

Nonconservative Robust Control: Optimized and Constrained Sensitivity Functions

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Abstract—An automated procedure for optimization of proportional–integral–derivative (PID)-type controller parameters for single-input, single-output (SISO) plants with explicit model uncertainty is presented. Robustness to the uncertainties is guaranteed by the use of Horowitz–Sidi bounds, which are used as constraints when low-frequency performance is optimized in a nonconvex but smooth optimization problem. In the optimization (and hence the parameter tuning), separate criteria are formulated for low-, mid-, and high-frequency (HF) closed-loop properties. The tradeoff between stability margins, control signals, HF robustness, and low-frequency performance is clarified, and the final parameter choice is facilitated. We use a combination of global and local optimization algorithms in the TOMLAB optimization environment and obtain robust convergence without relying on good initial estimates for the controller parameters. The method is applied to a controller structure comparison for a plant with an uncertain mechanical resonance and a plant with uncertain time delay and time constants. For a given control activity, stability margin, and HF robustness, it is shown that a PID controller with a second-order filter and an \mathcal{H}_∞ controller based on loop-shaping achieve approximately the same low-frequency performance.

Index Terms—Control systems, convergence of numerical methods, \mathcal{H}_∞ control, optimal control, optimization methods, process control, proportional control, robustness.

I. INTRODUCTION

IN MANY controller design techniques, a mixed, possibly weighted, performance criterion is used to ensure that the closed loop achieves desirable behavior. The criterion includes multiple closed-loop objectives and is minimized to obtain a solution optimal with respect to the weighted performance objectives (as in mixed-sensitivity optimization). However, by considering separate criteria at different frequency regions, instead of aggregating the closed-loop properties into a single criterion,

the tradeoff between performance and robustness can be evaluated, especially in the case of a change of closed-loop specifications. Such a procedure has been demonstrated for the tuning of PI and proportional–integral–derivative (PID) controllers by optimization when no uncertainties are considered [1], [2].

For plants with uncertainties, the mid-frequency (MF) robustness properties are crucial. Particularly within process control, where plant uncertainties can be large, integral action is common, and then the low-frequency (LF) performance and robustness are less affected by the uncertainties [15]. For high frequencies (HF), good performance and robustness are simply a question of having a small loop gain. If explicit descriptions of the plant uncertainties have been formulated, the quantitative feedback theory (QFT) [3] can be used to design controllers such that specified bounds on the magnitudes of the sensitivity function $S(j\omega)$ and the control sensitivity function $KS(j\omega)$ (for example) are satisfied in spite of the uncertainties. The basis for this method is a translation of the constraints on S and KS to so-called Horowitz–Sidi bounds on the nominal open loop. For this purpose, a toolbox QSYN [4] running on MATLAB [5] can be used.

The traditional QFT design method aims to minimize the HF open-loop gain [6], [7]. It assumes no fixed structure of the controller and gives, in its general form, an unlimited number of tuning parameters. However, the QFT approach can be applied to fixed structure controllers, such as in [8], where it was applied to an ideal PID controller. The procedure uses bounds on the complementary sensitivity when minimizing the derivative gain. The basis for the method is a simplification of the optimization using the fact that by specifying the phase of the compensator for two frequencies, the phase is defined for all frequencies because it only depends on two parameters (integral time and derivative time). This method is extended in [9] to two other three-parameter compensators. Yaniv and Nagurka [10] have also developed an optimization method restricted to three-parameter PID controllers, but for the case when the phase margin is specified and one sensitivity function is bounded. The problem can then be formulated to rely on (repeated) solutions to fourth-order polynomials, which appears to avoid the problem of local minima. To deal with uncertainties other than gain uncertainty, the problem must still be solved for every chosen frequency and plant parameter value.

Garcia *et al.* [11] describe a method for PID tuning for uncertain plants that considers multiple frequency-domain \mathcal{H}_∞ closed-loop measures. However, the optimization is based on a standard Gauss–Newton algorithm and suffers from problems of local optima. The optimized criterion used is also a weighted

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sum of squared frequency characteristics, and unstructured disc uncertainties are used to modify the modulus margins to make the design robust.

All of the above methods need frequency gridding to be solved numerically, with a consequent increase in computational effort with gridding density. By use of the Kalman Yacubovich-Popov lemma, Hara *et al.* [12] transform frequency-domain constraints on PIDs into linear matrix inequalities (LMIs) and then avoid the approximations caused by frequency gridding. However, the design is by open-loop shaping and does not apply directly to closed-loop specifications. When applied to plants with parametric uncertainties, the problem is still transformed into an LMI optimization problem albeit with potential conservatism.

Neither the QFT-based methods [6]–[9] nor the other recent methods discussed [10]–[12] consider the general tradeoff between the LF, MF, and HF properties of the closed loop. This tradeoff is important because the process disturbance rejection, for example, can often be significantly improved at only a marginal reduction of the HF robustness [13], [14]. To pursue this, Fransson *et al.* developed a constrained optimization procedure where PID and PID weighted \mathcal{H}_∞ loop-shaping controllers were designed based on an optimization of the LF performance subject to specified bounds on the maximum sensitivity and the maximum nominal control sensitivity [15], [16]. Robustness of the sensitivity function to plant uncertainties was guaranteed by Horowitz–Sidi bounds, but the procedure suffered from the fact that local optimization methods were used to solve highly nonlinear problems with potential discontinuities in the parameter space. As a result, difficulties were frequently experienced with initial guesses, convergence, and local optima.

In [17], the design procedure in [15] and [16] was generalized to include robustness to plant model uncertainties for the control sensitivity function, and a global optimization algorithm was applied to the design problem. This paper summarizes earlier work by the authors [15]–[17] and improves the methods used in the following ways.

- The numerical treatment for solving the design problem is improved, which results in fast convergence towards a globally optimal controller (of a fixed structure).
- A reliable test is given that determines if the nominal loop transfer function is (pointwise) inside or outside the Horowitz–Sidi bounds in the Nichols chart.
- In the evaluation procedure, closed-loop properties (in terms of stability robustness, control activity, and high-frequency (HF) robustness) are constrained identically in the comparison of low-frequency performance.

The suggested approach applies to fixed structure controllers in general, with multiple closed-loop sensitivity constraints, and there is no theoretical limitation in the number of controller parameters. Basically, the same optimization problem, i.e., minimization of a low-frequency performance criterion subject to bounds on additional performance and robustness measures, has been solved for multiple-input, multiple-output (MIMO) systems by the authors, using the structured singular value (μ) [18]. The same methods may naturally be applied to single-input, single-output (SISO) systems as well. However, for many SISO cases, the QFT-based method presented here is superior to the

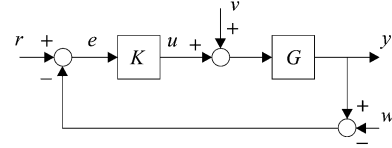


Fig. 1. Closed-loop system.

use of structured singular values [19]. For systems where the same uncertain parameter occurs in many places of a system model, the dimension of the nominal closed-loop system matrix (Q), resulting from linear fractional transformations, may become very large. This can make structured singular value determinations unfeasible, while the method presented here is quite insensitive to this [19].

This paper is organized as follows. In Section II, we define frequency-domain closed-loop performance measures and describe how they are used to pose the design problem. Section III presents the controller structures used, and Section IV discusses how robustness to plant model uncertainties can be ensured by use of the Horowitz–Sidi test. Section V details the numerical treatment of the method and we give an algorithm for solving the design problem. The method is illustrated by two examples in Section VI, and Section VII summarizes and concludes the paper.

