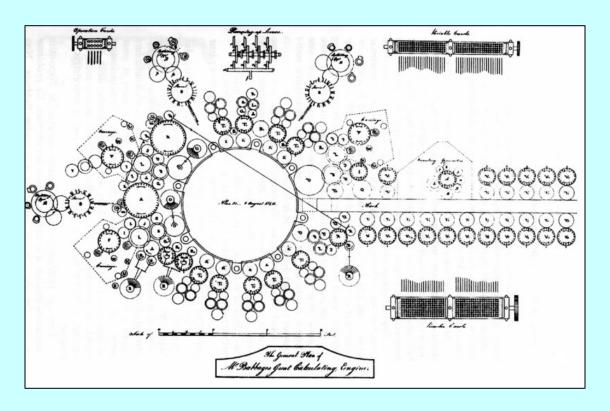
The Analytical Engine



Chris Gregg, based on slides by Eric Roberts
CS 208E
September 27, 2018

CS 208E—Topic Overview

Week 1	Introductions; course overview; Babbage machines; Ada Lovelace
Week 2	Karel the Robot; beginning JavaScript; algorithms
Week 3	Binary arithmetic; digital logic
Week 4	Stored-program machines; the Toddler machine
Week 5	Turing machines; the Busy Beaver problem; undecidability
Week 6	Computational complexity; the $P = NP$ question
Week 7	Cryptography; public-key cryptography; digital signatures
Week 8	Networking; networking algorithms; Google page rank
Week 9	Artificial intelligence; machine learning; big data
Week 10	Computers and ethics; promise and peril of the digital age

Ada Byron, The First Programmer



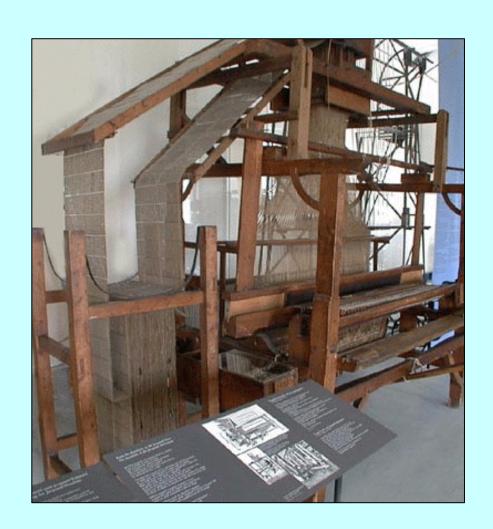
Augusta Ada Byron, Lady Lovelace (1815–1852)

Augusta Ada Byron, the daughter of the English poet Lord Byron and his wife Anne, was encouraged to pursue her interests in science and mathematics at a time when few women were allowed to study those subjects. At the age of 17, Ada met Charles Babbage and became fascinated by his machines. Ada was convinced of the potential of Babbage's Analytical Engine and wrote extensive notes on its design, along with several complex mathematical programs that have led many people to characterize her as the first programmer. In 1980, the U.S. Department of Defense named the programming language Ada in her honor.

The Analytical Engine

- As Babbage built prototypes of his Difference Engine, he began to envision a much more powerful computing device he called the Analytical Engine.
- Babbage's initial notes on the Analytical Engine appear in 1837, but the most complete description appears in a 1842 paper by Luigi Federico Menabrea, who was reporting on a lecture Babbage gave in 1840. Ada Lovelace translated Menabrea's paper from French into English and provided notes that were three times longer than the original.
- The essential difference between the Difference Engine and the Analytical Engine is that the Analytical Engine was designed to be *programmable*, allowing users to perform any sequence of calculations. The programs were encoded on punched cards in the manner of the Jacquard loom, which Ada and her mother had seen in their visits to the English industrial areas.

