

Stanford CS224W: Exam Preparation

CS224W: Machine Learning with Graphs
Xuan Su & Serina Chang, Stanford University
<http://cs224w.stanford.edu>



Exam Information

- **Percentage: 35%** of your course grade
- **Time:** a consecutive, **120-minute** slot from Nov 19, 10:00AM to Nov 20, 09:59AM
 - The make-up exam is 2 days prior
- **Exam Format:** The exam is administered through Gradescope
 - You can typeset your answers in **LaTeX** or handwrite your answers + upload them as **images**
 - The exam should take around 110 minutes, and you have 10 minutes to upload images

Exam Information

- There will be **11** questions
 - Some questions are easy, and some are harder
 - Try to spend **5-15 minutes on each question**
 - If stuck on a particular question for too long, please skip that question and come back later
- **Types of questions:**
 - **True/False** questions with explanation
 - Give **examples of graphs**
 - Comparison of approaches
 - Mathematical calculations and derivations
- We feel that the exam is **medium difficulty**

General Advice for the Exam

- We suggest that you **read through all lecture slides** carefully
- **Topics** that are **important** for the exam:
 - Node centrality measures, PageRank
 - GNN model and design space (e.g., message, aggregation, update)
 - Knowledge graph embeddings, Query2Box, recommender systems (LightGCN)
- **Lectures** that are **important** for the exam:
lectures 2, 4, 6, 7, 8, 10, 11, 13

General Advice for the Exam

- We suggest that you **read through all lecture slides** carefully
- Lectures that are relatively unimportant for the exam: lectures 1, 3, 5, 9, 12, 14
 - You can spend less time studying these lectures
 - However, you should still read through them and understand the concepts as there may be miscellaneous questions

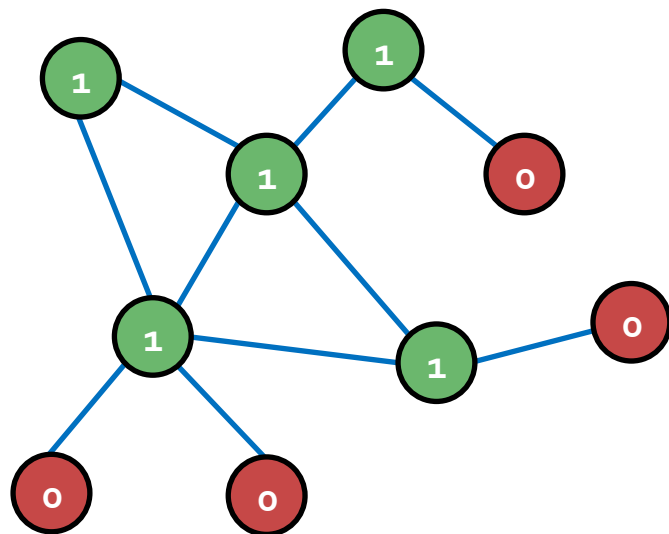
Stanford CS224W: Homework Review

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Homework 1, Q4.6

- We use GNNs to execute the BFS algorithm
- Initially, all nodes have input features 0, except a source node with feature 1
- At every step, nodes reached by BFS have embedding 1, and nodes not reached by BFS have embedding 0
- Describe the **message**, **aggregate**, **update** functions
- Advice: Think from the **perspective of nodes** in the graph

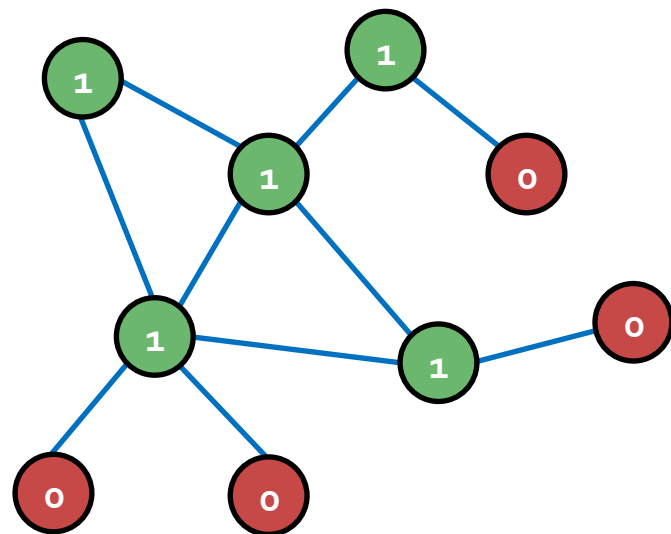


Homework 1, Q4.6

(1) Message passing

- Imagine you are a node in the graph. What information would you tell your neighbors?
 - “I have been visited by the BFS algorithm!” or “I have not been visited!”
 - Simply pass my embedding to my neighbors

$$\text{message}_{v \rightarrow u} \left(h_v^{(k-1)}, e_{v,u} \right) = h_v^{(k-1)}$$

