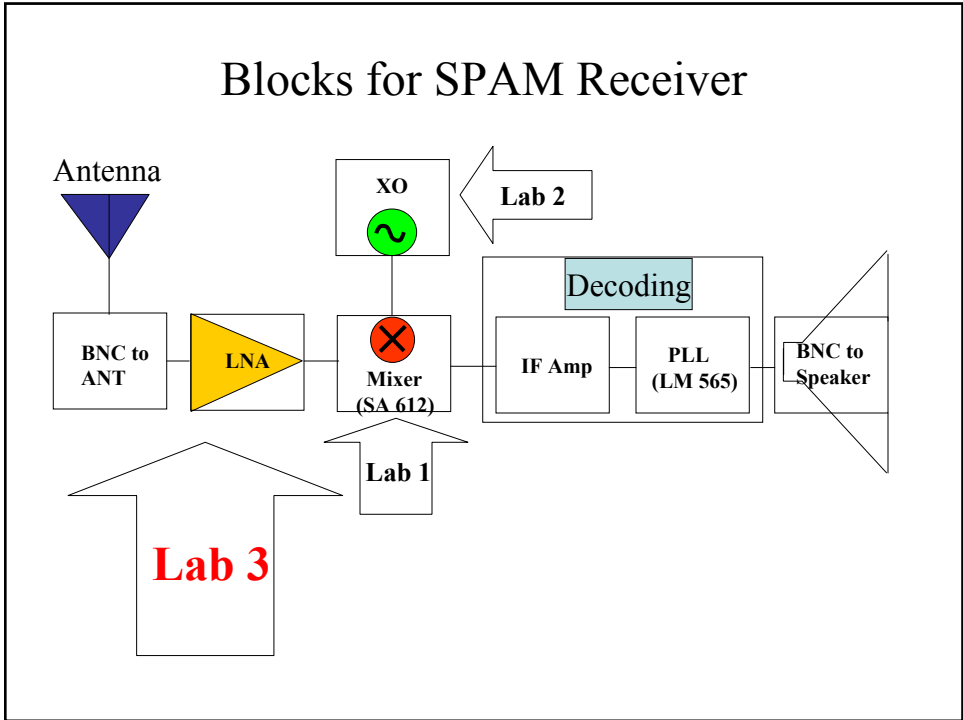
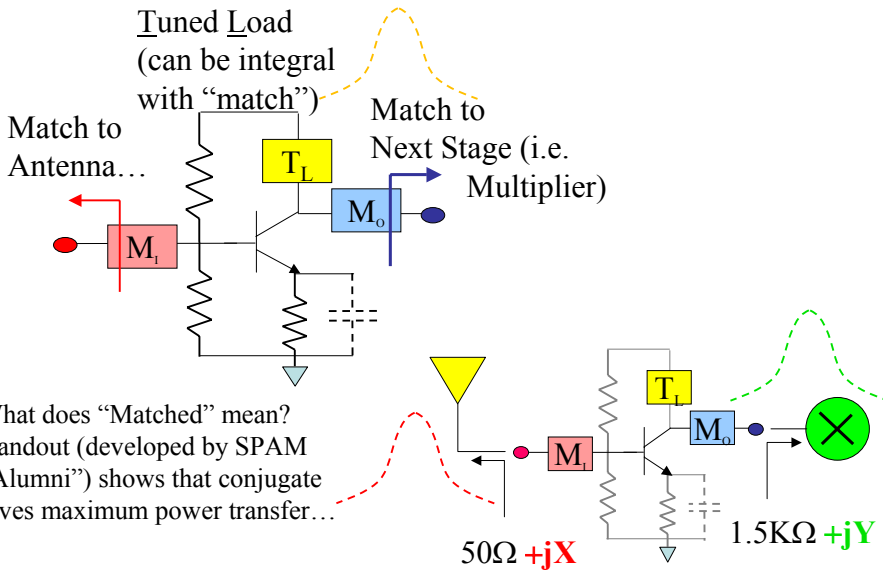