II. CONTROL PROBLEM

A. Robustness and Performance Measures

It is well known that improvement of a controller design in one respect will often cause deterioration in another respect. Different closed-loop properties, such as stability, tracking, disturbance attenuation, and the magnitude of the control signals due to reference steps or disturbances, are often related to different frequency ranges of the closed loop and are not independent of each other. Therefore, a method for comparing controllers with each other should have the property that important closed-loop properties not immediately compared are identically constrained for all controllers. The method presented here fulfills this demand. It is based on four measures [13], each of them related to essential performance and robustness qualities of the closed loop and also roughly related to different frequency ranges as follows:

$$\begin{aligned} J_v &= \|s^{-1}G_{vy}\| = \|s^{-1}S(s)G(s)\|_\infty && \text{(LF)} \\ & && \|S(s)\|_\infty && \text{(MF)} \\ \|G_{wu}\| &= \|K(s)S(s)\|_\infty && \text{(MF/HF)} \\ J_{\text{HF}} &= \|s^m K(s)S(s)\|_\infty && \text{(HF)} \end{aligned}$$

where $G(s)$ denotes the plant, $K(s)$ denotes the controller, $S(s) = 1/(1 + G(s)K(s))$ is the sensitivity function, and m represents the roll-off rate of the controller (see Fig. 1).

It is obvious that J_v is a measure of the ability of the closed loop to handle process disturbances related to the low-frequency range. $1/\|S\|_\infty$ is the shortest distance from the loop transfer function to the instability point in the Nyquist diagram, and, hence, $\|S\|_\infty$ is a natural stability robustness measure. $\|KS\|_\infty$

is a measure of the control activity due to measurement noise, related to the MF and HFy region around (or somewhat above) the closed-loop bandwidth. J_{HF} is a measure of the robustness to unmodelled dynamics in the HF region. Recall the small gain theorem ($\|T\Delta\|_\infty < 1$) and the fact that KS is related to the complementary sensitivity function T as $KS = G^{-1}T$. Then, for a proper (but not strictly proper) controller, such as a PID controller with a first-order filter, $m = 0$, and hence $J_{\text{HF}} = \|KS\|_\infty$.

Each of the presented measures relates to a different region of the frequency range (LF, MF, and HF). Thus, simultaneous use of these measures in a design procedure facilitates determination of controllers that give acceptable behavior of the closed-loop system for all frequencies. However, since the plant is assumed to be uncertain, all of the measures above will be functions of the plant uncertainty.

B. Plant Uncertainty

An uncertain plant transfer function can be defined as a member of a set of transfer functions [4]

$$G(s) \in \{G_i(s)\}$$

where the set may contain finitely or infinitely many plant cases. By defining a set of n_ω frequencies as $\{\omega_k\}_{k=1}^{n_\omega} \in \Omega$, we have that for each frequency ω_k , the set $\{G_i(j\omega_k)\}$ in the complex plane is called a *template*, or value set, for ω_k [3]. The template should enclose all possible frequency responses of the plant at the frequency ω_k . This paper concerns a special class of uncertainty, namely, the parametric plant uncertainty defined by

$$G(s, \Delta) \in \{G(s, \Delta_i)\}, \quad \Delta_i \in \mathbf{\Delta} \subset \mathfrak{R}^p \quad (1)$$

where Δ_i is a vector of uncertain parameters. The *nominal* plant is denoted $G_{\text{nom}}(s)$ and reflects the choice of a particular Δ_i .

C. Design Problem

The design problem is posed by incorporating the uncertainty description into the robustness and performance measures. A controller that, despite the uncertainties in the plant, achieves acceptable behavior of the closed-loop system for all frequencies can be obtained by solving the following optimization problem:

$$\begin{aligned} K^* &= \arg \min_K J_v(\Delta) & (2) \\ \text{s.t. } \|S(s, \Delta)\|_\infty &\leq c_S \quad \forall \Delta \in \mathbf{\Delta} \\ \|KS(s, \Delta)\|_\infty &\leq c_{KS} \quad \forall \Delta \in \mathbf{\Delta} \\ J_{\text{HF}}(\Delta) &\leq c_{\text{HF}} \quad \forall \Delta \in \mathbf{\Delta}. & (3) \end{aligned}$$

Thus, K^* is the controller obtained by minimizing the LF performance measure J_v subject to user-defined constraints c_S , c_{KS} , and c_{HF} on $\|S(s, \Delta)\|_\infty$, $\|KS(s, \Delta)\|_\infty$ and $J_{\text{HF}}(\Delta)$, respectively.

D. Simplifications

If a general expression for controllers with integral action is introduced as

$$K(s) = \frac{\kappa_i}{s} + \tilde{K}(s) \quad (4)$$

where $\lim_{\omega \rightarrow 0} |\tilde{K}(j\omega)|$ is bounded, it can readily be shown that $|(j\omega)^{-1}SG(j\omega)| \rightarrow \kappa_i^{-1}$ as $\omega \rightarrow 0$ (provided $|G(j0) \neq 0|$) [15], [20]. Thus, for PID controllers and SISO systems, the inverse κ_i^{-1} of the integral gain serves as a close approximation to J_v (this conclusion is based on the fact that good damping—i.e., appropriate stability margin, is assumed). Hence, J_v will be relatively independent of the plant uncertainty. Also, J_{HF} depends weakly on the uncertainties, which predominantly affect the mid-frequency region of the closed loop. With this in mind, (2) and (3) can be simplified to

$$K^* = \arg \min_K J_v \quad (5)$$

$$\begin{aligned} \text{s.t. } \|S(s, \Delta)\|_\infty &\leq c_S, \quad \forall \Delta \in \mathbf{\Delta} \\ \|KS(s, \Delta)\|_\infty &\leq c_{KS}, \quad \forall \Delta \in \mathbf{\Delta} \\ J_{\text{HF}} &\leq c_{\text{HF}} \end{aligned} \quad (6)$$

where J_v and J_{HF} are based on the nominal plant. If, for some reason, J_v is expected to depend significantly on the uncertainties, an approximation of the expected value taking the covariance of the parameters into consideration can be used (see [19]).

III. CONTROLLER STRUCTURES

In this study, both PID controllers and \mathcal{H}_∞ synthesis by loop-shaping [21] are considered when solving (5) and (6). The loop-shaping procedure has the great advantage of not including the γ -iteration in standard \mathcal{H}_∞ synthesis. Instead, suboptimality is introduced in terms of a scaling factor $\alpha > 1$, which must be properly chosen.

A. PID Controllers

Traditionally, the well-known PID controller, with a first-order filter on the derivative part, used to be formulated with the parameters controller gain k_p , integral time T_i , derivative time T_d , and filter constant T_f as

$$K_{\text{PID}}(s) = k_p \left(1 + \frac{1}{sT_i} + \frac{sT_d}{1 + sT_f} \right).$$

As shown in several papers (e.g., [13]), a PID controller that gives good closed-loop performance and robustness, at least for stable nonoscillating plants, has a complex pair of zeros. This makes it natural to formulate the transfer function of the controller as

$$K_{\text{PID}} = k_i \frac{1 + s\zeta\tau s + (\tau s)^2}{s(1 + s\frac{\tau}{\beta})} \quad (7)$$

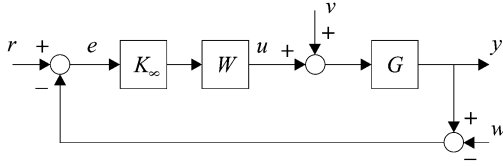


Fig. 2. Closed-loop system with an \mathcal{H}_∞ loop-shaping controller K and a plant G .

where k_i is the integral gain, ζ is the damping ratio, τ is the inverse of the natural frequency, and β is the ratio of the breaking point of the denominator to that of the numerator.

