



Residential energy demand elasticities: what lessons can be learned from bottom-up and top-down methodologies

International Energy Workshop

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Outline

- Background - developing guidelines
- Energy demand elasticity \Leftrightarrow Energy service elasticity
- Conceptual differences: optimisation models \Leftrightarrow econometrics
- Bottom-up model
- Econometric approach
- Comparing results and conclusions
- Guidelines

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Background

- Energy optimisation models:
 - representing supply structure of energy service
 - in early nineties complemented with demand characteristics => service demand elasticities
 - energy service elasticities not observable
- Econometric methodology
 - Cointegration analysis: methodology for determining long term elasticities.
 - New estimation methods

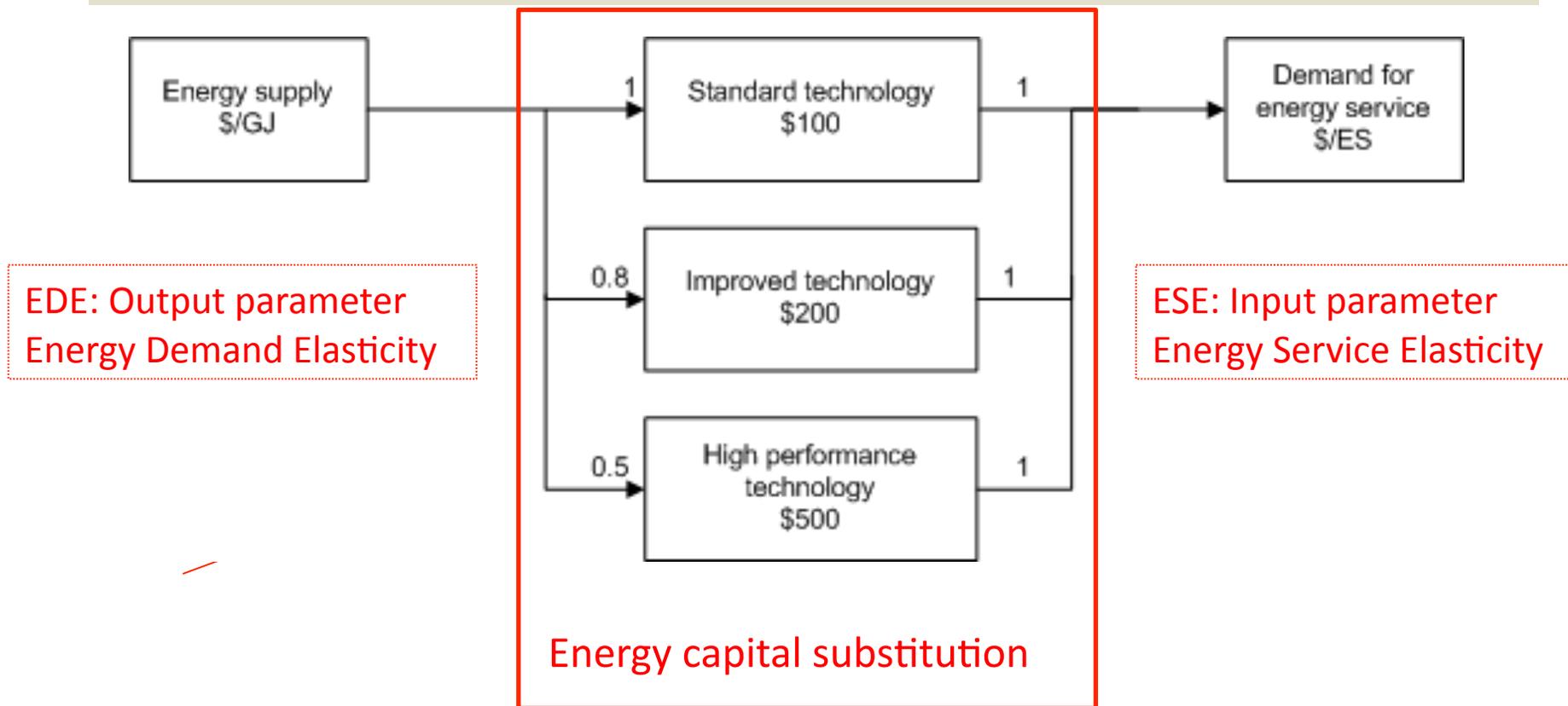
Objective

- → Providing guidance in quantifying energy service elasticities
- Indirect methodology
