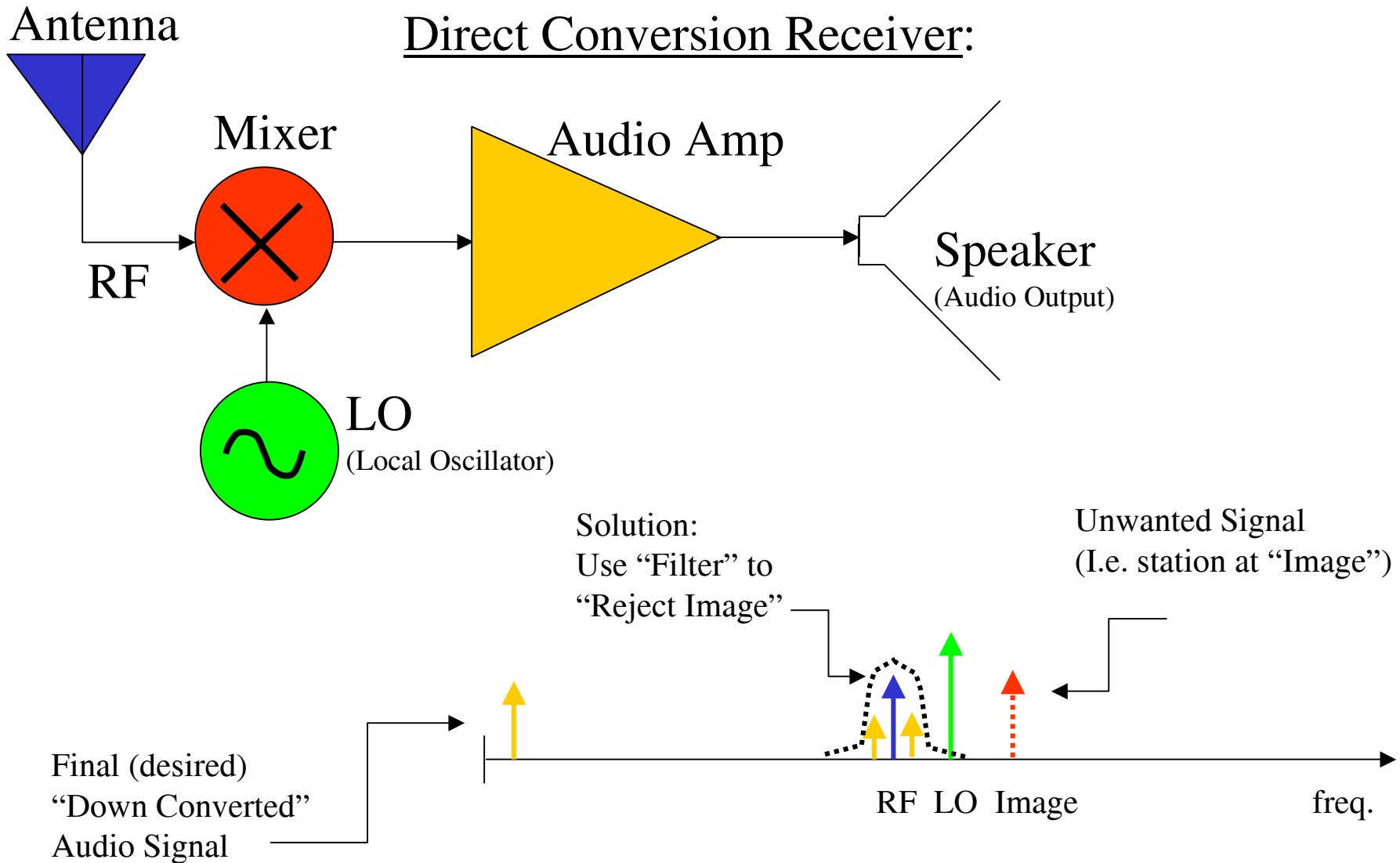
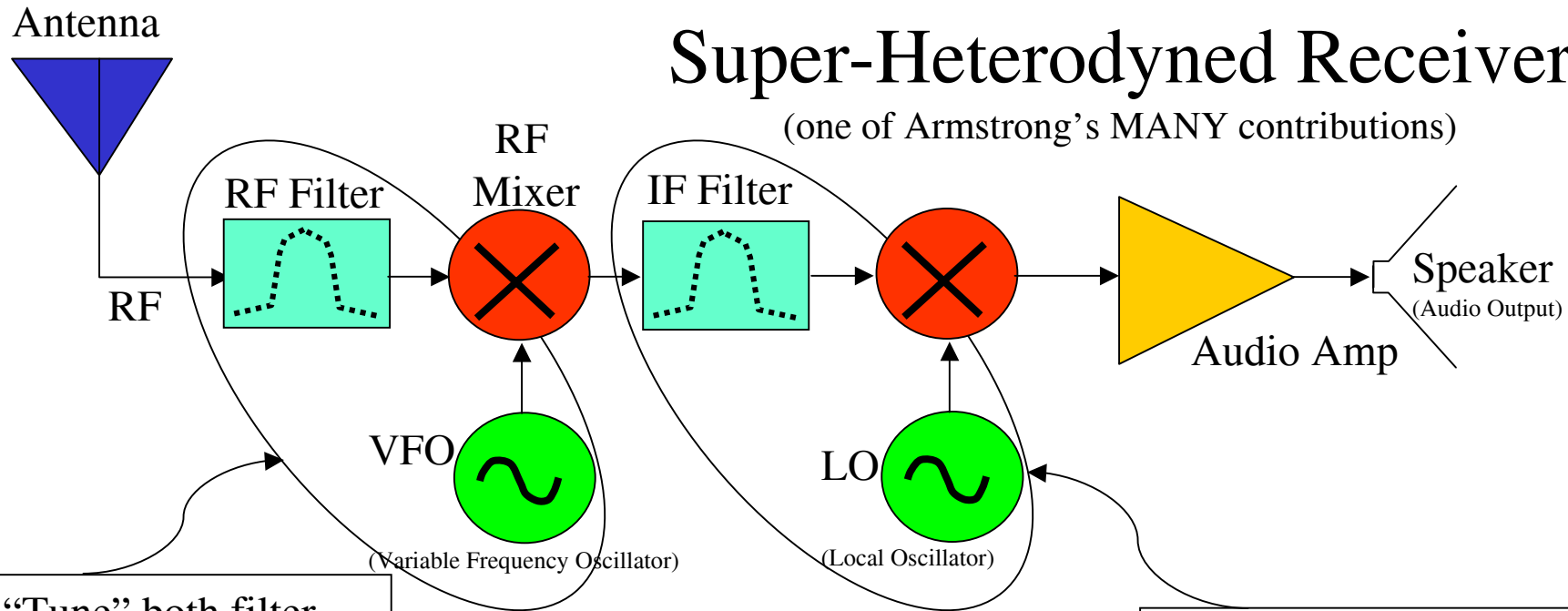


