

Test Description	Order of data	$X\beta$	Hypothesis Test
<p>One-sample t-test. 6 observations</p>	<p>G_1 G_2 G_3 G_4 G_5 G_6</p>	$\begin{pmatrix} 1 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1 \end{pmatrix} \begin{pmatrix} \beta_1 \end{pmatrix}$	<p>H_0: Overall mean=0 H_0: $\beta_1=0$ H_0: $c\beta=0$ $c=[1]$</p>
<p>Two-sample t-test. 5 subjects in group 1 (G1) and 5 subjects in group 2 (G2)</p>	<p>$G1_1$ $G1_2$ $G1_3$ $G1_4$ $G1_5$ $G2_1$ $G2_2$ $G2_3$ $G2_4$ $G2_5$</p>	$\begin{pmatrix} 1 & 0 \\ 1 & 0 \\ 1 & 0 \\ 1 & 0 \\ 1 & 0 \\ 0 & 1 \\ 0 & 1 \\ 0 & 1 \\ 0 & 1 \\ 0 & 1 \end{pmatrix} \begin{pmatrix} \beta_{G1} \\ \beta_{G2} \end{pmatrix}$	<p>H_0: mean of G1 different from G2 H_0: $\beta_{G1} - \beta_{G2} = 0$ H_0: $c\beta = 0$ $c = [1 \ -1]$</p>
<p>Paired t-test. 5 paired measures of A and B.</p>	<p>A_{S1} B_{S1} A_{S2} B_{S2} A_{S3} B_{S3} A_{S4} B_{S4} A_{S5} B_{S5}</p>	$\begin{pmatrix} 1 & 1 & 0 & 0 & 0 & 0 \\ -1 & 1 & 0 & 0 & 0 & 0 \\ 1 & 0 & 1 & 0 & 0 & 0 \\ -1 & 0 & 1 & 0 & 0 & 0 \\ 1 & 0 & 0 & 1 & 0 & 0 \\ -1 & 0 & 0 & 1 & 0 & 0 \\ 1 & 0 & 0 & 0 & 1 & 0 \\ -1 & 0 & 0 & 0 & 1 & 0 \\ 1 & 0 & 0 & 0 & 0 & 1 \\ -1 & 0 & 0 & 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} \beta_{diff} \\ \beta_{S1} \\ \beta_{S2} \\ \beta_{S3} \\ \beta_{S4} \\ \beta_{S5} \end{pmatrix}$	<p>H_0: A is different from B H_0: $\beta_{diff} = 0$ H_0: $c\beta = 0$ $c = [1 \ 0 \ 0 \ 0 \ 0 \ 0]$</p>
<p>Two way ANOVA. Factor A has two levels and factor B has 3 levels. There are 2 observations for each A/B combination.</p>	<p>$A1B1_1$ $A1B1_2$ $A1B2_1$ $A1B2_2$ $A1B3_1$ $A1B3_2$ $A2B1_1$ $A2B1_2$ $A2B2_1$ $A2B2_2$ $A2B3_1$ $A2B3_2$</p>	$\begin{pmatrix} 1 & 1 & 1 & 0 & 1 & 0 \\ 1 & 1 & 1 & 0 & 1 & 0 \\ 1 & 1 & 0 & 1 & 0 & 1 \\ 1 & 1 & 0 & 1 & 0 & 1 \\ 1 & 1 & -1 & -1 & -1 & -1 \\ 1 & 1 & -1 & -1 & -1 & -1 \\ 1 & -1 & 1 & 0 & -1 & 0 \\ 1 & -1 & 1 & 0 & -1 & 0 \\ 1 & -1 & 0 & 1 & 0 & -1 \\ 1 & -1 & 0 & 1 & 0 & -1 \\ 1 & -1 & -1 & -1 & 1 & 1 \\ 1 & -1 & -1 & -1 & 1 & 1 \end{pmatrix} \begin{pmatrix} \beta_{mean} \\ \beta_{A1} \\ \beta_{B1} \\ \beta_{B2} \\ \beta_{A1B1} \\ \beta_{A1B2} \end{pmatrix}$	<p>F-tests for all contrasts</p> <p>H_0: Overall mean=0 H_0: $\beta_{mean} = 0$ H_0: $c\beta = 0$ $c = [1 \ 0 \ 0 \ 0 \ 0 \ 0]$</p> <p>$H_0$: Main A effect=0 H_0: $\beta_{A1} = 0$ H_0: $c\beta = 0$ $c = [0 \ 1 \ 0 \ 0 \ 0 \ 0]$</p> <p>$H_0$: Main B effect=0 H_0: $\beta_{B1} = \beta_{B2} = 0$ H_0: $c\beta = 0$ $c = \begin{bmatrix} 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 \end{bmatrix}$</p> <p>$H_0$: A/B interaction effect=0 H_0: $\beta_{A1B1} = \beta_{A1B2} = 0$ H_0: $c\beta = 0$ $c = \begin{bmatrix} 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \end{bmatrix}$</p>