToString(ch);
            }
        }
    }

    return sortedString;
}
```

This check isn't strictly required, but it does avoid unnecessary things being added to the map via auto-insertion.
string countingSort(string s) {
    Map<char, int> freqMap;
    for (char ch : s) {
        // taking advantage of map auto-insertion!
        freqMap[ch] = freqMap[ch] + 1;
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    string sortedString;
    for (char ch = 'a'; ch <= 'z'; ch++) {
        if (freqMap.containsKey(ch)) {
            for (int i = 0; i < freqMap[ch]; i++) {
                sortedString += charToString(ch);
            }
        }
    }

    return sortedString;
}
Challenge for home:

What other types of data could you efficiently sort in this manner?
How can we use the unique properties of different abstractions to solve problems?
Examples of interesting problems to solve using ADTs

- Simulate potential impacts of flooding on a topographical landscape (how does water flow outwards from a source and settle into the surrounding areas)
- Generate simulated text in the style of a certain author. Similarly, do textual analysis to determine who the author of a provided piece of text was.
- Spell check and autocomplete for a word document editor
- Manage information about the natural landmarks and state parks to help tourists plan their trip to the state
- Develop a ticketing management system for a stadium
- Aggregate and analyze reviews for an online shopping website
- Solve fun puzzles
Examples of interesting problems to solve using ADTs

- Simulate potential impacts of flooding on a topographical landscape (how does water flow outwards from a source and settle into the surrounding areas)
- Generate simulated text in the style of a certain author. Similarly, do textual analysis to determine who the author of a provided piece of text was.
- Spell check and autocomplete for a word document editor
- Manage information about the natural landmarks and state parks in California to help tourists plan their trip to the state
- Develop a ticketing management system for Stanford Stadium
- Aggregate and analyze reviews for an online shopping website
- Solve fun puzzles
Word Ladders
Write the missing letter for each word. As you go down the ladder, change one letter to show how the words connect.

```
<table>
<thead>
<tr>
<th>r</th>
<th>u</th>
<th>g</th>
</tr>
</thead>
<tbody>
<tr>
<td>u</td>
<td>g</td>
<td>g</td>
</tr>
<tr>
<td>g</td>
<td>b</td>
<td>g</td>
</tr>
<tr>
<td>b</td>
<td>a</td>
<td>t</td>
</tr>
<tr>
<td>a</td>
<td>t</td>
<td>t</td>
</tr>
</tbody>
</table>
```

Start word

Ending word
Word Ladder

Write the missing letter for each word. As you go down the ladder, change one letter to show how the words connect.

rug → bug → bat → hat
Word Ladder

Write the missing letter for each word. As you go down the ladder, change one letter to show how the words connect.

r u g
b u g
b u g
b a t
h a t
Write the missing letter for each word. As you go down the ladder, change one letter to show how the words connect.

- Rug
- Bug
- Bag
- Bat
- Hat
Word Ladder

Write the missing letter for each word. As you go down the ladder, change one letter to show how the words connect.

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h a t
Word Ladder

Write the missing letter for each word. As you go down the ladder, change one letter to show how the words connect.

r u g
b u g
b a g
b a t
h a t
Word Ladder

Write the missing letter for each word. As you go down the ladder, change one letter to show how the words connect.

- rug
- bug
- bag
- bat
- rat
- hat
How can we come up with an algorithm to generate these word ladders?
Word Ladder Generation First Attempt

- Given a start word and a target word, a natural place to start would be to model how a human might attempt to solve this problem.
Word Ladder Generation First Attempt

- Given a start word and a target word, a natural place to start would be to model how a human might attempt to solve this problem
  - Start at the start word
  - Make an educated guess about what letter to change first
  - Modify that letter to get to a new English word
  - From there, make another educated guess about which letter to change and modify that letter
  - Keep repeating this process until you reach the target word (unlikely) or hit a dead end (likely)
  - If you hit a dead end, start over again, taking a different first step
Word Ladder Generation First Attempt

- Given a start word and a target word, a natural place to start would be to model how a human might attempt to solve this problem
  - Start at the start word
  - Make an educated guess about what letter to change first
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  - From there, make another educated guess about which letter to change and modify that letter
  - Keep repeating this process until you reach the target word (unlikely) or hit a dead end (likely)
  - If you hit a dead end, start over again, taking a different first step

- What are the issues with this approach?
  - Requires intuition – does a computer have intuition?
  - Unorganized – no organized strategy for the exploration
  - No guarantee that you'll ever find a solution!
Breadth-First Search (BFS)
Breadth-First Search

- We need a structured way to explore words that are "adjacent" to one another (one letter difference between the two of them)
Breadth-First Search

- We need a structured way to explore words that are "adjacent" to one another (one letter difference between the two of them)
- What's the simplest possible word ladder we could find?