# Brief Preview of RF Systems (and architectures)



# Super-Heterodyned Receiver

(one of Armstrong's MANY contributions)



“Tune” both filter and VFO at the same time...giving output of mixer ALWAYS at **I**ntermediate **F**req.

## **Advantages of Super-Het:**

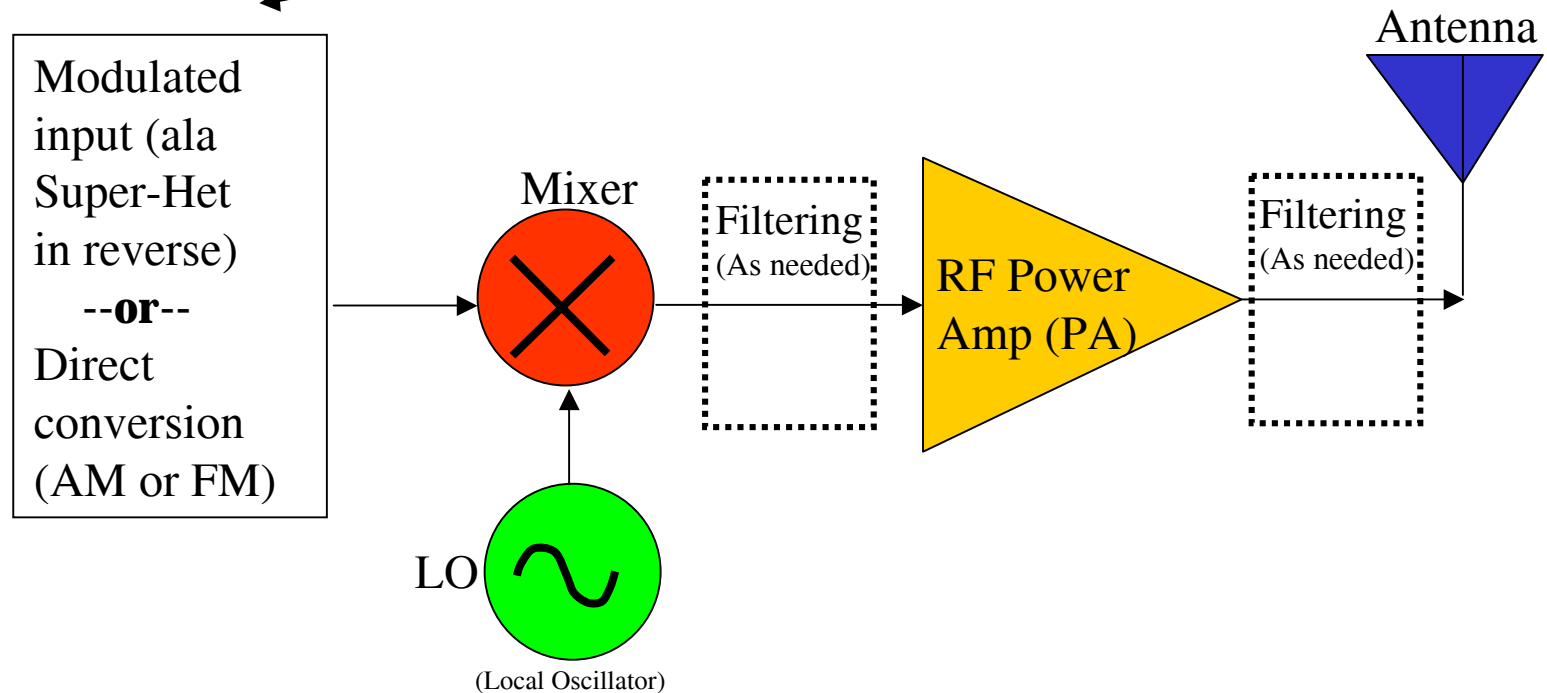
- Tuning/Image Rej. Decoupled from detection
- IF filtering can be optimized and also reused (I.e. both AM and FM bands)
- MUCH easier to work at IF vs. directly at RF (especially at high frequencies)