 - Developing relationship between energy demand and energy service elasticities
 - Comparing energy demand elasticities from state of the art optimisation model and econometric analysis

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Energy demand elasticity \Leftrightarrow Energy service elasticity



Energy demand elasticity \Leftrightarrow Energy service elasticity

$$PES = f(PK, PE)$$

$$\delta = Q_e \cdot P_e / (Q_k \cdot P_k + Q_e \cdot P_e)$$

= budget share of energy in ES

$$0 < \delta < 1$$

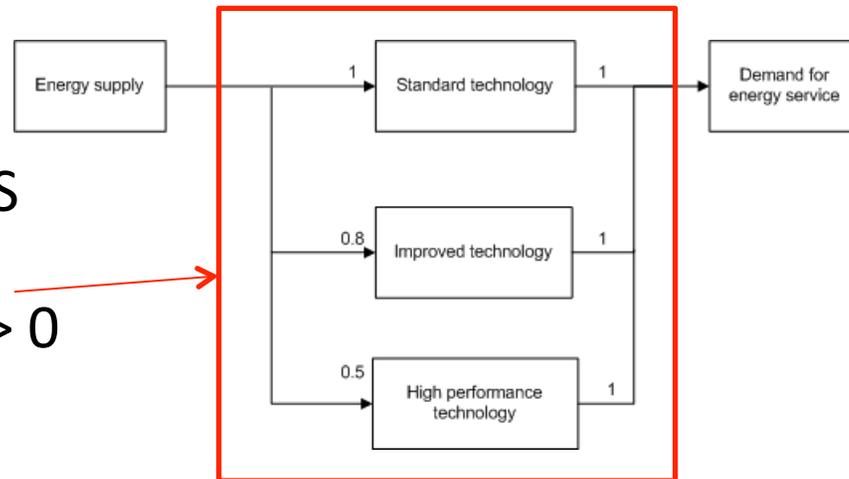
σ : elasticity of substitution > 0

$$EDE = -\sigma(1 - \delta) + \delta ESE$$

$EDE < ESE < 0$ if σ big

$ESE < EDE < 0$ if σ small

$ESE \nearrow$ then $EDE \nearrow$



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Conceptual differences

- Optimisation models
 - Economic reasoning
 - Price induced technology shifts
 - Future technology deployment
 - Competitive market
- Econometric models
 - Historical observations
 - Single parameter
 - Derived from historical (=paste) data
 - Historical market imperfections

