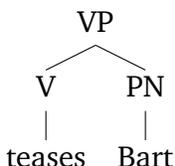


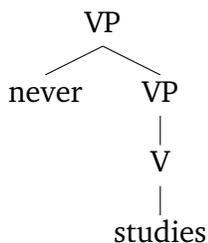
3 Compositional analysis

For each of the top (root) nodes in the following trees, provide (i) the name of the rule you used to derive that meaning from its constituent parts, according to the handout ‘Semantic composition’, and (ii) the meaning itself after all the allowable substitutions from function applications. Thus, for example, given the tree on the left, either answer at right would be complete and accurate:



Rule (TV) derives {  ,  }

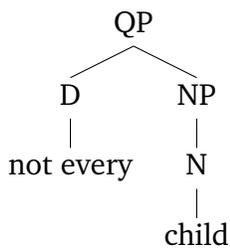
3.1



Model answer

Rule N derives $U - \llbracket studies \rrbracket = \{ \llbracket Bart \rrbracket, \llbracket Homer \rrbracket, \llbracket Maggie \rrbracket \}$

3.2



Model answer

Rule Q1 derives $\lambda Y (\top \text{ if } \llbracket child \rrbracket \notin Y, \text{ else } F)$

4 Extra functional application practice

Reduce the following expressions by applying the necessary application and substitution steps. You should reduce the expressions as far as is possible, including subexpressions.

i. $(\lambda x(4))(5)$

Model answer

4

ii. $(\lambda y(\lambda x(x > y)))(4)$

Model answer

$\lambda x(x > 4)$

iii. $((\lambda f(\lambda x(x < f(4))))(\lambda y(1 + y)))(2)$

Model answer

Optionally showing intermediate steps. Only the last line is required, and the lines before it would not earn full credit on their own due to lingering unconverted lambdas:

$$\Rightarrow (\lambda x(x < (\lambda y(1 + y))(4)))(2)$$

$$\Rightarrow (\lambda x(x < (1 + 4)))(2)$$

$$\Rightarrow 2 < (1 + 4)$$

5 Quantifier entailment

In the context of our semantic grammar, we can say that a determiner D entails a determiner D' if and only if, whenever $D(A)(B) = \top$, it holds that $D'(A)(B) = \top$, for all sets A and B . Does $\llbracket \text{not every} \rrbracket$ entail $\llbracket \text{some} \rrbracket$ in this sense? Either prove that this entailment relation holds or prove that it does not hold by presenting a counterexample and articulating why it is a counterexample. The meanings for $\llbracket \text{not every} \rrbracket$ and $\llbracket \text{some} \rrbracket$ are given in (11) and (5) of the 'Quantifier properties' handout.

Model answer

According to this theory, $\llbracket \text{not every} \rrbracket$ does not entail $\llbracket \text{some} \rrbracket$. Consider $A = \{1, 2\}$ and $B = \{3, 4\}$. $\llbracket \text{not every} \rrbracket(A)(B) = \top$; since A and B are disjoint, A is not a subset of B . But in virtue of these sets being disjoint, we have that $A \cap B = \emptyset$ and thus $\llbracket \text{some} \rrbracket(A)(B) = \text{F}$.

6 Intersective?

Consider the hypothetical quantificational determiner *uneq*:

$$\llbracket \textit{hartig} \rrbracket = \lambda X \left(\lambda Y \left(\top \text{ if } |X| = |Y|, \text{ else } \text{F} \right) \right)$$

Is this hypothetical determiner intersective (in the sense of our theory of quantificational determiners)? Either show that it is intersective or present a counterexample and explain why it is a counterexample.

Model answer

This determiner is intersective. This follows directly from the fact that the equality relation is order independent: if $|A| = |B|$, then $|B| = |A|$ for all A and B . Thus, $\llbracket \textit{hartig} \rrbracket(A)(B) = \llbracket \textit{hartig} \rrbracket(B)(A)$.

7 Monotonicity

Here is our usual definition of the quantificational determiner *not every*:

$$\llbracket \textit{not every} \rrbracket = \lambda X \left(\lambda Y \left(\top \text{ if } X \not\subseteq Y, \text{ else } \text{F} \right) \right)$$

Diagnose the first (restriction) argument as upward, downward, or nonmonotone, and explain why this holds using *not every*. (Note: this isn't a question about your intuitions, but rather about what we are predicting with *not every*.)

Model answer

The first argument of *not every* is upward monotone. To see this, assume that $\llbracket \textit{not every} \rrbracket(A)(B) = \top$ for some A and B . This means that there is some x such that $x \in A$ but $x \notin B$. Any X such that $A \subseteq X$ will also contain this element x , and thus $X \not\subseteq B$, which means $\llbracket \textit{not every} \rrbracket(X)(B) = \top$.