



aa.stanford.edu



damicos@stanford.edu  
people.stanford.edu/damicos



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# Pose Estimation of Uncooperative Spacecraft using Monocular Vision

Sumant Sharma

sharmas@stanford.edu

# Problem Statement

Utilizing a 3D model of an uncooperative target spacecraft in conjunction with monocular vision from a servicer spacecraft to estimate pose of the target relative to the servicer



[prismasatellites.se](http://prismasatellites.se)

# Overview

- Motivation
- Survey of state-of-the-art pose estimation
- Initial Pose Estimation
- Model Processing
- Image Rendering
- Comparative Assessment



## **ORBITAL EXPRESS VISCAM2**

COURTESY: [HTTP://ARCHIVE.DARPA.MIL/ORBITALEXPRESS/MISSION\\_UPDATES.HTML](http://archive.darpa.mil/orbitalexpress/mission_updates.html)

# PRISMA Mango

Avstånd: 7,6982 m

Radie: 1,3464 m

Apparent diameter: 17° 07' 20,8"

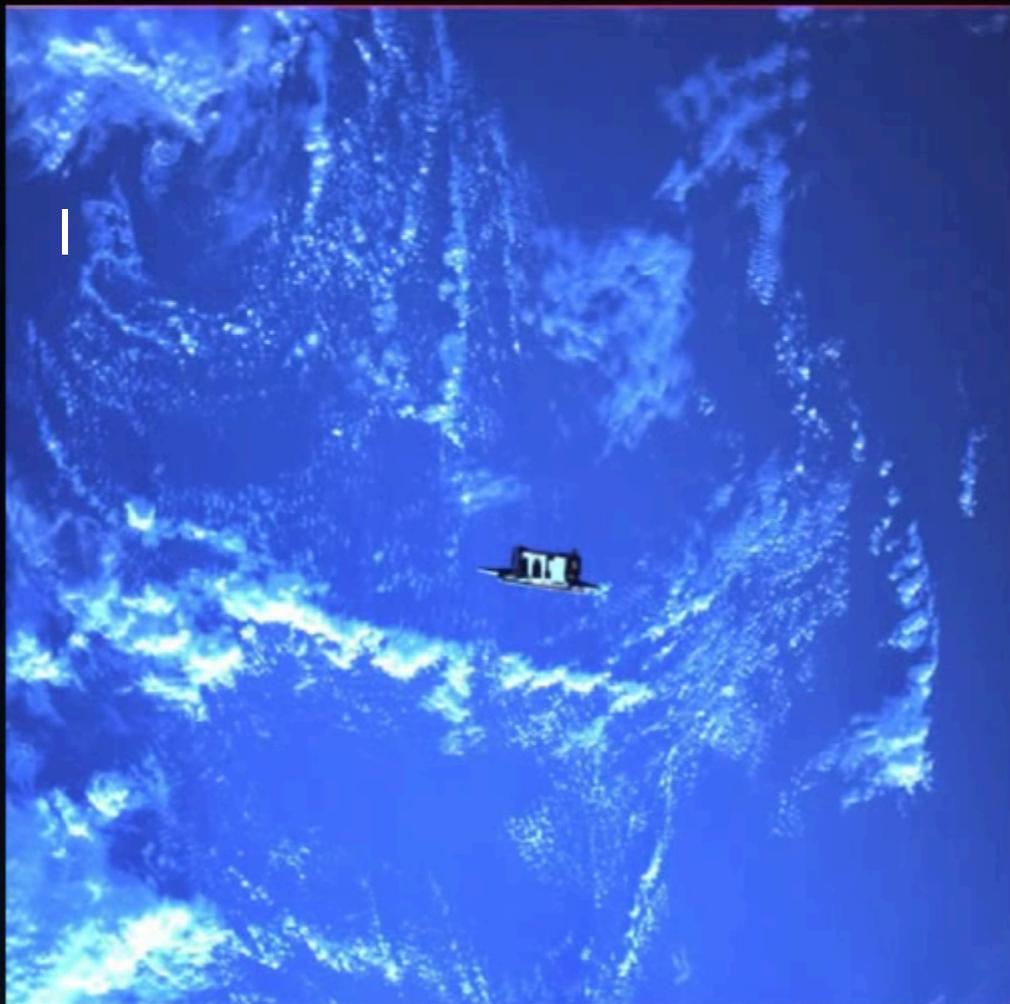
Phase angle: 94,0°

2010 Sep 14 19:55:21 UTC

20x snabbare



**PRISMA PR Camera**  
Courtesy: OHB Sweden



Hastighet: 0,00000 m/s

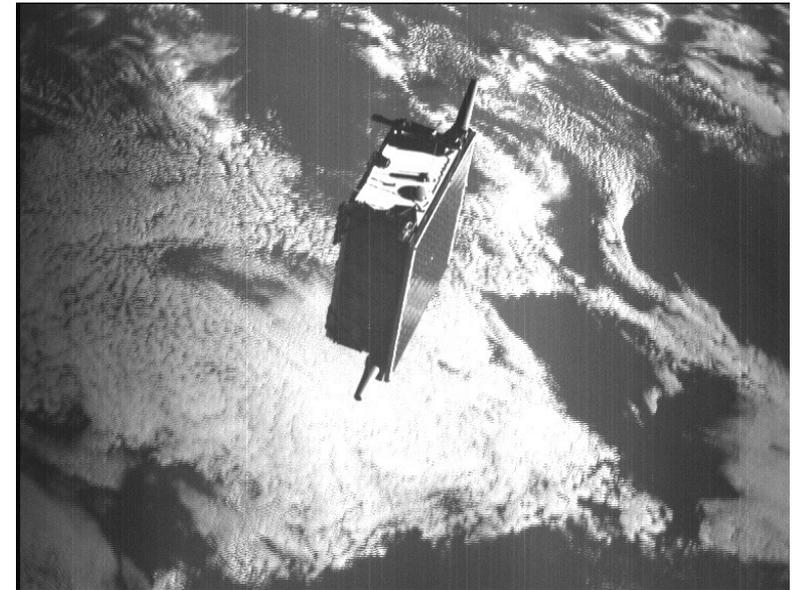
synkronisera omloppsbanan

Synfält: 26° 42' 59,3" (1,00x)