**IF** at **FIXED** Freq. and therefore LO Freq. is also fixed in taking output of IF down to “basedband”

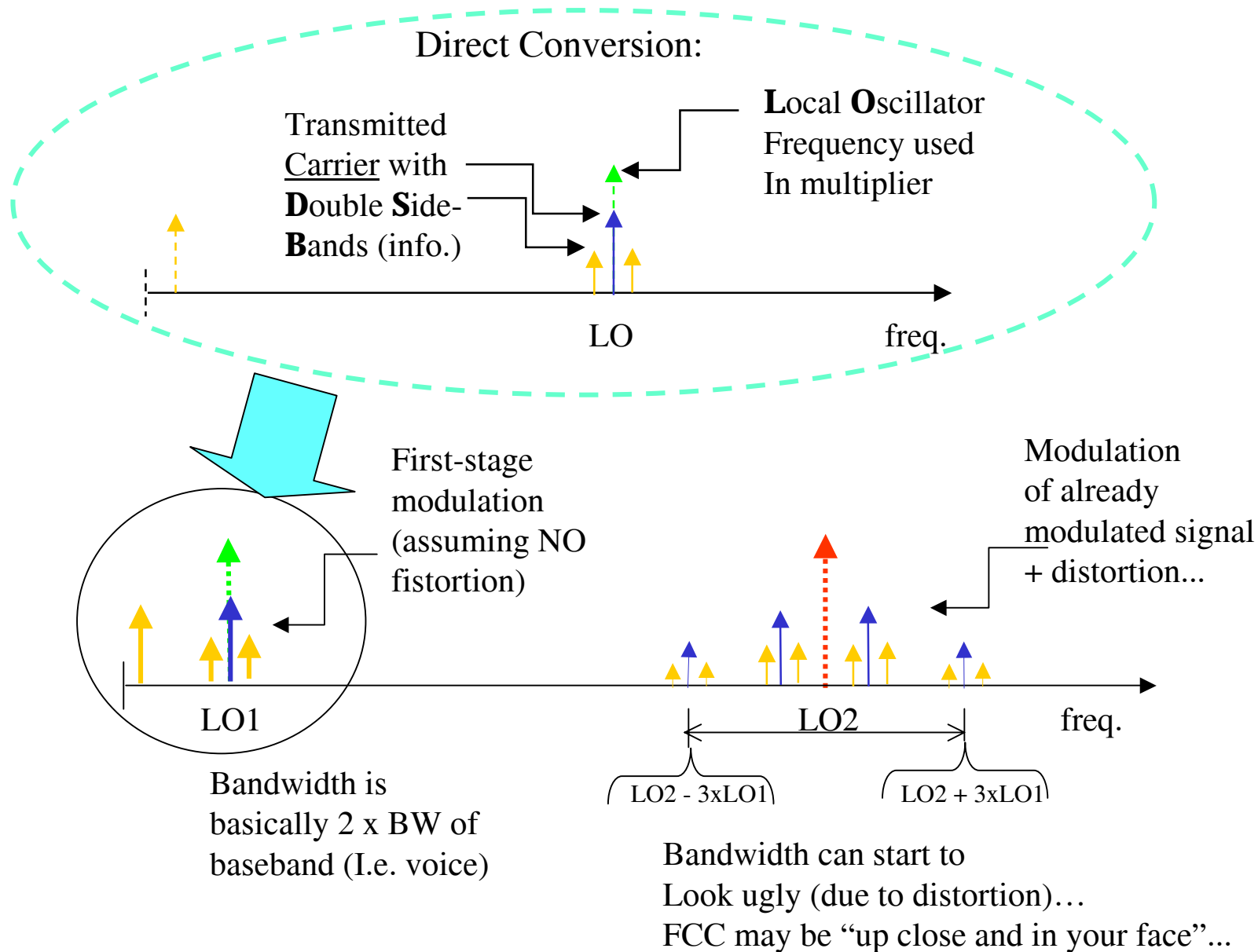
# Transmitter Side Issues...

There are LOTS of choices and combinations here:

- Baseband-up-to-10's MHz can be done with DSP!
- AM is really easy (it's below 2MHz anyway)
- FM is also easy...BUT, frequency stability is not (so easy)
- Impedance matching and filtering at RF poses challenges as well...



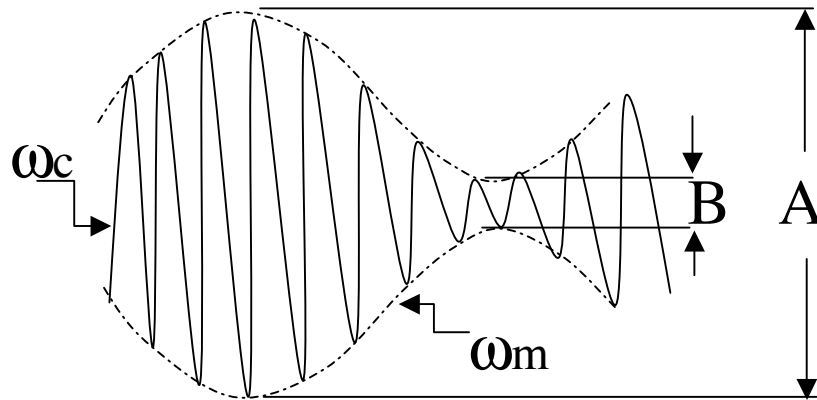
# A Quick Look at BW...(including preview of FCC perspective)