When there is a demand on more HF roll-off in the loop than can be offered by the plant, the PID controller can be augmented by a low-pass filter of arbitrary order. If the first-order filter is exchanged by a filter of second order, the controller can be formulated as

$$K_{\text{PIDf}} = k_i \frac{1 + s\zeta\tau s + (\tau s)^2}{s \left(1 + 2\zeta_f \frac{\tau}{\beta} s + \left(\frac{\tau}{\beta} s \right)^2 \right)}. \quad (8)$$

In Section VI, this controller structure is compared with a PID weighted \mathcal{H}_∞ controller. Note that the roll-off rate of (8) is $m = 1$, and the parameters subject to optimization with (8) are $k_i, \zeta, \tau, \zeta_f$, and β .

B. \mathcal{H}_∞ Loop-Shaping

The first step in the method by Glover and McFarlane [21] is to shape the nominal plant $G(s)$ with a weight $W(s)$ to give an open loop that meets some nominal performance specifications. For the shaped system $\tilde{G}(s) = G(s)W(s)$, a controller $K_\infty(s)$ is obtained by solving two Riccati equations. The final feedback controller for $G(s)$ is then $K(s) = W(s)K_\infty(s)$ (see Fig. 2). For a given weight $W(s)$, the controller derived in this way will, in some sense, have optimal robustness. The degree of optimality is determined by $\epsilon = \epsilon_{\max}\alpha^{-1}$, where ϵ_{\max} is called the maximum stability margin and $\alpha > 1$ is a scaling factor.

In this paper, $W(s)$ is parameterized as the PID controller (7) whose parameters (k_i, ζ, τ , and β) are subject to tuning by optimization so that a desired closed-loop behavior is obtained. Because of this choice of weight, the final \mathcal{H}_∞ controller will have a roll-off rate $m = 1$, thus explaining the need for using the PID controller with a second-order filter K_{PIDf} (8) when comparing the PID and \mathcal{H}_∞ controller structures.

IV. HOROWITZ–SIDİ BOUNDS

If the plant uncertainty is represented by a set of templates for a number of frequencies, QFT can be used to design a controller such that the closed loop satisfies specifications on the magnitudes of some frequency response functions (such as the sensitivity functions) for all plant variations within a given uncertainty set. The frequency response specifications, in turn, result in constraints on the nominal loop transfer function $L_{\text{nom}}(j\omega) = G_{\text{nom}}(j\omega)K(j\omega)$. These constraints are called Horowitz–Sidi bounds and reflect the interaction between the plant uncertainty and the closed-loop specifications.

We define

$$S_i(s) = \frac{1}{1 + G_i(s)K(s)}, \quad i = 1, 2, \dots$$

where G_i is the uncertain plant and impose an upper bound c_S on the maximum frequency response of this sensitivity function for all plants in $\{G_i\}$, i.e., the following must hold:

$$M_S \equiv \max_i \left| \frac{1}{1 + G_i(j\omega_k)K(j\omega_k)} \right| \leq c_S, \quad k = 1, \dots, n_\omega. \quad (9)$$

Thus, the controller must be chosen such that (9) is fulfilled for the complex numbers $K(j\omega_k)$. Clearly, for each G_i , there is a set for $K(j\omega)$ in the complex plane where (9) does not hold. The union of all such sets give one, or possibly several, sets containing the unacceptable values of $K(j\omega_k)$. The boundary of this set is called the Horowitz–Sidi bound for K with respect to S and ω_k and is denoted $B_S^K(\omega_k)$. Multiplying B_S^K by the nominal plant yields $B_L^S(\omega_k)$.

The computation of Horowitz–Sidi bounds is done in two steps. The first step demands the computation of the value sets of the plant transfer function. The simplest method is indeed the grid method, where the parameter space is gridded, e.g., equidistantly or randomly, see [22]. More advanced recursive grid or adaptive grid methods exist, see, e.g., [23], where the desired resolution of the computed value set determines the number of grid points, and hence the accuracy of the final result. For special types of transfer functions gridding in the parameter space can be avoided; see [24] and the references therein. Recently, interval analysis has been suggested for value set computation for transfer functions that can be decomposed into elementary functions whose maxima and minima can be analytically calculated [25]. The second step of the computation of Horowitz–Sidi bounds does not require the gridding of the parameter space, but, depending on the desired resolution of the resulting Horowitz–Sidi bound, the gridding of a set in the complex plane.

Horowitz–Sidi bounds can be computed with QSYN [4] and placed in a Nichols chart together with L_{nom} . To ensure that (9) is satisfied for all plants within the uncertainty set, L_{nom} must be shaped so that, at each frequency ω_k , it is outside the bound for that frequency (see Fig. 3). Analogously to (9), we also define

$$M_{KS} \equiv \max_i \left| \frac{K(j\omega_k)}{1 + G_i(j\omega_k)K(j\omega_k)} \right| \leq c_{KS} \quad \forall k \quad (10)$$

with a corresponding Horowitz–Sidi bound B_{KS}^L . In an automated procedure, one has to test whether or not $L_{\text{nom}}(j\omega_k)$ is outside $B_S^L(\omega_k)$ and $B_{KS}^L(\omega_k) \forall k = 1, \dots, n_\omega$.

Now, consider a single k and transform the origin in the Nichols chart to the interior of the Horowitz–Sidi bound B associated with ω_k (where the superscript L , the subscripts S, KS , and the argument ω_k have been dropped for clarity). If B is transformed to polar coordinates (r_B, θ_B) , we can write $r_B = B(\theta_B)$, and, if L_{nom} is transformed to the same coordinates, it can be represented by (r_L, θ_L) . As Fig. 4 illustrates, the test for L_{nom} being outside B is then simply

$$r_L > B(\theta_L) \quad (11)$$

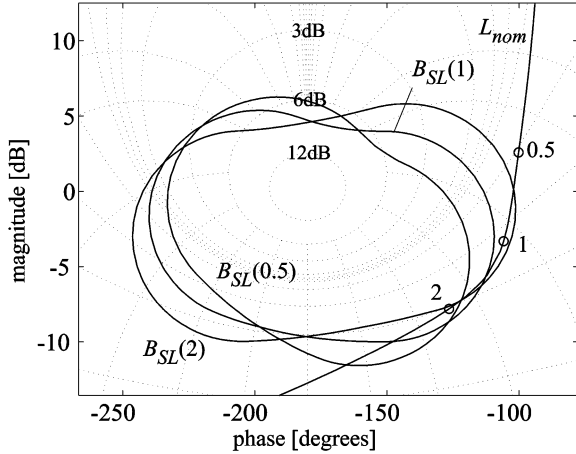


Fig. 3. Nichols chart with Horowitz–Sidi bounds and a nominal open loop for $\omega_k = 0.5, 1, \text{ and } 2$.

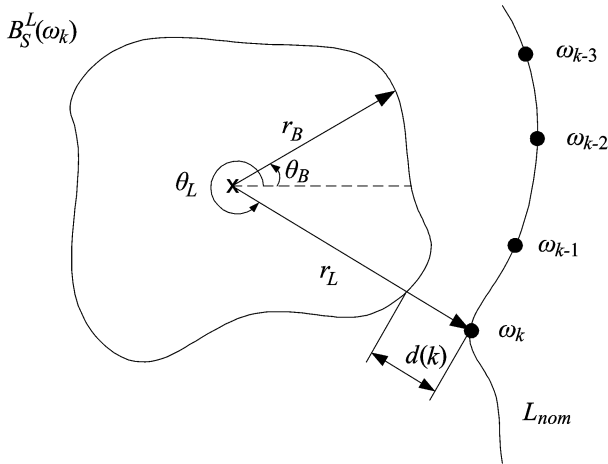


Fig. 4. Nominal open loop and the corresponding Horowitz–Sidi bound for ω_k transformed to polar coordinates.

and the distance $d(k)$ in the figure is a measure of how close L_{nom} is to B at the frequency ω_k . We refer to this as the *Horowitz–Sidi test*. Note that the choice of origin is trivial, provided that the nominal case is a member of the template itself. In such a case, the instability point in the Nichols chart is “inside” the Horowitz–Sidi bound. We also note that, for example, the Horowitz–Sidi sensitivity bound will be a single closed curve in the Nichols diagram (the curve may touch itself) if the plant template is simply connected [4]. When the plant template is not simply connected, the Horowitz–Sidi bound can consist of a set of closed curves, and, to handle a situation like this, a different origin for each of the closed curves will have to be chosen.

