

# Contract-Signing Protocols

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# Before contract signing ...

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## ◆ Questions about projects? Want help?

- Contact Arnab this week for suggestions

## ◆ Discussion of security properties

- Authentication
- Secrecy

## ◆ Precise definitions

- Set of runs of a system
- When a run violates a security condition
  - Definition of *successful attack*
- Safety vs liveness properties

# Protocol

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- ◆ A Protocol is defined by a set of roles, and initial conditions (if needed)
- ◆ What is a role?
  - A "program" executed at one site
  - Includes communication, internal actions
- ◆ What are initial conditions?
  - Example: each agent has a secret key, shared only with the server
  - Example: each agent knows the public verification key for every other agent's digital signature key

# Example roles: NSL protocol

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new m;

send encrypt( Key(Y),  $\langle X, m \rangle$  );

recv encrypt( Key(X),  $\langle m, Y, n \rangle$  );

send encrypt( Key(Y), n )

"Alice"

recv encrypt( Key(Y),  $\langle X, m \rangle$  );

new n;

send encrypt( Key(X),  $\langle m, Y, n \rangle$  );

recv encrypt( Key(Y), n )

"Bob"

**Initial conditions:** each agent has a private key and knows the public keys of other agents

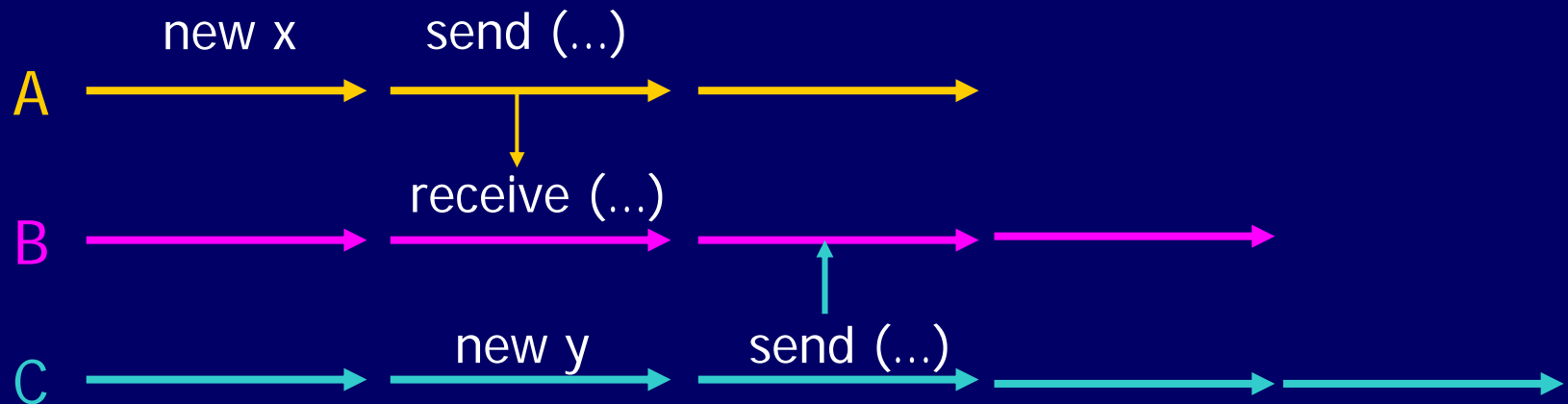
# Execution model

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## ◆ Initial configuration

- Set of principals and keys
- Assignment of  $\geq 1$  role to each principal

## ◆ Run



Honest principals follow roles of the protocol; some agents may be dishonest  
Actions can be arranged in a linear trace

# Data "known" to agent

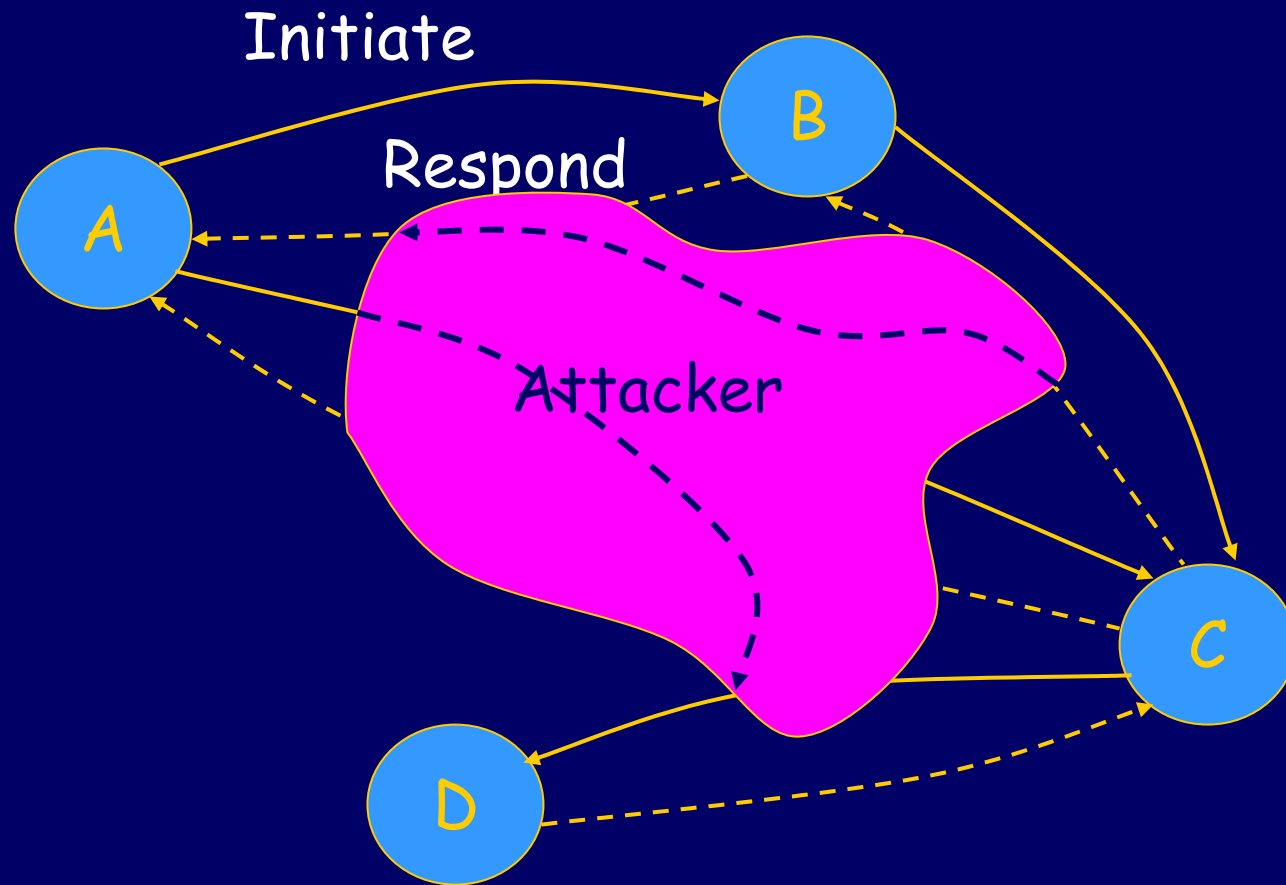
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- ◆ At each point in run, each agent knows
  - All the data provided by initial conditions
    - Public keys, a private key, shared secret key, ...
  - All the data generated by that agent
    - Fresh nonces chosen at random, new keys, ...
  - All the messages received
  - Any data derivable from this information
    - Can decrypt a message if decryption key known

Symbolic representation of data and symbolic characterization of "data knowledge" is called "the Dolev-Yao model."

# Protocol correctness

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Correct if no security violation in any run

# Correctness conditions

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## ◆ Authentication

- Idea: "I know I am talking to you"
- Formalization 1
  - If Alice initiates conversation by sending to Bob, then data she receives was generated by Bob for Alice.
- Formalization 2
  - If Alice completes the initiator role, sending messages to Bob, then Bob completes the responder role with the same messages in the same order.
  - One-to-one correspondence between sessions
- Your thoughts and alternatives?



# Correctness conditions

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## ◆ Secrecy

- Idea: "The attacker does not know our secrets"
- Formalization 1
  - The session key cannot be computed from the data available to the attacker.
- Formalization 2
  - The entire conversation between Alice and Bob is indistinguishable (to others) from a run with completely different nonces, keys, etc.
- Your thoughts and alternatives?

# Safety vs Liveness

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## ◆ Trace property

- Property is true of a system iff it is true for all traces (runs) of the system

## ◆ Safety property

- Bad things do not happen
- Examples: no deadlock, no page fault, ...