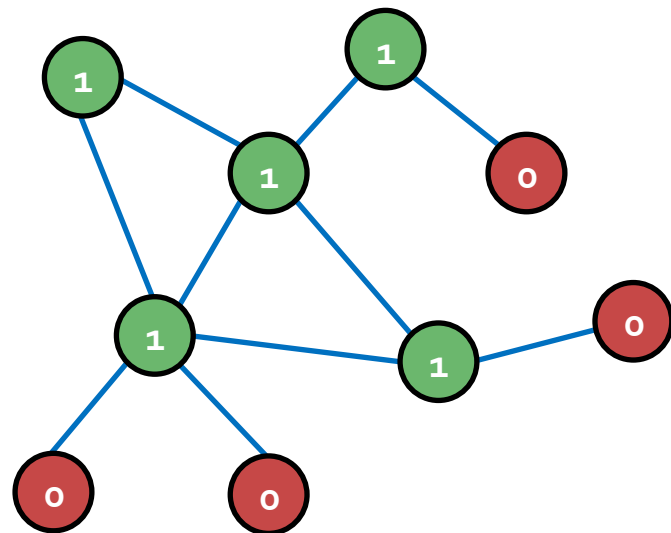


Homework 1, Q4.6

(2) Aggregation

- What information should you get from your neighbors?
 - I want to know whether any of my neighbors have been visited
- Node u aggregates neighbors' information via:

$$\text{aggregate}(\{\text{message}_{v \rightarrow u}, \forall v \in \mathcal{N}(u)\}) = \max_{v \in \mathcal{N}(u)} \text{message}_{v \rightarrow u}$$



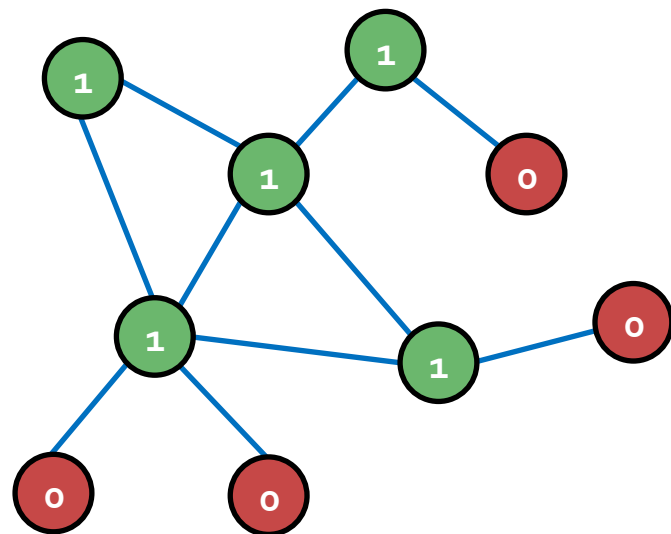
Homework 1, Q4.6

(3) Update

- Don't forget the **self-link** to the previous embedding for node u
 - BFS: I am visited if (1) I have been visited, or (2) any of my neighbors has been visited

$$\text{update} \left(h_u^{(k-1)}, \text{aggregate}(\dots) \right) = \max \left(h_u^{(k-1)}, \text{aggregate}(\dots) \right)$$

- This is one solution to Q4.6, there are alternatives



Homework 2, Q3.1

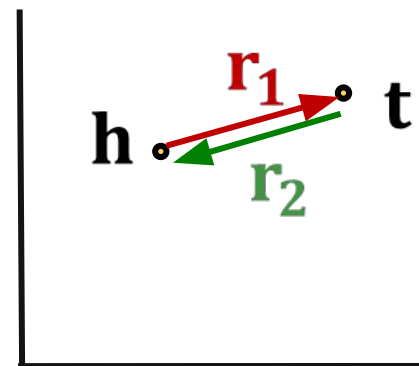
- There are **common patterns** in knowledge graph embeddings
 - **Symmetry**: A is married to B, and B is married to A
 - **Inverse**: A is teacher of B, and B is student of A
 - **Composition**: A is son of B, and C is sister of B, then C is aunt of A
- **KG method: TransE**
 - Given a triplet (h, l, t) , TransE trains entity and relation embeddings to follow the equation $h + l \approx t$
- Can we use TransE to model each of the relation patterns?

Homework 2, Q3.1

- Given (h, l, t) , TransE equation is: $\mathbf{h} + \mathbf{l} \approx \mathbf{t}$
- **Key question:** For the given relation pattern, what equations should hold true?
- **Symmetry:** A is married to B, and B is married to A
- Can we use TransE to model *symmetry*? **No**
 - For two triplets (h, l, t) and (t, l, h) to both hold true, we will have: $\mathbf{h} + \mathbf{l} \approx \mathbf{t}$ and $\mathbf{t} + \mathbf{l} \approx \mathbf{h}$
 - The only possibility for both equations to be true is if $\mathbf{l} = \mathbf{0}$ and $\mathbf{h} = \mathbf{t}$, which is a problem since two different entities should have different embeddings