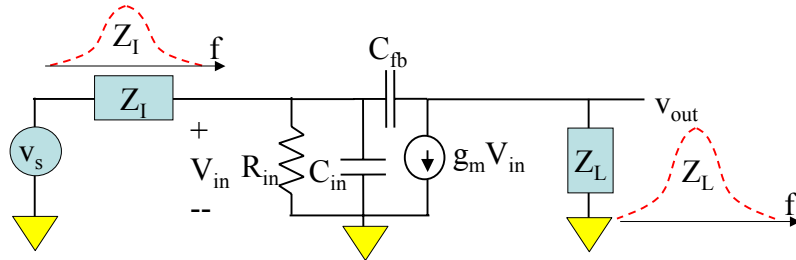
Blocks for SPAM Receiver



RF Amplifier from Antenna (and "LNA")



Small-Signal View of Amplifier



At low frequencies (neglecting resonance effects) :

V_{in} = voltage divider (at R_{in})

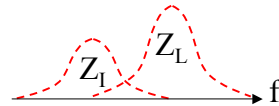
$$V_{out} = -g_m V_{in} R_L$$

Look Ahead:

If ω_0 for two $Z(\omega)$ are NOT the same... problems

At high frequencies:

We need to consider both $Z(\omega)$'s and C 's...



Reminders about ac Parameters

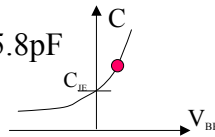
For $I_C=5\text{mA}$, $\beta=80$, $\tau_F=30\text{ps}$ (and other parameters per SPICE deck)

$$g_m = qI_C/kT = 0.193 \text{ and } r_\pi = \beta/g_m = 414\Omega$$

$$C_\pi = C_{JE}(V_{BE}) + g_m \tau_F$$

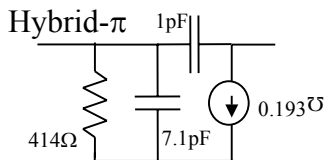
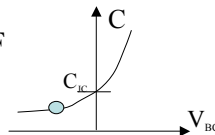
$$= 1.3\text{pF } f(V_{BE}) + 5.8\text{pF}$$

$$\sim 7.1\text{pF}$$

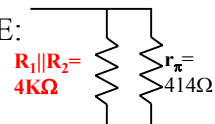


Parameter	Value
β	80
τ_F	30ps
C_{JE}	1.3pF
C_{JC}	1.0pF

$$C_\mu = C_{JC}(V_{BC}) \sim C_{JC} = 1\text{pF}$$

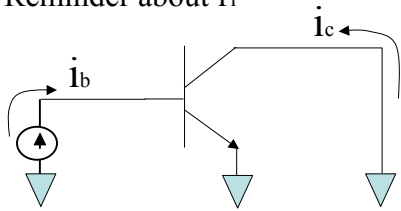


$R_{in} \sim 200\Omega$ for CE:



A quick comment about f_T

Reminder about f_T



$$\frac{i_c(s)}{i_b(s)} = \beta(s)$$

$$\text{at } \omega_T \dots \beta(s) = 1$$

(a review from EE113 notes...)

$$\beta(s) = \frac{\beta}{1 + s r_{\pi} (C_{\pi} + C_{\mu})} \ll 1/2\pi f_{3dB}$$

$$\omega_T = \frac{g_m}{C_{\pi} + C_{\mu}} = 2\pi f_T$$

(from data sheet)