## ◆ Liveness property

- Good things do happen (eventually)
- Example: every process gets scheduled to run

# Safety vs Liveness

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## ◆ Safety property

- “Bad things do not happen”

$\forall$  traces  $t$ , possibly infinite:

$$P(t) \text{ iff } \forall t' < t. P(t')$$

- If a safety property fails, it fails at some finite point

## ◆ Liveness property

- “Good things do happen (eventually)”

$\forall$  finite initial traces  $s$ :  $\exists$  trace  $t. P(st)$

- A liveness property holds if every beginning of a trace can be extended to one with the desired property

# Contract Signing

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- ◆ Two parties want to sign a contract
  - Multi-party signing is more complicated
- ◆ The contract is known to both parties
  - The protocols we will look at are *not* for contract negotiation (e.g., auctions)
- ◆ The attacker could be
  - Another party on the network
  - The “person” you think you want to sign a contract with

# Example

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Seller advertises and  
receives bids

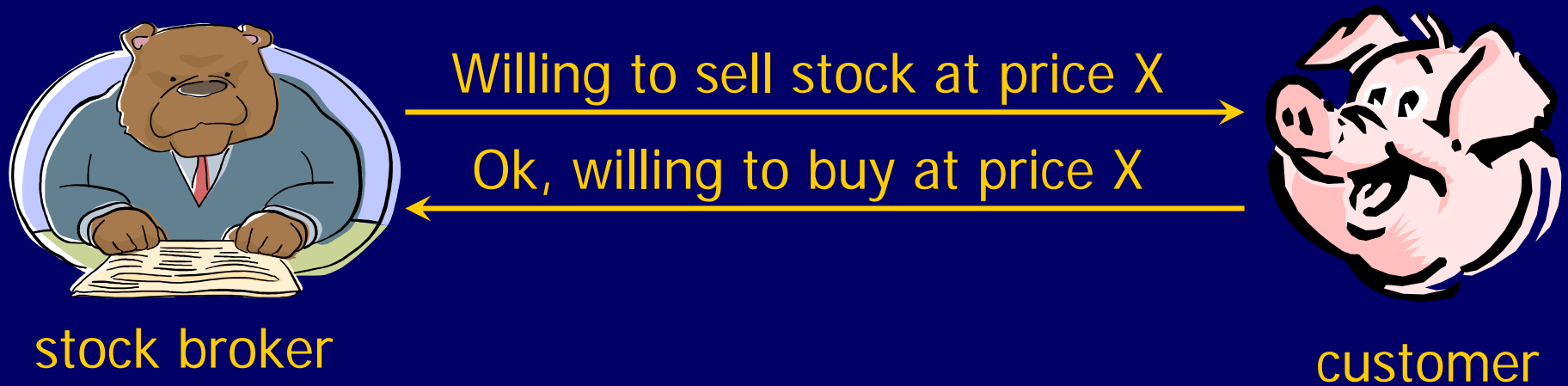
Buyer may have several  
choices



- ◆ Both parties want to sign a contract
- ◆ Neither wants to commit first

# Another example: stock trading

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## ◆ Why signed contract?

- Suppose market price changes
- Buyer or seller may want proof of agreement

# Network is Asynchronous

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## ◆ Physical solution

- Two parties sit at table
- Write their signatures simultaneously
- Exchange copies

## ◆ Problem

- How to sign a contract on a network?

Fair exchange: general problem of exchanging information so both succeed or both fail

# Fundamental limitation

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## ◆ Impossibility of consensus

- *Very weak consensus is not solvable if one or more processes can be faulty*

## ◆ Asynchronous setting

- Process has *initial* 0 or 1, and eventually *decides* 0 or 1
- *Weak termination*: some correct process decides
- *Agreement*: no two processes decide on different values
- *Very weak validity*: there is a run in which the decision is 0 and a run in which the decision is 1

## ◆ Reference

- M. J. Fischer, N. A. Lynch and M. S. Paterson,  
*Impossibility of Distributed Consensus with One Faulty Process*. J ACM 32(2):374-382 (April 1985).



# Implication for fair exchange

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## ◆ Need a trusted third party (TTP)

- It is impossible to solve strong fair exchange without a trusted third party.

The proof is by relating strong fair exchange to the problem of consensus and adapting the impossibility result of Fischer, Lynch and Paterson.

## ◆ Reference

- H. Pagnia and F. C. Gärtner, On the impossibility of fair exchange without a trusted third party. Technical Report TUD-BS-1999-02, Darmstadt University of Technology, March 1999

# Two forms of contract signing

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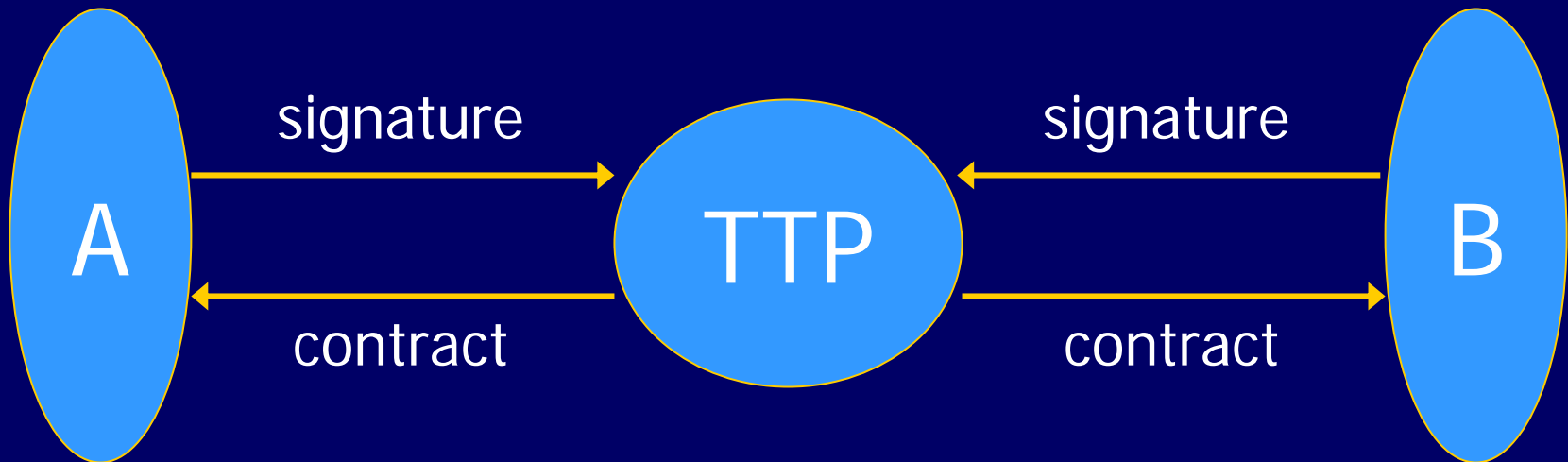
## ◆ Gradual-release protocols

- Alice and Bob sign contract
- Exchange signatures a few bits at a time
- Issues
  - Signatures are verifiable
  - Work required to guess remaining signature decreases
  - Alice, Bob must be able to verify that what they have received so far is part of a valid signature

## ◆ Add trusted third party

# Easy TTP contract signing

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## ◆ Problem

- TTP is bottleneck
- Can we do better?

# Optimistic contract signing

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## ◆ Use TTP only if needed

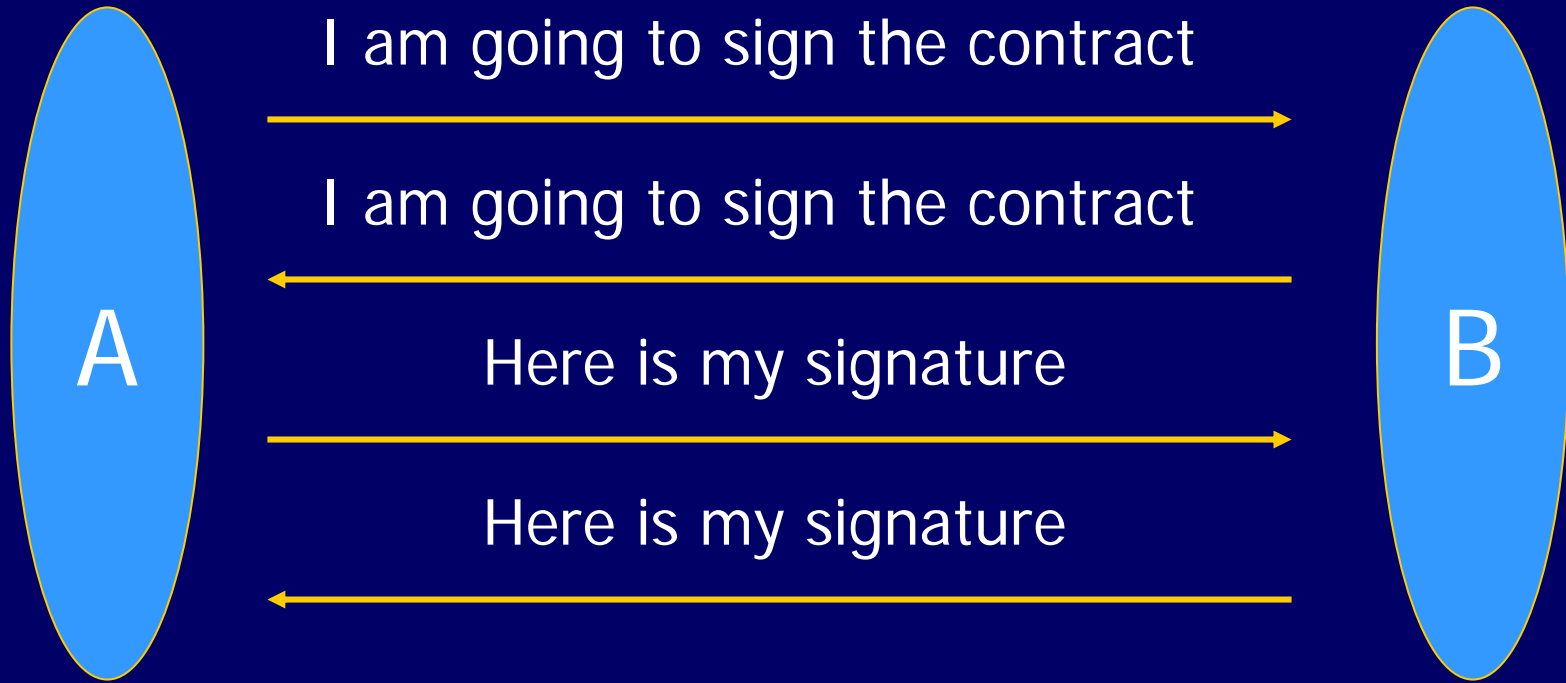
- Can complete contract signing without TTP
- TTP will make decisions if asked

## ◆ Goals

- Fair: no one can cheat the other
- Timely: no one has to wait indefinitely (assuming that TTP is available)
- Other properties ...