Looks like we are comparing the incomparable

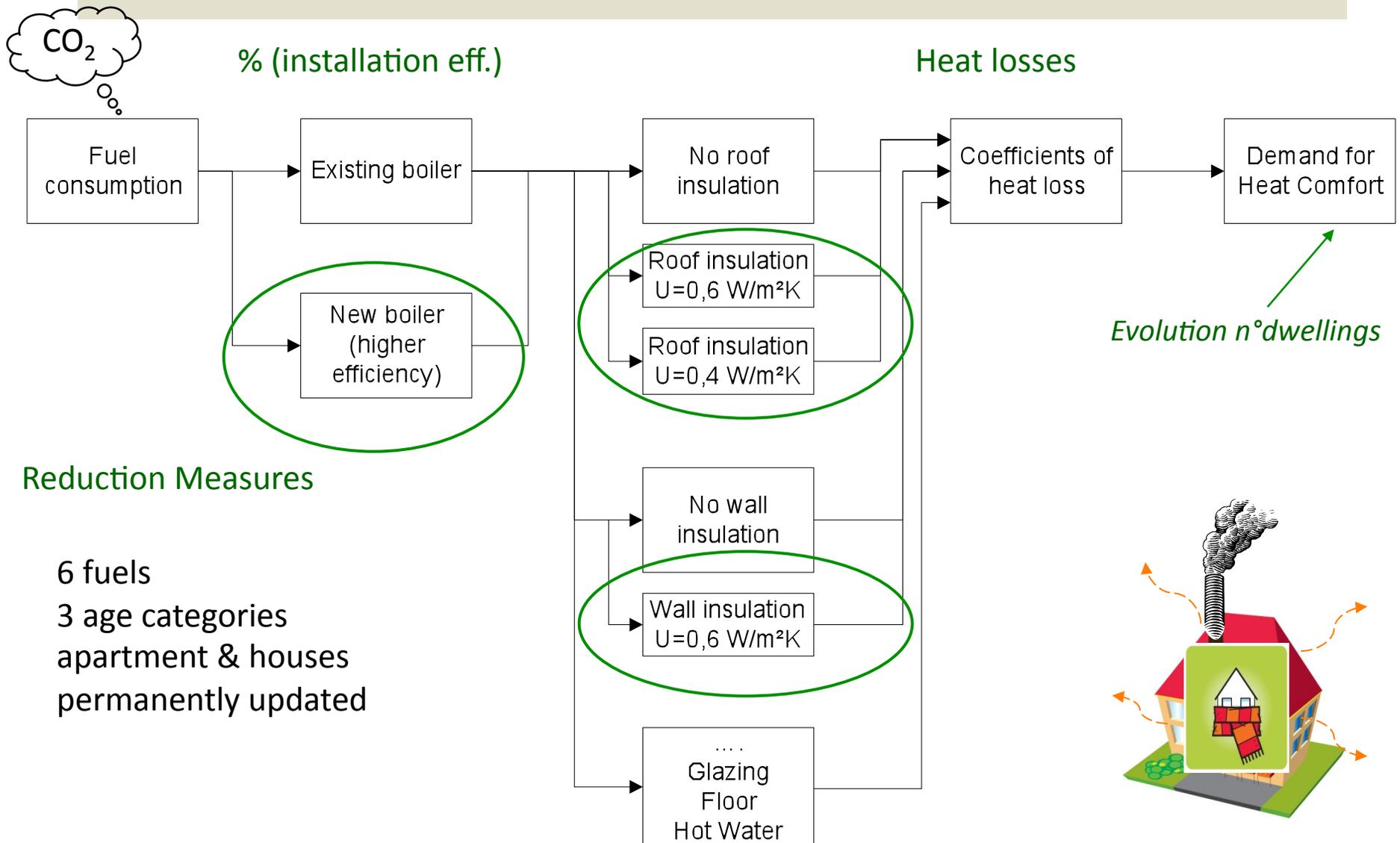
However

Both types of models used for similar policy analysis

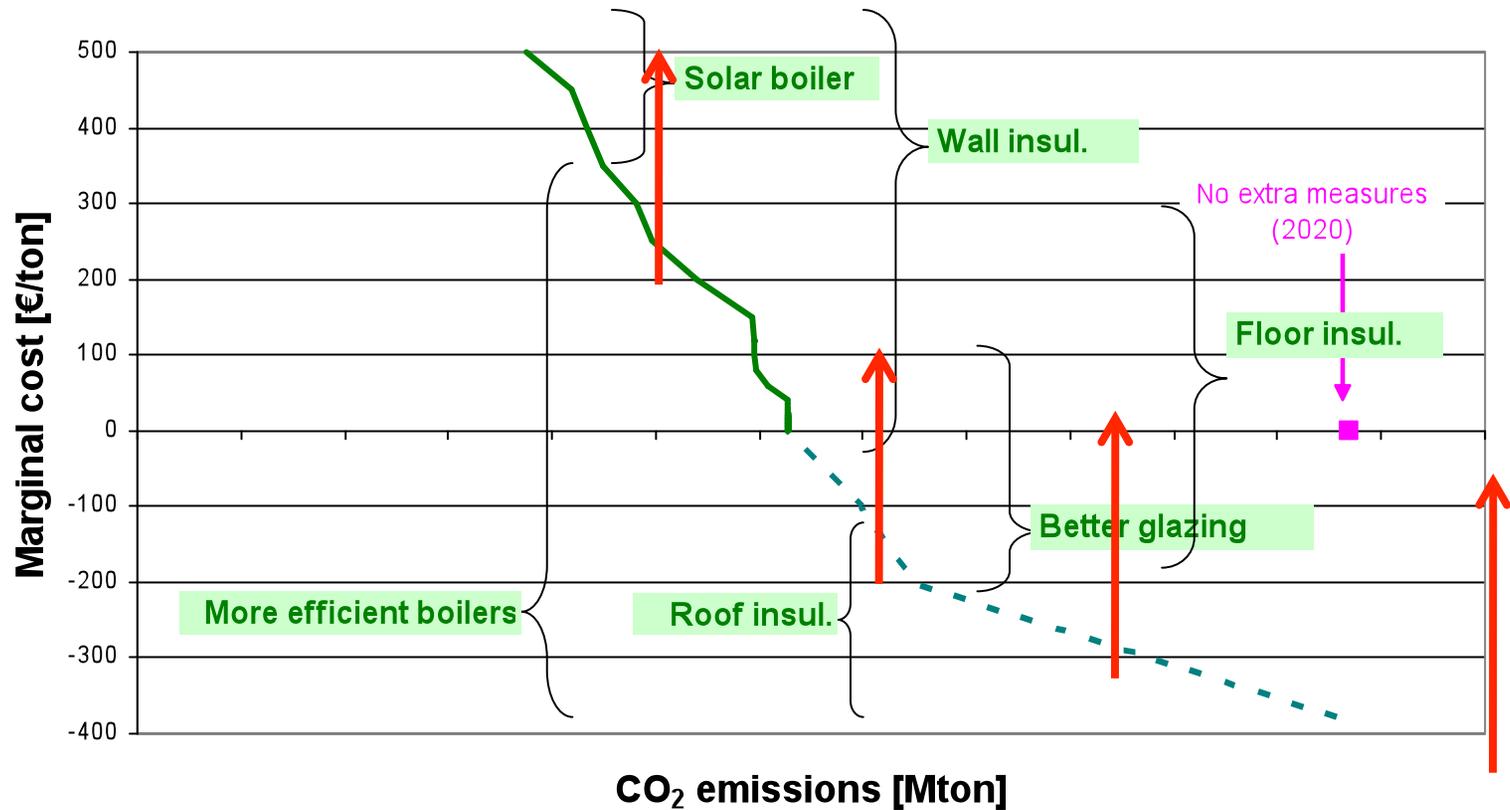
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Model Structure in Markal (1)



Overview of reduction measures



15 % Hurdle rate

Results

Hurdle rate: 15 %, Energy price increase: 20 %

| | | Total | Existing | New |
|------------|----------|-------|----------|-------|
| ESE = 0 | EDE | -0.63 | -0.25 | -1.43 |
| ESE = -0.2 | EDE | -0.78 | -0.42 | -1.53 |
| | δ | 0.75 | 0.86 | 0.50 |
| | σ | 2.52 | 1.76 | 2.84 |

Hurdle rate: 15 %, Energy price increase: 100%

| | | Total | Existing | New |
|------------|----------|-------|----------|-------|
| ESE = 0 | EDE | -0.23 | -0.16 | -0.38 |
| ESE = -0.2 | EDE | -0.39 | -0.31 | -0.54 |
| | δ | 0.78 | 0.76 | 0.82 |
| | σ | 1.04 | 0.65 | 2.13 |