If the choice of origin is bad or B is nonconvex, there could be several solutions to $B(\theta_L)$, which means that (11) must be modified in order to serve its purpose. Define a crossing between r_L and B as a pair of consecutive points (r_1, θ_1) and (r_2, θ_2) on B such that $\theta_1 < \theta_L < \theta_2$. L_{nom} is then inside B if there is an even number of crossings and outside if there is an odd number of crossings, as shown in Fig. 5.

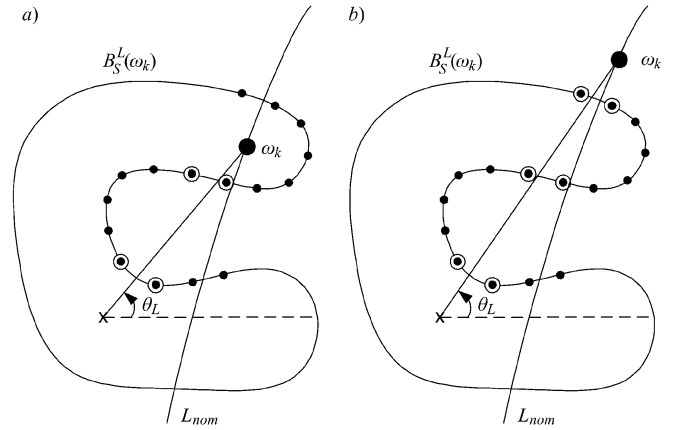


Fig. 5. Illustration of (a) unacceptable and (b) acceptable scenarios when performing the Horowitz–Sidi test (11).

V. NONLINEAR OPTIMIZATION

Based on the discussion in Section IV, the design problem (5) and (6) can be approximated using (9) and (10) to obtain

$$\begin{aligned} \min_{\rho} J_v(\rho) \quad \text{subject to} \\ M_S(\rho, k) \leq c_S, \quad \forall k = 1, \dots, n_\omega \\ M_{KS}(\rho, k) \leq c_{KS}, \quad \forall k = 1, \dots, n_\omega \\ J_{HF}(\rho) \leq c_{HF} \end{aligned} \quad (12)$$

where ρ is the controller parameterization. In the comparison in the next section, the HF-constraint is only used in the optimization for the K_{PID} controller. c_{HF} is then chosen to be equal to the roll-off of the optimal \mathcal{H}_∞ controller to ensure equal HF robustness of the two controller structures. By use of the Horowitz–Sidi test, (12) is equivalent to

$$\begin{aligned} \min_{\rho} J_v(\rho) \quad \text{subject to} \\ \{d_S(\rho, k)\}_{k=1}^{n_\omega} \geq 0 \\ \{d_{KS}(\rho, k)\}_{k=1}^{n_\omega} \geq 0 \\ J_{HF}(\rho) \leq c_{HF} \end{aligned} \quad (13)$$

where the quantities in braces denote the closest distances between the nominal open loop and the Horowitz–Sidi sensitivity bounds and control sensitivity bounds at each frequency.

The optimization problem (13) is smooth but nonconvex. For some initial specifications c_S and c_{KS} , we use a constrained *global* optimization algorithm, DIRECT [26], to find a set of controller parameters ρ_0 reasonably close to a global optimum ρ^* .

Thereafter, we use a gradient-based *local* optimizer, SNOPT [27], to obtain more rapid convergence to ρ^* and to solve a sequence of nearby problems (13) as c_S and c_{KS} change slowly in a specified pattern.

We summarize the main features of DIRECT and SNOPT before describing the optimization strategy in detail.

A. Global Optimization

The original DIRECT algorithm of Jones *et al.* [28] finds the global minimum of a multivariate function $f(x)$ subject to

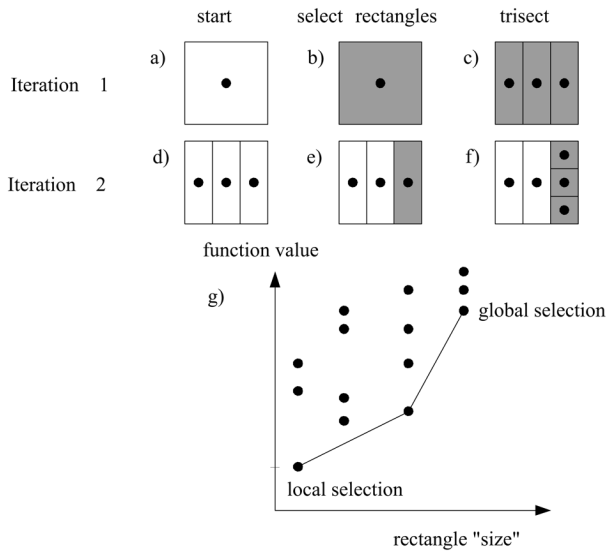


Fig. 6. (a)–(f) Two iterations of a 2-D example of the DIRECT algorithm, illustrating the partitioning of the search space. (g) Midpoint function values of sampled rectangles (dots) versus corresponding rectangle “size.” The solid line indicates the rectangles chosen by DIRECT for trisection.

simple bounds $x_L < x < x_U$, using no derivative information. The algorithm modifies the standard Lipschitzian approach [29]–[31] such that the need to specify a Lipschitz constant C is eliminated. Normally, C must be large because it should constrain the maximum rate of change of the objective function:

$$\|f(x) - f(x')\| \leq C\|x - x'\| \quad \forall x, x' \in [x_L, x_U].$$

The result is an emphasis on global rather than local search, leading to slow convergence. In contrast, DIRECT carries out simultaneous searches using different values of C (among all possible ones) and therefore operates on both the global and local level.

The search strategy is based on three steps: start, rectangle selection, and trisection. Fig. 6 shows the first two iterations of DIRECT for a 2-D example. In the first step, the center point of the initial rectangle is sampled [Fig. 6(a)]. Since there is only one rectangle in the first iteration, the entire search space is included in the rectangle that is selected in the second step [Fig. 6(b)]. In the third step, the search space selected in the second step is partitioned into three regions of equal size around the center point, and the center points of the outer thirds are then sampled. This step is called trisection and is illustrated in Fig. 6(c). The information from this step is then transferred to iteration 2 [Fig. 6(d)]. In the rectangle selection step, DIRECT determines that one, or more, of the existing rectangles has a better chance of including the global optimum. This rectangle is therefore selected [Fig. 6(e)] and trisected [Fig. 6(f)], and the algorithm proceeds to the third iteration. Fig. 6(g) illustrates the rectangle selection step, i.e., how DIRECT determines which rectangles to select for further investigation. In the figure, the function values for a number of sampled center points are plotted versus the corresponding rectangle “size” (measured by the distance from the rectangle center point to one of its corners). We first note that a pure global strategy would select the rectangle with “largest” size, while a pure local algorithm

would choose the rectangle with the least function value. DIRECT forms the lower convex hull of the sampled points and proceeds to the trisection step with all points on this curve simultaneously. Hence, it selects both the global and the local extremes but also some spaces with intermediate Lipschitz constants.