# A general protocol outline

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- ◆ **Trusted third party can force contract**
  - Third party can declare contract binding if presented with first two messages.

# Commitment (idea from crypto)

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## ◆ Cryptographic hash function

- Easy to compute function  $f$
- Given  $f(x)$ , hard to find  $y$  with  $f(y)=f(x)$
- Hard to find pairs  $x, y$  with  $f(y)=f(x)$

## ◆ Commit

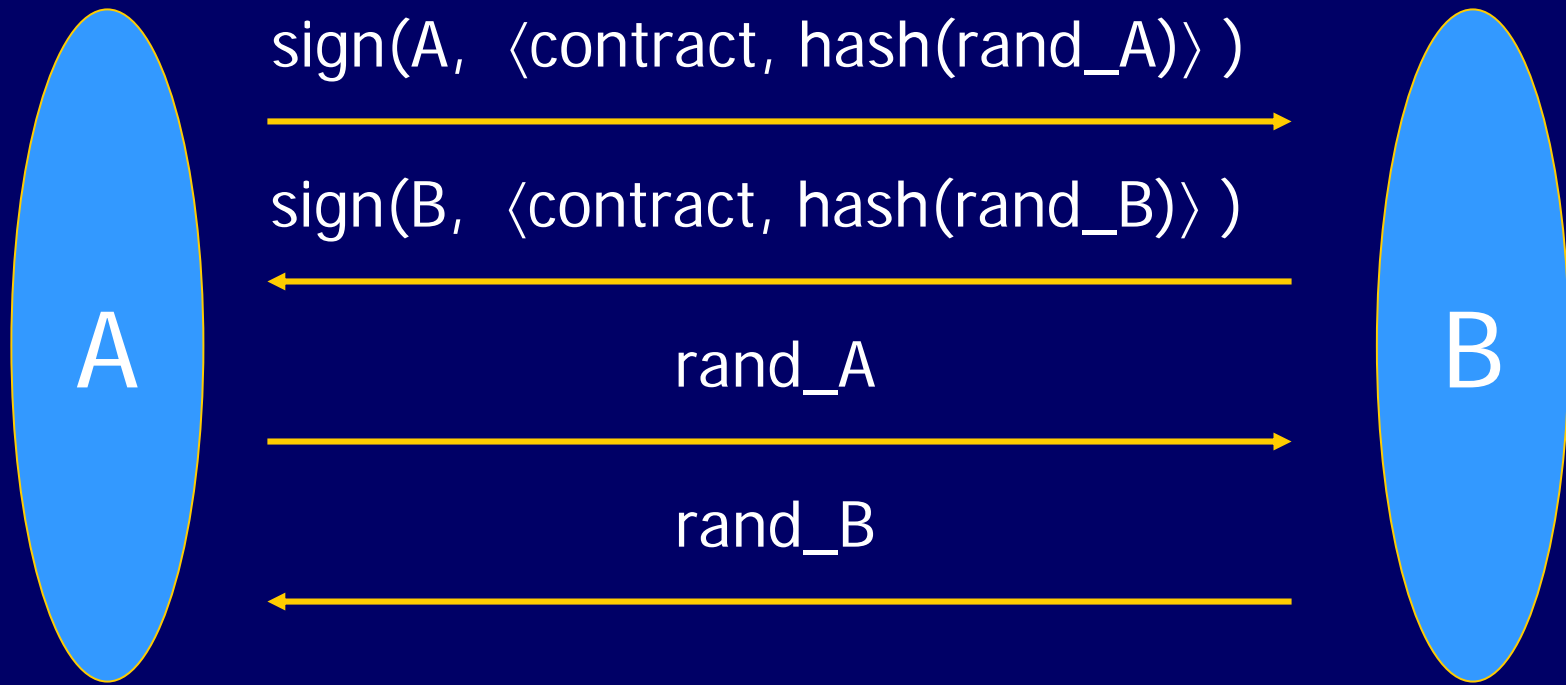
- Send  $f(x)$  for randomly chosen  $x$

## ◆ Complete

- Reveal  $x$

# Refined protocol outline

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- ◆ Trusted third party can force contract
  - Third party can declare contract binding by signing first two messages.

# Optimistic Protocol [Asokan, Shoup, Waidner]

Input:

$PK_A, T, \text{text}$

Input:

$PK_B, T, \text{text}$



$$m_1 = \text{sig}_A(PK_A, PK_B, T, \text{text}, \text{hash}(R_A))$$



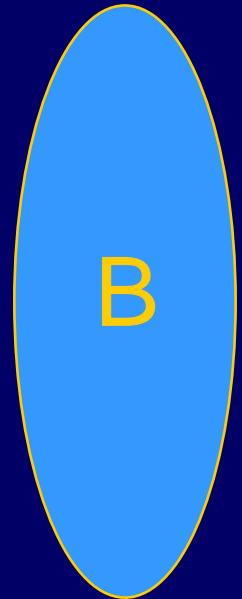
$$m_2 = \text{sig}_B(m_1, \text{hash}(R_B))$$



$$m_3 = R_A$$



$$m_4 = R_B$$



$m_1, R_A, m_2, R_B$





# Asokan-Shoup-Waidner Outcomes

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## ◆ Contract from normal execution