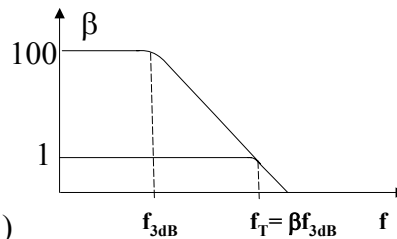
$$\text{@20mA } g_m = 0.772$$

$$C_{\pi} + C_{\mu} = (0.772) / (2\pi \cdot 5 \times 10^9) \quad \leftarrow \text{(I.e. } f_T)$$

$$= 24.6 \text{ pF}$$

$$C_{\pi} + C_{\mu} = C_{JE} + C_{JC} + g_m \tau_F$$

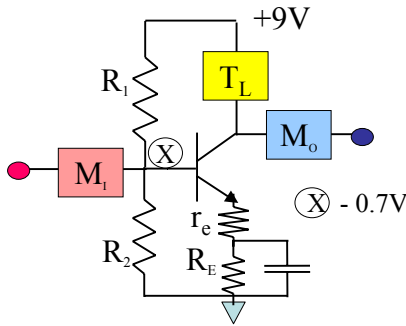
(now check out the SPICE deck...)



About Today's Lecture:

- More on Feedback (**HO#11**)
(including example with r_e)
- Smith Chart (**HO#10 + #12**)
- Examples on Matching (**HO#10**)
 - ✓ (Radmanesh examples...HO#8!!)
 - ✓ Last Year's MT... (no HO#... solutions in another week)

A Simple (Practice) Biasing Example



Assume $I_C = 5\text{mA}$
 $I_{R1} = I_{R2} = 0.5\text{mA}$ (a bit big but...)
 and $V_{BE} = 0.7\text{V}$

$9\text{V} / (R_1 + R_2) = 0.5\text{mA}$
 thus $R_1 + R_2 = 18\text{K}\Omega$
 and given $V_{BE} = 0.7\text{V}$

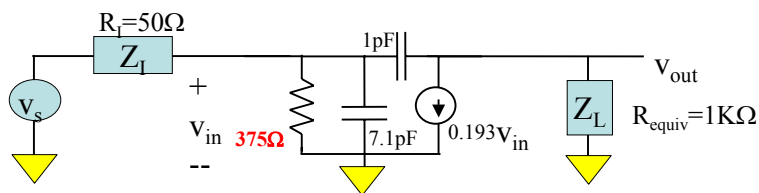
$R_2 = 6\text{K}\Omega$, $R_1 = 12\text{K}\Omega$
 $R_1 || R_2 = 4\text{K}\Omega$

Turning to the I_C biasing
 $(3\text{V} - 0.7\text{V}) / R_E = 5\text{mA}$
 which in turn gives $r_e + R_E = 460\Omega$

Note: for “fun” you might think about finding R ’s for **3mA** and **1mA** = I_C

Now, moving on the the small-signal (ac) modeling...
 (we’ll continue to consider the matching issues, per the last few lectures, after we address the basic small-signal issues)

Putting these numbers together...



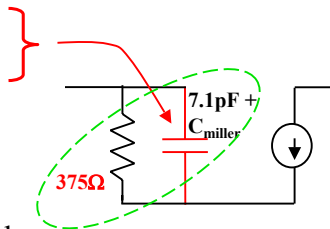
$$g_m R_{\text{equiv}} = 0.193 \times 10^3 = 193$$

$$C_{\text{miller}} = C_{\text{fb}} (1 + g_m R_{\text{equiv}}) = 194 \text{pF}$$

$$C_{\text{in}} = 7.1 \text{pF}$$

$$v_{\text{in}} = v_s \cdot 375 / (375 + 50) = 0.88 v_s$$

$$v_{\text{out}} = -(194)(0.88) v_s = -171 v_s$$



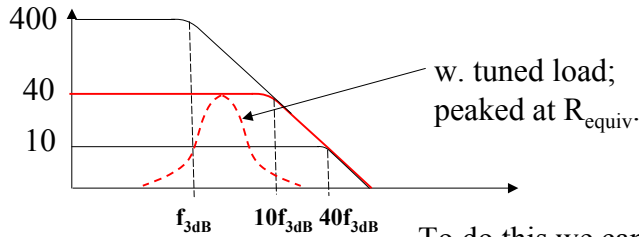
Large voltage gain is not always good...