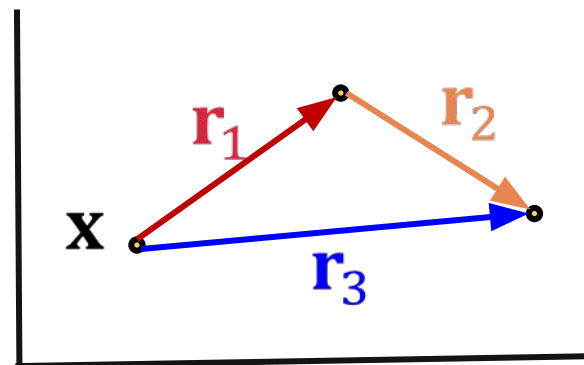
Homework 2, Q3.1

- Given (h, l, t) , TransE equation is: $h + l \approx t$
- **Inverse:** A is teacher to B, and B is student to A
- Can we use TransE to model *inverse*? **Yes**
 - For two triplets (h, r_1, t) and (t, r_2, h) to both hold true, we will have: $h + r_1 \approx t$ and $t + r_2 \approx h$
 - It suffices to set the inverse relation $r_2 = -r_1$



Homework 2, Q3.1

- Given (h, l, t) , TransE equation is: $h + l \approx t$
- **Composition:** A is son of B, and C is sister of B, then C is aunt of A
- Can we use TransE to model *composition*? **Yes**
 - Given three triplets, (a, r_1, b) , (b, r_2, c) , (a, r_3, c) , where r_3 is the composition of r_2 and r_1
 - For all triplets to be true, we will have: $a + r_1 \approx b$, $b + r_2 \approx c$, $a + r_3 \approx c$
 - Set $r_3 = r_1 + r_2$ for composition



Stanford CS224W: Miscellaneous Topics

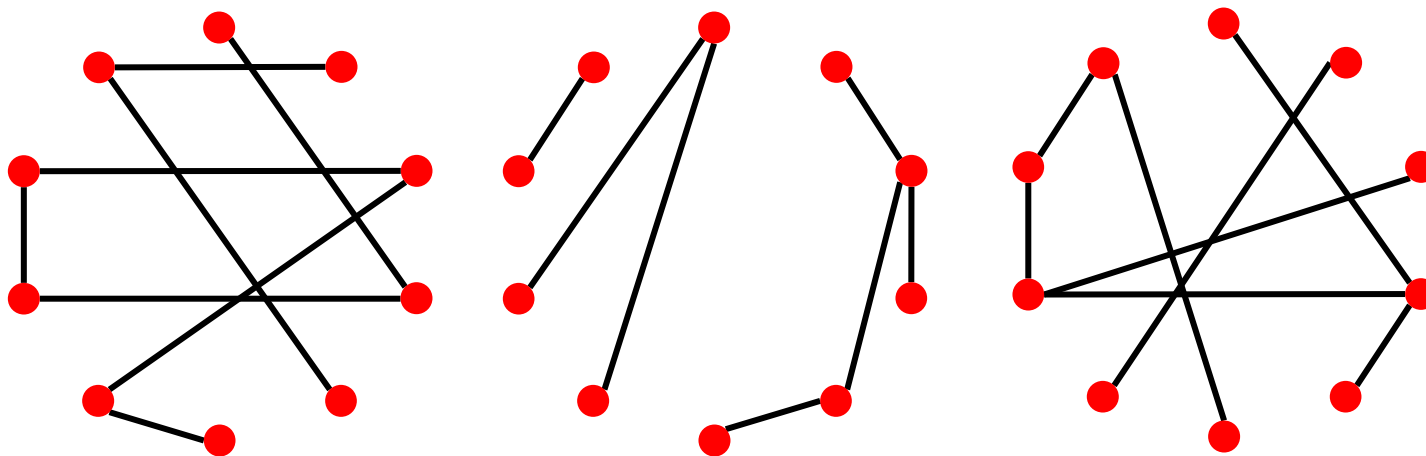
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Erdős-Rényi Random Graph

- To produce an undirected graph $G = (V, E)$, the ER model uses a fixed likelihood to generate edges connecting any pair of nodes:

$$\mathbb{P}[(u, v) \in E] = r, \quad \forall u, v \in V, u \neq v$$



$n = 10$
 $r = 1/6$

Erdős-Rényi Random Graph

What is the expected average node degree, $\mathbf{E}[d]$, of a graph generated by ER?

- **Key idea:** summing the edge connectivity over nodes to compute the expected node degree

$$|E| = \frac{1}{2} \sum_{u \in V} \sum_{v \in V \setminus \{u\}} 1 \cdot \mathbb{1}[(u, v) \in E]$$

$$\mathbb{E}[|E|] = \frac{1}{2} \sum_{u \in V} \sum_{v \in V \setminus \{u\}} 1 \cdot \mathbb{E}[\mathbb{1}[(u, v) \in E]]$$

$$= \frac{1}{2} \sum_{u \in V} \sum_{v \in V \setminus \{u\}} 1 \cdot r$$

$$= \frac{|V|(|V| - 1)}{2} r$$

$$= \binom{|V|}{2} r$$

$$d = \frac{2|E|}{|V|} \quad \leftarrow \text{total degree in } G$$

$$\mathbb{E}[d] = \frac{2\mathbb{E}[|E|]}{|V|}$$

$$= (|V| - 1)r$$

All the Best

- All the best with your exam preparation!