$m_1, R_A, m_2, R_B$

## ◆ Contract issued by third party



$sig_T(m_1, m_2)$

## ◆ Abort token issued by third party



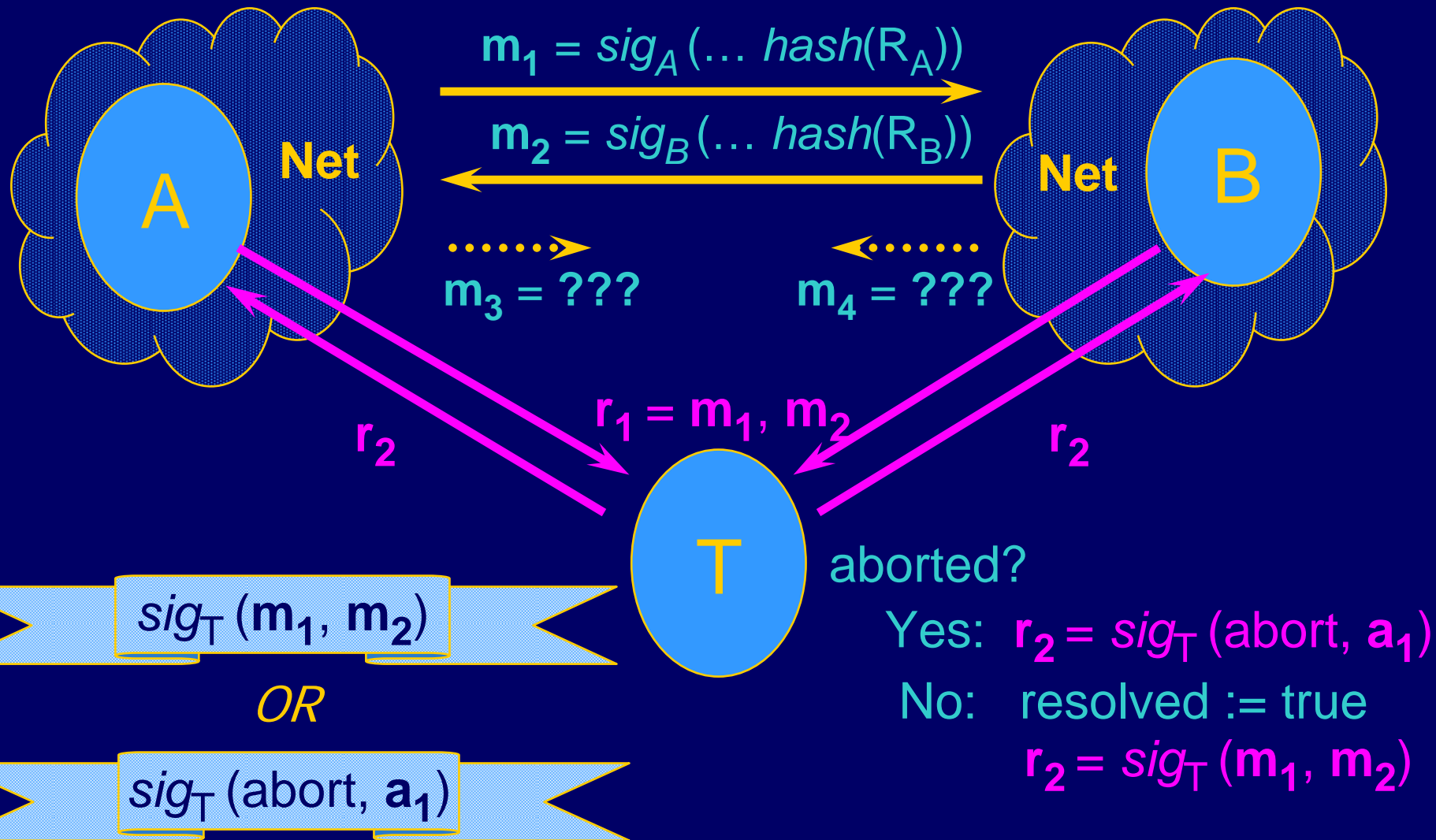
$sig_T(\text{abort}, a_1)$

# Role of Trusted Third Party

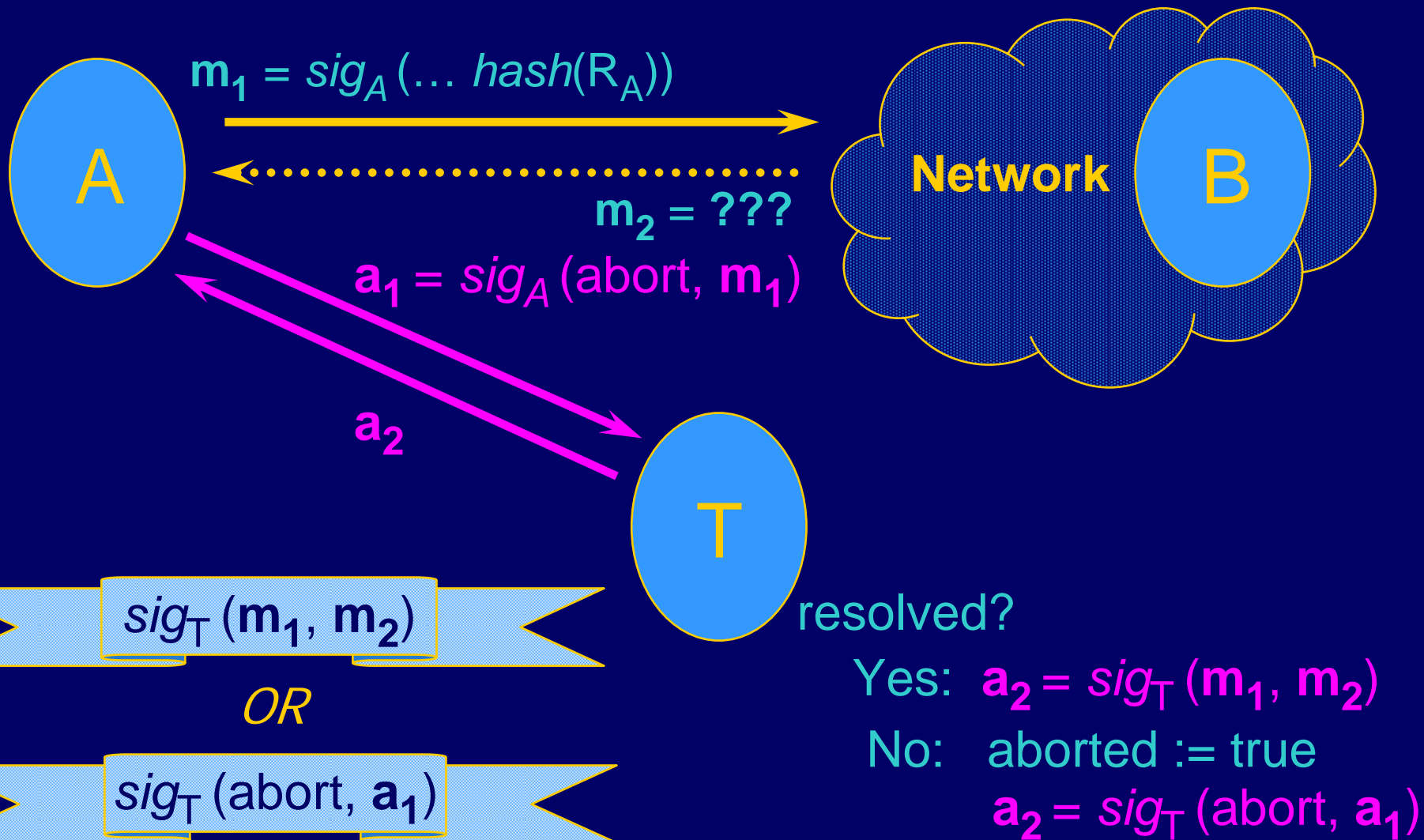
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- ◆ T can issue a replacement contract
  - Proof that both parties are committed
- ◆ T can issue an abort token
  - Proof that T will not issue contract
- ◆ T acts only when requested
  - decides whether to abort or resolve on the first-come-first-serve basis
  - only gets involved if requested by A or B

# Resolve Subprotocol



# Abort Subprotocol



# Fairness and Timeliness

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## Fairness

If A cannot obtain B's signature, then  
B should not be able to obtain A's signature

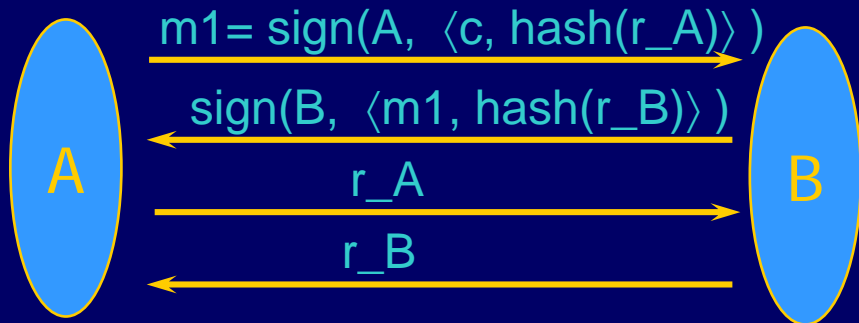
and vice versa

## Timeliness

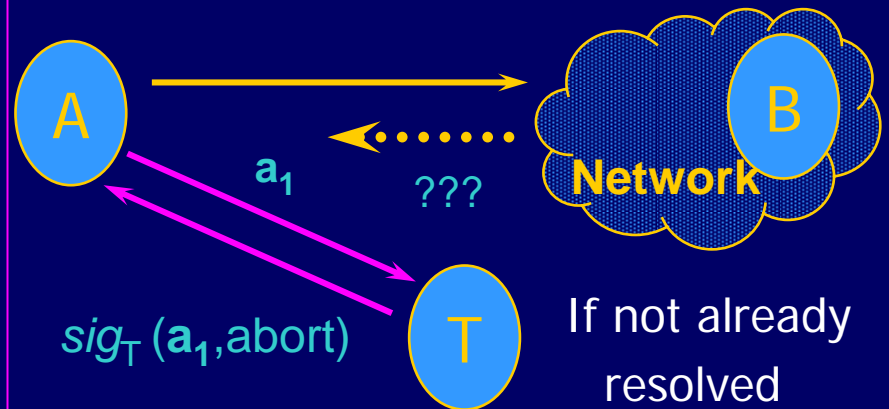
"One player cannot force the other to wait --  
a fair and timely termination can always be  
forced by contacting TTP"