Jacquard Loom

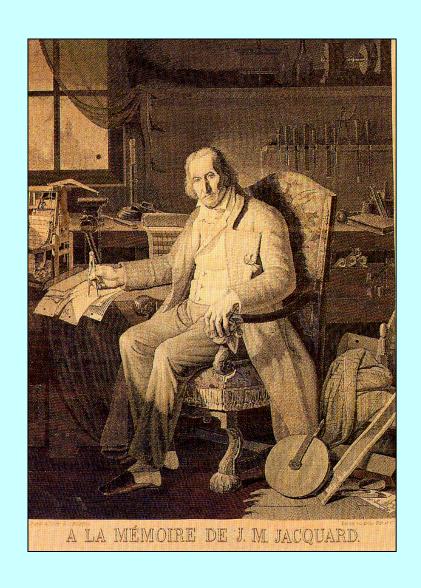


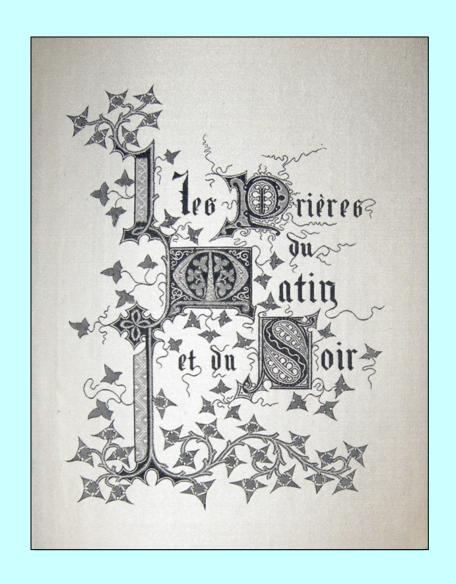


Jacquard Loom

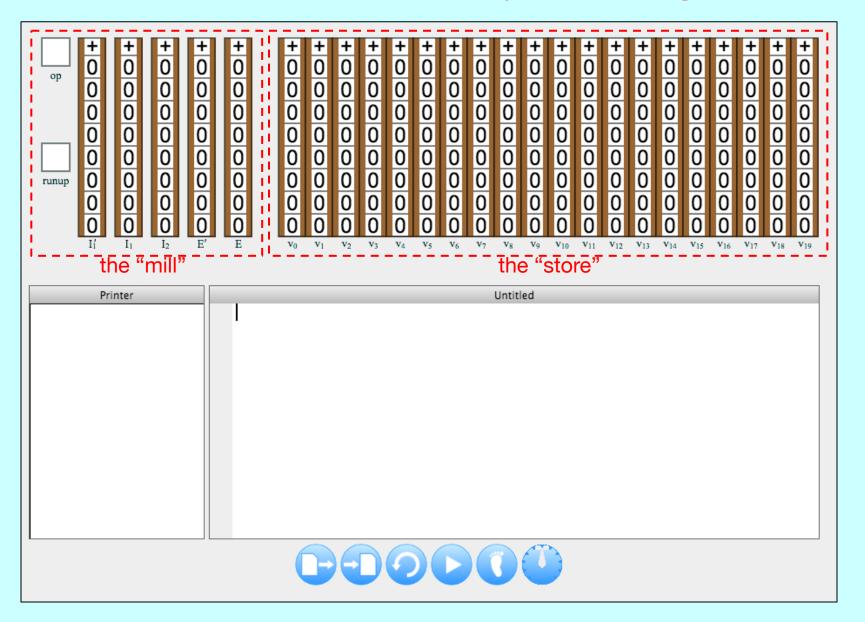
https://www.youtube.com/watch?v=K6NgMNvK52A

Products of the Jacquard Loom





Structure of the Analytical Engine



The Store and the Mill



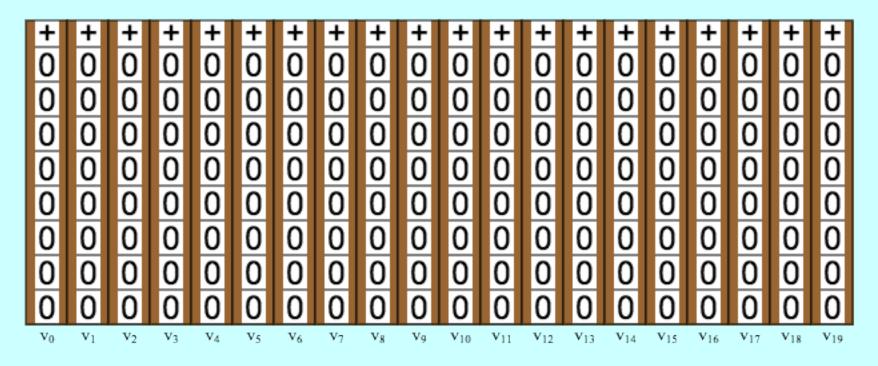
The Analytical Engine: Computerphile

https://www.youtube.com/watch?v=5rtKoKFGFSM

Notes:

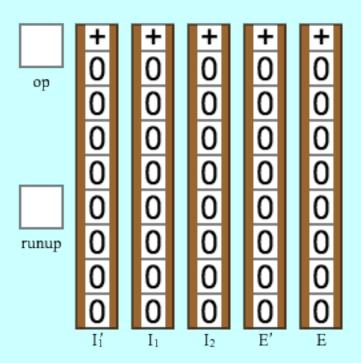
http://www.eprg.org/computerphile/new-adatalk.pdf

The "Store"



- Each column holds a single integer as in the Difference Engine.
- Numbers in the Analytical Engine are signed.
- Each column has a numeric address: v_0 , v_1 , v_2 , v_3 , and so on.

