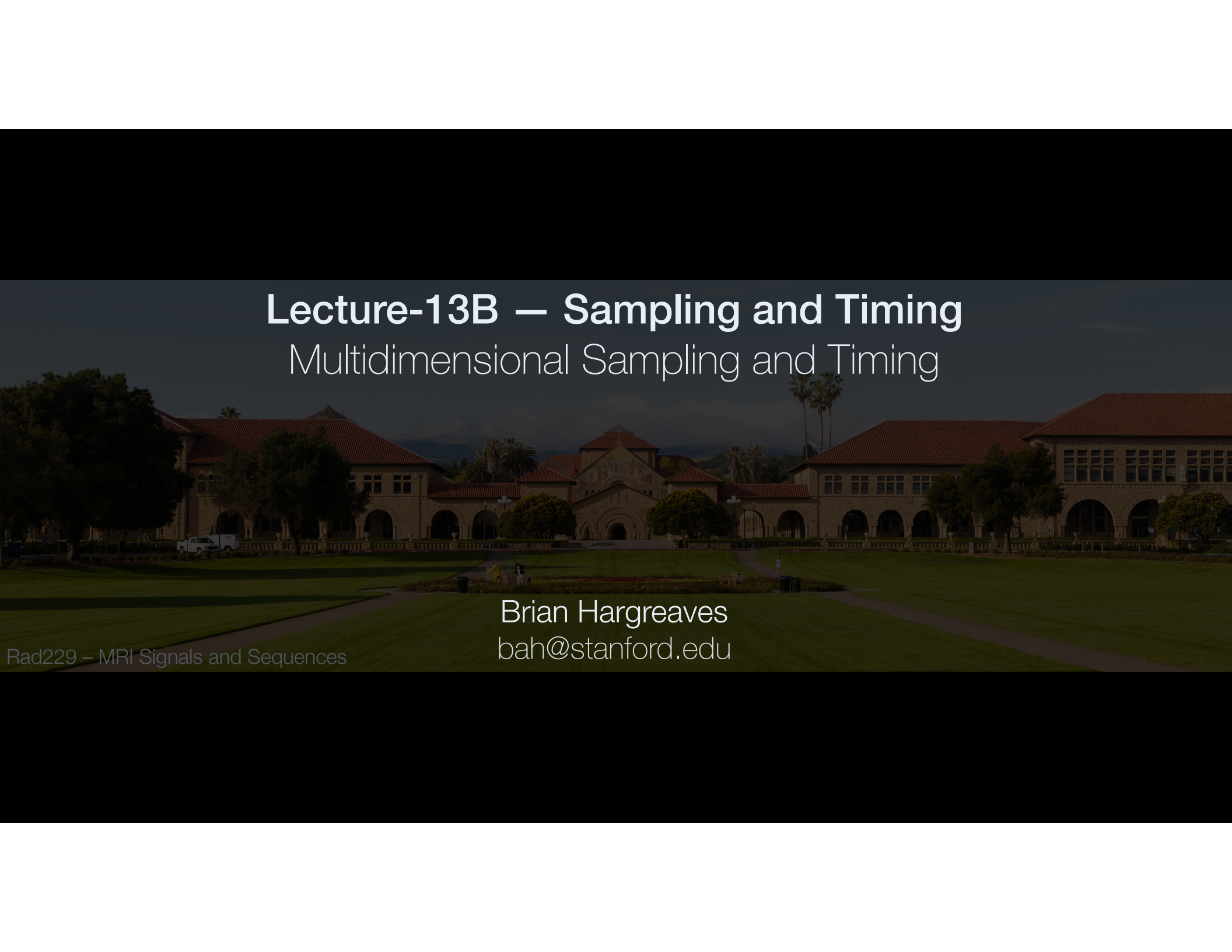


A photograph of a large, multi-story building with a red-tiled roof and arched windows, likely a Stanford University building. The building is set against a dark, overcast sky. In the foreground, there is a green lawn and a paved path. The text is overlaid on the image.

# Rad229 – MRI Signals and Sequences

**Daniel Ennis & Brian Hargreaves**

[dbe@stanford.edu](mailto:dbe@stanford.edu) –or– [bah@stanford.edu](mailto:bah@stanford.edu)

A wide-angle photograph of the Stanford University campus at dusk. The central building, the Main Quad, is illuminated by warm lights, and its red-tiled roof and arched windows are prominent. The surrounding green lawn is dark, and a few palm trees are visible in the background. The sky is a deep, dark blue.

# Lecture-13B — Sampling and Timing

## Multidimensional Sampling and Timing

Brian Hargreaves  
bah@stanford.edu

# Learning Objectives

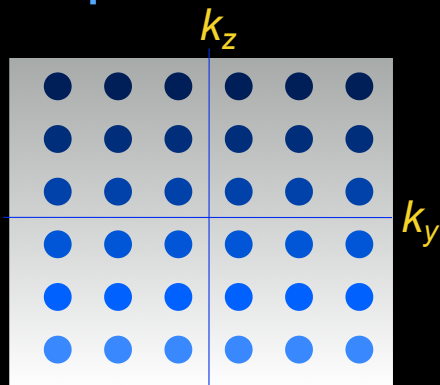
- Explain sampling approaches for 3D Cartesian imaging
- Describe temporal sampling approaches
- Understand strategies for slice interleaving
- Explain principles of multiband sampling and controlled aliasing



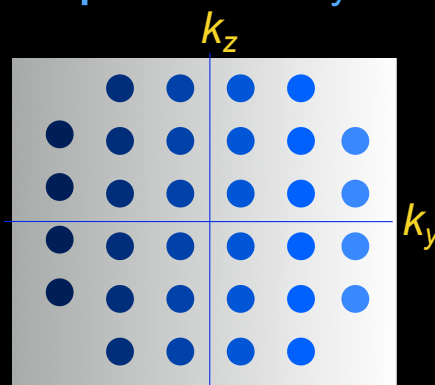
# 3D Image ( $k_y$ - $k_z$ ) View Ordering/Grouping

- Freedom to sample arbitrarily
- Centric (ordered by radius first or azimuth ( $\varphi$ ) first)
- Segment groups by  $k_y$ ,  $k_z$ ,  $\varphi$ ,  $k_r$
- Sub-segment groups ( $k_y$ ,  $k_z$ ,  $\varphi$ ,  $k_r$ , randomly)

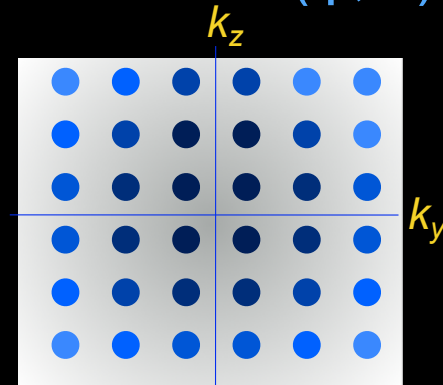
Sequential  $k_z$



Sequential  $k_y$



Center-out ( $\varphi, k_r$ )

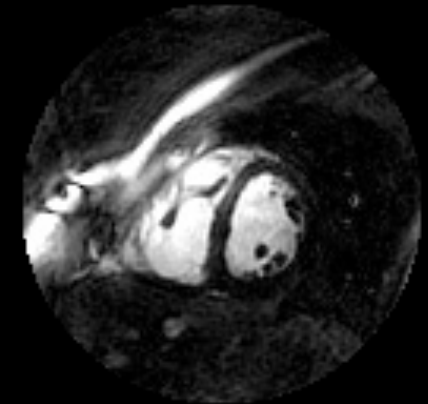


Cartesian sampling in 3D allows freedom to sample in arbitrary order in  $k_y$ - $k_z$