# Asokan-Shoup-Waidner protocol

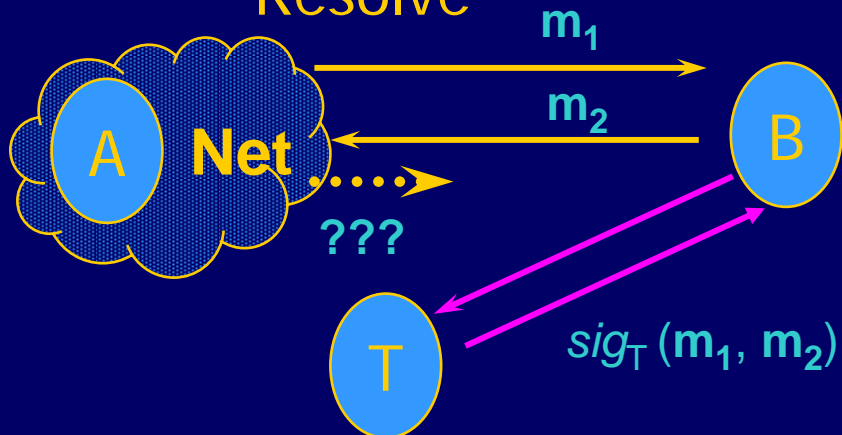
## Agree



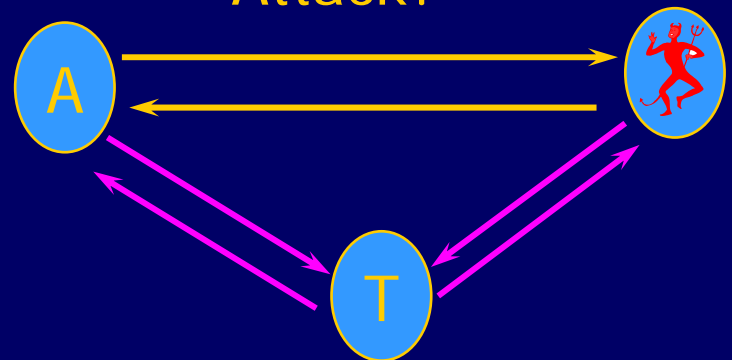
## Abort



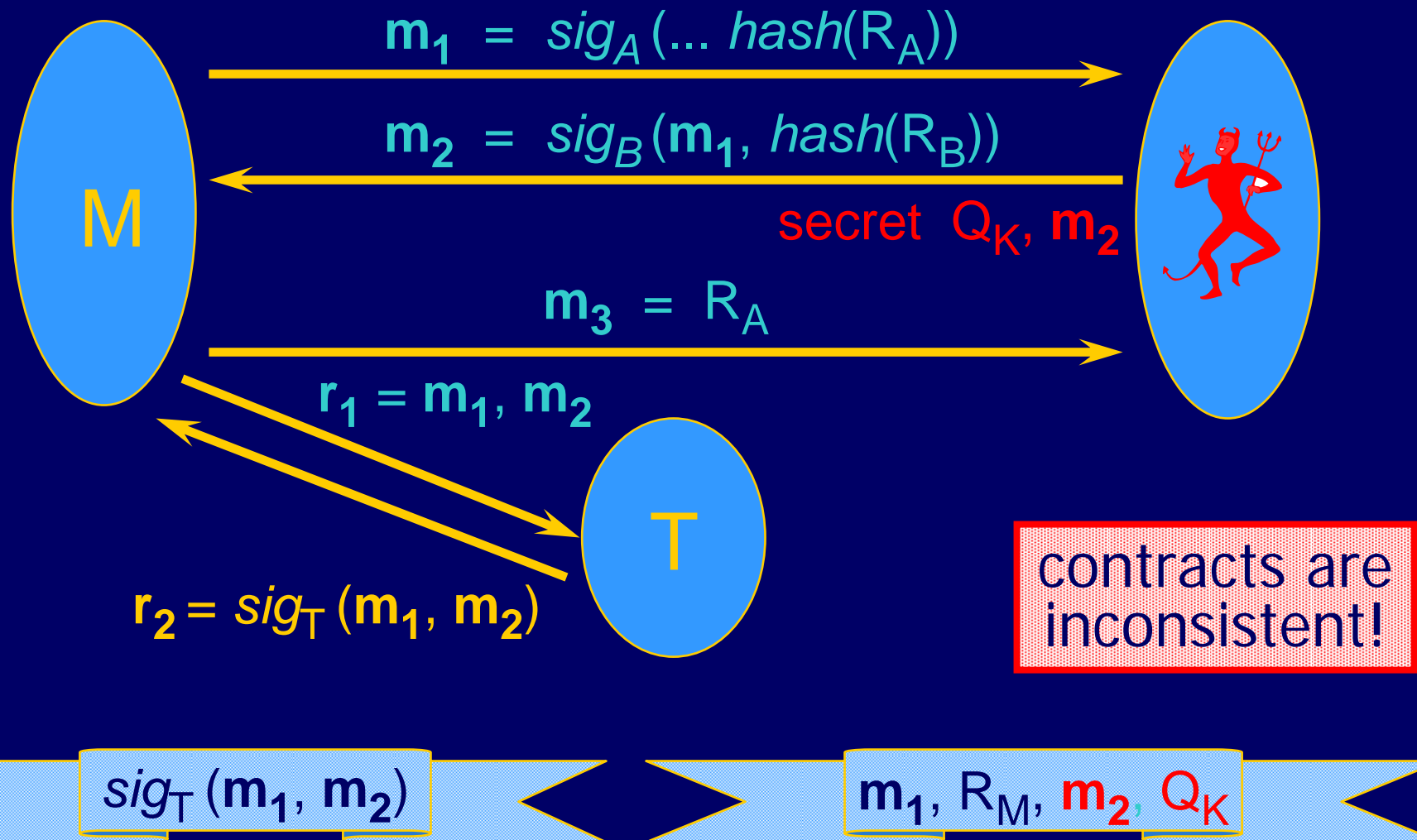
## Resolve



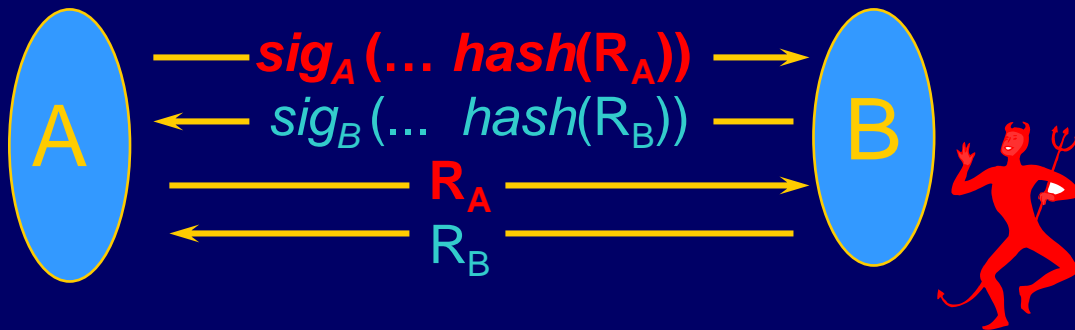
## Attack?



# Contract Consistency Attack

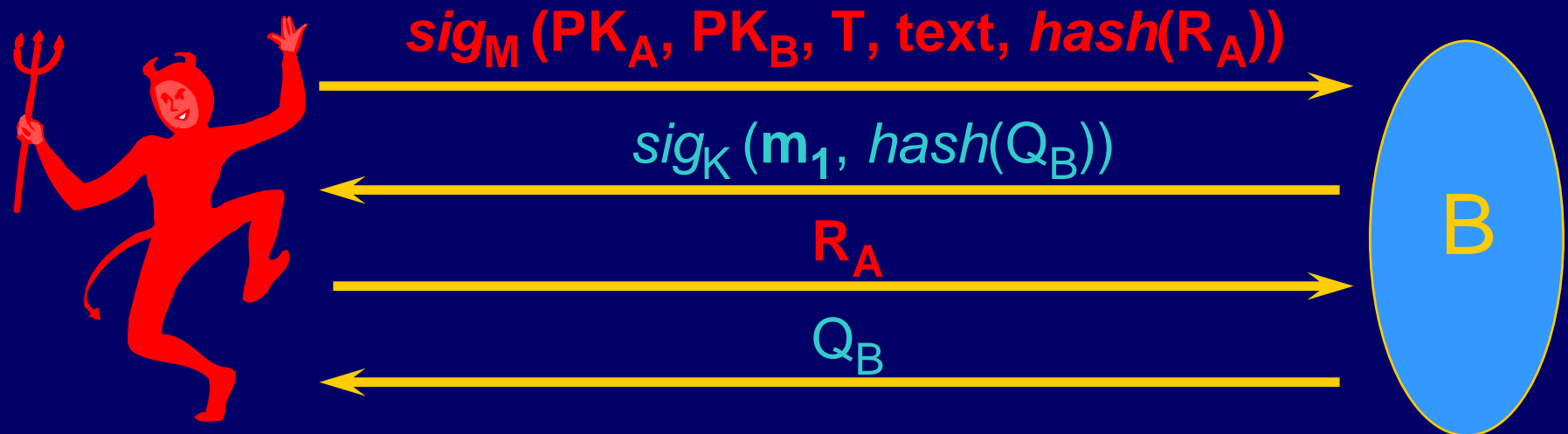


# Replay Attack



Intruder causes B to commit to old contract with A

Later ...



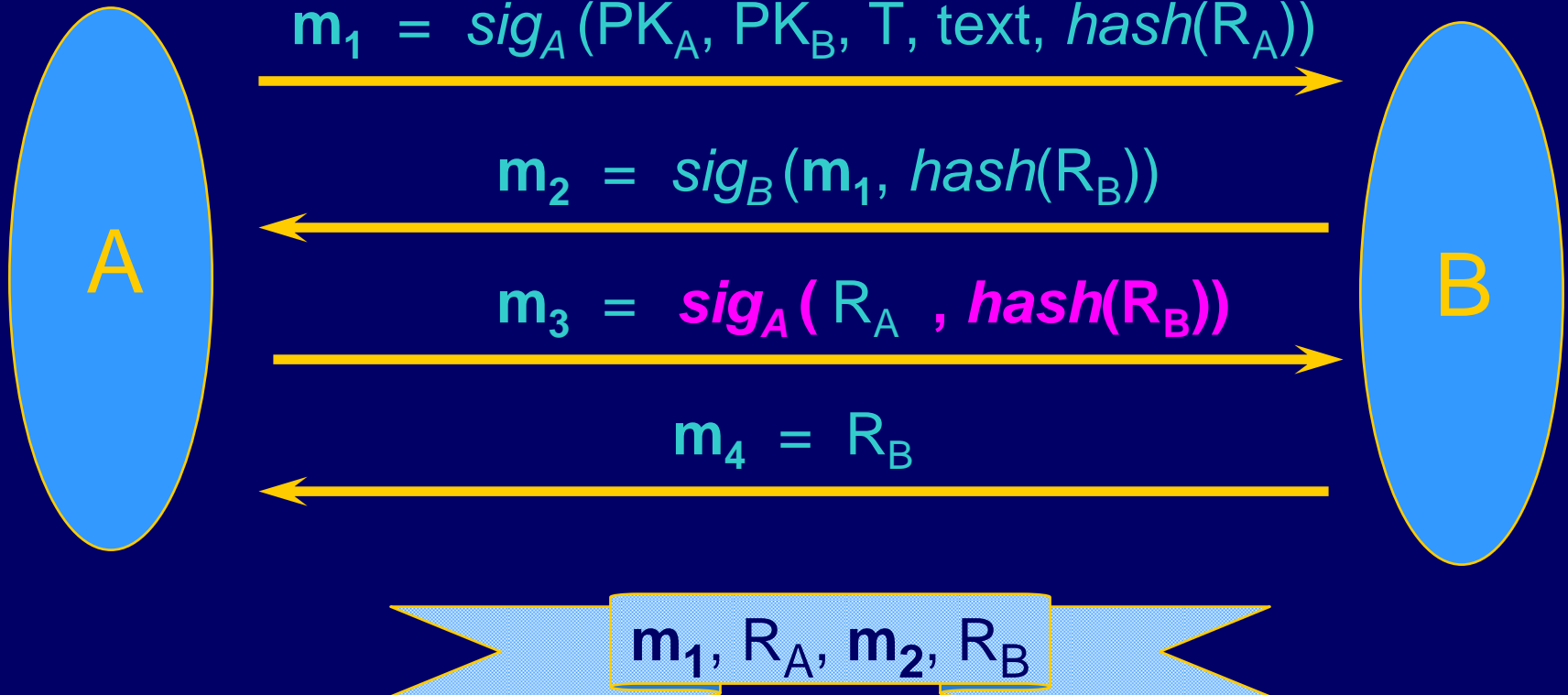


# Fixing the Protocol

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Input:  
 $PK_A, T, \text{text}$