# Amplitude Modulation (AM) & Circuits

## AM Modulation

$$v(t) = \underbrace{v_c (1 + m \cos \omega_m t)}_{v_c + v_m \cos(\underbrace{2\pi f_m t}_{\omega_m})} \cos \underbrace{2\pi f_c t}_{\omega_c}$$

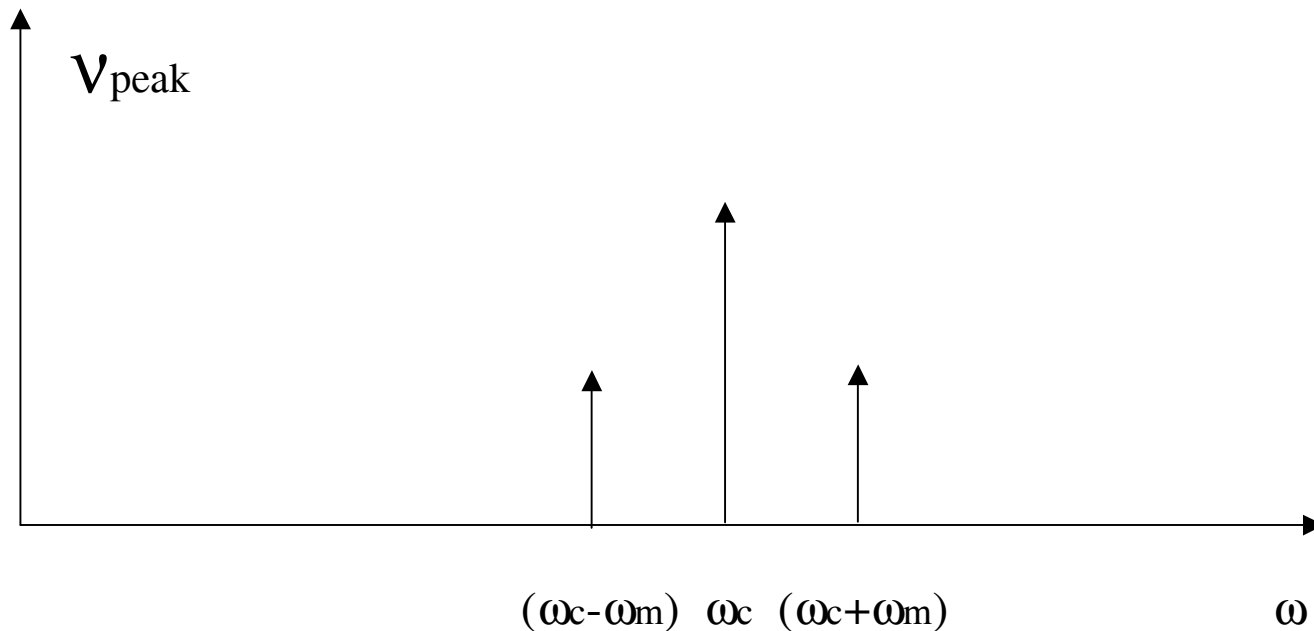


$$m \equiv \frac{V_m}{V_c} = \frac{A - B}{A + B}$$

$$v(t) = v_c \cos \omega_c t + v_m \cos \omega_m t \cdot \cos \omega_c t$$

Using Law of Cosines

$$v(t) = v_c \cos \omega_c t + \frac{v_m}{2} \cos(\omega_c - \omega_m)t + \frac{v_m}{2} \cos(\omega_c + \omega_m)t$$



This is the ideal situation...

How do we get modulation in reality and what are limitations?

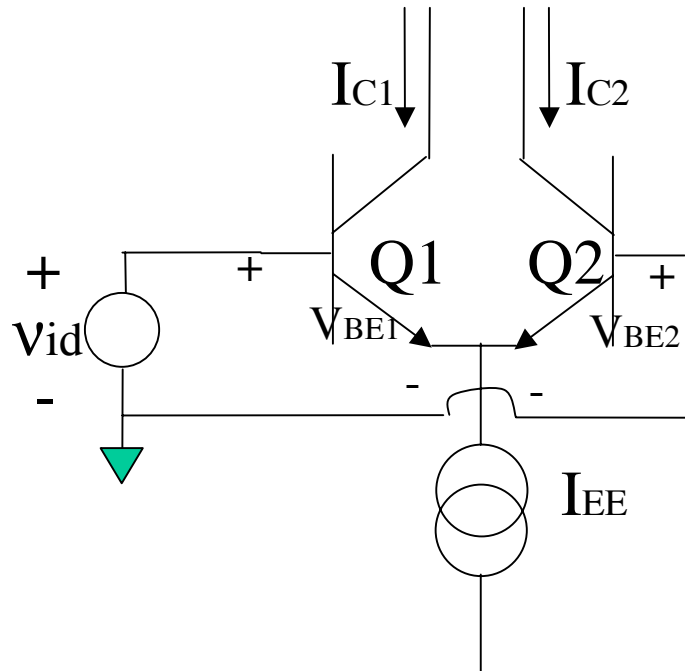
Circuits to realize AM:

A few simple cautions (about AM) ---

- a)  $m \leq 1$  otherwise information is lost
- b) law of Cosine => ideal multiplication...
- c) lets start here from circuits point of view

For high frequencies and at impedance levels often used, differential circuits with matched impedance lines are very convenient...