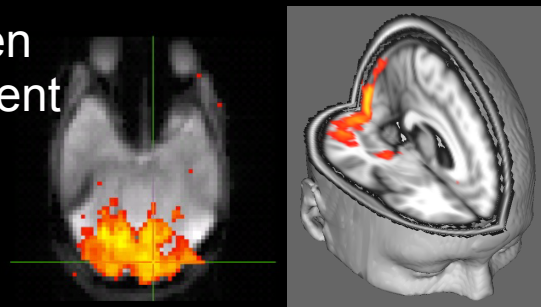
# Dynamic Imaging Applications

- Often want to image over time:
  - Resolve motion: cardiac, joints, swallowing, peristalsis (etc)
  - Contrast-enhancement
  - Functional MRI
- Spectroscopic imaging (related)



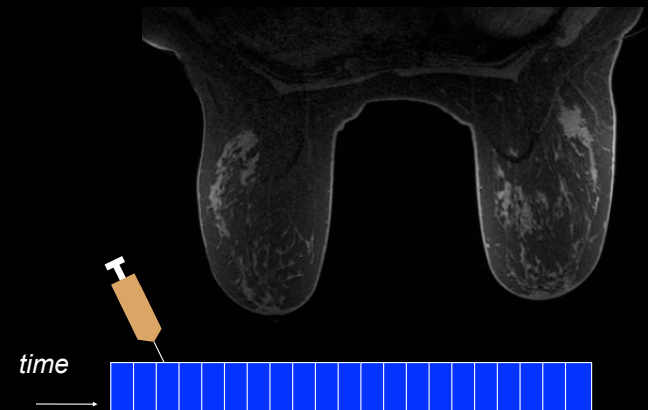
*(Courtesy of Krishna Navak)*

Blood-Oxygen  
Level Dependent  
(BOLD)



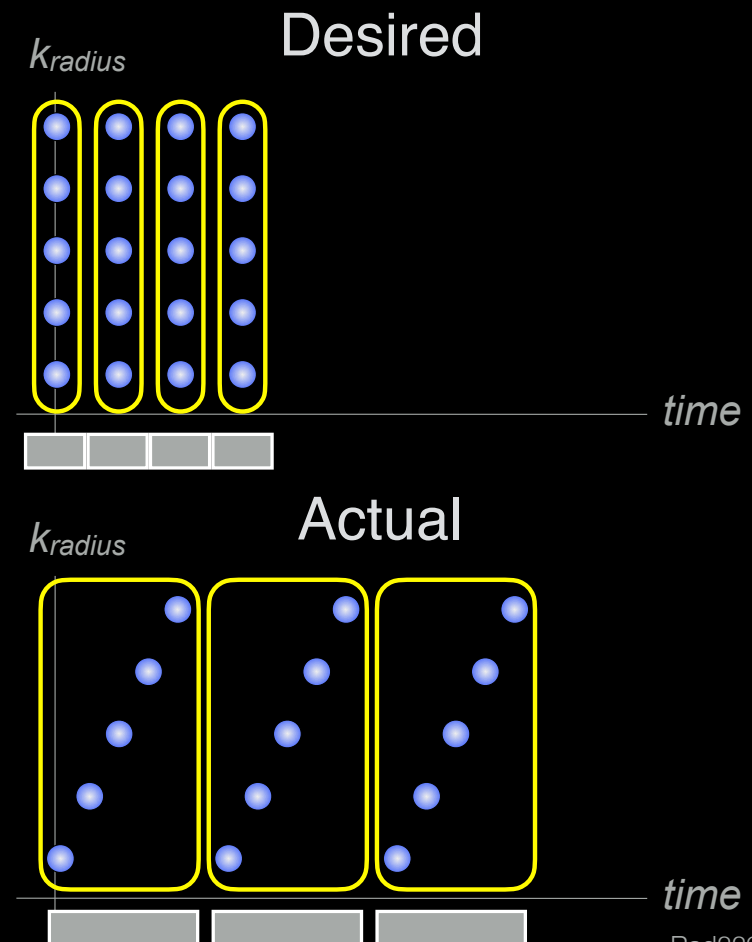
*(Courtesy of Karla Miller)*

There are numerous applications that demand continuous imaging over time



# Spatial and Temporal (Spatiotemporal) Resolution

- Fundamental Trade-off
- Skip samples?
  - Reduce resolution
  - Reduce FOV
- Exploit temporal and spatial information



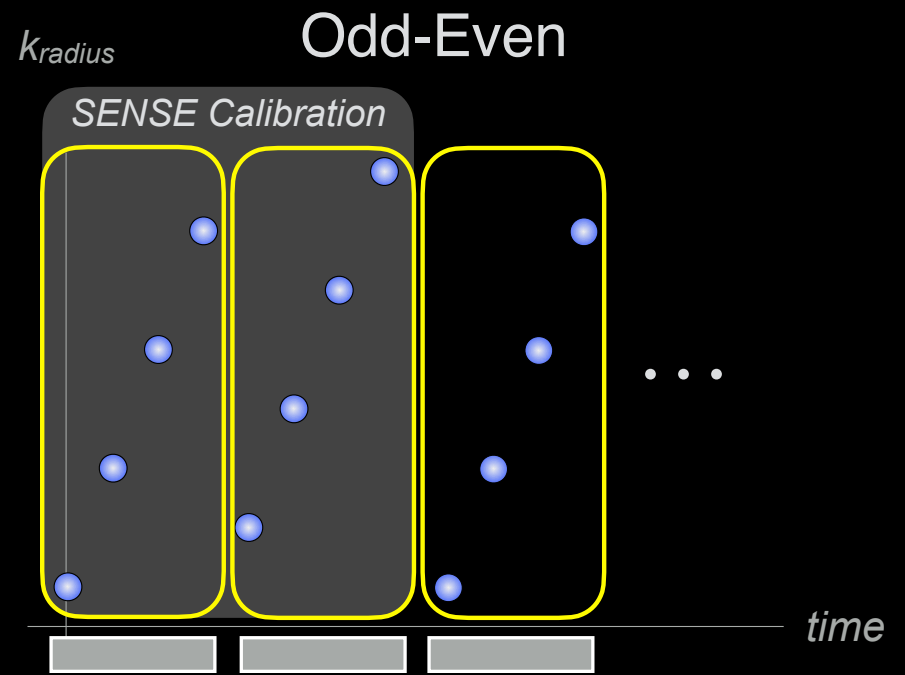
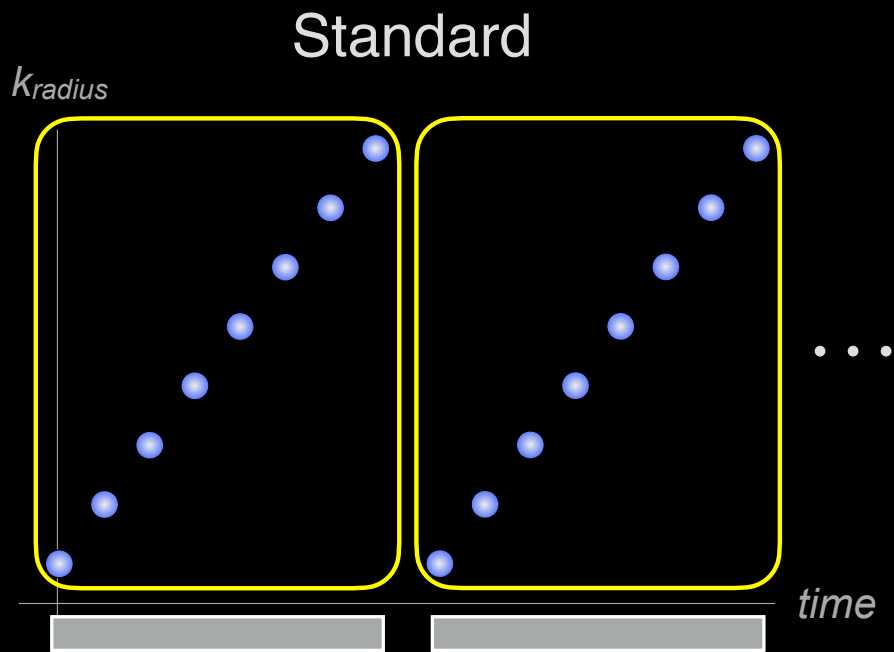
Since it takes finite time to obtain MR images, spatiotemporal imaging always involves a tradeoff between frame rate and image quality