Input:  
 $PK_B, T, \text{text}$



# Desirable properties

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## ◆ Fair

- If one can get contract, so can other

## ◆ Accountability

- If someone cheats, message trace shows who cheated

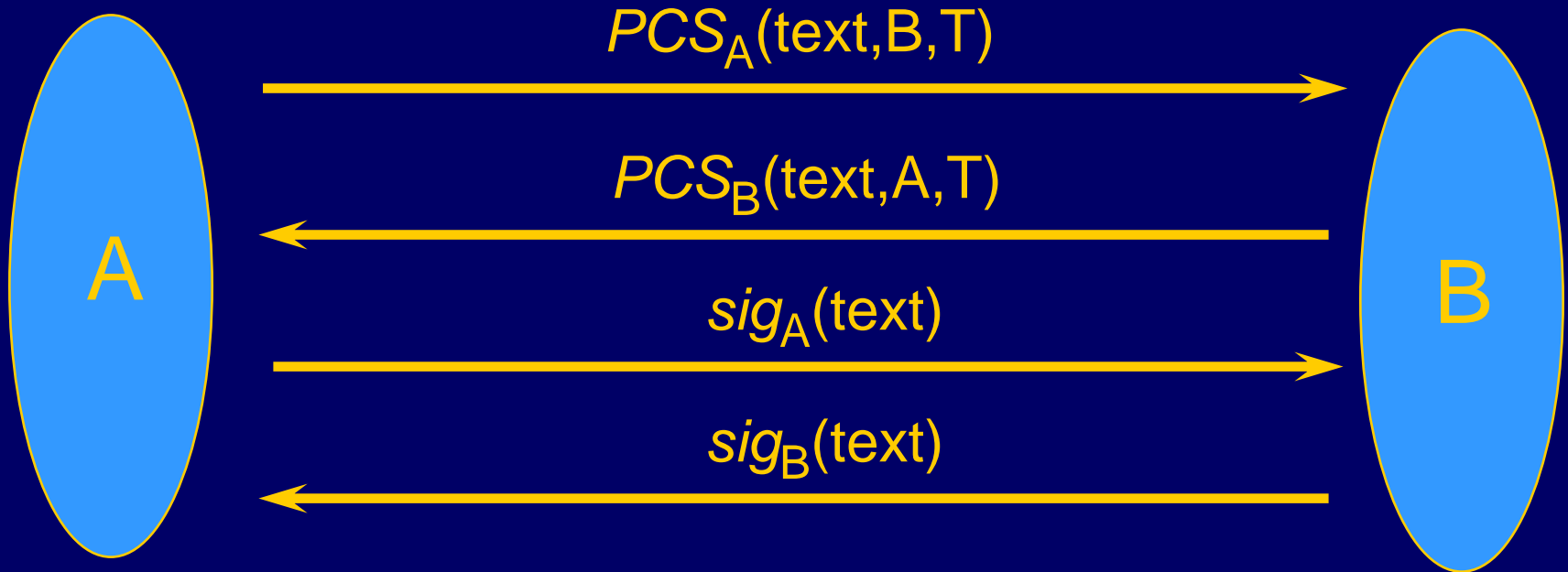
## ➡ Abuse free

- No party can show that they can determine outcome of the protocol

# Abuse-Free Contract Signing

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[Garay, Jakobsson, MacKenzie]



# Preventing "abuse" [Garay, Jakobsson, MacKenzie]

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## ◆ Private Contract Signature

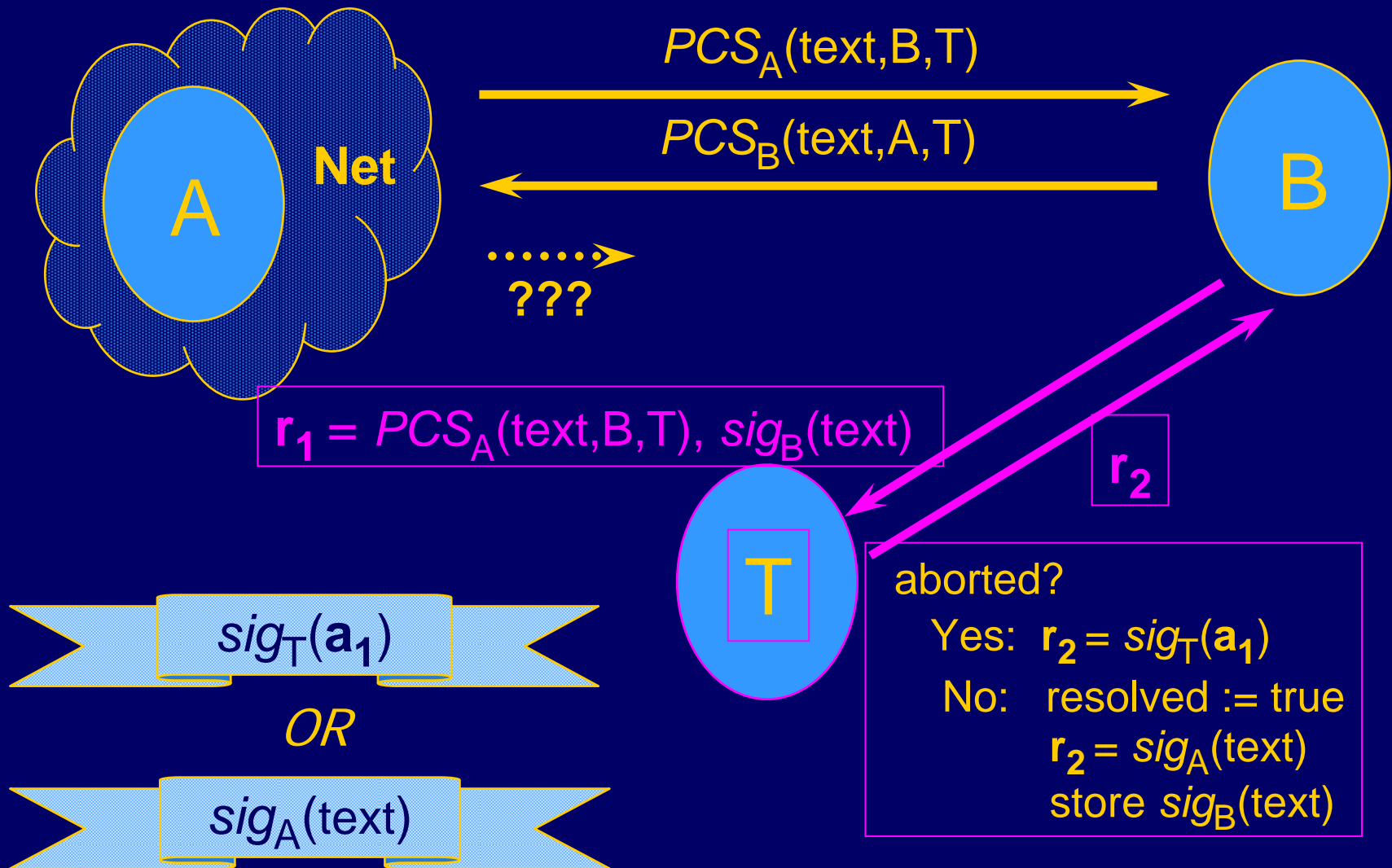
- Special cryptographic primitive
- B cannot take msg from A and show to C
- T converts signatures, does not use own

# Role of Trusted Third Party

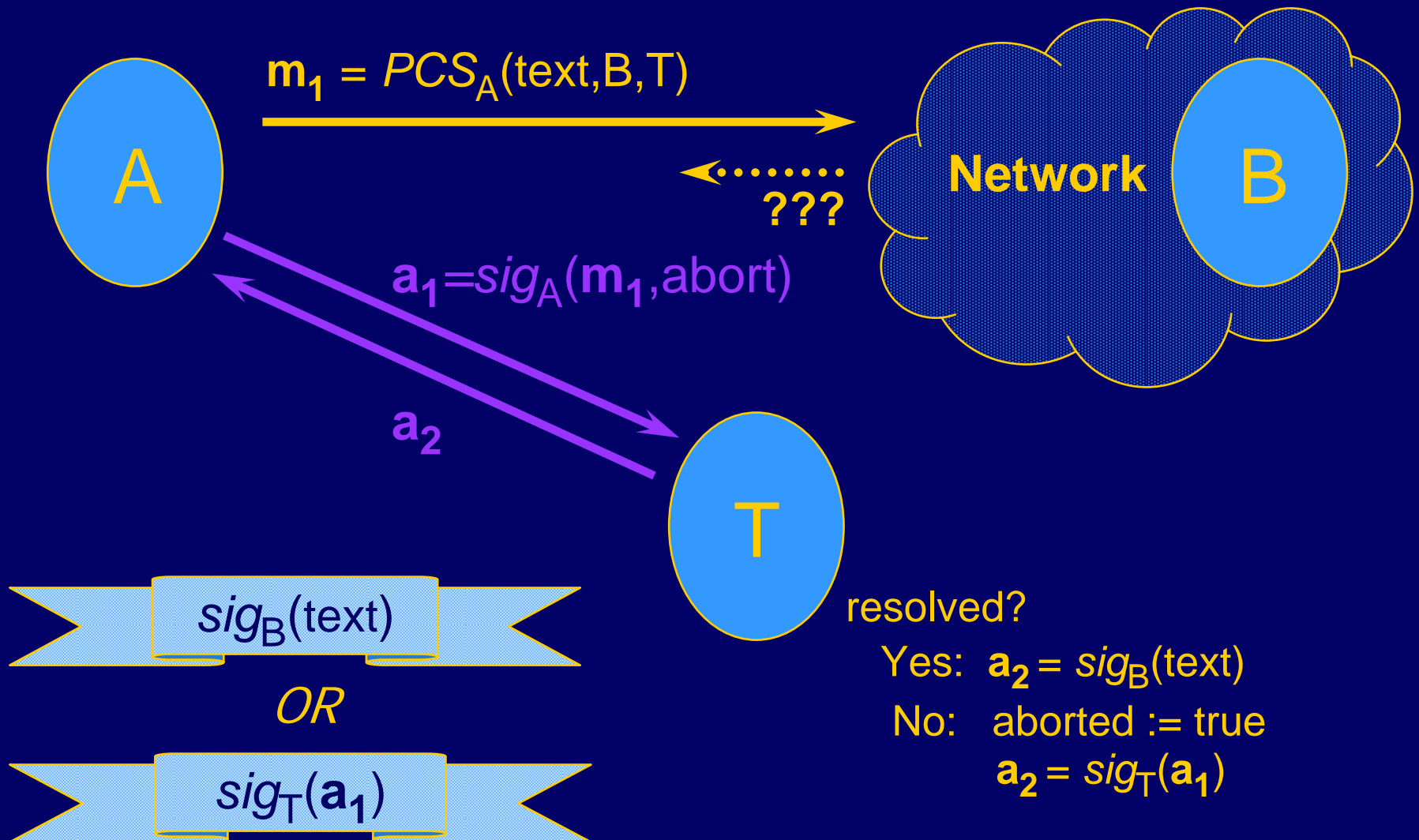
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- ◆ T can convert PCS to regular signature
  - Resolve the protocol if necessary
- ◆ T can issue an abort token
  - Promise not to resolve protocol in future
- ◆ T acts only when requested
  - decides whether to abort or resolve on a first-come-first-served basis
  - only gets involved if requested by A or B