The "Mill"



- The **op** indicator holds the current operation $(+, -, \times, \div)$
- The mill has five columns:
 - I_1 and I_2 are the input values
 - E is the output value
 - I_1' and E' are used to store extra digits for the \times and \div operations
- The **runup** indicator is set when the result of an operation changes sign.

Instructions for the Analytical Engine

N	address value	Store value in address
+		Set the machine to addition
-		Set the machine to subtraction
×		Set the machine to multiplication
÷		Set the machine to division
L	address	Load from <i>address</i> , preserving data
Z	address	Load from address, clearing data
S	address	Store egress register in address
P	address	Print value in <i>address</i>

Program to Add Two Numbers

```
N 0 25 /* First number is in \mathbf{v}_0
N 1 17
          /* Second number is in v<sub>1</sub>
          /* Set machine for addition
          /* Load first number into I,
                                              */
          /* A second load does the add
                                              */
S 2
          /* Store result in v<sub>2</sub>
          /* Print the result
```

Adding Control Operations

N	address value	Store <i>value</i> in <i>address</i>
+		Set the machine to addition
-		Set the machine to subtraction
×		Set the machine to multiplication
÷		Set the machine to division
L	address	Load from <i>address</i> , preserving data
Z	address	Load from <i>address</i> , clearing data
S	address	Store egress register in <i>address</i>
P	address	Print value in <i>address</i>
В	number	Move backward specified number of cards
F	number	Move forward specified number of cards
?I	3 number	Move backward if runup lever is set
?I	r number	Move forward if runup lever is set

Exercise: Produce a Table of Squares

Use the Analytical Engine to produce a table of squares.

	Printer
0	
1	
4	
4 9	
16	
25	
25 49 64	
64	
81	

The simplest approach is to simulate the operation used by the Difference Engine to accomplish the same task.

Multiplication and Division

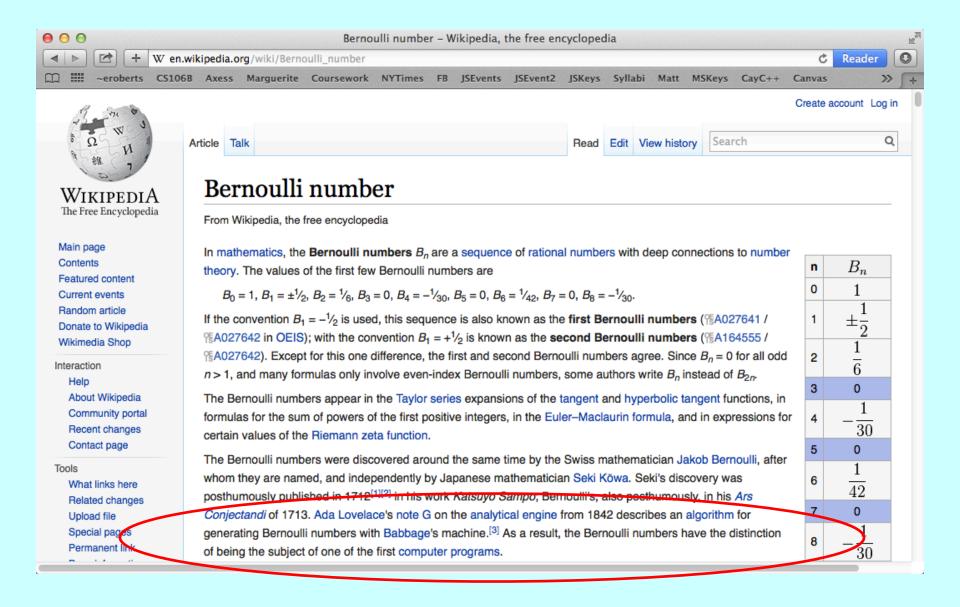
- Babbage recognized that multiplying two integers produces a result that typically has twice the number of digits that appear in the original values.
- To take account of this fact, the multiplication operation for the Analytical Engine produces its result in a pair of columns. Column E shows the *low-order digits* of the product, which are the digits on the right that include the units value. Column E' shows the *high-order digits*.
- The division operation uses two columns to store the dividend. You set up the division by loading the low-order digits into column I_1 and the high-order digits (if any) into column I_1 .
- As long as you know that the numbers won't exceed the number of digits in a column, you can ignore E' and I₁' altogether.