# Question 1: Temporal Odd/Even Sampling?

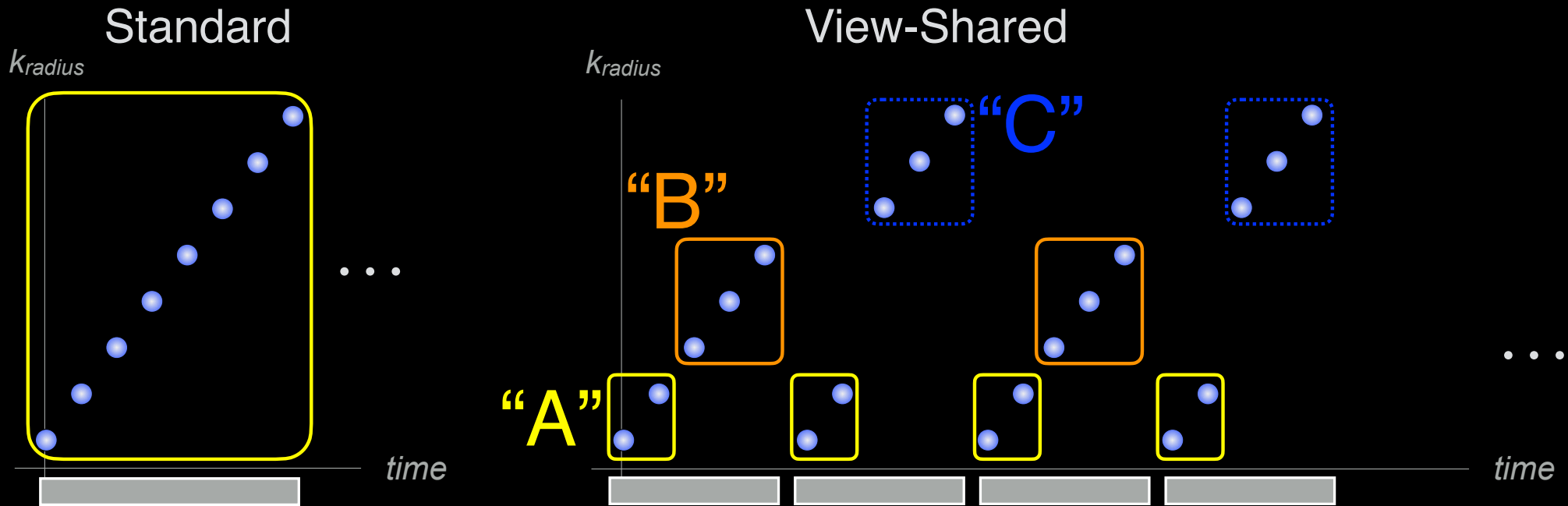


# Spatiotemporal Trade-offs: FOV



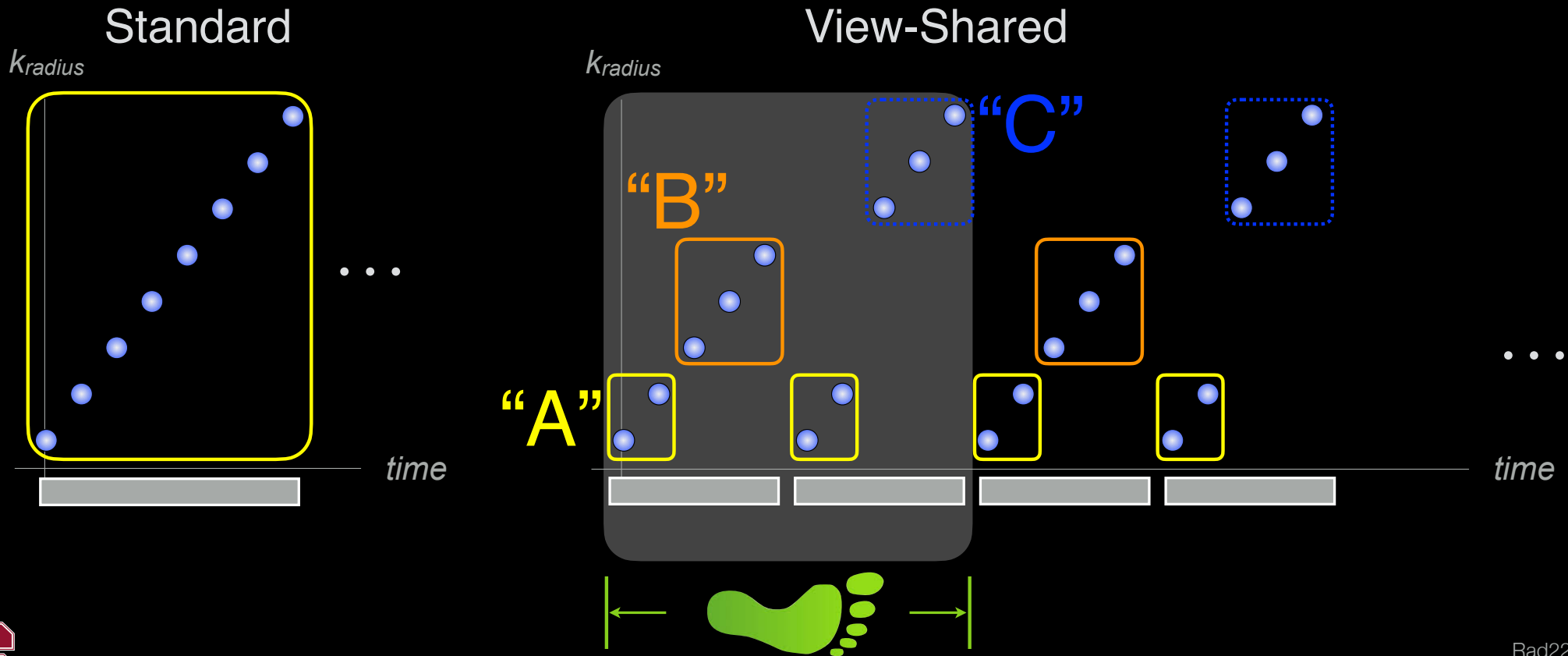


# Spatiotemporal Trade-offs: View-Sharing



View-sharing is standard in many dynamic acquisitions as contrast changes in low-spatial frequencies are dominant

# Spatiotemporal Trade-offs: View-Sharing



View-sharing is standard in many dynamic acquisitions as contrast changes in low-spatial frequencies are dominant



# Temporal $k_y$ - $k_z$ Undersampling Patterns

Time-Resolved Imaging  
of Contrast Kinetics  
(TRICKS)