# Resolve Subprotocol

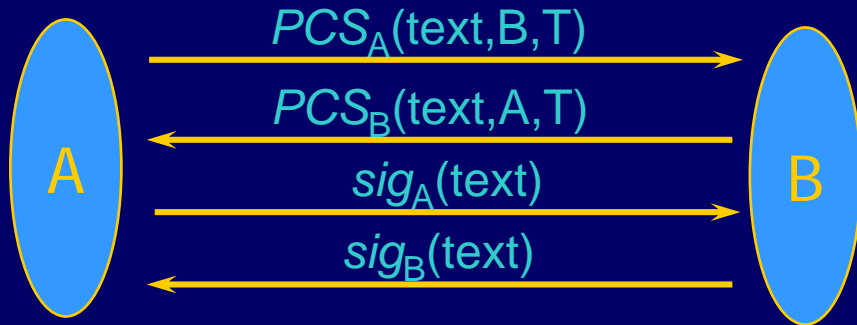


# Abort Subprotocol

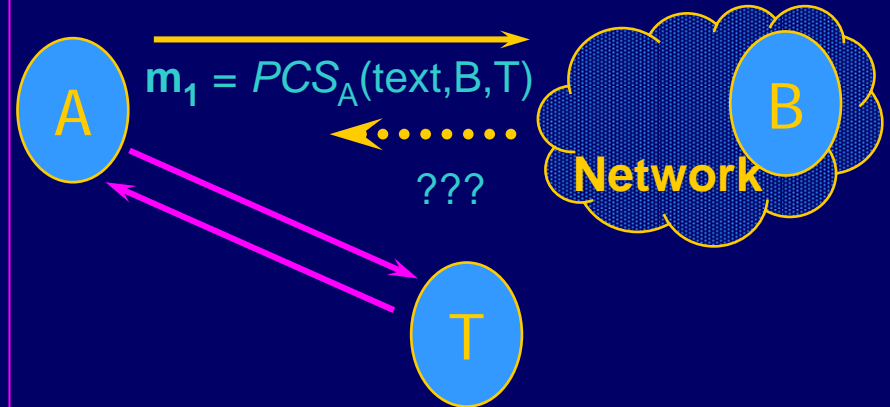


# Garay, Jakobsson, MacKenzie

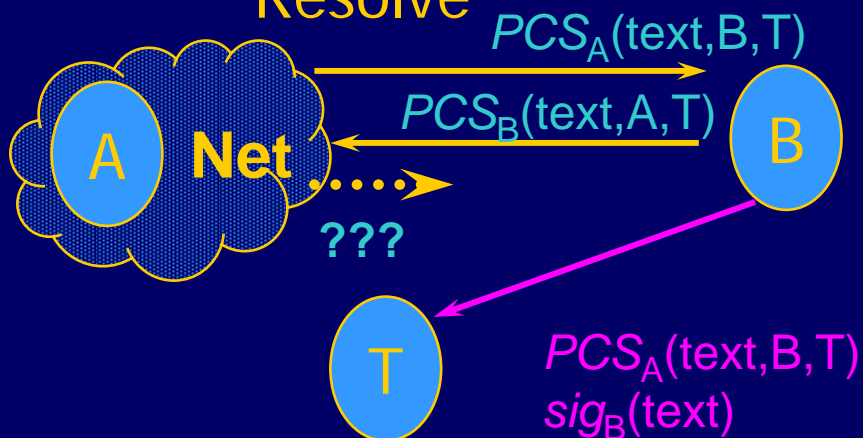
## Agree



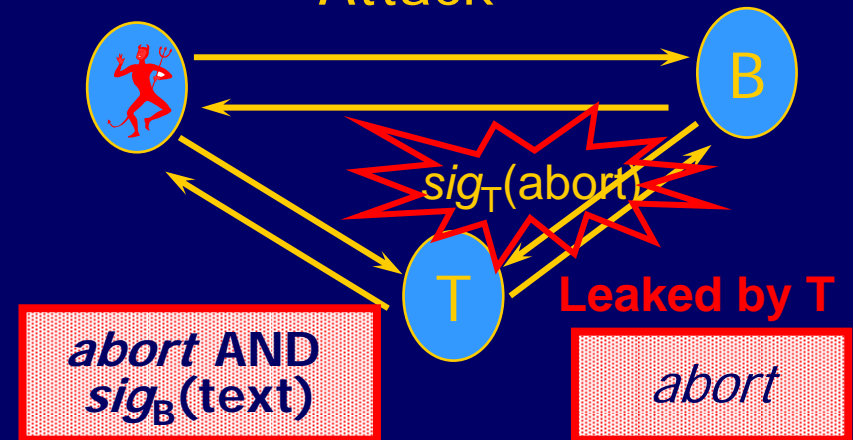
## Abort



## Resolve

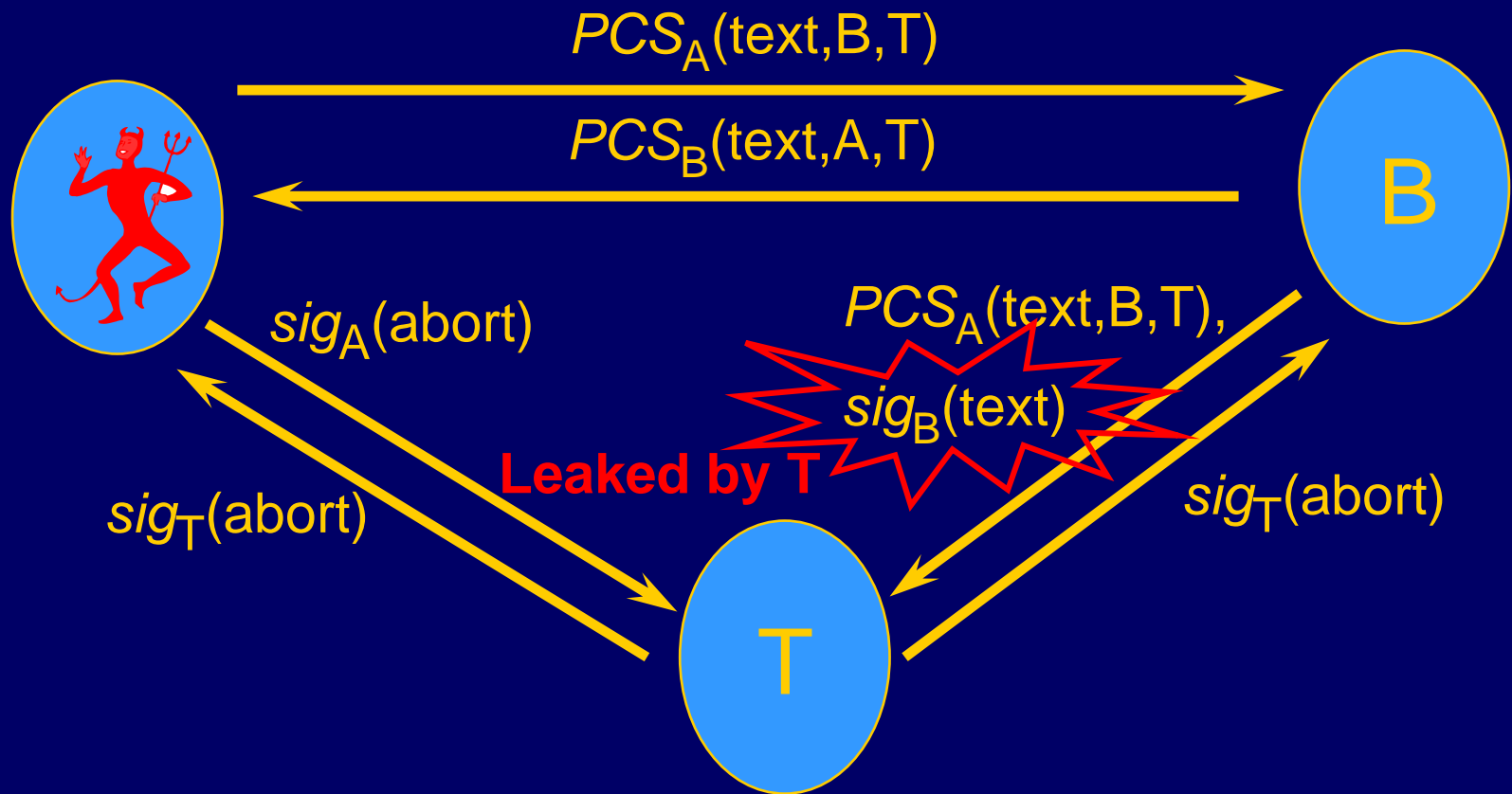


## Attack





# Attack

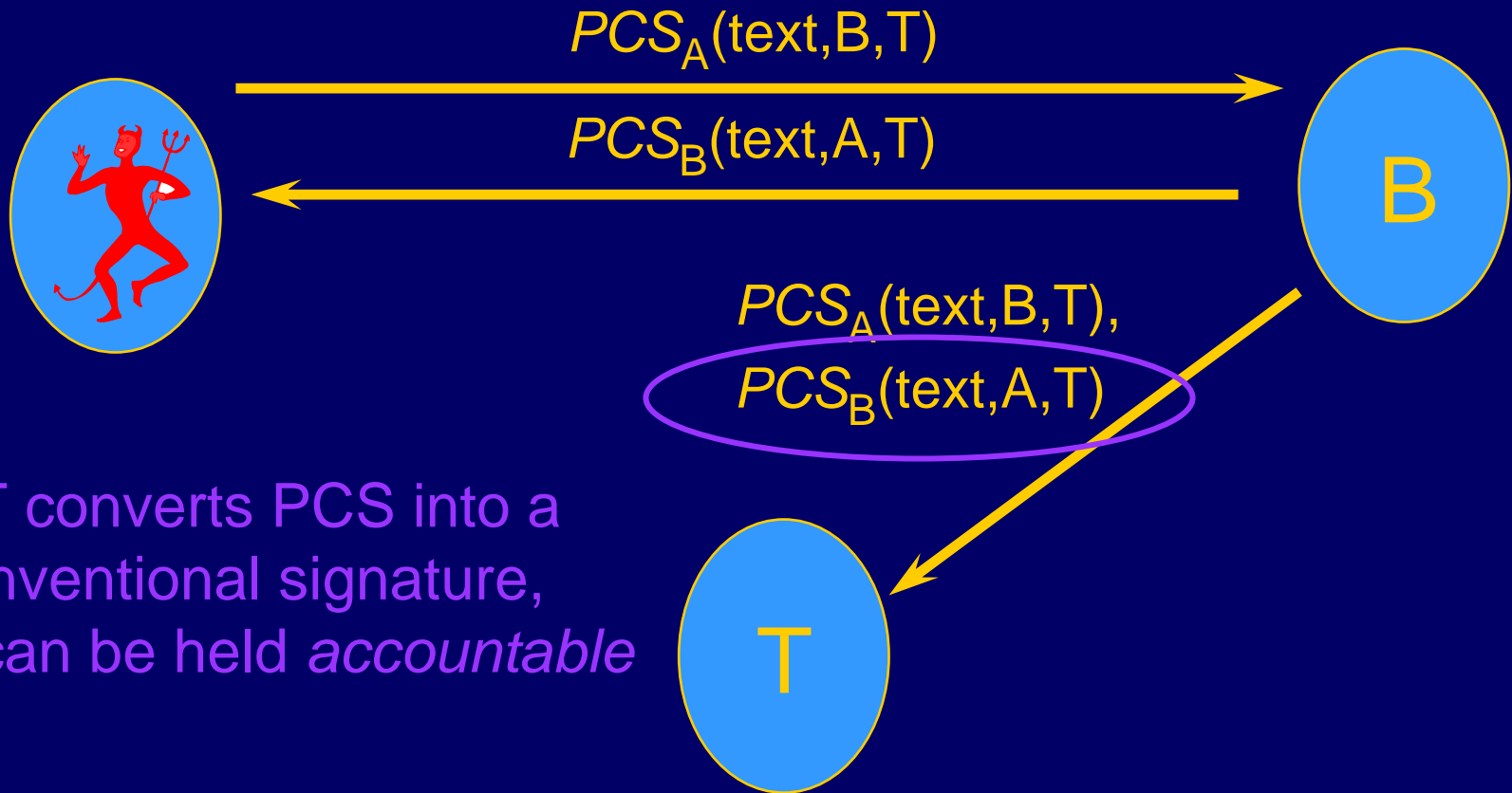


*abort AND  $sig_B(\text{text})$*

*only abort*

# Repairing the Protocol

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If T converts PCS into a conventional signature, T can be held *accountable*

# Balance

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No party should be able to **unilaterally** determine the outcome of the protocol

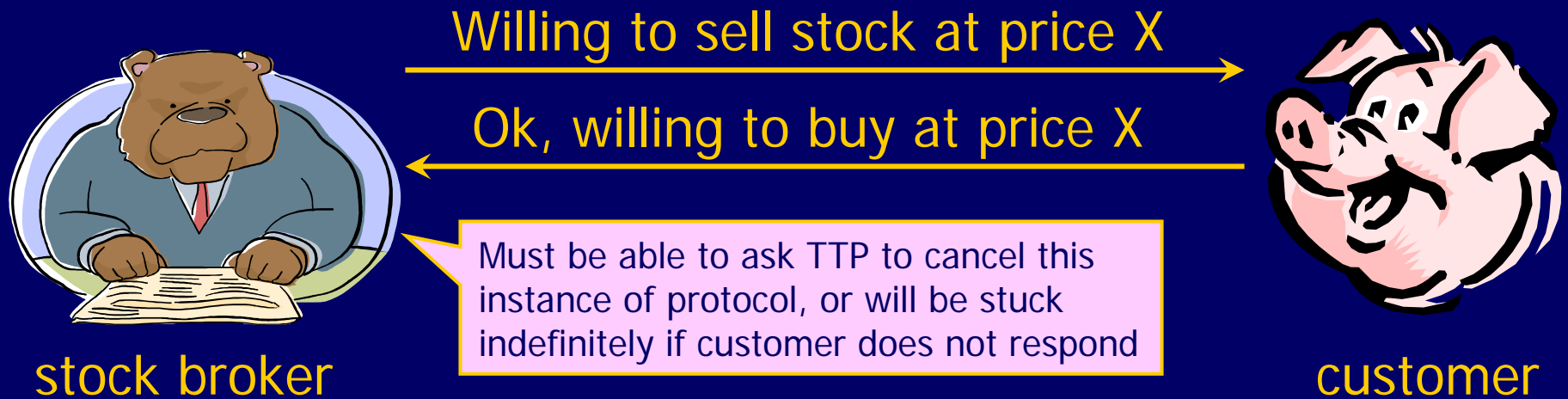
Balance may be violated even if basic fairness is satisfied!

Stock sale example: there is a point in the protocol where the broker can unilaterally choose whether the sale happens or not

Can a timely, optimistic protocol be fair AND balanced?

# Advantage

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Can go ahead and complete the sale, OR  
can still ask TTP to cancel  
(TTP doesn't know customer has responded)

Chooses whether deal will happen:  
does not have to commit stock for sale,  
can cancel if sale looks unprofitable

Optimistically waits for broker to respond ...

Cannot back out of the deal:  
must commit money for stock

# "Abuse free": as good as it gets

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## ◆ Specifically:

- One signer always has an advantage over the other, no matter what the protocol is
- Best case: signer with advantage cannot *prove* it has the advantage to an outside observer

# Theorem

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- ◆ In any fair, optimistic, timely contract-signing protocol, if one player is optimistic\*, the other player has an advantage.

\* optimistic player: waits a little before going to the third party

# Abuse-Freeness

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~~Balance~~ impossible ☹