The bounds on x and the maximum number of function evaluations are the only tuning parameters in the procedure. Another appealing feature is that a global optimum can be found to any specified accuracy as long as the number of iterations is sufficient. The drawbacks are that rather tight bounds on x must be specified, and that a large number of iterations may be needed. DIRECT is also limited to low-dimensional problems (say, today less than 20 unknowns) because of its space-partitioning approach.

DIRECT is guaranteed to converge to the global optimal function value if the objective function is continuous in the neighborhood of a global optimum. (As the number of iterations goes to infinity, the set of points sampled by DIRECT forms a dense subset of an n -dimensional hypercube.)

While the original algorithm handles bound constraints only, the most recently developed DIRECT algorithm [26] handles nonlinear and integer constraints as well. The constrained problem is reformulated so that the constraints can be treated in a similar manner to the objective function. Both algorithms have been implemented in TOMLAB as the routines **glbFast** and **glcFast** [32], and they have been successfully used in train design optimization [33] and for the design of trading algorithms in computational finance [34].

B. Local Optimization

TOMLAB provides access from MATLAB to many other optimization algorithms, including the large-scale constrained solver SNOPT. For problems with smooth objective and constraint functions, SNOPT is a reliable *local* optimizer. It implements a sequential quadratic programming (SQP) algorithm and requires relatively few evaluations of the functions and their gradients.

Each major iteration of SNOPT linearizes the constraints and solves a QP subproblem to generate a search direction, along which an augmented Lagrangian merit function is reduced. SNOPT deals methodically with infeasible problems and infeasible QP subproblems, and it also takes advantage of a good starting point. These features are important for large and small problems alike. Given suitable starting points, SNOPT has proved effective for solving problems of the same type as (13). (Since analytic gradients are not available for the constraints in (13), SNOPT uses numerical differences.) The TOMLAB interface to SNOPT is denoted by **snopt**.

C. The Optimization Algorithm

Since **glcFast** can handle nonlinear constraints, it is suitable for locating a global optimum for (13) within specified upper and lower bounds on the independent variables. A maximum number of function evaluations **maxfun** must also be specified.

Our strategy is to choose an initial set of variables c_S and c_{KS} , and apply **glcFast** with reasonably wide bounds on ρ

but a moderate value of $maxfun$. When the global solver finds a feasible point or reaches the $maxfun$ limit, its best estimate ρ_0 is used as a starting point for **snopt**. If the local solver fails to converge, or analysis suggests that the result is not a global optimum, we call **glcFast** again with an increased $maxfun$, and then restart **snopt** with the new initial point. With this approach, the probability of finding the global minimizer ρ^* increases significantly compared to using local methods alone.

In the next step, c_{KS} is slightly increased and **snopt** is called directly with ρ^* as starting point, returning a new local solution that is likely to be a new global minimizer ρ^* (and so on). The complete design procedure is summarized as follows.

Algorithm 1:

- Step 1) Define the plant model and its uncertainty set Δ and specify c_S and c_{KS} .
- Step 2) Generate $B_S^L(\omega_k)$ and $B_{KS}^L(\omega_k)$ with QSYN.
- Step 3) Specify lower bounds ρ_L and upper bounds ρ_U for the PID parameters.
- Step 4) Run **glcFast** until a feasible point ρ_0 has been found. Typically $maxfun = 100\text{--}200$ is required.
- Step 5) Run **snopt** with ρ_0 (or the previous ρ^*) as starting point, and record the new ρ^* .
- Step 6) Evaluate ρ^* with respect to the proposed LF, MF, and HF measures as well as other system properties, especially in the time domain.
- Step 7) If needed, repeat from step 4) with an increased $maxfun$.
- Step 8) If needed, repeat from step 3) with different bounds ρ_L and ρ_U .
- Step 9) If needed, specify new c_S or c_{KS} , generate $B_S^L(\omega_k)$ and $B_{KS}^L(\omega_k)$ with QSYN, and repeat from step 5).

VI. EXAMPLES

Consider the following plant transfer functions:

$$G_1(s) = \frac{4s + 800}{Js^2 + d(1 + 0.08J)s + 16J + 200}$$

$$G_2(s) = \frac{e^{-\frac{0.4}{Q}}}{(Q + s)(Q + 0.5s)}$$

where $J \in [5 \ 15]$, $d \in [5 \ 10]$, and $Q \in [0.7 \ 1.3]$. $G_1(s)$ is a driveline model for heavy duty trucks with variable load inertia J and damping d . (A method to tune PI controllers for systems of type $G_1(s)$ can be found in [20].) $G_2(s)$ describes the influent dose rate to effluent concentration of a system with two liquid tanks in series and a variable flow Q . To reflect the magnitude of the uncertainties and their different characters, some Bode plots of the systems are shown in Figs. 7 and 8. The nominal plants are described by $J = 10$, $d = 7.5$ and $Q = 1$, and the time delay is modeled by a fourth-order Padé approximation.

The value sets for $G_1(s)$ and $G_2(s)$ are computed with the grid method. If an exact solution is required, the set $\{G_i(s)\}$ would have to include an infinite number of plant cases (since the uncertain parameters are defined in terms of intervals). Clearly, that would not lead to a practical method, and instead we discretize each uncertain parameter in 32 equidistant points. As in all numerical methods, an accurate final result can only be guaranteed if the gridding has been sufficiently dense. For both plants, the design parameters were first chosen as $c_S = 1.7$ and

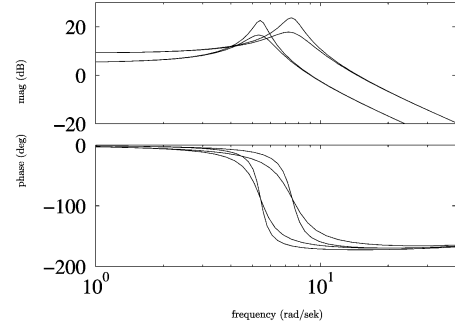


Fig. 7. Bode plots of $G_1(s)$ at the ends of the parameter intervals.

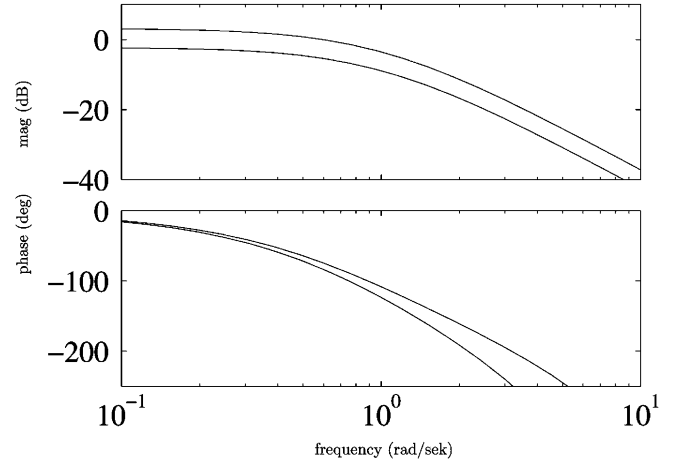


Fig. 8. Bode plots of $G_2(s)$ at the ends of the parameter intervals.

$c_{KS} = 1.5$, for which Horowitz-Sidi bounds for 25 frequencies were computed. Algorithm 1 was then performed for both an \mathcal{H}_∞ controller (choosing the scaling factor $\alpha = 1.005$) and a PID controller with a second-order filter. c_{KS} was gradually increased up to 15 to reflect less strict constraints on the control signal, and the entire procedure was repeated for $c_S = 1.5$. All calculations were done with MATLAB on a 1-GHz Pentium III. Note that the number of constraints in the optimization problem is $2n_\omega = 50$ for the \mathcal{H}_∞ design and $2n_\omega + 1 = 51$ for the K_{PID} controller (one extra because of the constraint on the HF roll-off).