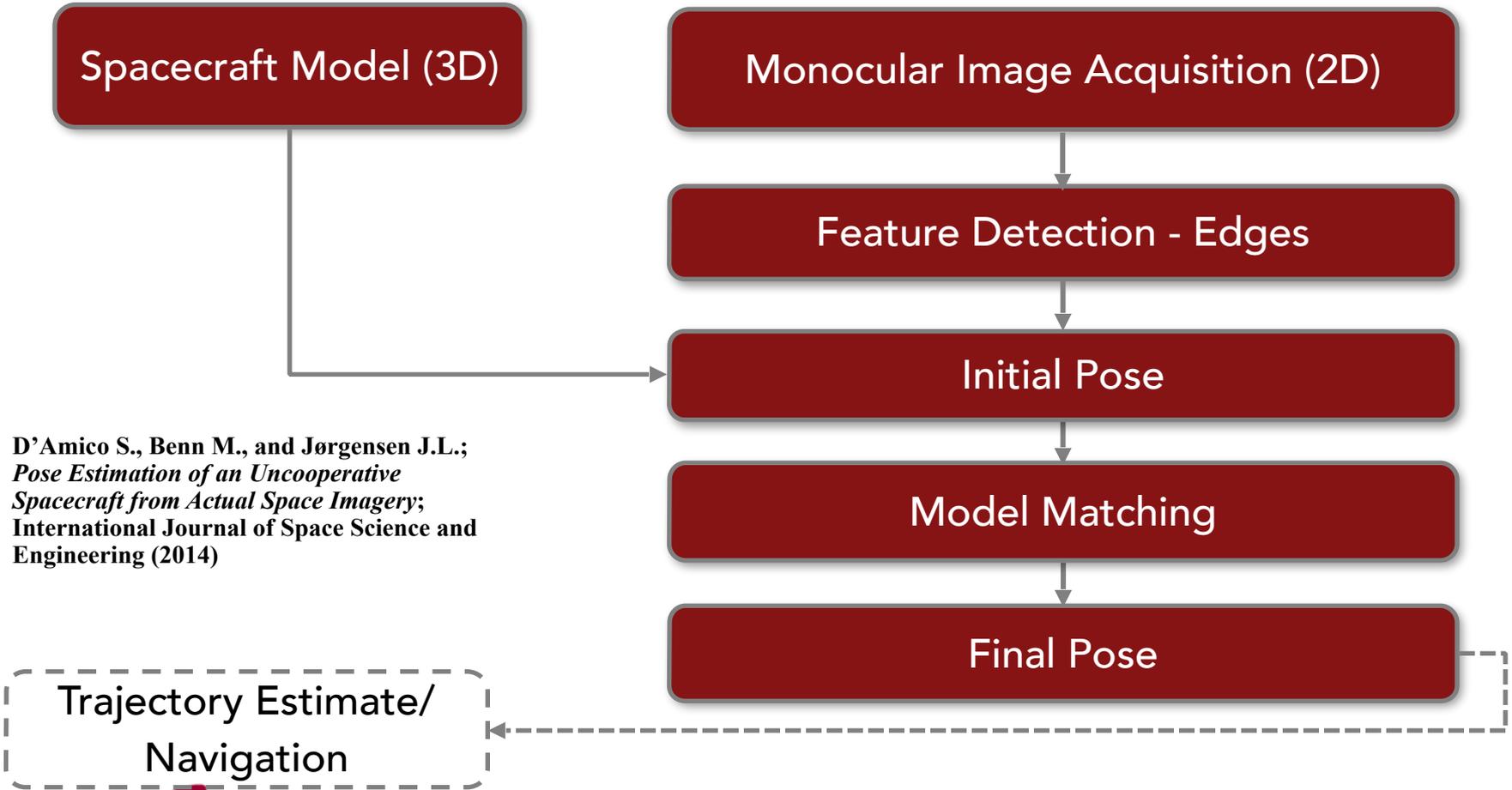
# Challenges



- Carrier-to-Noise Ratio
- Scene illumination
- Processing limitations
- Low image acquisition rate
- Background interaction
- Occlusion
- Lack of depth information