Hence, lets revisit the Emitter Coupled Pair (ECP) from 113



Basic BJT "Laws":

$$I_c = I_s e^{V_{BE}/V_T}$$

$$V_T = kT/q$$

$$V_{BE} = \frac{kT}{q} \ln(I_c/I_s)$$

$$I_{c1} = I_s e^{V_{BE1}/V_T}; \quad I_{c2} = I_s e^{V_{BE2}/V_T}$$

$$v_{id} = V_{BE1} - V_{BE2} = V_T \ln\left(\frac{I_{c1}}{I_s}\right) - V_T \ln\left(\frac{I_{c2}}{I_s}\right)$$

$$= V_T \ln\left(\frac{I_{c1}}{I_{c2}}\right)$$

$$I_{c1} = I_{c2} e^{(v_{id}/V_T)} \quad \text{or} \quad I_{c2} = I_{c1} e^{(-v_{id}/V_T)}$$

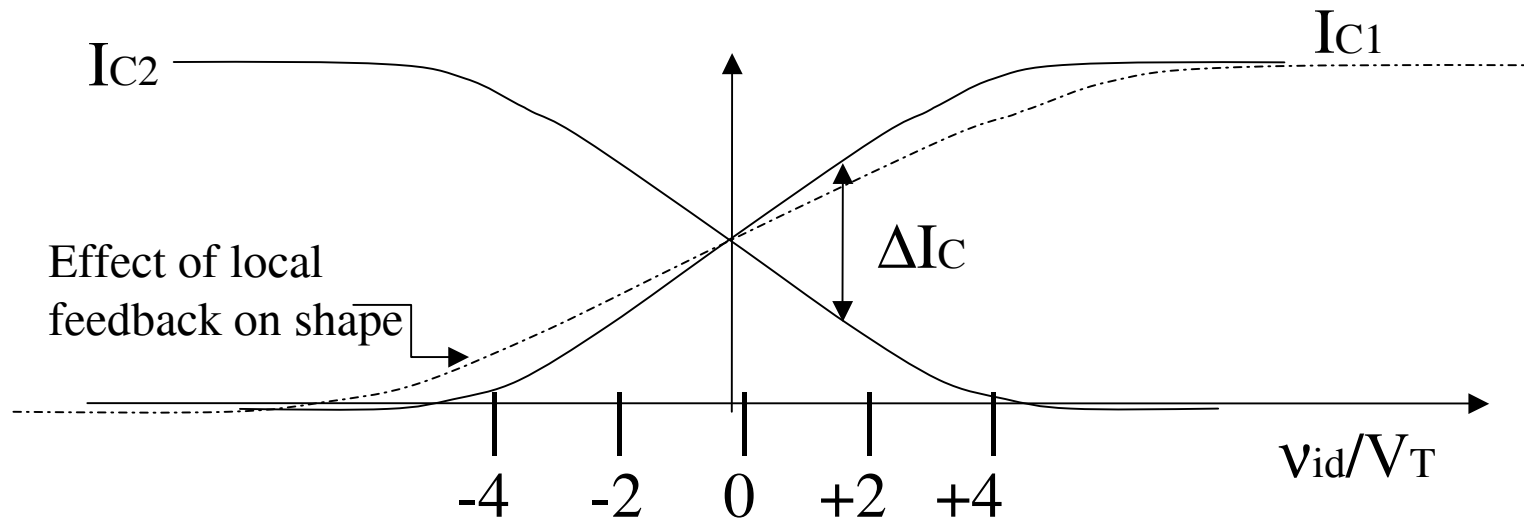
$$I_{c1} + I_{c2} = I_{EE}$$

Now, for a bit of hacking to get the transfer function.

$$I_{c1} = I_{EE} - I_{c2} = \frac{I_{EE}}{1 + e^{-vid/V_T}}$$

$$I_{c2} = I_{EE} - I_{c1} = \frac{I_{EE}}{1 + e^{+vid/V_T}}$$

$$\begin{aligned} \Delta I_c &= I_{c1} - I_{c2} = I_{EE} \left( \frac{1}{1 + e^{-vid/V_T}} - \frac{1}{1 + e^{+vid/V_T}} \right) \\ &= I_{EE} \tanh \left( \frac{vid}{2V_T} \right) \end{aligned}$$



Comments: a) Hyperbolic Tan function gives symmetry about  $v_{id}=0$ , b) "linear" for about  $1V_T$  (then "distortion" as we'll discuss below), c) local feedback can stretch linearity if desired.