A. Discussion

For illustration, we present some details on the \mathcal{H}_∞ design case with $c_S = 1.5$ and $c_{KS} = 1.5$. The bounds on the PID parameters $\rho = [k_i \ \zeta \ \tau \ \beta]^T$ were chosen to be $\rho_L = [0.1 \ 0.1 \ 0.01 \ 1]^T$ and $\rho_U = [10 \ 1 \ 1 \ 10]^T$. **glcFast** required 250 iterations (250 function evaluations, 60 s) to find a feasible solution to (13). With this solution as an initial point, **snopt** converged after 12 SQP iterations (150 function evaluations, 40 s). Fig. 9(a) shows the reduction in the merit function of **snopt**, and Fig. 9(b) shows how the logarithm of the feasibility measure (the norm-sum of the constraint violations) and optimality measure (the norm sum of the reduced gradients) [27] vary with iteration number. Note that the output from the global solver ρ_0 (input to the local solver) is feasible (satisfies all the constraints), and that the output from the local solver

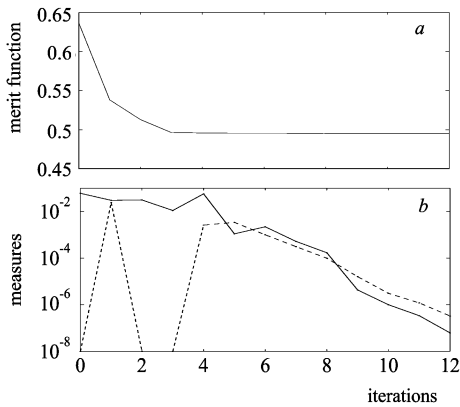


Fig. 9. Example (\mathcal{H}_∞ , G_1 , $c_S = 1.5$, and $c_{KS} = 1.5$) of convergence of **snopt**. (a) Merit function versus iteration number. (b) Feasibility measure (dashed line) and optimality measure (solid line) versus iteration number.

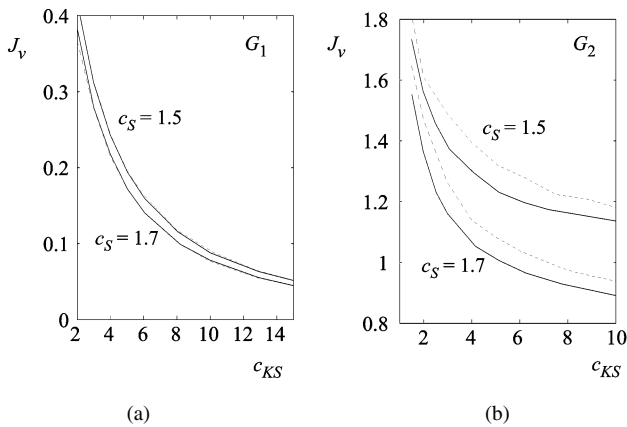


Fig. 10. LF performance (J_v) versus control activity (c_{KS}) as obtained by Algorithm 1 for (a) G_1 and (b) G_2 with PIDf control (solid line) and PID weighted \mathcal{H}_∞ control (dashed line).

ρ^* is feasible and optimal to within the specified tolerances of 10^{-6} . c_{KS} was then increased to 2 and the optimal ρ from the previous design was used as a starting point for **snopt**, without another global search. Convergence was achieved in four iterations (15 s).

This can be compared to 10–20 min of computation in [15] and [16] to solve a smaller problem than here. Fig. 10 shows the results of the optimization in terms of obtained J_v versus specified c_{KS} and c_S , and we note the general tradeoff between performance and control activity for all controllers. Thus, increased performance (reduced J_v) can be achieved without reducing the stability margin, but at a cost of higher control signals (increased c_{KS}). Importantly for both plants, Algorithm 1 resulted in two sets of controllers (\mathcal{H}_∞ and KPIDf) with equal J_{HF} values. This makes it easy to compare the two controller structures, because all closed loop properties that are not immediately compared are identically constrained. We see that the two controller structures perform similarly for both plants. This may be considered somewhat surprising, since the \mathcal{H}_∞ controller is of order six for G_1 and ten for G_2 , compared to three for the KPIDf controller. Although the weighting function in the \mathcal{H}_∞ design is of PID type, the resulting sixth order controller is obviously more restricted than a lowpass filtered PID controller of third order. The reason

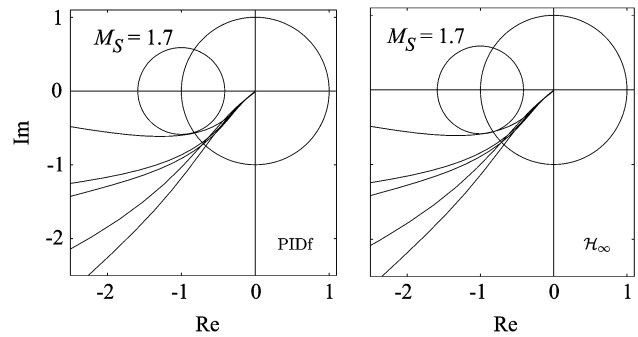


Fig. 11. Nyquist diagram for G_1 with controllers optimized for $c_S = 1.7$ and $c_{KS} = 10$. The five curves correspond to the cases $[J \ d] = [10 \ 7.5], [15 \ 10], [15 \ 5], [5 \ 5]$ and $[5 \ 10]$.

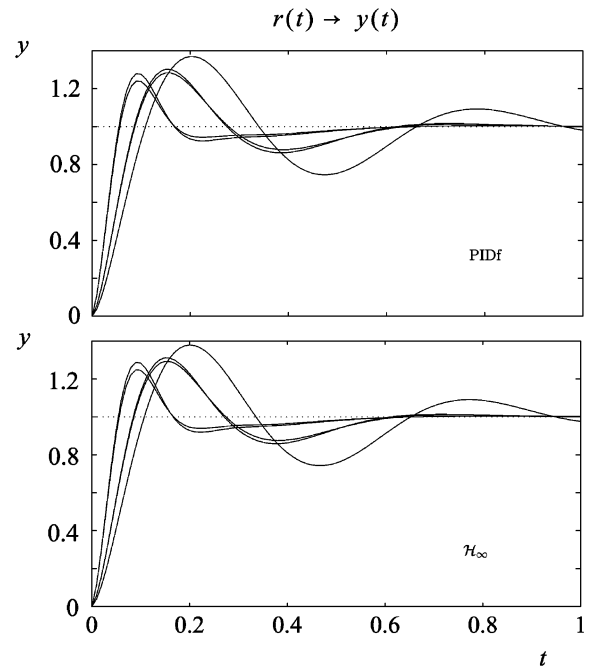


Fig. 12. Step responses from reference r to output y for G_1 with controllers optimized for $c_S = 1.7$ and $c_{KS} = 10$. The five curves correspond to the cases $[J \ d] = [10 \ 7.5], [15 \ 10], [15 \ 5], [5 \ 5]$, and $[5 \ 10]$.

is that the parameters in the third order controller may take any value in the optimization of (13), while the \mathcal{H}_∞ design means that the stability robustness for a specific uncertainty model, related to a normalized coprime factorization of the plant model, is optimized, cf. [21]. The benefit of SISO \mathcal{H}_∞ design is mainly for plants where an ordinary PID controller can be insufficient, for example, plants that are unstable, highly resonant, and non-minimum phase.