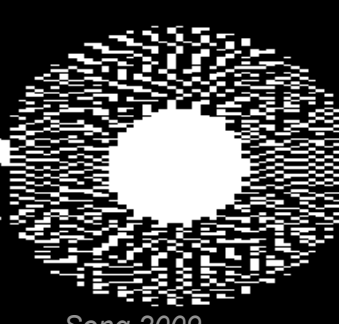


Korosec 1996

Cartesian Acquisition with  
Projection Reconstruction  
(CAPR) DISCO,  
TWIST

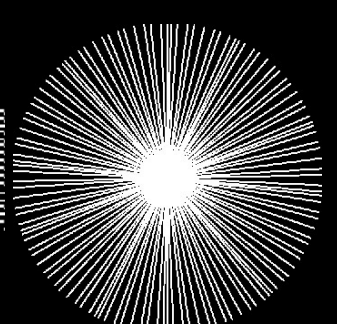


Madhuranthakam 2006



Song 2009,  
Saranathan 2012

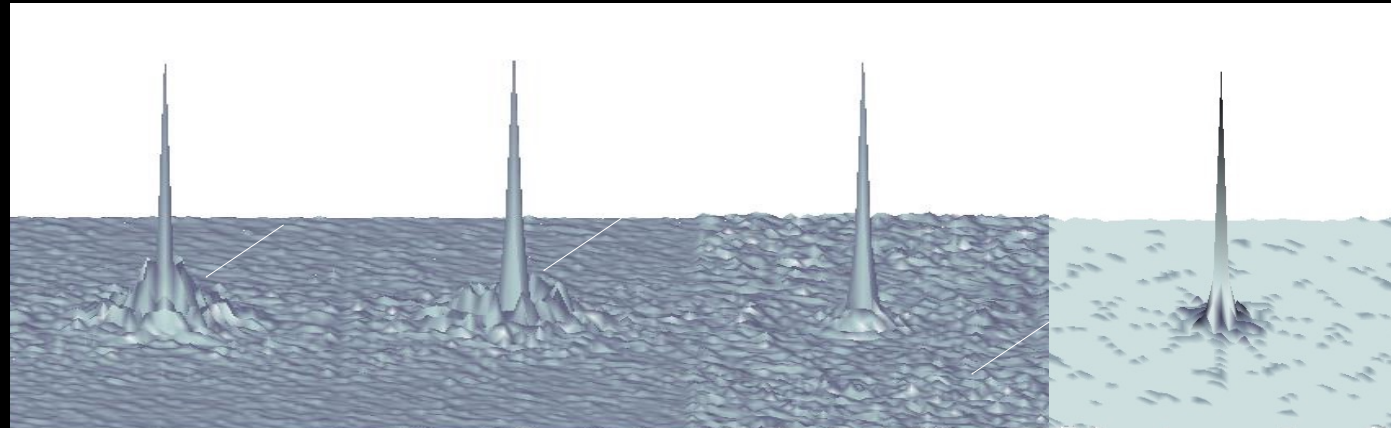
Radial  
(Golden Angle)



Winkelmann 2007

Data  
Acquisition  
( $k_y$ - $k_z$ , except radial)

Single-Frame  
Point-Spread Functions

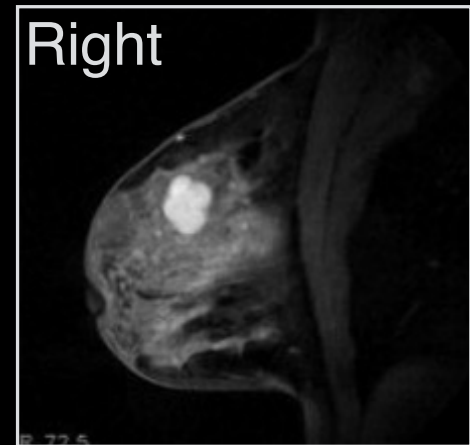
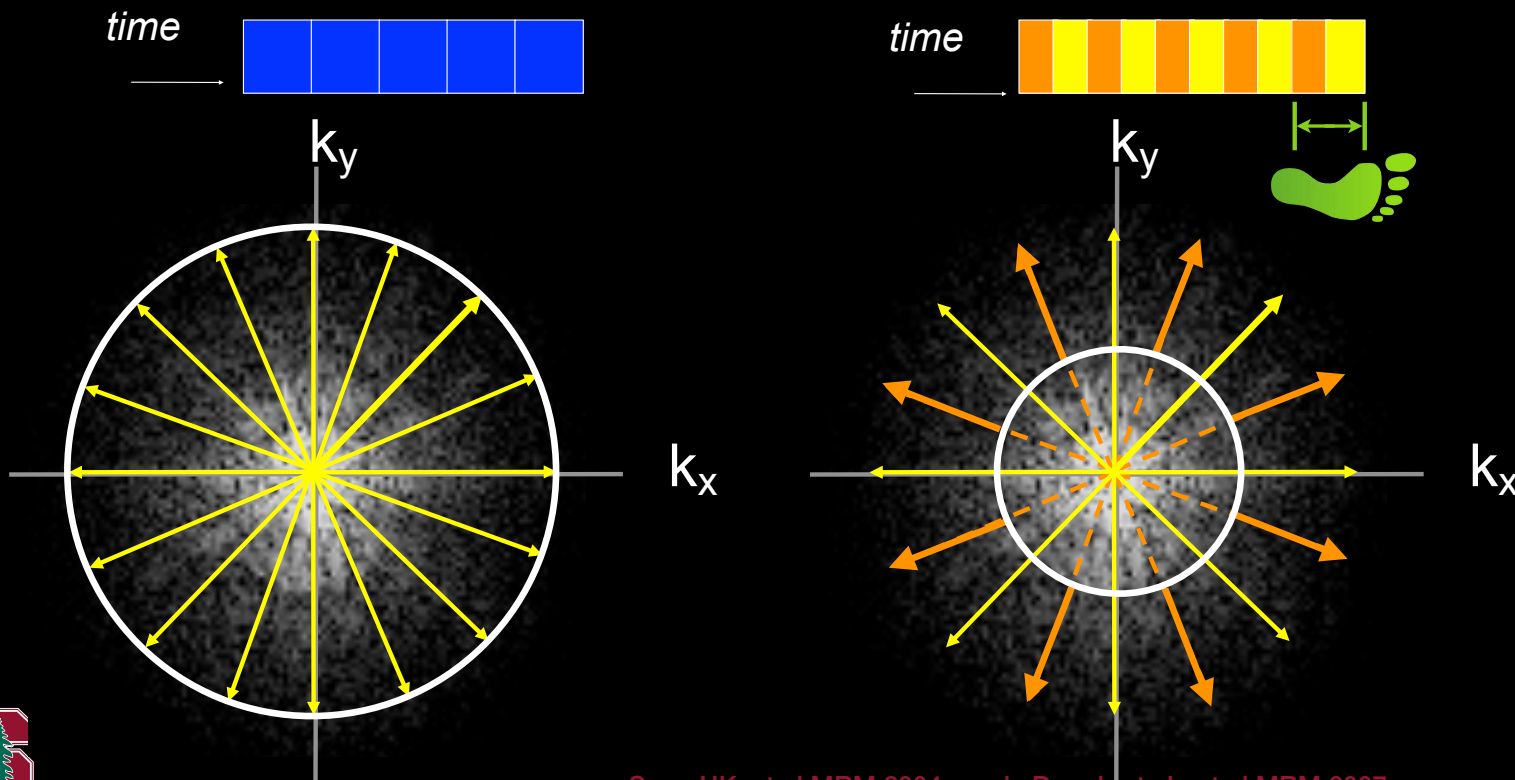


