Lecture 9 Textual Data: Vector Space Model and TF-IDF

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Textual Data



- 1 "Hello darkness, my old friend." Simon & Garfunkel
 - "Returning hate for hate multiplies hate, adding deeper darkness to a night already devoid of stars. Darkness cannot drive out darkness; only light can do that." –MLK

	darkness	hate	
0	2	1	
1	1	0	
2	3	3	

Which document is most similar to document O?



Using Euclidean distance, document l appears closer than document 2!









In the **vector space model**, documents are represented as *vectors* instead of points.



The **length of a vector** is its distance from the origin **0**:

$$||\mathbf{v}|| = \sqrt{\sum_{j=1}^{|V|} v_j^2}.$$

The distance between two vectors corresponds to the angle between them:

$$d(\mathbf{x}, \mathbf{x}') = 1 - \cos \theta = 1 - \frac{\sum_{j=1}^{|V|} x_j x'_j}{||\mathbf{x}|| \, ||\mathbf{x}'||}.$$

Using cosine distance, document 2 now appears closer

Implementing the Vector Space Model

```
documents = [
    "whoever has hate for his brother is in the darkness and walks in the dark.
    "hello darkness my old friend",
    "returning hate for hate multiplies hate adding deeper darkness to a night
]
```

First, we use Pandas to get the term-frequency matrix.

```
import pandas as pd
from collections import Counter

tf = pd.DataFrame(
    [Counter(doc.split()) for doc in documents],
).fillna(0)
```

tf

	whoever	has	hate	for	 light	can	do	that
0	1.0	1.0	1.0	1.0	 0.0	0.0	0.0	0.0
1	0.0	0.0	0.0	0.0	 0.0	0.0	0.0	0.0
2	0.0	0.0	3.0	1.0	 1.0	1.0	1.0	1.0

3 rows × 35 columns

Now we just have to implement the formula for cosine distance.

Implementing the Vector Space Model

 whoever
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 ...
 light
 can
 do
 that

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Now we just have to implement the formula for cosine distance.

$$d(\mathbf{x}, \mathbf{x}') = 1 - \frac{\sum_{j=1}^{|V|} x_j x'_j}{||\mathbf{x}|| \, ||\mathbf{x}'||}.$$

```
import numpy as np
def length(v):
    return np.sqrt((v ** 2).sum())
def cos_dist(v, w):
    return 1 - (v * w).sum() / (length(v) * length(w))
cos_dist(tf.loc[0], tf.loc[1]), cos_dist(tf.loc[0], tf.loc[2])
(0.8048199854102933, 0.6460038372976056)
```

Vector Space Model in Scikit-Learn

It's always easier to do it in Scikit-Learn.

from sklearn.feature_extraction.text import CountVectorizer

```
vec = CountVectorizer(token_pattern=r"\w+")
vec.fit(documents)
tf_matrix = vec.transform(documents)
tf_matrix.todense()
```

```
matrix([[0, 0, 0, 1, 1, 1, 0, 0, 2, 0, 0, 0, 0, 0, 1, 0, 1, 1, 0, 1, 2, 1, 0,
        0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 2, 0, 1, 1],
        [0, 0, 0, 0, 0, 0, 0, 1, 0, 0, 0, 0, 1, 0, 0, 1, 0, 0, 0, 0,
        0, 1, 0, 0, 1, 0, 0, 0, 0, 0, 0, 0, 1, 0, 0, 1, 0, 0, 0, 0,
        0, 1, 1, 0, 0, 1, 1, 3, 1, 1, 1, 1, 0, 0, 3, 0, 0, 0, 0, 1,
        1, 0, 1, 1, 0, 1, 1, 1, 1, 0, 1, 0, 0]])
```

array([[0. , 0.80481999, 0.64600384]])









tf-idf

So far, we've simply counted the **term frequency** tf(d, t): how many times each term t appears in each document d.

<u>Problem:</u> Common words like "is" or "the" tend to dominate because they have high counts.

We need to adjust for how common each word is:

1. Count the fraction of documents the term appears in:

$$df(t, D) = \frac{\# \text{ documents containing term } t}{\# \text{ documents}} = \frac{|\{d \in D : t \in d\}|}{|D|}$$

2. Invert and take a log to obtain **inverse document frequency**:

$$\operatorname{idf}(t, D) = 1 + \log \frac{1}{\operatorname{df}(t, D)}.$$

3. Multiply tf by idf to get tf-idf:

$$tf\text{-}idf(d, t, D) = tf(d, t) \cdot idf(t, D).$$

Now we can use the **tf-idf matrix** just like we used the term-frequency matrix.



tf-idf by Hand

The term-frequency matrix for this corpus is:

- "Whoever has hate for his brother is in the darkness and walks in the darkness."
- 1 "Hello darkness, my old friend."
- 2 "Returning hate for hate multiplies hate, adding deeper darkness to a night already devoid of stars. Darkness cannot drive out darkness; only light can do that."

Now let's calculate the tf-idf matrix!

1. Calculate the document frequencies:

$$\mathrm{df}(\mathrm{``darkness"},D) = \frac{3}{3} = 1 \qquad \qquad \mathrm{df}(\mathrm{``hate"},D) = \frac{2}{3}$$

2. Calculate the inverse document frequencies:

$$\operatorname{idf}(\operatorname{``darkness''}, D) = 1 + \log 1 = 1 \quad \operatorname{idf}(\operatorname{``hate''}, D) = 1 + \log \frac{3}{2} \approx$$

3. Multiply tf by idf to get tf-idf:

	darkness	hate	
0	2	1	
1	1	0	
2	3	3	

0

1.176

	1		2	
	darkness	hate	•••	
0	2	1.176		
1	1	0		
2	3	3.528		

tf-idf in Scikit-Learn

```
from sklearn.feature_extraction.text import TfidfVectorizer
# The options ensure that the numbers match our example above.
vec = TfidfVectorizer(smooth_idf=False, norm=None)
vec.fit(documents)
tfidf_matrix = vec.transform(documents)
```

Now we can use this tf-idf matrix just as we used the term frequency matrix!

array([[0. , 0.94612045, 0.84453506]])



Dr. Seuss Example

Let's go into Colab and find the Dr. Seuss book that is most similar to One Fish, Two Fish, Red Fish, Blue Fish.