Bandwidth and Low Noise are key metrics...

$$1/2\pi R_{\text{in}} C_T \sim 2.1 \text{MHz!}$$

How do we get modest gain and BW!

Gain-BandWidth-Product (GBP)...trade-off gain for BW*



Comment about Noise (as in LNA):
Resistor (Thermal or Johnson) Noise--
 $\bar{v}^2=4kT R [BW]$
Reduced BW->less total noise
(more about noise soon...)

To do this we can use

FEEDBACK...**

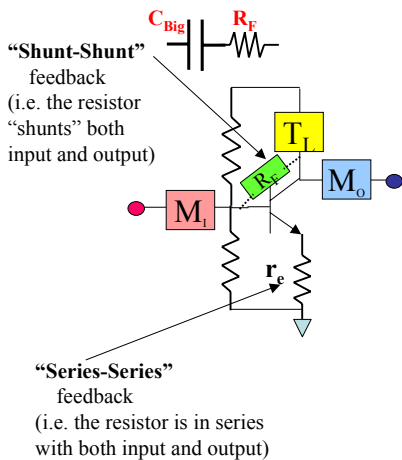
$$A_{cl} = A_{ol} / (1 + A_{ol}f)$$

Where “ol” is “open-loop” and
“cl” is “closed-loop”

* Assumption: Single-pole roll-off

** For the full story...see Brodersen Notes (UCB :)

FB Configurations and “bottom-line” Results-- Gain, Resistances and BW



Gain Expressions:

(extreme limiting cases...see supplemental notes for derivations)

$$A_v(\text{shunt-shunt}) \sim R_F / R_S$$

$$A_v(\text{series-series}) \sim R_L / r_e$$

Impedances (either Output or Input) :

$$\text{Series} \dots R_{in|o-l} [1+T] \dots T = A_{ol}f$$

$$\text{Shunt} \dots R_{in|o-l} / [1+T] \dots (\text{same } T)$$

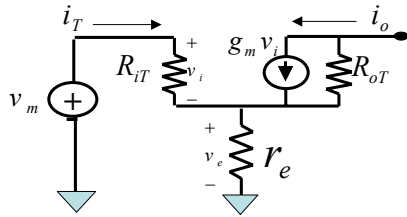
Bandwidth:

$$\omega_{3dB|c-l} = \omega_{3dB|o-l} [1+T]$$

What is T? (“loop gain”)...

(now let's see what this really means!)

Series-Series--Nodal Analysis Results...



Comment: Natural Units are
"transconductance gain" i_o/v_{in}

$$f = v_{fb}/i_o = R_e$$

$$\frac{v_m}{i_T} \approx R_{iT}(1 + g_m r_e)$$

$$i_o = \frac{g_m}{(1 + g_m r_e)} \cdot v_m$$

All three terms are
"scaled" by:

$$(1 + g_m r_e)$$

$$\frac{v_o}{v_m} = \frac{-g_m R_L}{1 + g_m r_e}$$

going to $A_v \dots$

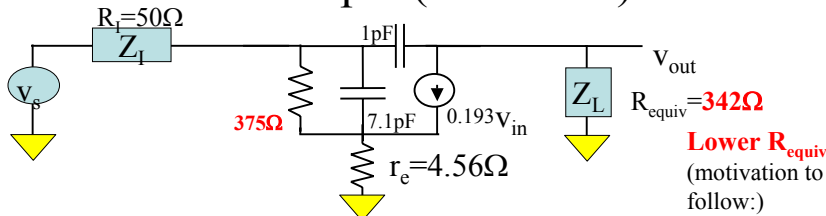
$$\frac{v_{Test}}{i_o} \approx R_{oT}(1 + g_m r_e)$$