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Panel cointegration approach

- Cointegration
 - Long term property of non-stationary time series.
 - Many economic time series are non-stationary
 - Appropriate methodology for long term elasticities
 - Avoiding spurious regressions
- Panel data
 - Short time dimension in the data
 - Panel dimension partly replaces time dimension in tests
 - Panel unit root tests: stationary character of panel time series
 - Panel cointegration tests: spurious character of regressions

Panel cointegration approach

- Yearly observations
 - Q: Log (fuel consumption)
 - Y: Log (real income)
 - P: Log (Price fuels /consumer price index)
 - hdd: Log (Heating degree days)
- Data from EUROSTAT
 - DK,FR,DE,IT,NL,ES,UK 1991-2008
 - SI 1992-2008
 - FI,HU,IE,PT 1995-2008
 - AT 1996-2008
- Homogeneous panel estimates: identical elasticities
- Heterogeneous panel estimates: country specific elasticities

Model specification - proposal

$$Q_{i,t} = \alpha_i + \beta_i Y_{i,t} + \gamma_i P_{i,t} + \theta_i hdd_{i,t} + \varepsilon_{i,t}$$

Unit root tests

| | Q | | Y | | P | | hdd | |
|--|--------|-----|--------|-----|--------|-----|--------|-----|
| DK | -2.747 | (0) | -0.561 | (0) | -1.628 | (1) | -2.316 | (0) |
| FR | -2.693 | (0) | -0.088 | (0) | 0.124 | (0) | -4.208 | (0) |
| DE | -3.770 | (0) | -1.790 | (0) | 0.422 | (0) | -3.027 | (0) |
| IT | -1.822 | (0) | -1.615 | (0) | -2.141 | (0) | -2.670 | (2) |
| NL | -1.397 | (0) | -1.335 | (0) | 0.787 | (0) | -2.944 | (0) |
| ES | -1.450 | (2) | -0.661 | (1) | -0.851 | (0) | -3.542 | (0) |
| UK | -2.492 | (0) | -1.610 | (0) | -0.192 | (2) | -2.844 | (0) |
| Panel Levin-Lin | -1.922 | | -1.300 | | 3.533 | | -4.514 | |
| N observations | 117 | | 118 | | 116 | | 117 | |
| Critical values: ADF -t- test 10 % -2.64, 5% -2.99, 1% -3.75 for 25 observations | | | | | | | | |
| Panel Levin-Lin test: 10 % -1.282, 5% -1.645, 1% -2.326 | | | | | | | | |

Unit root tests

- Conclusion:
 - Y: Log(real income): non-stationary
 - P: Log(real price): non-stationary
 - Hdd: Log(heating degree days): stationary
 - Q: Log(fuel consumption): ???
- ➔ Cointegration analysis requires all variables to be non-stationary

New approach

Step 1 : regression to determine elasticity of hdd

$$\Delta Q_{i,t} = \gamma_i + \theta_i^* \Delta hdd_{i,t} + \varepsilon_{i,t}$$

Step 2: Derive new time series, removing noise from hdd and perform new unit root test