The algorithm resulted in nonconservative solutions for all specifications c_S and c_{KS} in the sense that both $d_S(\rho, k) = 0$ and $d_{KS}(\rho, k) = 0$ for at least one frequency ω_k (i.e., at least two constraints are always active). This is, in fact, a necessity for a global optimum, as pointed out by Gera and Horowitz [7]. The curves in Fig. 10 are smooth, further indicating that each point of the curves corresponds to a global optimum. This was also verified by running **glcFast** for several thousand iterations for each set of specifications. To investigate the impact of the parameter α on the \mathcal{H}_∞ design, α was changed from 1.005 to

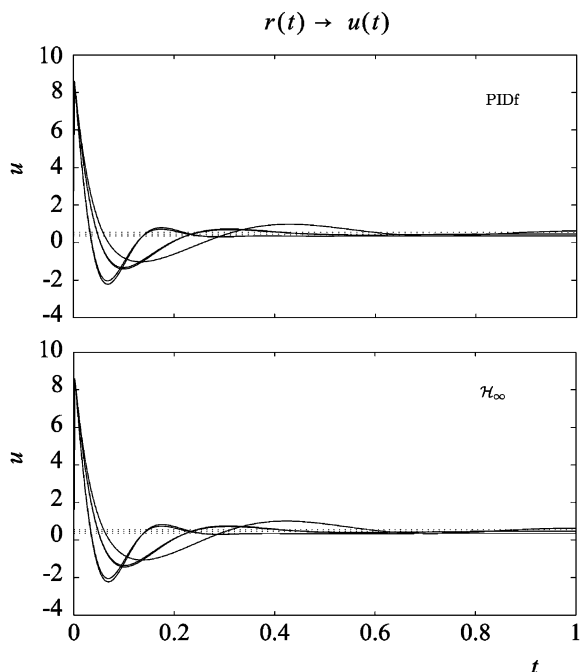


Fig. 13. Step responses from reference r to control signal u for G_1 with controllers optimized for $c_S = 1.7$ and $c_{KS} = 10$. The five curves correspond to the cases $[J \ d] = [10 \ 7.5], [15 \ 10], [15 \ 5], [5 \ 5]$, and $[5 \ 10]$.

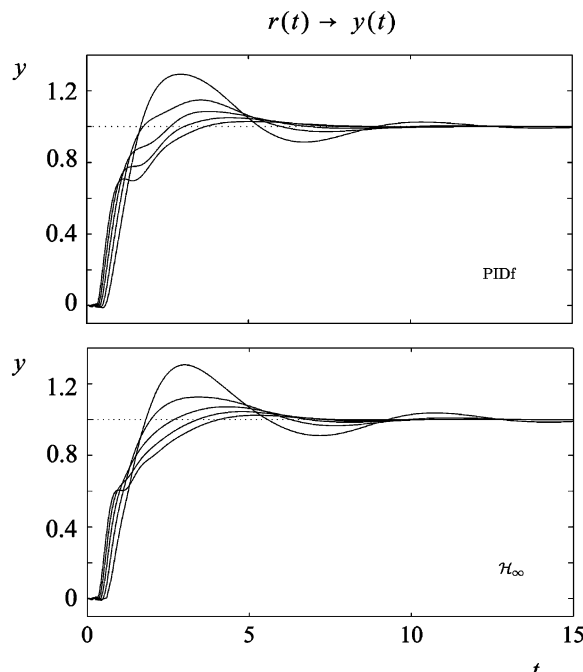


Fig. 15. Step responses from reference r to output y for G_2 with controllers optimized for $c_S = 1.7$ and $c_{KS} = 10$. The five curves correspond to the cases $Q = 0.7, 0.85, 1.0, 1.15$, and 1.3 .

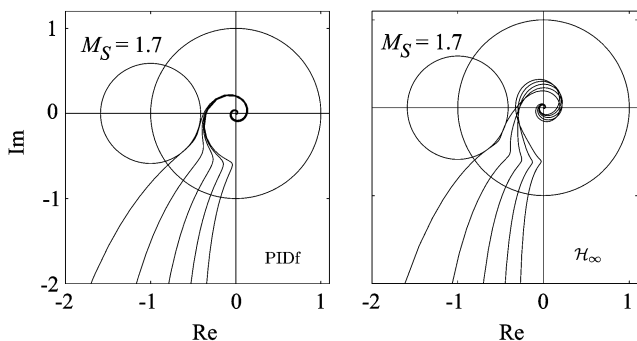


Fig. 14. Nyquist diagram for G_2 with controllers optimized for $c_S = 1.7$ and $c_{KS} = 10$. The five curves correspond to the cases $Q = 0.7, 0.85, 1.0, 1.15$, and 1.3 .

1.0005 and 1.05, respectively. It was concluded that the smaller value improved J_v by 1% and the larger value resulted in a 3% increase of J_v . A smaller value of α , however, implies a larger J_{HF} , which in turn results in deteriorating HF robustness properties.

We also choose to study Nyquist plots and step responses for both plants from reference signal $r(t)$ to output signal $y(t)$, and from reference signal $r(t)$ to control signal $u(t)$, using the controllers that result in $c_S = 1.7$ and $c_{KS} = 10$. Figs. 11–13 show these plots for $G_1(s)$ with both the PID controller and the \mathcal{H}_∞ controller for the following values of the uncertain parameters: $[J \ d] = [10 \ 7.5], [15 \ 10], [15 \ 5], [5 \ 5]$ and $[5 \ 10]$. Figs. 14–16 show the corresponding results for $G_2(s)$ for the flow rates: $Q = 0.7, 0.85, 1.0, 1.15$, and 1.3 .

The Nyquist plots verify that $M_S = 1.7$ for both plants, indicating that the approximations made when defining the Horowitz-Sidi bounds were acceptable. The step responses indicate that the closed loop performance for the two controller

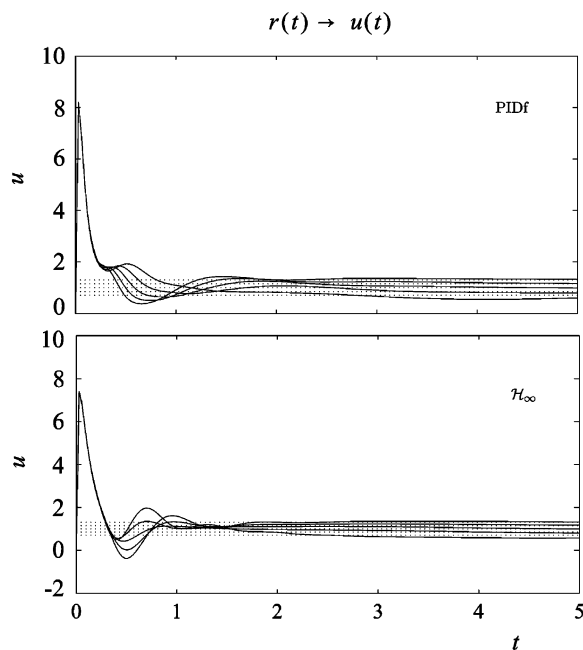


Fig. 16. Step responses from reference r to control signal u for G_2 with controllers optimized for $c_S = 1.7$ and $c_{KS} = 10$. The five curves correspond to the cases $Q = 0.7, 0.85, 1.0, 1.15$, and 1.3 .

structures is practically identical for $G_1(s)$, and almost the same for $G_2(s)$, as indicated by the trade-off curves in Fig. 10.

VII. CONCLUSION

An optimization method for the design of robust PID and \mathcal{H}_∞ loop-shaping controllers has been described. The new method includes a combination of global and local optimization algorithms and results in a fast algorithm with robust convergence towards a global optimum. A reliable test has also been given

to determine if the nominal open loop is (point wise) inside or outside the Horowitz–Sidi bounds in the Nichols chart.