  - If the words are only one letter different from one another (pig and fig), then finding the word ladder is relatively easy – we look at all words that are one letter away from the current word
Breadth-First Search

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- What's the simplest possible word ladder we could find?
  - If the words are only one letter different from one another (pig and fig), then finding the word ladder is relatively easy – we look at all words that are one letter away from the current word
- What's the next simplest possible word ladder we could find?
  - If the word ladder requires two steps, then we can break down the problem into the problem of exploring one step away from all the words that are one step away from the starting word
Breadth-First Search

- We need a structured way to explore words that are "adjacent" to one another (one letter difference between the two of them)
- What's the simplest possible word ladder we could find?
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- What's the next simplest possible word ladder we could find?
  - If the word ladder requires two steps, then we can break down the problem into the problem of exploring one step away from all the words that are one step away from the starting word
- **Important observation:** In order to keep our search organized, we first explore all word ladders of "length" 1 before we explore any word ladders of "length" 2, and so on.
Breadth-First Search Example
Breadth-First Search Example

- Let's try to apply this approach to find a word ladder starting at the word "map" and ending at the word "way"
Breadth-First Search Example

start: map
destination: way
Breadth-First Search Example

start: map
destination: way

0 steps away
Breadth-First Search Example

start: map
destination: way

0 steps away
1 step away
Breadth-First Search Example

start: map
destination: way

0 steps away
1 step away
Breadth-First Search Example

start: map
destination: way

0 steps away
1 step away
Breadth-First Search Example

start: map
destination: way

0 steps away
1 step away
Breadth-First Search Example

start: map
destination: way

0 steps away
1 step away
Breadth-First Search Example

0 steps away
1 step away

Note: For the sake of brevity/demonstration, we will not enumerate all possible words that are 1 step away
Breadth-First Search Example

start: map
destination: way

0 steps away
1 step away
Breadth-First Search Example

start: map
destination: way
Breadth-First Search Example

Observation: 2 steps away from "map" is really just 1 step away from any of its neighbors.
Breadth-First Search Example

start: map
destination: way

0 steps away
1 step away
2 steps away
Breadth-First Search Example

0 steps away
1 step away
2 steps away

start: map
destination: way

map

rap

man

mop

nap

may

lop

map
Breadth-First Search Example

Visiting a word we've already been at before is basically like going backwards in our search. We want to avoid this at all costs!

start: map
destination: way

0 steps away
1 step away
2 steps away
Breadth-First Search Example

start: map
destination: way

Idea: Keep track of a collection of visited words, and don't double visit

0 steps away
1 step away
2 steps away
Breadth-First Search Example

start: map
destination: way

0 steps away
1 step away
2 steps away
Breadth-First Search Example

start: map
destination: way

0 steps away
1 step away
2 steps away
Breadth-First Search Example

- start: map
- destination: way

0 steps away: map
1 step away: mop, rap
2 steps away: man, lop, mop, mow, ray, nap, mow, ray
Breadth-First Search Example

start: map
destination: way

0 steps away
1 step away
2 steps away
Breadth-First Search Example

start: map
destination: way

0 steps away
1 step away
2 steps away
Breadth-First Search Example

start: map
destination: way

0 steps away
1 step away
2 steps away
Breadth-First Search Example

start: map
destination: way

0 steps away
1 step away
2 steps away
Breadth-First Search Example

start: map
destination: way

Success! We have found a valid word ladder
map -> may -> way
Formalizing Breadth-First Search (BFS)
Breadth-First Search Data Structures

We need...

1) A data structure to represent (partial word) ladders
   ○ Desired characteristics: can easily access the most recent word added to the word ladder
Breadth-First Search Data Structures

We need...

1) A data structure to represent (partial word) ladders
   ○ Desired characteristics: can easily access the most recent word added to the word ladder

2) A data structure to store all the partial word ladders that we have generated so far and have yet to explore
   ○ Desired characteristics: can maintain an ordering of partial word ladders so that all ladders of a certain length get explored before ladders of longer length get explored
Breadth-First Search Data Structures

We need...

1) A data structure to represent (partial word) ladders
   ○ Desired characteristics: can easily access the most recent word added to the word ladder

2) A data structure to store all the partial word ladders that we have generated so far and have yet to explore
   ○ Desired characteristics: can maintain an ordering of partial word ladders so that all ladders of a certain length get explored before ladders of longer length get explored

3) A data structure to keep track of all the words that we’ve explored so far, so that we avoid getting stuck in loops
   ○ Desired characteristics: can check quickly whether a word has been seen before
Breadth-First Search Data Structures

We need...