View-sharing performance can be compared by looking at the PSF of a single frame



# Radial Imaging Options

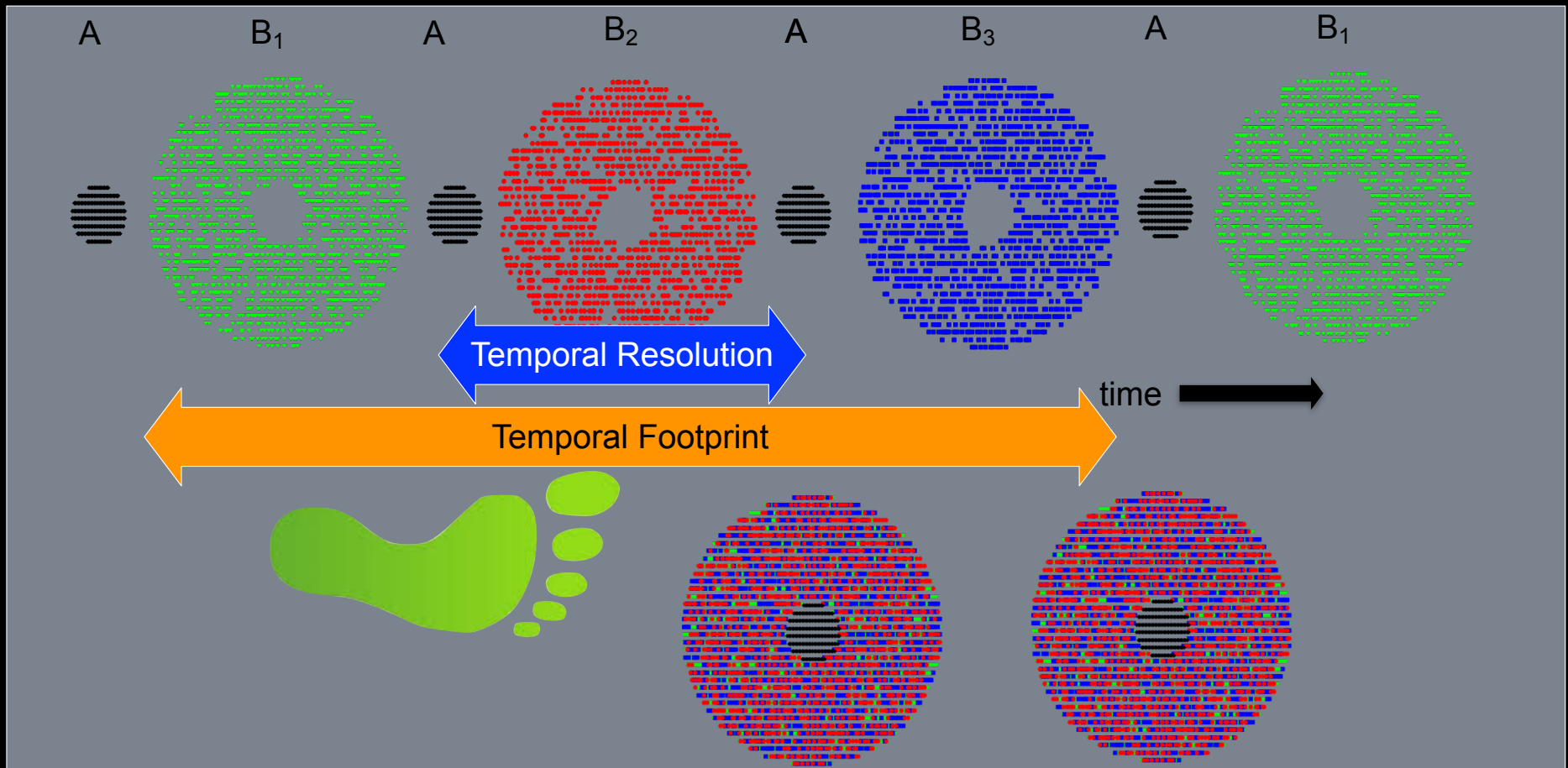
- Low-resolution image from reduced #spokes
- Retrospective Spatial vs temporal resolution tradeoff



Song HK, et al MRM 2004 and Dougherty L, et al MRM 2007

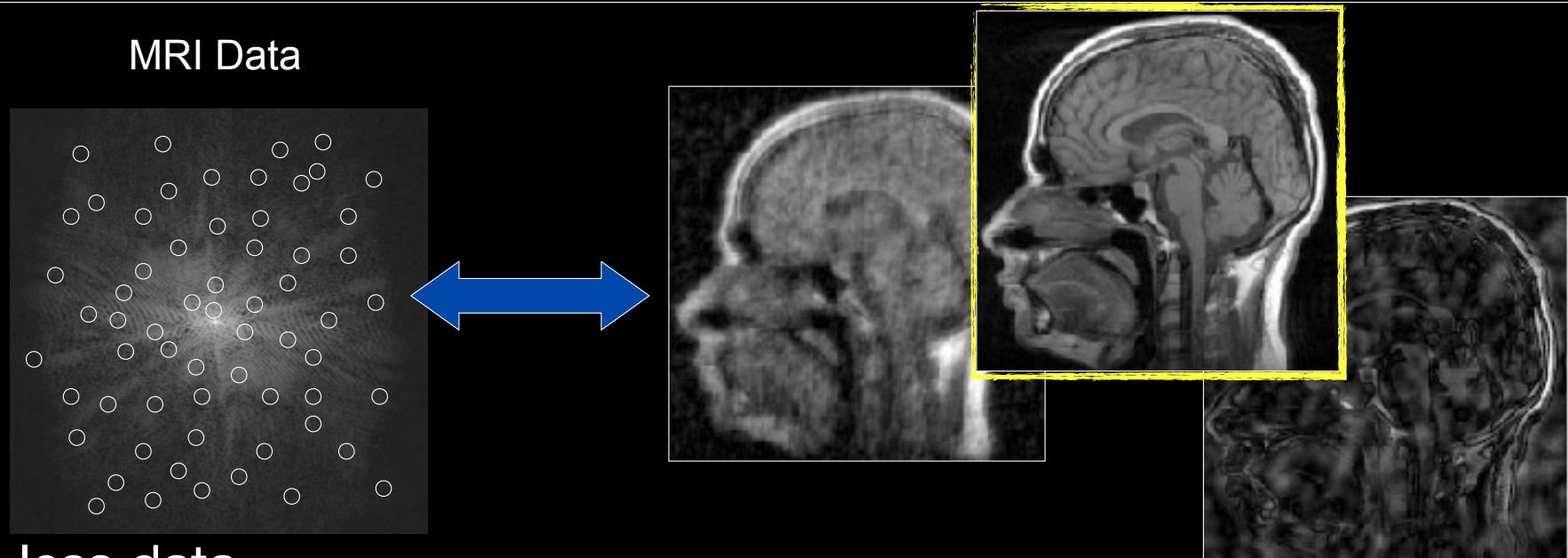


# DISCO $k_y - k_z$ - time Pattern (TWIST similar)



Saranathan M, MRM 2012, Song MRM 2009, Tudorica LA MRI 2012

# Compressed Sensing MRI



- Sample less data
- Choose image matching data that is most “compressible” (sparse)

$$\min_x \left\| D_t F S x - d_t \right\|_2 + \lambda_{CS} \left\| \Psi x \right\|_1$$