$$Q_{i,t}^* = Q_{i,t} - \theta_i^* (hdd_{i,t} - \overline{hdd}_i)$$

Step 3: New model specification

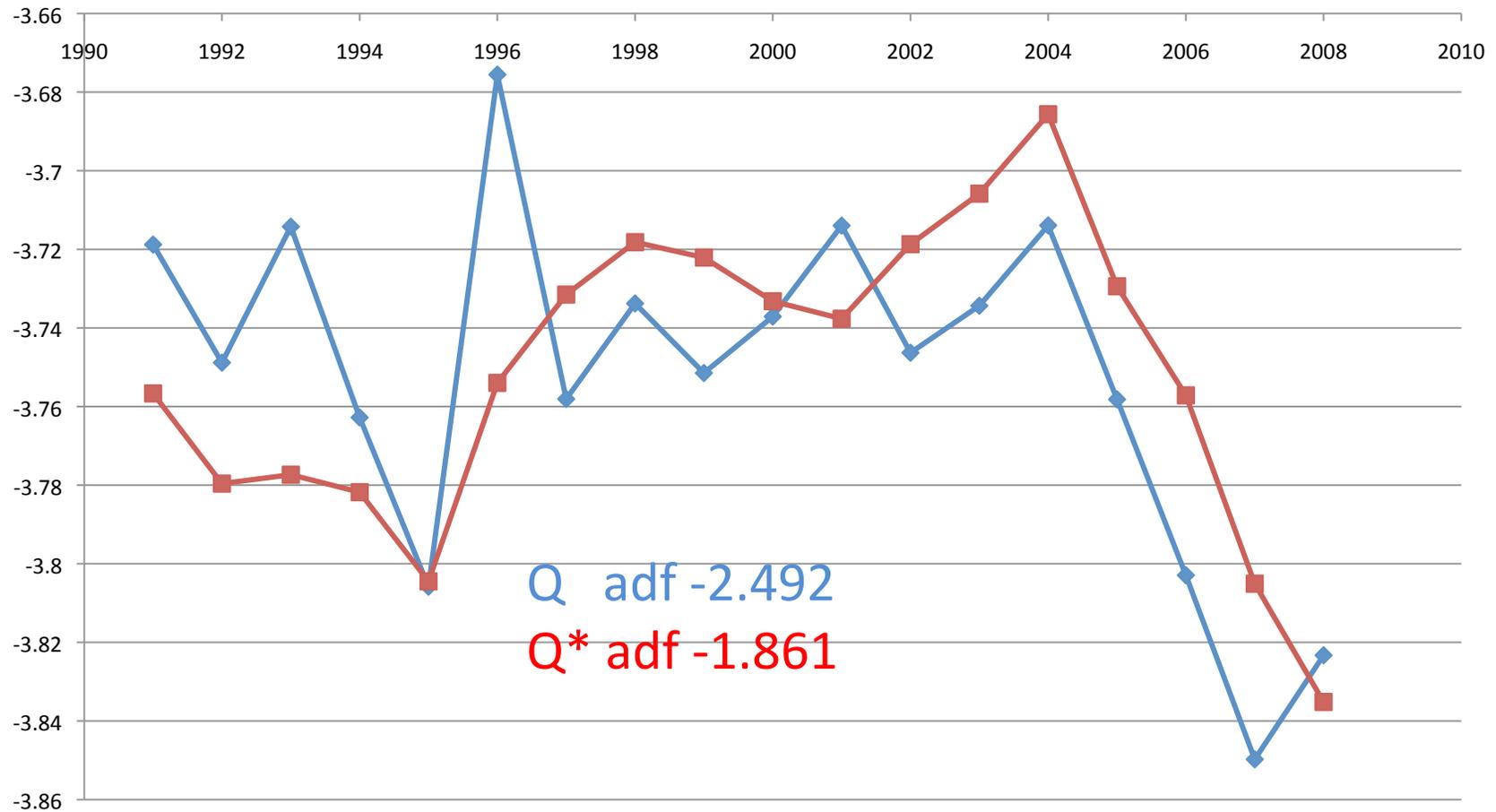
$$Q_{i,t}^* = \alpha_i + \beta_i Y_{i,t} + \gamma_i P_{i,t} + \varepsilon_{i,t}$$

New model specification

$$Q_{i,t}^* = \alpha_i + \beta_i Y_{i,t} + \gamma_i P_{i,t} + \varepsilon_{i,t}$$

| | θ^* estimate | Q^* Unit root test | |
|-----------------|------------------------|----------------------------|-----|
| DK | 0.567 | -1.685 | (0) |
| FR | 0.474 | -2.008 | (2) |
| DE | 0.597 | -2.339 | (0) |
| IT | 0.613 | -1.261 | (0) |
| NL | 0.745 | 0.515 | (0) |
| ES | 0.126 | -0.793 | (0) |
| UK | 0.734 | -1.861 | (2) |
| Panel Levin-Lin | | 1.221 | |
| N observations | | 115 | |

