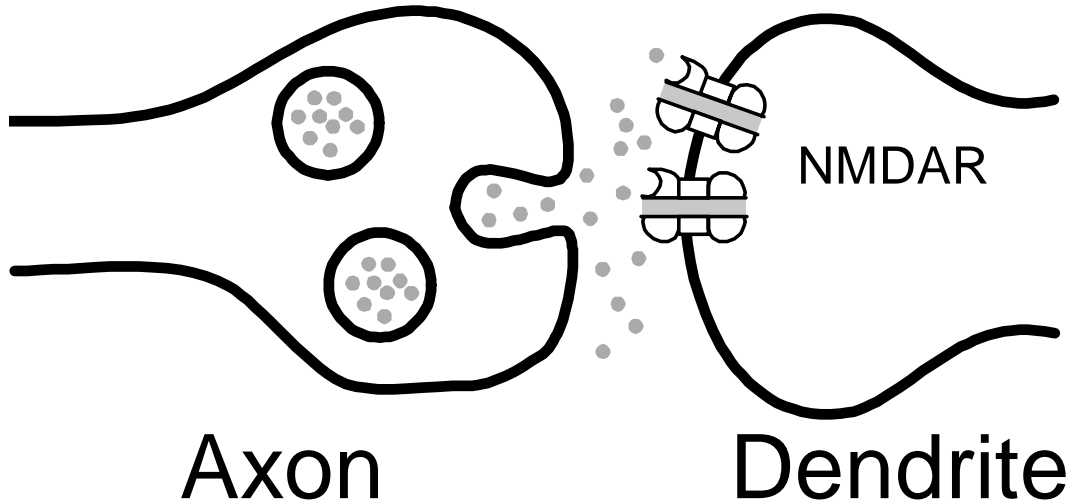


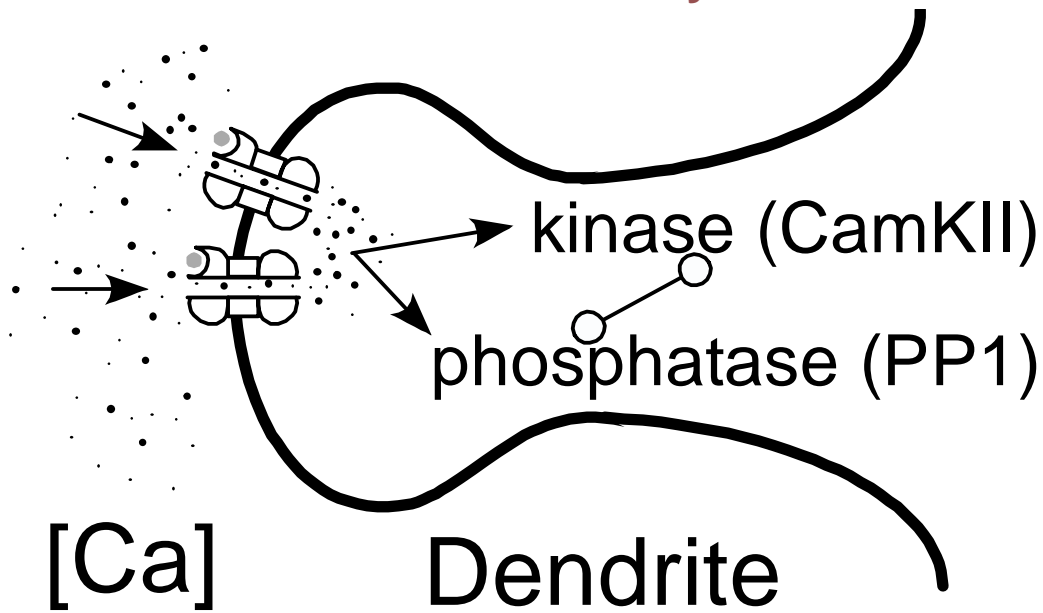
## Synaptic Plasticity-I: Spike Timing-Dependence



An axon terminal releases the neurotransmitter glutamate at an excitatory synapse

Activity drives changes in the efficacy of synapses .