No party should be able to unilaterally determine the outcome of the protocol

## Abuse-Freeness

No party should be able to **prove** that it can unilaterally determine the outcome of the protocol

# How to prove something like this?

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## ◆ Define "protocol"

- Program for Alice, Bob, TTP
- Each move depends on
  - Local State (what's happened so far)
  - Message from network
  - Timeout

## ◆ Consider possible optimistic runs

## ◆ Show someone gets advantage



# Key idea (omitting many subtleties)

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- ◆ Define “power” of a signer (A or B) in a state  $s$

$$\text{Power}_A(s) = \begin{cases} 2 & \text{if A can get contract by reading} \\ & \text{a message already in network,} \\ & \text{doing internal computation} \\ 1 & \text{if A can get contract by} \\ & \text{communicating with TTT,} \\ & \text{assuming B does nothing} \\ 0 & \text{otherwise} \end{cases}$$

- ◆ Look at *optimistic* transition  $s \rightarrow s'$  where  $\text{Power}_B(s') = 1 > \text{Power}_B(s) = 0$ .

# Advantage

(intuition for main argument)

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- ◆ If  $\text{Power}_B(s) = 0 \rightarrow \text{Power}_B(s') = 1$  then
  - This is result of some move by A
    - $\text{Power}_B(s) = 0$  means B cannot get contract without B's help
  - The move by A is not a message to TTP
    - The proof is for an *optimistic* protocol, so we are thinking about a run without msg to T
  - B could abort in state  $s$ 
    - We assume protocol is timely and fair: B must be able to do something, cannot get contract
  - B can still abort in  $s'$ , so B has advantage!

# Conclusions

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- ◆ Online contract signing is subtle
  - Fair
  - Abuse-free
  - Accountability
- ◆ Several interdependent subprotocols
  - Many cases and interleavings
- ◆ Finite-state tools great for case analysis!
  - Find bugs in protocols proved correct
- ◆ Proving properties of all protocols is harder
  - Understand what is possible and what is not