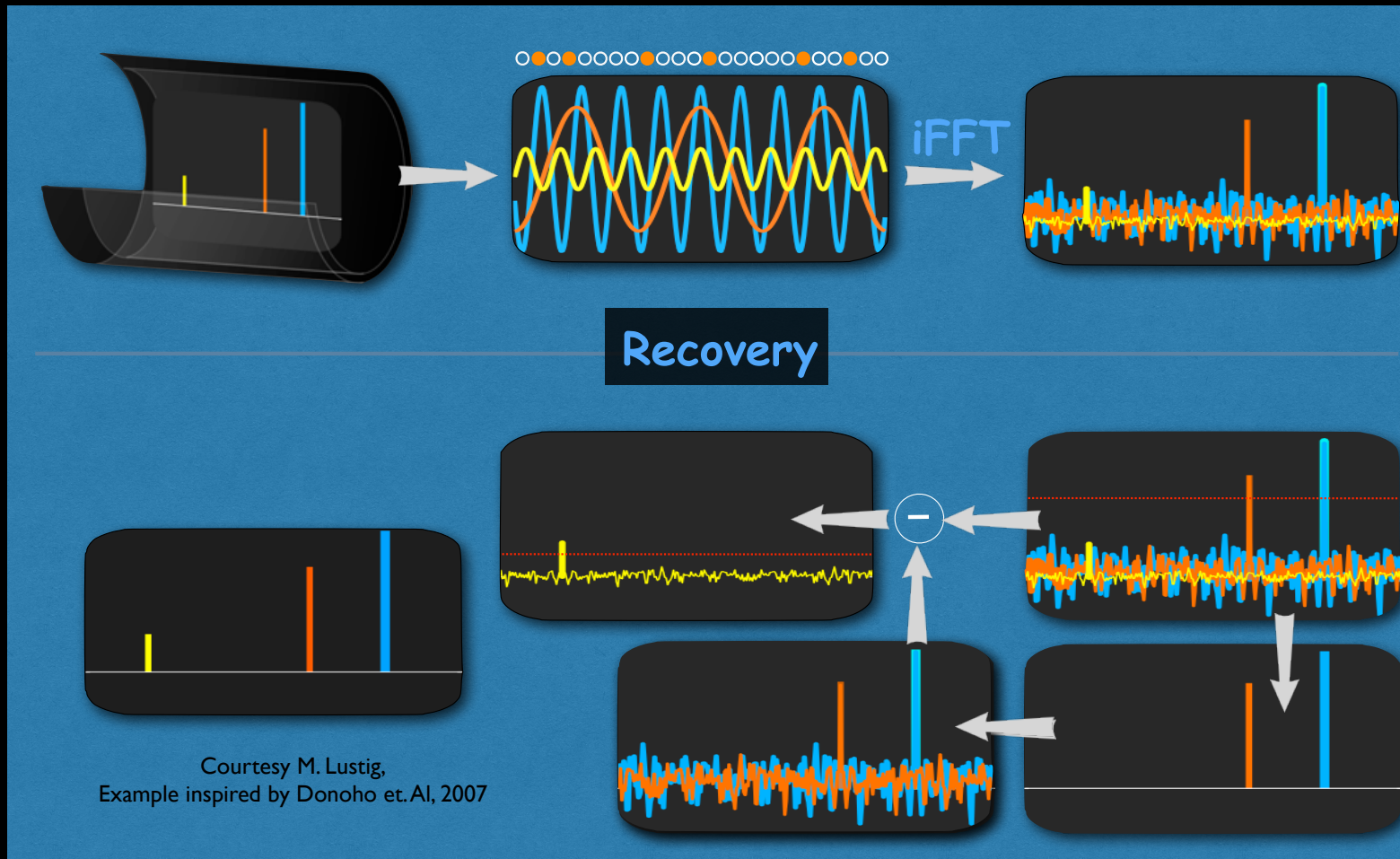
Data Match

Sparsity

Lustig, et al. MRM 2007



# CS Reconstruction and PSFs



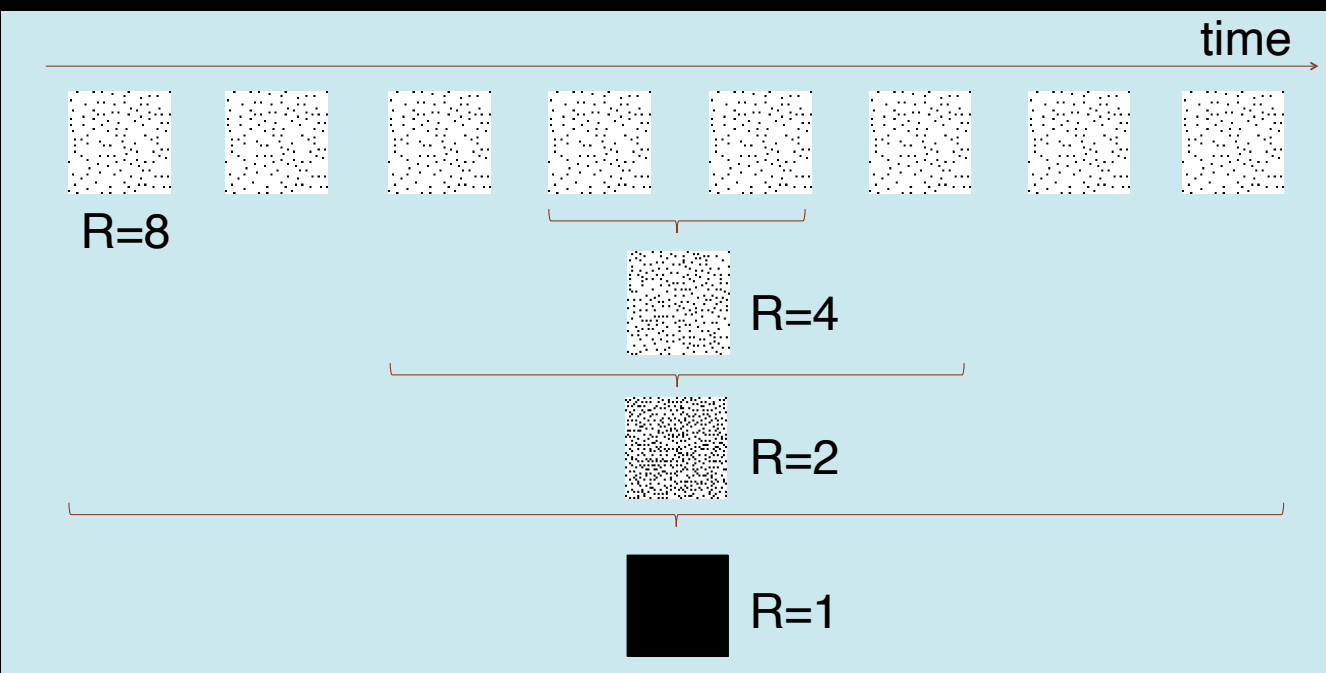
Courtesy M. Lustig,  
Example inspired by Donoho et. Al, 2007

Constrained reconstruction can remove noise-like artifact from random undersampling