## Calcium Influx Influences Plasticity



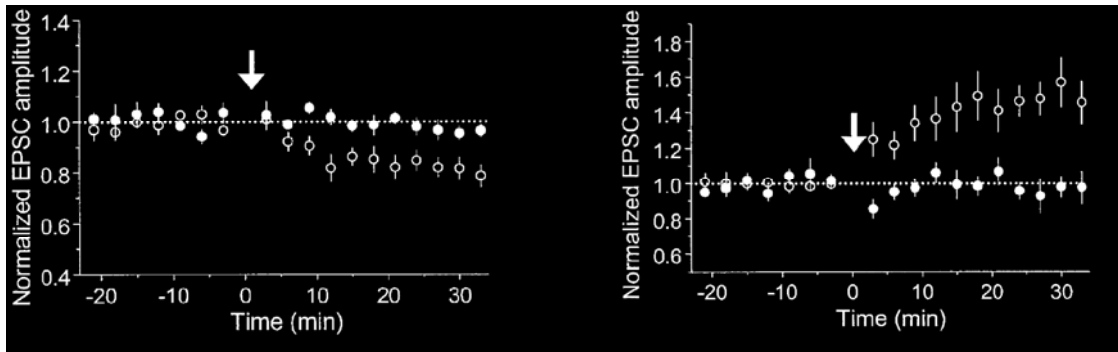
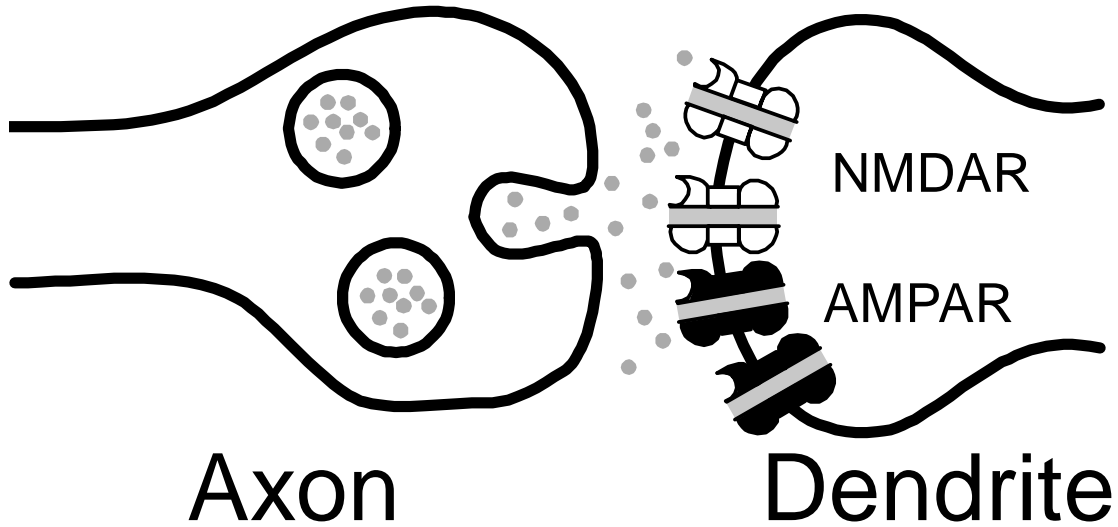
Calcium influences plasticity by activating a kinase pathway and a phosphatase pathway

When high calcium levels activate the kinase pathway (CamKII), the synapse undergoes long-term potentiation (LTP).

When moderate calcium levels activate the phosphatase pathway (PP1), the synapse undergoes long-term depression (LTD).



### Potentiation inserts AMPARs



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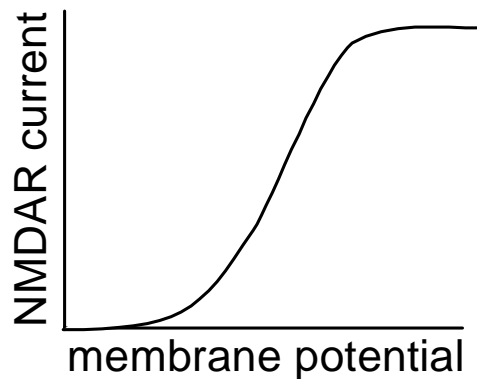
When a synapse is potentiated AMPARs are inserted into its membrane.