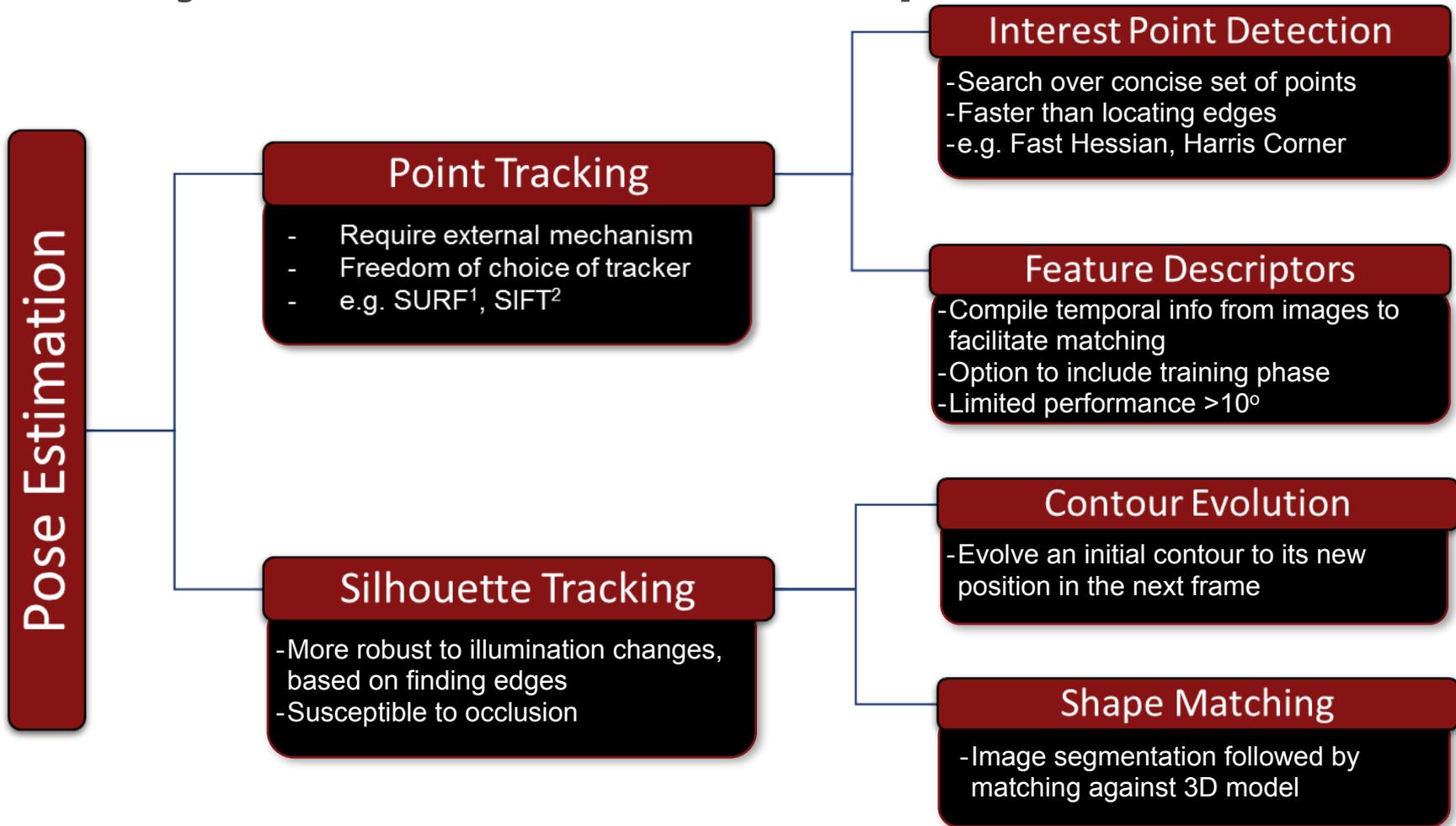
# Previous Work



D'Amico S., Benn M., and Jørgensen J.L.;  
*Pose Estimation of an Uncooperative  
Spacecraft from Actual Space Imagery;*  
*International Journal of Space Science and  
Engineering* (2014)