### Small Signal Regime

$$\tanh \frac{v_{id}}{2V_T} \approx \frac{v_{id}}{2V_T}$$

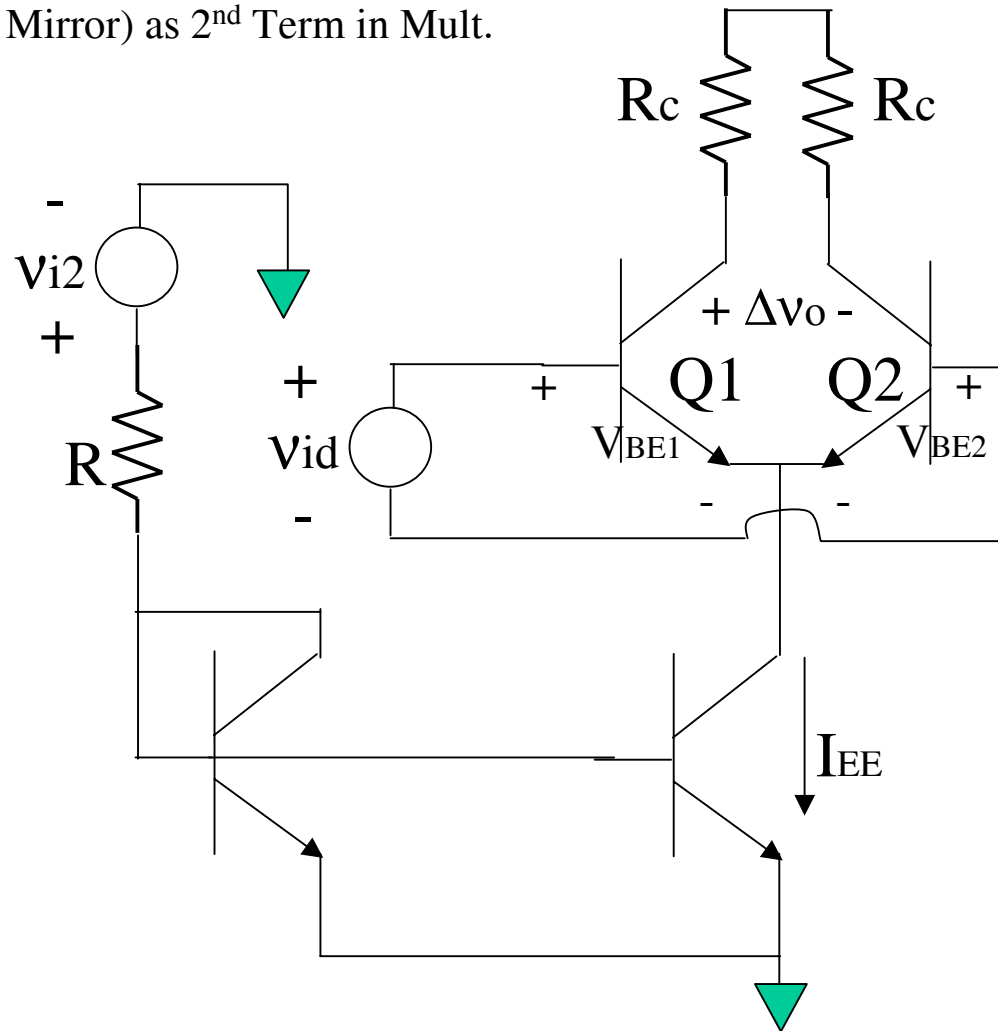
$$\Delta I_c \approx I_{EE} \frac{v_{id}}{2V_T} \quad \text{and} \quad I_{c1} = I_{c2} = \frac{I_{EE}}{2} = I_c$$

$$g_m \equiv \frac{I_c}{V_T}$$

$$\text{then} \quad \Delta I_{c1} = g_m v_{id}$$

But, let's not stop here... (i.e. what we've done in 113)

$I_{EE}$  (Via Current Mirror) as 2<sup>nd</sup> Term in Mult.



$$I_{EE} = \frac{v_{i2} - V_{BE}}{R} \quad \text{assume} \quad v_{i2} = v_{i2}(dc) + v_{i2}(ac)$$

$$= \frac{v_{i2}(dc) - V_{BE}}{R} + \frac{v_{i2}(ac)}{R} \cos(\omega_m t)$$

$$I_{EE} = \frac{v_c}{R} + \frac{v_m}{R} \cos(\omega_m t) \quad \text{where } v_c \equiv v_{i2}(dc) - V_{BE}$$

$$v_m \equiv v_{i2}(ac)$$

Now, using this expression for  $I_{EE}$  back in  $\Delta I_c$  expression

$$\Delta I_c = I_{EE} \tanh\left(\frac{v_{id}}{2V_T}\right) = \frac{1}{R} (v_c + v_m \cos \omega_m t) \tanh\left(\frac{v_{id}}{2V_T}\right)$$

Adding  $R_c$ 's (see above figure) and looking at  $\Delta v_o$

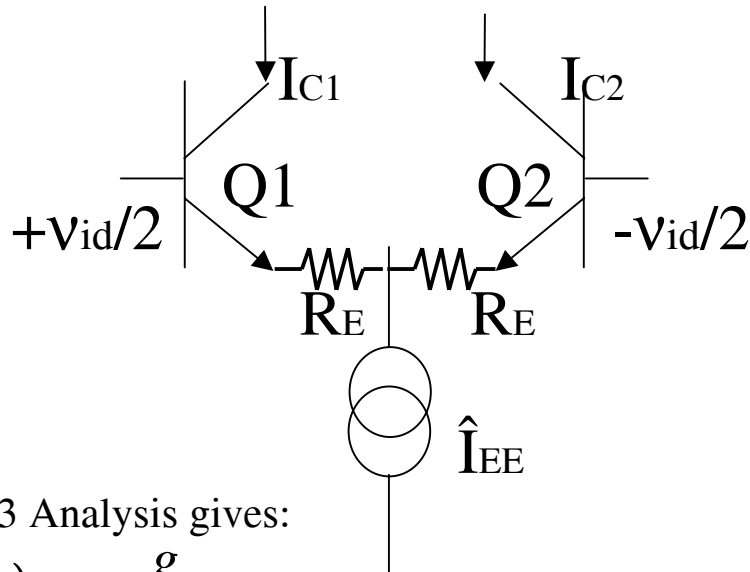
$$\Delta v_o = -\Delta I_c R_c = -\frac{R_c}{R} (v_c + v_m \cos \omega_m t) \tanh\left(\frac{v_{id}}{2V_T}\right)$$

Again, using small signal regime ( $v_{id} \ll V_T$ )

$$\Delta v_o = \frac{-R_c}{2V_T R} (v_c + v_m \cos \omega_m t) (\bar{v}_{id} \cos \omega_c t)$$

$$\text{note : } v_{id} \equiv \bar{v}_{id} \cos \omega_c t$$

Although tanh formulation was used, with small signal approx. ( $v_{id} \ll V_T$ ), one can slightly improve dynamic range by local feed back with  $R_E$ 's on the diff pair.