Exercise: Calculate Factorials

How would you program the Analytical Engine to calculate the factorial of a number supplied as data using a number card.

$$N! = 1 \times 2 \times 3 \times \ldots \times N$$

Bernoulli Numbers

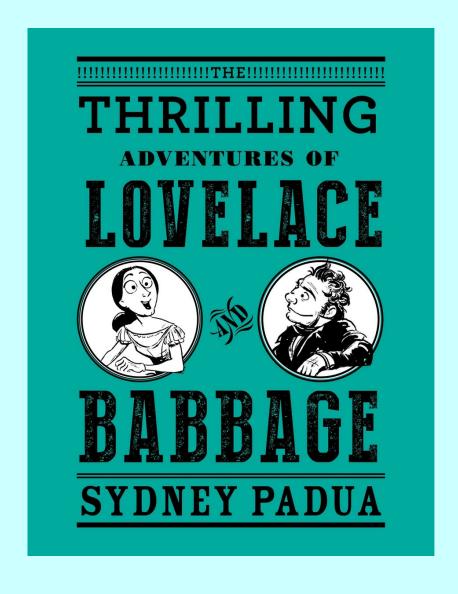


Ada's Program for Bernoulli Numbers

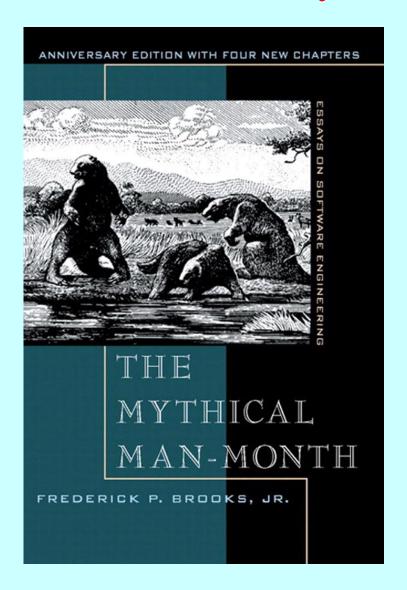
ns.	ls.			Working Variables.									Variables for Results.					
Number of Operations.	Nature of Operations.	$^{1}V_{0}$	$^{1}V_{1}$	$^{1}V_{2}$	$^{1}V_{3}$	$^{1}V_{4}$	$^{1}V_{5}$	$^{0}V_{6}$	$^{0}V_{7}$	$^{0}V_{8}$	$^{0}V_{9}$	$^{0}V_{10}$	$^{0}V_{11}$	$^{0}V_{12}$	$^{0}V_{13}$	$^{0}V_{14}$	$^{0}V_{15}$	$^{0}V_{16}$
<u> </u>	per	+	+	+	+	+	+	+	+	+	+	+	+	+	+	+	+	+
J.C	l O J	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
j	e 0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
l qu	atur	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
Z	$\left \ddot{Z}\right $	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
		m		d	m'	n'	ď										$\frac{dn'-d'n}{mn'-m'n} = x$	$\frac{d'm - dm'}{mn' - m'n} = y$
1	x	m				n'		mn'										
2	x		n		m'				m'n									
3	x			d						dn'								
4	x		0				d'				d'n							
5	x	0					0					d'm						
6	x			0	0								dm'					
7	-							0	0					(mn'-m'n)				
8	-									0	0				(dn'-d'n)			
9	-											0	0			(d'm-dm')		
10	÷				•••••									(mn'-m'n)	0		$\frac{dn'-d'n}{mn'-m'n} = x$	
11	÷			•••••		•••••								0		0		$\frac{d'm - dm'}{mn' - m'n} = y$

https://twobithistory.org/2018/08/18/ada-lovelace-note-g.html

How the Analytical Engine Worked



The Mythical Man-Month



11. Plan to Throw One Away

In most projects, the first system built is barely usable. It may be too slow, too big, awkward to use, or all three. There is no alternative but to start again, smarting but smarter, and build a redesigned version in which these problems are solved. . . .

The management question, therefore, is not whether to build a pilot system and throw it away. You will do that. The only question is whether to plan in advance to build a throwaway, or to promise to deliver the throwaway to customers.

The End