**CamKII inserts AMPARs into the synapse, whereas PP1 removes them.**

**What determines calciums influx?**



## NMDARs' Part



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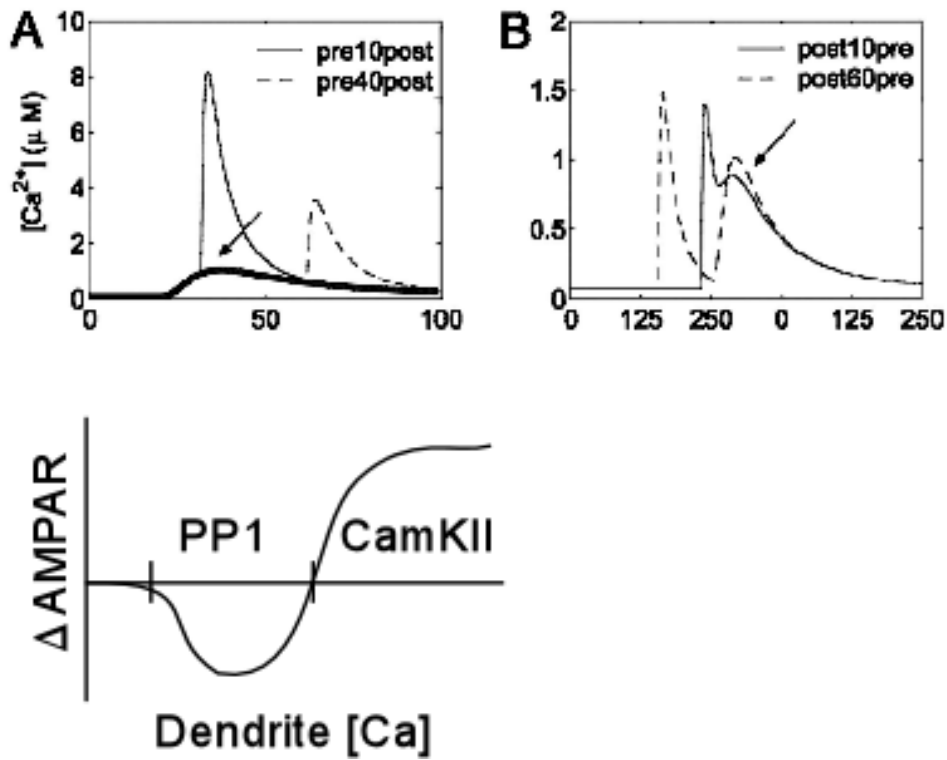
NMDARs gate current depending both on glutamate concentration and membrane potential.

**NMDARs allow calcium (and other cations) to flow into the synapse depending on the membrane potential, gating the level of calcium influx and the resulting plasticity.**

**How does timing influence NMDARs and calcium?**



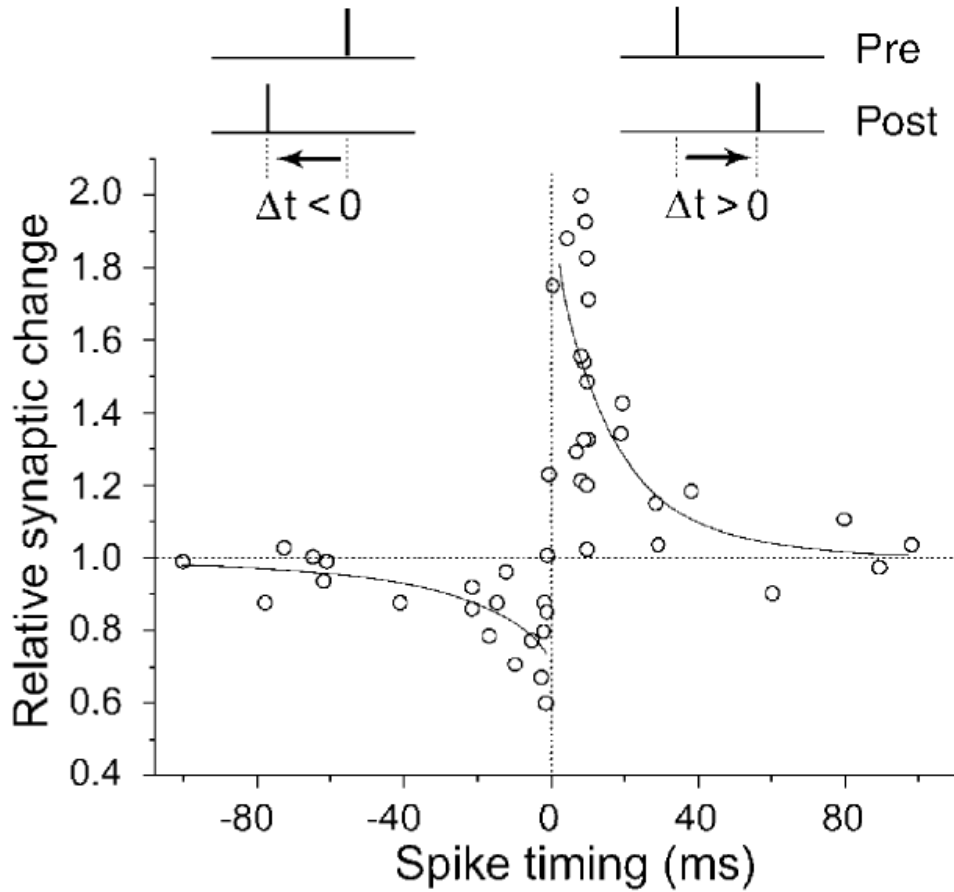
## The Role of Spike Timing



When presynaptic spike's precede postsynaptic spikes calcium levels rise higher than when the order is reversed.