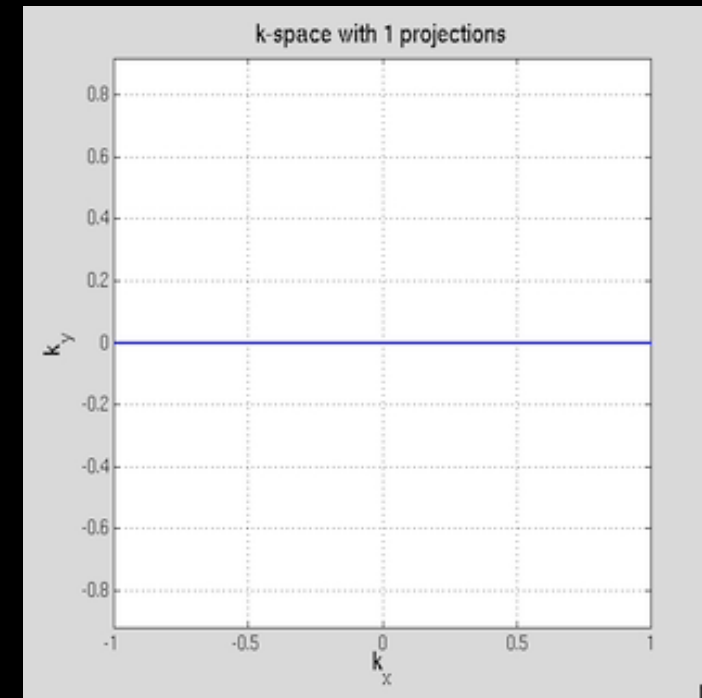


# Variable View Sharing

## Uniform Random Density



## Golden Angle Radial



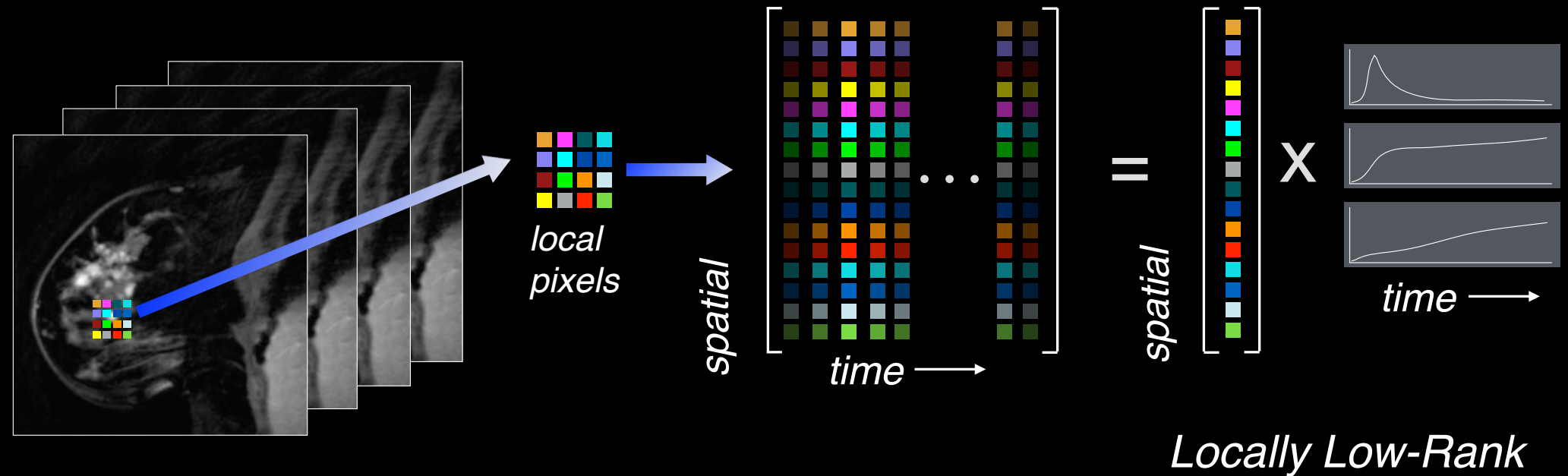
- Retrospectively select temporal footprint





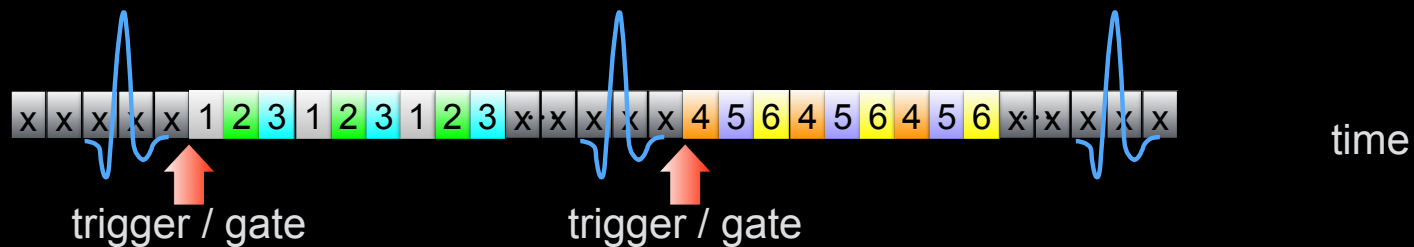
# Locally Low-Rank

- Model-free, Data-driven, Sparsity



# Cardiac/Respiratory Acquisition Timing

- Cine: Exploit periodicity of cardiac/respiratory cycle
  - Sample  $N$   $k_y$  lines repeatedly, next  $N$  lines on next heartbeat.
  - High frame rate and spatial resolution
- Triggering: Start acquisition based on external trigger (EKG, plethysmograph, respiratory bellows)
- Gating: Excite continuously, but acquire only after trigger
- Can combine any/all of these

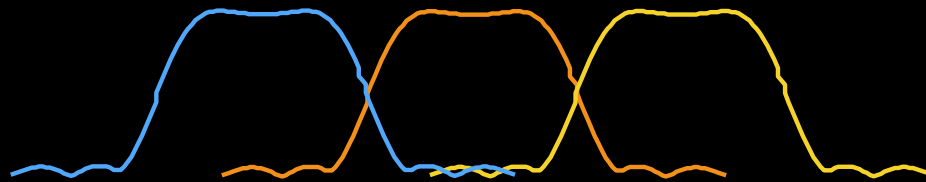
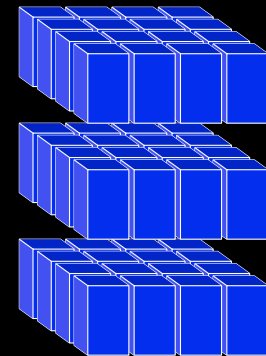


## Question 2: Cine Acquisition?



# Slice Interleaving

- Multislice acquisitions allow volumetric imaging
- Acquisitions can be *sequential* or *interleaved*
- Interleaving is time efficient if there is “dead time”
- Different ways to interleave (reduce adjacent-slice-saturation)
  - Sequential: 0, 1, 2, 3, 4, 5, 6, 7
  - Odd/Even: 0, 2, 4, 6, 1, 3, 5, 7
  - Bit-reversed: 0, 4, 2, 6, 1, 5, 3, 7

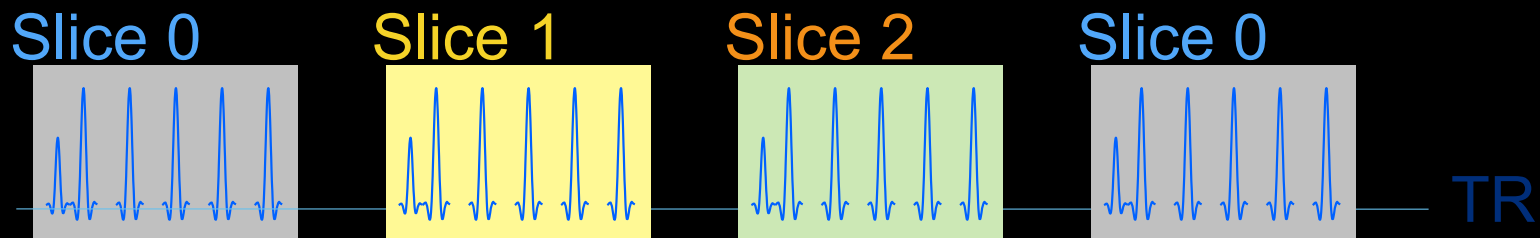


Interleaving is a common approach to improve acquisition efficiency for multislice scans



# How Many Slices to Interleave?

- Usually specify TR, TI, Echo-train-length (ETL), Resolution, ...
  - Give “pulse durations” ( $T_{\text{seq}}$ ) and RF power ( $T_{\text{min}}$ )
  - $N_{\text{max}} = \text{TR} / T_{\text{seq}}$  or  $\text{TR} / T_{\text{min}}$
  - Can re-order slices in “time slots”
  - Additional slices require another “acquisition”