Limitation:

Basic EE113 Analysis gives:

$$g_m(\text{eff}) = \frac{g_m}{1 + g_m R_E}$$

If  $g_m R_E \gg 1$ , then :

$$g_m(\text{eff}) \approx \frac{1}{R_E}$$

$$\therefore \Delta I_{c1} \approx \frac{v_{id}}{R_E} \quad \Delta I_{c2} \approx -\frac{v_{id}}{R_E}$$

$$\Delta I_c = \Delta I_{c1} - \Delta I_{c2} \approx \frac{v_{id}}{R_E}$$

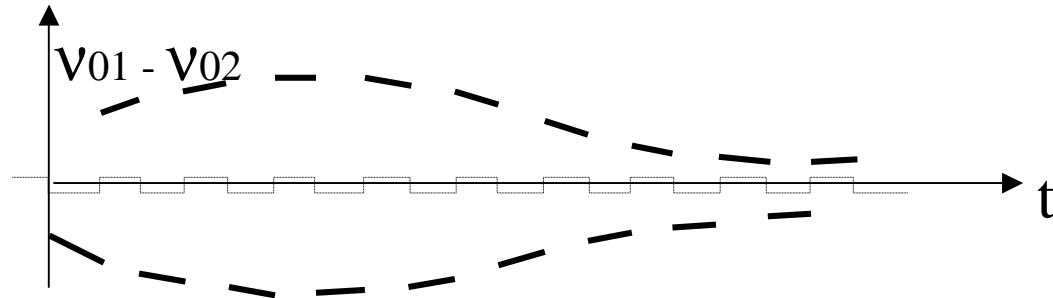
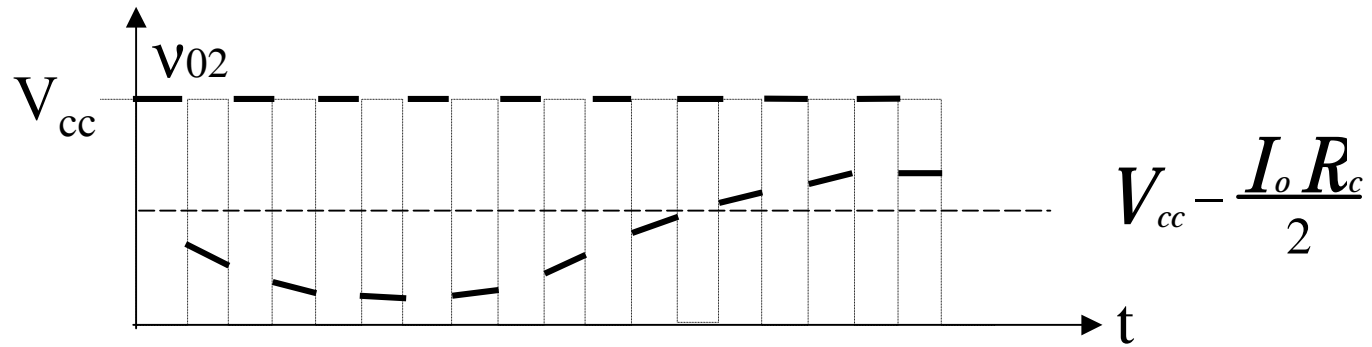
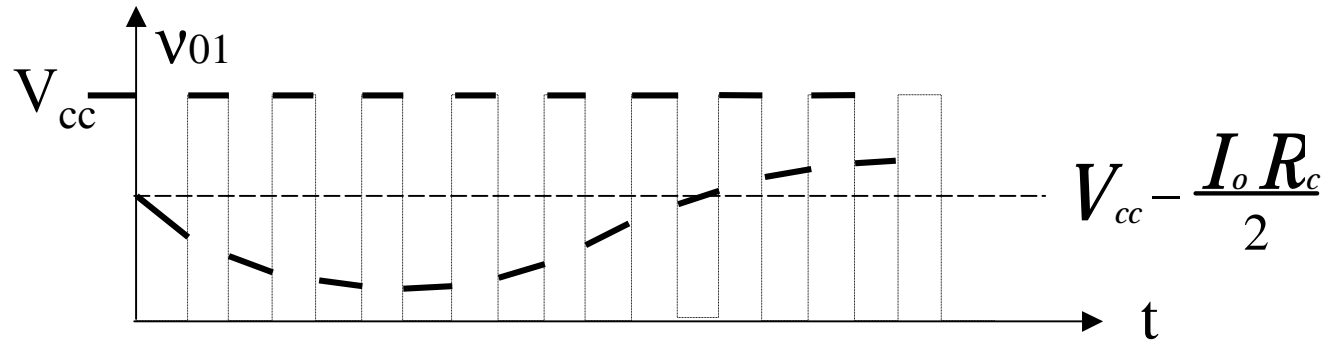
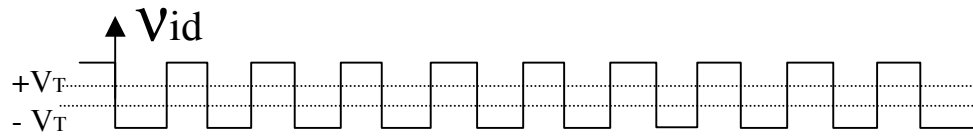
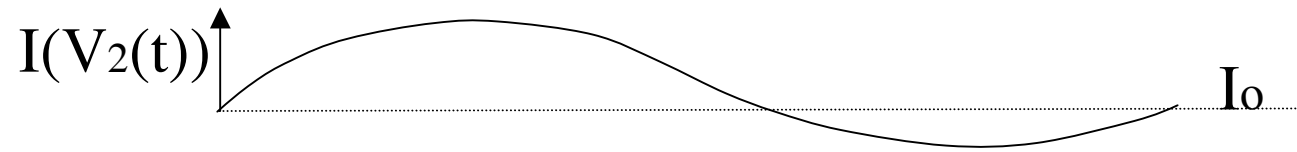
But! There's no  $I_{EE}$  left (ala  $g_m = I_{EE}/(2V_T)$ ) and hence multiplication is gone which is not what we wanted. Hence,  $gmR_E \approx 1$  could increase dynamic range but not kill mult.