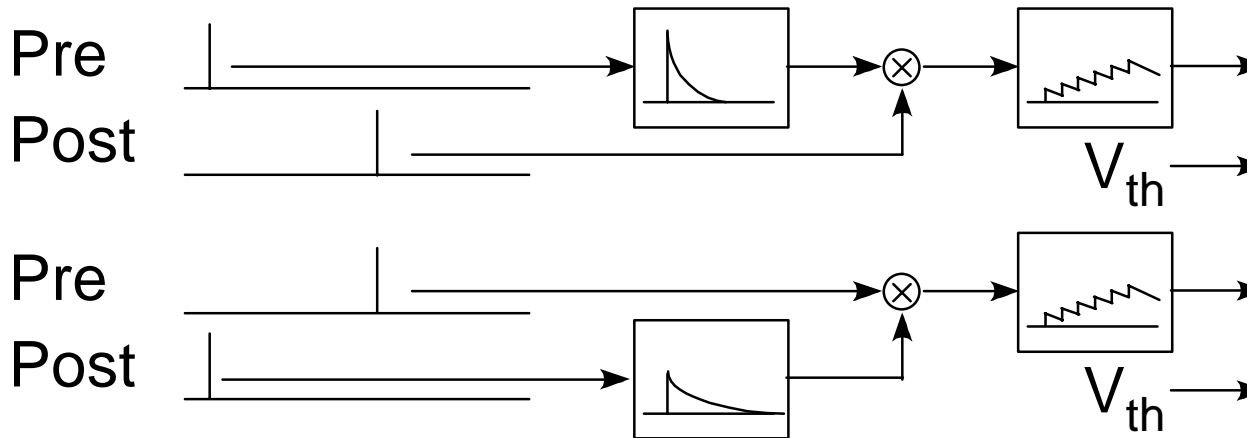
**Pre-before-post pairings result in high calcium, which drives LTP.**  
**Post-before-pre pairings result in moderate calcium, which drives LTD.**

## Spike Timing-Dependent Plasticity



Pre-before-post pairings result in LTP and Post-before-pre pairings result in LTD.

## A Model of STDP



The LTP and LTD implementation rely on delay elements and integrators.

**When a presynaptic spike occurs, a delay element is activated. When a subsequent postsynaptic spike occurs it samples the delay.**

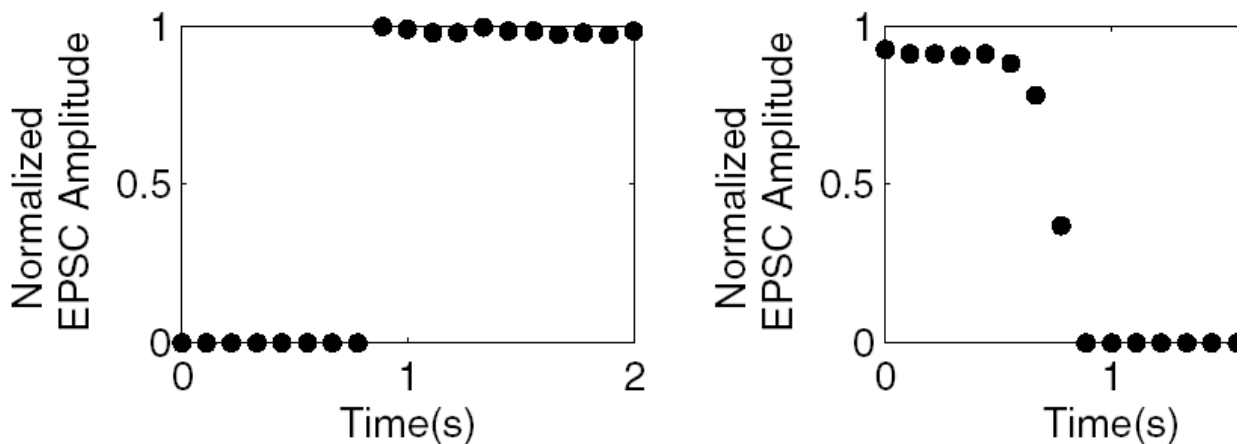
**The closer the two are together the larger the increment of the integrator element. If the integrator reaches a threshold, the synapse undergoes LTP.**

**LTD works the same but the roles of the pre- and post- synaptic spikes are reversed.**

**A state-holding element (binary) remembers which way last LTP or LTD and determines if AMPARs should be present at the synapse.**

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## LTP and LTD



LTP and LTD insert or remove all AMPARs from a synapse.

