Problem 1 - Convolution of simple shapes.

Create two copies of an image that consists of a white square in a black background as:

![Black background with a white square](image_url)

Convolve these two images using the matlab time-domain convolution function conv2, with the shape parameter set to 'same'.

a.) Time the execution interval using matlab commands tic and toc. Display and submit the output image. Plot cuts through the image along one axis and also along a 45 degree angle through the origin.

b.) Derive the convolution of two equal-size squares analytically, and compare your result to the numerical values you have determined.

Problem 2 - Convolution with the Convolution Theorem.

Using the same image as in problem 1, convolve using fft's and the convolution theorem. Time the result again and compare with the result from problem 1.

You will have to be careful with your fftshift operations at the end, as ffts reference the origin to the upper left hand corner, while conv2 uses an origin in the center.

Problem 3 - Convolution end effects.

Create two images of white on black squares with the following parameters:
a) Calculate the convolution of image A with image B using conv2. What happens to the points that fall off the end of the 256 by 256 array?

b) Repeat with fft techniques. Now what is the fate of the off the end points?

Problem 4 - Autocorrelation of a circular disk.

Calculate the autocorrelation (that is, the correlation of a function with itself) of a circular disk. Use a disk of radius 32 in the center of a 512 by 512 array of zeroes. Display and submit. Also submit a plot through the peak on the function.

Problem 5 - Where, o where has my dog gone?

Copy the files lab6prob5data and lab6prob5dog to your disk area from the class web area. Display the image in lab6prob5data, it is a byte image 512 by 512 points. There are some dogs hiding in the image, one of which is reproduced in lab6prob5dog, which is a 64 by 64 image.

How many copies of the dog can you see using your eye directly?

Now use correlation techniques to locate dogs in the larger picture. Note: you will need to make the reference dog a zero mean image to achieve the highest performance. Identify dogs with correlation peaks in the resulting image. Which ones are easiest to recognize? What is it about the background that leads to the best correlation peaks?