Measurement of the vector character of electric fields by optical second-harmonic generation

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We present a scheme for the determination of the vector nature of an electric field by optical second-harmonic generation. We demonstrate the technique by mapping the two-dimensional electric-field vector of a biased transmission line structure on silicon with a spatial resolution of \( \sim 10 \, \mu \text{m} \). © 1999 Optical Society of America

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The capability of measuring electric fields with ultrafast time resolution is of interest and importance for both fundamental and technological reasons. A promising new technique for probing transient electric fields is optical second-harmonic generation (SHG). SHG has been employed to detect electrical pulses and microwave signals in transmission line structures as well as freely propagating terahertz radiation. This method, which utilizes the nonresonant material response of the sample, provides exceptional time resolution. For current experimental implementations with state-of-the-art mode-locked lasers, a response time of \( \sim 10 \, \text{fs} \) may be expected. The approach of field-induced SHG complements the powerful and well-established laser-based techniques of electro-optic and photoconductive sampling. The principle for extracting information on the vector components of the electric field \( \mathbf{E}^0 \) of interest can be seen by examination of the field-induced nonlinear polarization at the second-harmonic (SH) frequency:

\[
P_i^{(2)} = \sum_{jkl} \chi_{ijkl}^{(3)} E_j^{\omega} E_k^{\omega} E_l^{0}. \tag{1}
\]

Here \( \mathbf{E}^{\omega} \) denotes the pump laser field at fundamental frequency \( \omega \) and \( \chi_{ijkl}^{(3)} \) is the third-order nonlinear susceptibility tensor that is responsible for the field-induced SHG process. With respect to optical measurements, we can describe this nonlinear material response in the presence of field \( \mathbf{E}^0 \) as an effective second-order nonlinear susceptibility of \( \chi_{ijk}^{(2),\text{eff}} = \sum_{l} \chi_{ijkl}^{(3)} E_l^{0} \).

In terms of this formulation, the extraction of the field vector \( \mathbf{E}^0 \) is conceptually clear. One performs appropriate measurements of the SHG process to determine the relevant values of \( \chi_{ijk}^{(2),\text{eff}} \) and \( \chi_{ijkl}^{(3)} \) can then be inferred from a comparison of \( \chi_{ijk}^{(3)} \) and the known (or separately measured) values of \( \chi_{ijkl} \). Here we restrict our attention to materials of cubic or higher symmetry. In this case the form of \( \chi_{ijk}^{(3)} \) is considerably simplified, having as independent elements only \( \chi_{iii}, \chi_{ijj}, \chi_{ijj}, \) and \( \chi_{ijji} \), where \( \{i, j\} = \{x, y, z\} \) and \( i \neq j \) correspond to the crystalline axes. Two useful relations that follow for symmetry-allowed elements of \( \chi_{ijk}^{(2),\text{eff}} \) are

\[
\chi_{iii}^{(2),\text{eff}} = \chi_{iii} E_i^0, \tag{2a}
\]

\[
\chi_{ji}^{(2),\text{eff}} = \chi_{ji}^{(3)} E_i^0. \tag{2b}
\]


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Either of these equations alone is, in principle, sufficient for deducing all three components of $E^0$. If we consider a pump laser field that is polarized along the $y$ direction, Eqs. (2) yield

$$\chi_{xyy}^{(2), \text{eff}} = \chi_{xyy}^{(3)} E_y^0,$$

$$\chi_{yyy}^{(2), \text{eff}} = \chi_{yyy}^{(3)} E_y^0,$$

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By measuring the SH signals for various polarization configurations and incidence angles, we can obtain the effective susceptibilities $\chi_{xyy}^{(3)}$ and $\chi_{yyy}^{(3)}$, as is well established for surface SHG measurements.\(^7\) From an appropriate set of calibration measurements, we can thus determine the sign of the field- and field-independent background, as was the case in this instance.\(^8\) The measured SH intensity polarized along direction $i$ then becomes

$$I_{2\omega,i} \propto |E_{\text{ref},i}^{2\omega} + E_{\text{FD},i}^{2\omega}|^2 = |E_{\text{ref},i}^{2\omega}|^2 + 2 E_{\text{ref},i}^{2\omega} E_{\text{FD},i}^{2\omega}.$$ 

Hence it follows from Eqs. (4) and (5) that $I_{2\omega,i} \propto E_{\text{FD},i}^{2\omega}$.