1) A data structure to represent (partial word) ladders
   ○ Desired characteristics: can easily access the most recent word added to the word ladder

2) A data structure to store all the partial word ladders that we have generated so far and have yet to explore
   ○ Desired characteristics: can maintain an ordering of partial word ladders so that all ladders of a certain length get explored before ladders of longer length get explored

3) A data structure to keep track of all the words that we’ve explored so far, so that we avoid getting stuck in loops
   ○ Desired characteristics: can check quickly whether a word has been seen before
Breadth-First Search Data Structures

We need...

1) A data structure to represent (partial word) ladders
   ○ Stack<string>

2) A data structure to store all the partial word ladders that we have generated so far and have yet to explore
   ○ Desired characteristics: can maintain an ordering of partial word ladders so that all ladders of a certain length get explored before ladders of longer length get explored

3) A data structure to keep track of all the words that we've explored so far, so that we avoid getting stuck in loops
   ○ Desired characteristics: can check quickly whether a word has been seen before
Breadth-First Search Data Structures

We need...

1) A data structure to represent (partial word) ladders
   ○ Stack$string$

2) A data structure to store all the partial word ladders that we have generated so far and have yet to explore
   ○ Queue$\text{Stack}<\text{string}>>$

3) A data structure to keep track of all the words that we’ve explored so far, so that we avoid getting stuck in loops
   ○ Desired characteristics: can check quickly whether a word has been seen before
Breadth-First Search Data Structures

We need...

- A data structure to represent (partial word) ladders
  - `Stack<string>`
- A data structure to store all the partial word ladders that we have generated so far and have yet to explore
  - `Queue<Stack<string>>`
- A data structure to keep track of all the words that we've explored so far, so that we avoid getting stuck in loops
  - `Set<string>`
Breadth-First Search Pseudocode
Breadth-First Search Pseudocode

Create an empty queue and an empty set of visited locations
Create an initial word ladder containing the starting word and add it to the queue
Breadth-First Search Pseudocode

Create an empty queue and an empty set of visited locations
Create an initial word ladder containing the starting word and add it to the queue
While the queue is not empty
Breadth-First Search Pseudocode

Create an empty queue and an empty set of visited locations
Create an initial word ladder containing the starting word and add it to the queue
While the queue is not empty
   Remove the next partial ladder from the queue
   Set the current search word to be the word at the top of the ladder
   If the current word is the destination, then return the current ladder
Breadth-First Search Pseudocode

Create an empty queue and an empty set of visited locations
Create an initial word ladder containing the starting word and add it to the queue
While the queue is not empty
    Remove the next partial ladder from the queue
    Set the current search word to be the word at the top of the ladder
    If the current word is the destination, then return the current ladder
    Generate all "neighboring" words that are valid English words and one letter away from the current word
    Loop over all neighbor words
Breadth-First Search Pseudocode

Create an empty queue and an empty set of visited locations  
Create an initial word ladder containing the starting word and add it to the queue  
While the queue is not empty  
  Remove the next partial ladder from the queue  
  Set the current search word to be the word at the top of the ladder  
  If the current word is the destination, then return the current ladder  
  Generate all "neighboring" words that are valid English words and one letter away from the current word  
  Loop over all neighbor words  
    If the neighbor hasn't yet been visited
Breadth-First Search Pseudocode

Create an empty queue and an empty set of visited locations
Create an initial word ladder containing the starting word and add it to the queue
While the queue is not empty
  Remove the next partial ladder from the queue
  Set the current search word to be the word at the top of the ladder
  If the current word is the destination, then return the current ladder
  Generate all "neighboring" words that are valid English words and one letter away from the current word
  Loop over all neighbor words
    If the neighbor hasn't yet been visited
      Create a copy of the current ladder
      Add the neighbor to the top of the new ladder and mark it visited
      Add the new ladder to the back of the queue of partial ladders
Implementing Breadth-First Search

[Qt Creator]
Implementing Breadth-First Search

We hope that you find this to be a helpful resource when working on Assignment 2. However, we do not encourage trying to copy the code as a starting point. The problems are distinctly different, and you will benefit from explicitly developing your own problem-specific pseudocode first.
Announcements
Announcements

• Assignment 2 was released last night. It will be due at the end of the day on **Wednesday, July 7**.

• YEAH will be tomorrow, 7/1 at 7pm PT. Link is on the course website on the zoom info page.

• Check out the A2 warmup to ensure that your Qt debugger works nicely with the Stanford C++ collections **before** starting on the assignment.

• This assignment is a step-up in complexity compared to A1 – get started early!
Goals for this Course

Learn how to model and solve complex problems with computers.

- Explore common abstractions for representing problems.
- Harness recursion and understand how to think about problems recursively.
- Quantitatively analyze different approaches for solving problems.
What’s next?
Roadmap

Object-Oriented Programming

- vectors + grids
- stacks + queues
- sets + maps

C++ basics

User/client

- testing

Core Tools

- algorithmic analysis

Implementation

- diagnostic
- real-world algorithms
- recursive problem-solving

Life after CS106B!
Big O and Algorithmic Analysis