The criteria used in the optimization procedure take into account important aspects for achieving robust control performance, including a guaranteed robustness to explicit plant uncertainties by use of Horowitz–Sidi bounds. Having separate criteria for the closed-loop properties in the different frequency regions facilitates the tradeoff between robustness and performance to be studied easily and clarifies the consequences of a change of specifications. The method also simplifies the task of comparing closed-loop performance between different controller structures, since closed loop properties in terms of stability robustness, control activity, and HF robustness are constrained identically.

The design method has been applied to two examples and it has been shown that a PID controller with a second-order filter on the derivative part achieves, more or less, the same low-frequency performance as an \mathcal{H}_∞ controller based on loop-shaping. Computationally, a substantial efficiency factor has been gained compared to an earlier, less general version of the design procedure.

REFERENCES

- [1] B. Kristiansson and B. Lennartson, "Robust and optimal tuning of PI and PID controllers," in *IEE Proc. Control Theory Appl.*, 2002, vol. 149, no. 1, pp. 17–25.
- [2] B. Lennartson and B. Kristiansson, "Pass band and high frequency robustness for PID control," in *Proc. 36th Conf. Decision Control*, San Diego, CA, Dec. 1997, pp. 2666–2671.
- [3] I. Horowitz, *Quantitative Feedback Design Theory (QFT)*, D. D. Wagman, Ed. Boulder, CO: QFT Publications, 1993.
- [4] P. O. Gutman, Qsyn, the Toolbox for Robust Control Systems Design for Use with Matlab [Online]. Available: www.math.kth.se/optsys/research/5B5782/index.html 1996
- [5] "MATLAB, Version 6, User's Guide," The Mathworks Inc., Natick, MA, 2000.
- [6] G. F. Bryant and G. D. Halikias, "Optimal loop-shaping for systems with large parameter uncertainty via linear programming," *Int. J. Control*, vol. 62, no. 3, pp. 557–568, 1995.
- [7] A. Gera and I. Horowitz, "Optimization of the loop transfer function," *Int. J. Control*, vol. 31, pp. 389–398, 1980.
- [8] A. C. Zolotas and G. D. Halikias, "Optimal design of PID controllers using the QFT method," in *IEE Proc. Control Theory Appl.*, 1999, vol. 146, no. 6, pp. 585–589.
- [9] G. D. Halikias, A. C. Zolotas, and R. Nandakumar, "Design of optimal robust fixed-structure controllers using the quantitative feedback theory approach," in *Proc. Inst. Mech. Engineers Part I–J. Syst. Control Eng.*, 2007, vol. 221, pp. 697–716.
- [10] O. Yaniv and M. Nagurka, "Design of PID controllers satisfying gain margin and sensitivity constraints on a set of plants," *Automatica*, vol. 40, pp. 111–116, 2004.
- [11] D. Garcia, A. Karimi, and R. Longchamps, "Robust proportional integral derivative controller tuning with specifications on the infinity-norm of sensitivity functions," *IET Control Theory Appl.*, vol. 1, no. 1, pp. 263–272, 2007.
- [12] S. Hara, T. Iwasaki, and D. Shiokata, "Robust PID control using generalized KYP synthesis—Direct open-loop shaping in multiple frequency ranges," *IEEE Control Syst. Mag.*, vol. 26, no. 1, pp. 80–91, Jan. 2006.
- [13] B. Kristiansson and B. Lennartson, "Simple and robust tuning of PI and PID controllers," *IEEE Control Syst. Mag.*, vol. 26, no. 1, pp. 55–69, Jan. 2006.
- [14] B. Kristiansson and B. Lennartson, "Evaluation and simple tuning of PID controllers with high frequency robustness," *J. Process Control*, vol. 16, no. 2, pp. 91–102, 2006.
- [15] C. M. Fransson, B. Lennartson, T. Wik, and P. O. Gutman, "On optimizing PID controllers for uncertain plants using Horowitz bounds," in *Proc. IFAC Workshop Digital Control: Past, Present, and Future of PID Control*, Terrassa, Spain, Apr. 2000, pp. 523–528.
- [16] C. M. Fransson, B. Lennartson, T. Wik, and P. O. Gutman, " \mathcal{H}_∞ control for uncertain plants using Horowitz bounds," in *Proc. Amer. Control Conf.*, Arlington, VA, Jun. 2001, vol. 1–6, pp. 4103–4107.
- [17] C. M. Fransson, B. Lennartson, T. Wik, K. Holmström, M. A. Saunders, and P. O. Gutman, "Global controller optimization using Horowitz bounds," presented at the IFAC World Congress, Barcelona, Spain, Jul. 2002.
- [18] C. M. Fransson, B. Lennartson, T. Wik, and K. Holmström, "Multi criteria controller design for uncertain MIMO systems using nonconvex global optimization," in *Proc. 40th Conf. Decision Control*, Orlando, FL, Dec. 2001, pp. 3976–3981.
- [19] T. Wik, C. M. Fransson, and B. Lennartson, "Feedforward feedback controller design for uncertain systems," in *Proc. 42nd Conf. Decision Control*, Maui, HI, Dec. 2003, pp. 5328–5334.
- [20] D. Galardini, M. Nordin, and P. O. Gutman, "Robust PI tuning for an elastic two-mass system," presented at the Eur. Control Conf., Brussels, Belgium, Jul. 1997.
- [21] D. McFarlane and K. Glover, "A loop shaping design procedure using \mathcal{H}_∞ synthesis," *IEEE Trans. Autom. Control*, vol. 37, no. 6, pp. 759–769, Jun. 1992.
- [22] J. Ackermann, *Robust Control*. Berlin, Germany: Springer-Verlag, 1993.
- [23] P. O. Gutman, M. Nordin, and B. Cohen, "Recursive grid methods to compute value sets and Horowitz-Sidi bounds," *Int. J. Robust Non-linear Control*, vol. 17, no. 2–3, pp. 155–171, 2007.
- [24] P. O. Gutman, C. Baril, and L. Neumann, "An algorithm for computing value sets of uncertain transfer functions in factored real form," *IEEE Trans. Autom. Control*, vol. 39, no. 6, pp. 1268–1273, Jun. 1994.
- [25] P. S. V. Nataraj and G. Sardar, "Template generation for continuous transfer functions using interval analysis," *Automatica*, vol. 36, pp. 111–119, 2000.
- [26] D. R. Jones, *The DIRECT Global Optimization Algorithm*. Norwell, MA: Kluwer, 2001.
- [27] P. E. Gill, W. Murray, and M. A. Saunders, "SNOPT: An SQP algorithm for large-scale constrained optimization," *SIAM J. Optimization*, vol. 12, no. 4, pp. 979–1006, 2002.
- [28] D. R. Jones, C. D. Perttunen, and B. E. Stuckman, "Lipschitzian optimization without the Lipschitz constant," *J. Optimization Theory Appl.*, vol. 79, no. 1, pp. 157–181, 1993.
- [29] E. Galperin, "The cubic algorithm," *J. Math. Anal. Appl.*, vol. 112, pp. 635–640, 1985.
- [30] J. Pinter, "Globally convergent methods for n-dimensional multiextremal optimization," *Optimization*, vol. 17, pp. 187–202, 1986.
- [31] B. Schubert, "A sequential method seeking the global maximum of a function," *SIAM J. Numer. Anal.*, vol. 9, pp. 379–388, 1972.
- [32] M. Björkman and K. Holmström, "Global optimization using the direct algorithm in Matlab," *Adv. Modeling Optim.*, vol. 1, no. 2, pp. 17–37, 1990.
- [33] M. Björkman and K. Holmström, "Global optimization of costly non-convex functions using radial basis functions," *Optim. Eng.*, vol. 1, no. 4, pp. 373–397, 2000.
- [34] T. Hellström and K. Holmström, "Parameter tuning in trading algorithms using ASTA," in *Computational Finance 1999*. Cambridge, MA: MIT Press, 1999.



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