Figure 1 illustrates the experimental setup schematically. The source of the SH probe radiation is a mode-locked Ti:sapphire laser, which produces pulses of 60-fs duration at a wavelength of 775 nm and a repetition rate of 80 MHz. The $y$-polarized laser beam is focused at normal incidence on the silicon sample with an average power of 180 mW. Before it reaches the sample, the fundamental beam is transmitted through a dichroic beam splitter. The beam then passes through a z-cut quartz crystal of 250-$\mu$m thickness, which generates the SH reference beam that is required for the homodyne detection scheme.\(^11\) The SH radiation arising from both the sample and reference is detected by the dichroic beam splitter and, after it passes through appropriate filters and a polarizer, is detected with gated photon-counting electronics. Both $x$ and $y$ polarizations of the SH radiation were detected.

Our sample was a silicon-on-sapphire substrate on which aluminum strip lines were deposited. The electrode geometry, shown in Fig. 1, consists of two 750-$\mu$m $\times$ 750-$\mu$m rectangular pads that are separated by 80-$\mu$m. Since the photon energy for the pump radiation in this measurement lay slightly above the bandgap, the absorption of pump radiation led to a certain degree of heating ($<$1 K) as well as to carrier generation in the sample. To reduce these effects one should choose a source of radiation with a photon energy lying below the bandgap. The sample was ion implanted, which rendered the 0.6-$\mu$m-thick silicon epilayer isotropic and the metallic contacts ohmic. Ion implantation also reduced the carrier lifetime significantly, thereby decreasing the screening of the bias field by the photogenerated carriers.\(^12\) For purposes of illustration a bias voltage of 360 V, corresponding to an average electric-field strength of approximately 45 kV/cm, was applied across the electrodes. The resistance between the electrodes had an average value of 5 M$\Omega$ under laser irradiation, similar to the value without laser exposure, and no appreciable current-induced heating was observed. The sensitivity of this technique has been established to be $\sim$100 (V/cm)/Hz$^{1/2}$, which should be amenable to
further optimization through improvements in laser and material parameters. We sampled the electric-field components by scanning along the x axis for each y position at 10-μm increments in a 180 μm x 180 μm square grid (inset of Fig. 1). For each sampling point the total data-collection time was 8 s, with a typical count rate of 10^5 Hz. The measurements were made differentially by subtraction of the signal in the absence of the electric field from that for an applied bias. The spatial resolution, which corresponds to a SH beam diameter of 14 μm at the sample, was determined by measurement of the change in the SH signal as the reference beam traveled across the boundary between the silicon and the metallic electrode.

Using the formalism discussed above, we obtained the in-plane components, E_0^x and E_0^y, of the field E_0 at each grid point. Figure 2 shows the resulting vector map of the electric field. Notice that in the area between the electrodes the electric field is aligned along the x direction, as expected. We attribute the weak irregularities in the electric-field direction that can be seen in certain spatial regions to local imperfections and inhomogeneities in the substrate and electrode structure. In the region beyond the end of the electrodes we observe the expected fringing pattern. The electric field in this region has both x and y components, which can be comparable, especially near the corners of the electrodes. Because of the finite spatial resolution of the SHG probe, the inferred amplitude of the electric field at grid points adjacent to the electrodes is reduced and, conversely, finite values for the electric field are found for grid points just inside the electrodes. Well inside the electrodes, no electric field was detected within experimental uncertainty.

A necessary step in this experiment is the calibration of the SH response for electric-field components along each of the x and y directions. For this purpose an applied field directed at an angle of 45° with respect to the polarization of the input laser beam was produced by rotation of the sample about its surface normal. Comparing the SH signals that were polarized along the original orthogonal axes of the analyzer, we then obtained the relative sensitivity of the measurement to the orthogonal components of E_0. An absolute calibration of sensitivity can also be made in this fashion, assuming that the strength of the electric field for the calibration is already known.

To summarize, we have presented a general scheme for measuring the vector character of electric fields by use of SHG, and we have demonstrated the method by mapping the spatial distribution of the in-plane electric field in a silicon sample. We are exploring the application of this technique to the study of the dynamics of changing polarization states of high-frequency electric fields.

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