Q – Q* : example



Regressions: results

| | OLS | | DOLS | |
|-----------------|--------|-------|--------|-------|
| | Income | Price | Income | Price |
| AT | 0.32 | -0.20 | | |
| DK | 0.09 | 0.00 | 0.17 | 0.00 |
| FI | 0.00 | -0.14 | | |
| FR | 0.04 | -0.07 | 0.64 | -0.51 |
| DE | 0.57 | 0.00 | 0.96 | -0.07 |
| HU | 0.43 | -0.14 | | |
| IE | 0.22 | -0.01 | | |
| IT | 1.59 | -0.34 | 2.70 | -0.02 |
| NL | 0.00 | -0.30 | 0.05 | -0.30 |
| PT | 0.28 | -0.06 | | |
| SI | 0.10 | -0.08 | | |
| ES | 0.59 | 0.00 | 0.96 | -0.35 |
| UK | 0.08 | -0.18 | 0.36 | -0.02 |
| Homogenous N=7 | 0.31 | -0.10 | 0.56 | -0.10 |
| Homogenous N=13 | 0.25 | -0.11 | 0.46 | -0.10 |

Pedroni cointegration tests

| | heterogeneous-slope (N=7) | | homogeneous-slope (N=7) | | Full sample (N=13) |
|----------------------|---------------------------|-----------|-------------------------|--------|--------------------|
| | OLS | DOLS | OLS | DOLS | OLS |
| Panel v | 0.202 | -1.508 | -1.795 | -2.280 | 0.129 |
| Panel ρ | -0.154 | -0.258 | 1.496 | 1.352 | -0.661 |
| Panel t | -1.959** | -2.885*** | 1.364 | 0.906 | -4.138 *** |
| Panel t parametric | -2.238** | -3.023*** | 1.510 | 1.225 | -4.368 *** |
| Group ρ | 0.223 | 0.625 | 2.832 | 2.523 | 0.345 |
| Group t | -6.562*** | -4.311*** | 2.844 | 2.441 | -8.738*** |
| Group t parametric | -3.845*** | -2.898*** | 2.482 | 1.694 | -5.095*** |
| Critical values | Panel v | | Other | | |
| | 10% | 1.282 | -1.282 | * | |
| | 5% | 1.645 | -1.645 | ** | |
| | 1% | 2.326 | -2.326 | *** | |

Conclusions from econometric analysis

- DOLS slightly better than OLS
 - Higher income and price elasticities
- Energy price elasticity between - 0.5 and 0.
 - average -0.18
 - Values above -0.3 not exceptional
- Significant differences between countries
 - Homogeneous estimates rejected

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Comparing results and conclusions

- Optimisation model
 - Elasticity not constant
 - 20 % -> -0.63 100 % -> -0.23
 - $EDE <$ econometric result
 - ➔ suggesting $ESE = 0$ in this particular case
- Econometric analysis
 - Differences between countries suggesting that elasticities are not constant in time
- Some (expert) judgement still required

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Guidelines for ESE quantification

- Assume *EDE is known*
- Determine δ and σ (3 model runs)
 - Price increase and $ESE = 0 \rightarrow EDE1$
 - Arbitrary $ESE2 \rightarrow ED2$
 - $\delta = (ED1-ED2)/ES2$, $\sigma = ED1/ (\delta - 1)$

$$\sigma \left(\frac{A}{A} \right) = \left(\frac{A}{A} + \left(\frac{A}{A} \right) (1 - \frac{A}{A}) \right) / \left(\frac{A}{A} \right)$$

Thank you for your attention