Looking at the other extreme, where  $v_{id}$  drives  $Q_1$  and  $Q_2$  into a "switching mode" behavior, we find that a quite acceptable "modulated" signal is realized. Consider voltage waveforms, rather than  $\Delta I_c$ :

$$v_{o1} = V_{cc} - I_{c1}(t)R_c$$

$$v_{o2} = V_{cc} - I_{c2}(t)R_c$$

The following set of figures show how the "tail current"  $I(V_2(t))$  gets switched between collectors C1 and C2 which gave the step-wise jumps downward for  $V_{cc}$





Assume that all  $V_{BE}$ 's for biasing are the same and given the following input to the current amplifier (mirror):

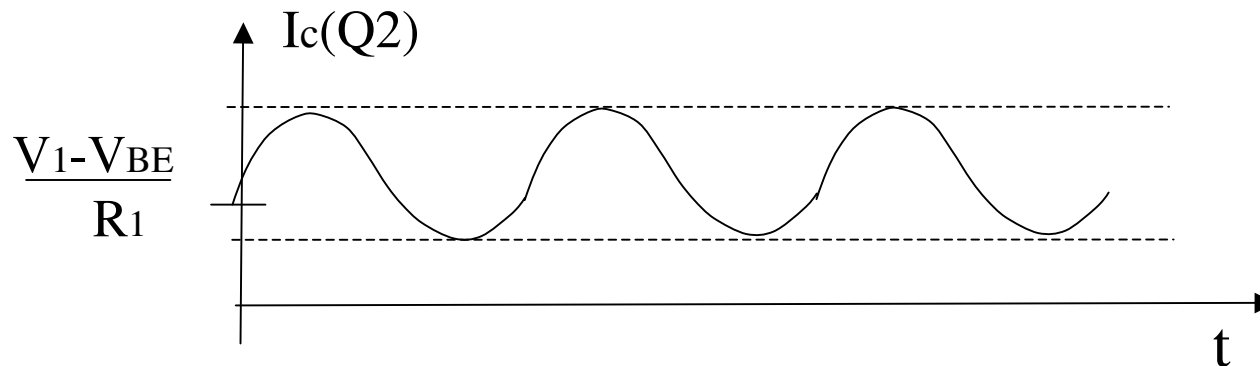
$$V_{s1} = V_1 + \frac{V_1}{2} \sin \omega_1 t$$

(Q) Write an expression for  $I_c(Q2)$  and sketch its value as a function of time.

$$I_c(Q1) = \frac{V_{s1} - V_{BE}}{R_1}$$

Current mirror gives  $I_c(Q1) = I_c(Q2)$

$$I_c(Q2) = \frac{V_1 - V_{BE}}{R_1} + \frac{V_1 - V_{BE}}{2R_1} \sin \omega_1 t$$



(Q) Initially assuming that  $V_{s2} = 0$  (inputs grounded), find the dc and ac signals at  $V_{o1}$  and  $V_{o2}$ .

$$I_c(Q3) = I_c(Q4) = \frac{\alpha I_c(Q2)}{2}$$

$$V_{o1} = V_{o2} = V_{cc} - \frac{\alpha I_c(Q2) R_c}{2}$$

$$= \underbrace{V_{cc} - \frac{\alpha R_c}{2R_1} (V_1 - V_{BE})}_{dc} - \underbrace{\frac{\alpha R_c}{4R_1} (V_1 - V_{BE}) \sin \omega_1 t}_{ac}$$

(Q) Now apply the following small signal input to the differential pair:

$$V_{s2} = V_2 \sin \omega_2 t$$

Write an expression for the ac signal  $V_{o1}$ . HINT: Since the bias current is not constant, instead of using a constant  $g_m$ , use

$$g_m = \frac{kT}{q} I_c(t)$$

$$v_{o1} = -\frac{gmR_c}{2} v_{s2}$$

$$= -\frac{kT}{2q} R_c \left[ \underbrace{\frac{\alpha(V_1 - V_{BE})}{2R_1}}_{I_{c3}} + \underbrace{\frac{\alpha(V_1 - V_{BE})}{4R_1}}_{I_{c3/2}} \sin \omega_1 t \right] V_2 \sin \omega_2 t$$

$$V_{o1} = \frac{-kT}{2q} I_{c3} R_c \left[ 1 + \frac{1}{2} \sin \omega_1 t \right] v_2 \sin \omega_2 t$$

Assuming  $\omega_2 = \frac{\omega_1}{10}$  sketch the Fourier Spectrum and suggest what such a circuit might be useful for. (this is for you to do now...)