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## STDP Equations

$$LTP = n \text{Decay}[\text{tdiff}] - (n - 1) L_{int}$$

If we drive the STDP synapse repeatedly with a constant pre-before-post pairing, we can determine how many pairings,  $n$ , (at a constant rate) are required to cause  $LTP$  to exceed its threshold,  $v_{th}$ .

$\text{Decay}[\text{tdiff}]$  is the decay elements response to a pairing  $\text{tdiff}$  apart.

$L_{int}$ ; is the integrator's leak per cycle (at a given constant pairing rate).

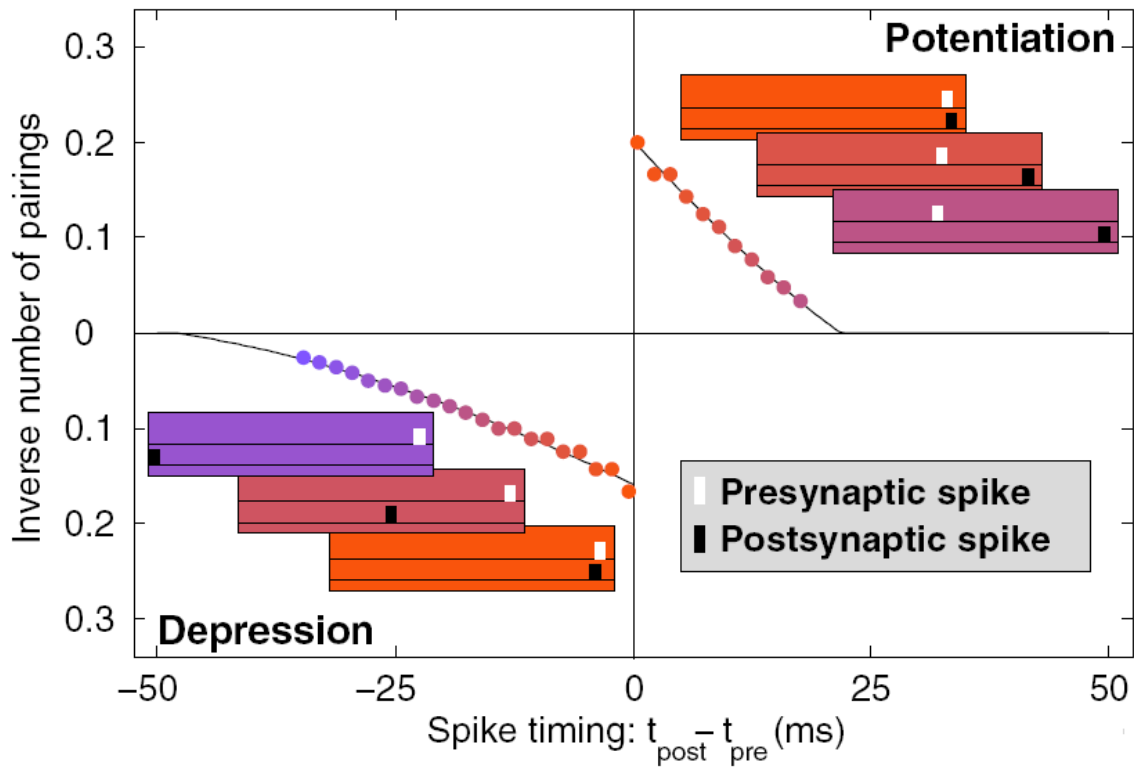
The same equations apply for depression, although the parameters may change.

We model `Decay[tdiff]` as a quadratic:

$$\text{Decay}[\text{tdiff}] = \left(1 - \frac{\text{tdiff}}{t_e}\right)^2, \quad \text{tdiff} < t_e$$

$$n = \frac{1}{\alpha \left(1 - \frac{\text{tdiff}}{t_e}\right)^2 - \beta}, \quad \frac{1}{n} = \alpha \left(1 - \frac{\text{tdiff}}{t_e}\right)^2 - \beta$$

## Spike Timing-Dependent Plasticity



Pre-before-post pairings result in LTP and Post-before-pre pairings result in LTD.