$$\approx \frac{-g_m R_L}{g_m r_e} = \frac{-R_L}{r_e}$$

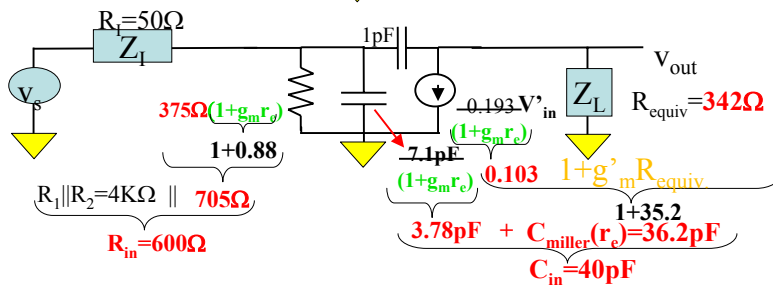
Approximately

(if 1 \ll than the second term in the denominator)

An Example (continued)



Lower R_{equiv}
(motivation to follow:)



$$R_1 || R_2 = 4K\Omega || 705\Omega$$

$$R_{in} = 600\Omega$$

$$375\Omega(1 + g_m r_e)$$

$$1 + 0.88$$

$$7.1pF(1 + g_m r_e)$$

$$0.103$$

$$1 + g_m^2 R_{equiv}$$

$$3.78pF + C_{miller}(r_e) = 36.2pF$$

$$1 + 35.2$$

$$C_{in} = 40pF$$

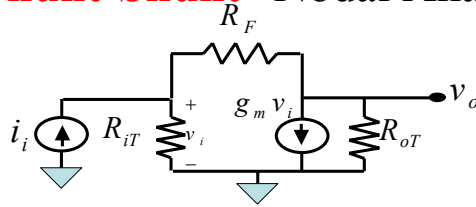


Voltage Gain (w.fb):

$$-35.2$$

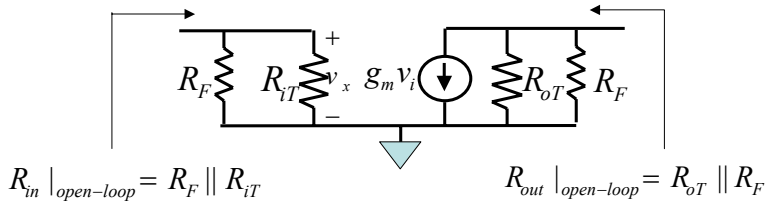
$$(-R_{equiv}/r_e = 75)$$

Shunt-Shunt--Nodal Analysis Results...



Comment: Natural Units are
“transresistance gain” V_o/I_{in}

$$f = i_{fb}/v_o = 1/R_F$$



$$R_{in} |_{open-loop} = R_F \parallel R_{iT}$$

$$R_{out} |_{open-loop} = R_{oT} \parallel R_F$$

Open-loop

$$v_o = -g_m (R_F \parallel R_{iT}) (R_{oT} \parallel R_F) \cdot i_i$$

$$a = v_o/i_i$$

The “closed-loop”
expressions will then be
modified by this expression
for $1+T$

$$1 + T = 1 + \frac{g_m (R_F \parallel R_{oT}) (R_F \parallel R_{iT})}{R_F}$$

$$af = T$$

Gain Expression (Shunt-Shunt)

Closed-loop \rightarrow

$$\frac{v_o}{i_i} = \frac{-g_m (R_F \parallel R_{oT}) (R_{iT} \parallel R_F)}{1 + \frac{g_m \cdot (R_F \parallel R_{oT}) \cdot (R_{iT} \parallel R_F)}{R_F}}$$

$$\frac{v_o}{i_i} \approx -R_F \leftarrow \text{Approximately} \quad (\text{if } 1 \ll \text{the second term in the denominator})$$

$$i_i = \frac{v_s}{R_S}$$

$$\therefore A_v = \frac{v_o}{v_s} = \frac{v_o}{i_i} \frac{1}{R_S}$$

$$A_v \approx \frac{-R_F}{R_S}$$