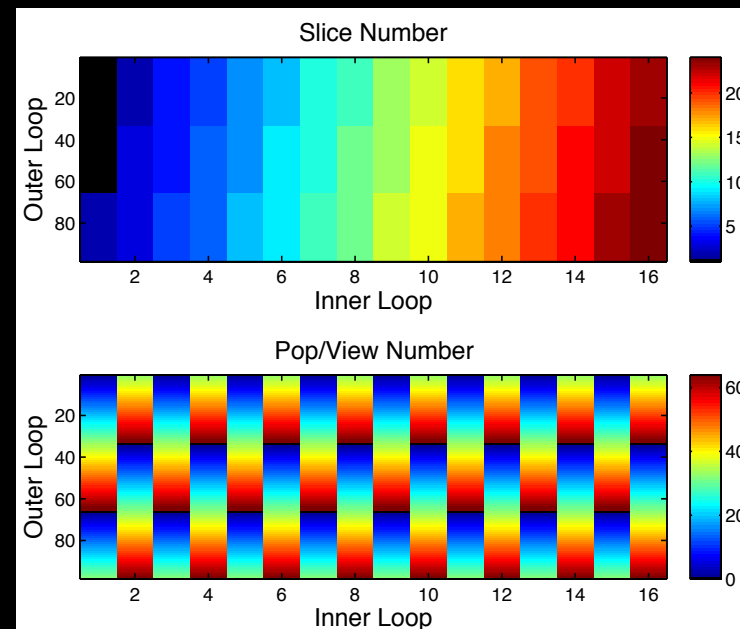
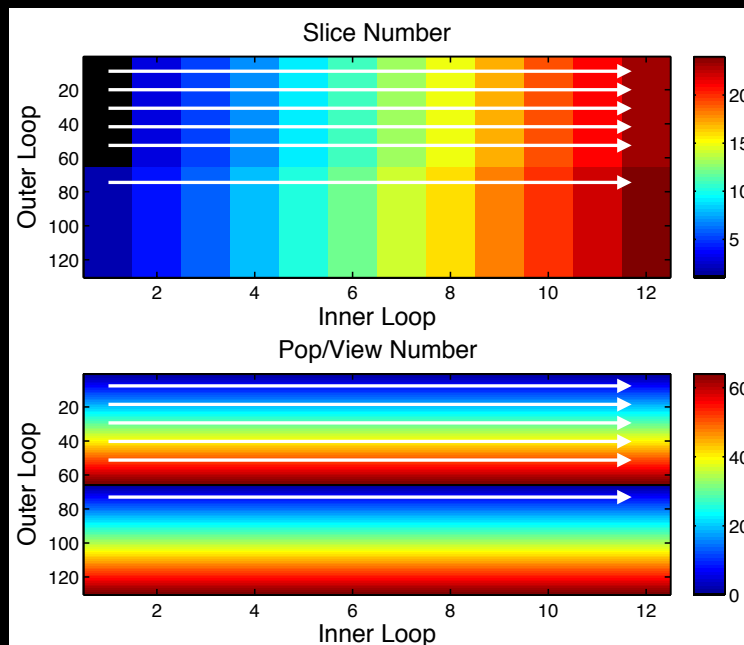


Maximum number of slices to interleave is a fairly simple calculation based on timing and RF power



# More Flexible Interleaving

- Typically consider slice number and phase-encode number
- If  $N_{\text{slices}} > N_{\text{max}}$ , scan is 2x, 3x, ... longer
- Decoupling phase encode number allows flexible interleaving

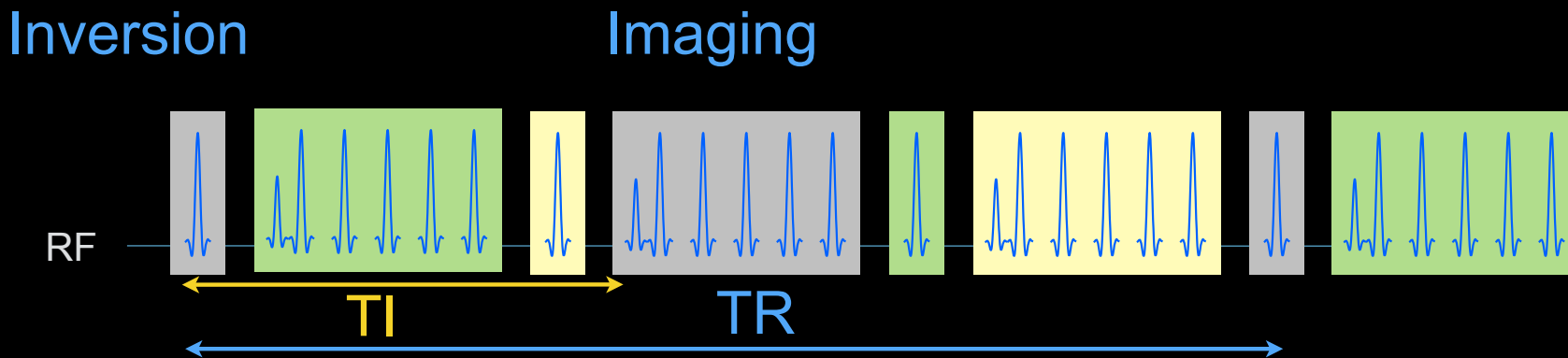


A simple "table" can be filled out column-first and read out row-first to interleave slices more efficiently



# FLAIR / STIR?

- Additional dead-time during TI interval
- Can sometimes interleave other acquisitions
- Additional constraints on TR, TI, Tseq

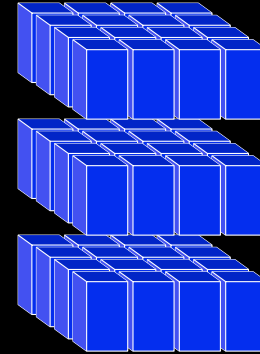


Interleaving acquisitions with IR blocks offers efficiency improvements



# Multiband Imaging

- Imaging multiple slices simultaneously
- Excitation: Multiply  $RF(t)$  by  $\cos(t+\phi)$ 
  - Increases SAR
- Imaging:
  - Hadamard: Excite “1,1” and “1,-1” pattern, add & subtract
  - POMP: Alternate patterns, increase y FOV
  - Parallel Imaging: Use coils to separate slices
  - Blipped sequences:  $G_z$  “blips” induce slice-dependent phase
    - Like 3D k-space with limited excitation
    - Similar to Dixon water/fat: slices are like spectral peaks



Simultaneous multislice imaging (SMS) offers flexibility in ways to acquire multiple slices



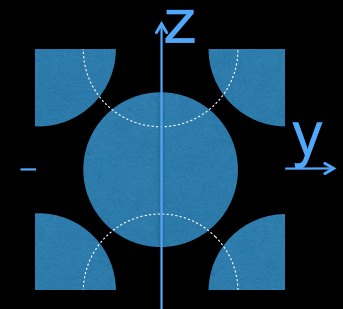
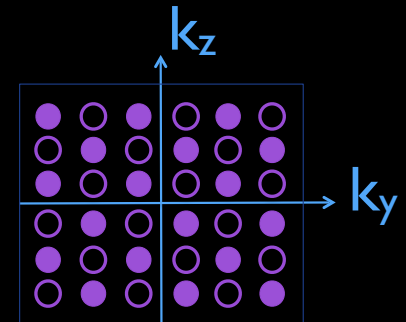


# Question 3: Slice-encoding Variations?



# “Controlled Aliasing in Parallel Imaging” (CAIPIRINHA)

- 3D ( $k_y$ - $k_z$ ) sampling:
  - Hexagonal sampling offsets replicas
  - Reduced aliasing (further apart)
- 2D Multislice:
  - Alternating phase during excitation or blips
  - Offset replicas allows in-plane coil sensitivities to help separate slices
  - Can think of as 3D  $k$ -space



# Question 4: Multiband Encoding?

Starting with a 1 kHz BW excitation, we want to excite two slices that are 5mm thick and 2cm apart (center-to-center)

- How do we modulate the pulse to excite 2 slices?

1kHz ... 5mm, +/-2kHz ... 2cm. Modulate with  $\cos(2\pi 2000 t)$

What is the image if we alternate excitations using the sequence cosine, sin, -cosine, -sin, ... modulation on successive ky lines, assuming slices are each 1cm away from center?

Slices are both shifted 1/4 FOV

Which FOV should we encode for 2x parallel imaging if we have 2 coils along y?

Large enough to separate objects (including parallel imaging)



# Summary

- Multidimensional sampling:
  - ky-kz order
  - k-t sampling for dynamic imaging
  - View sharing and PSFs
  - Random/incoherent sampling and compressed sensing
- Multislice interleaving
- Simultaneous multislice imaging / controlled aliasing



A photograph of a large, multi-story building with a red-tiled roof and arched windows, likely a Stanford University building. The building is set against a dark, overcast sky. In the foreground, there is a green lawn and a paved path. The text is overlaid on the image.

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