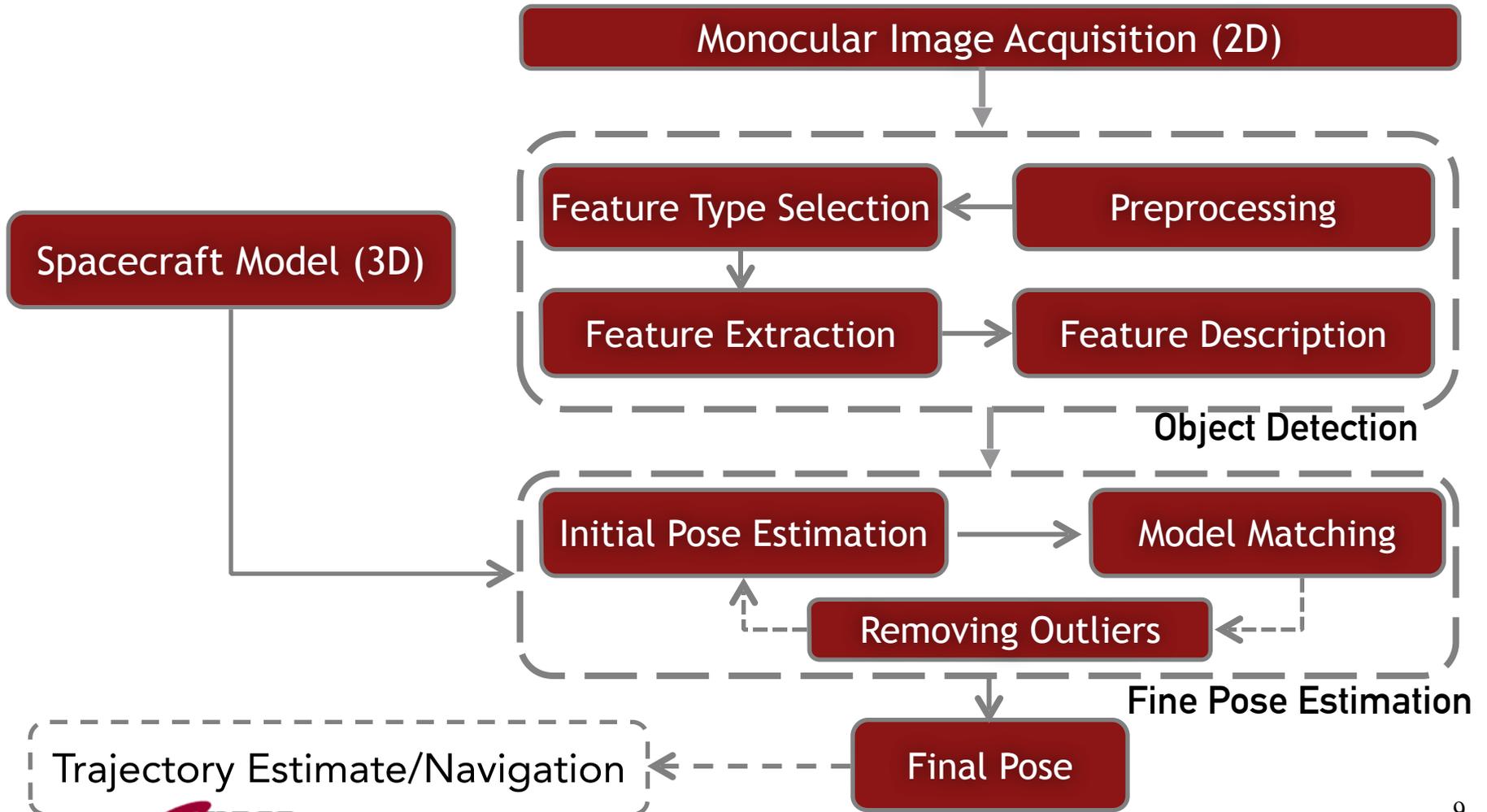


# Survey of Pose Estimation Techniques

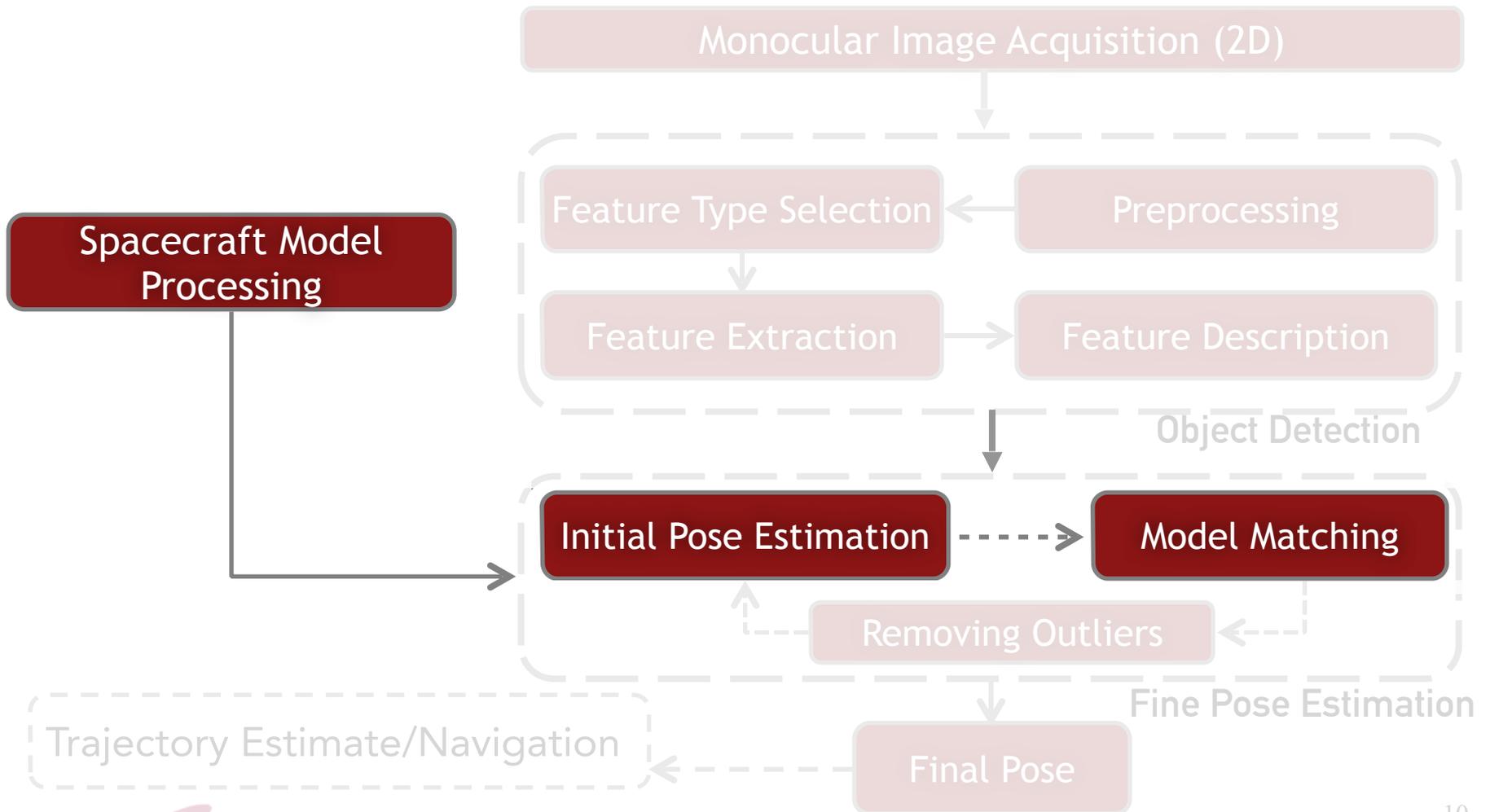


<sup>1</sup> [ Bay 2006 ]    <sup>2</sup> [ Lowe 1999]

# General Architecture



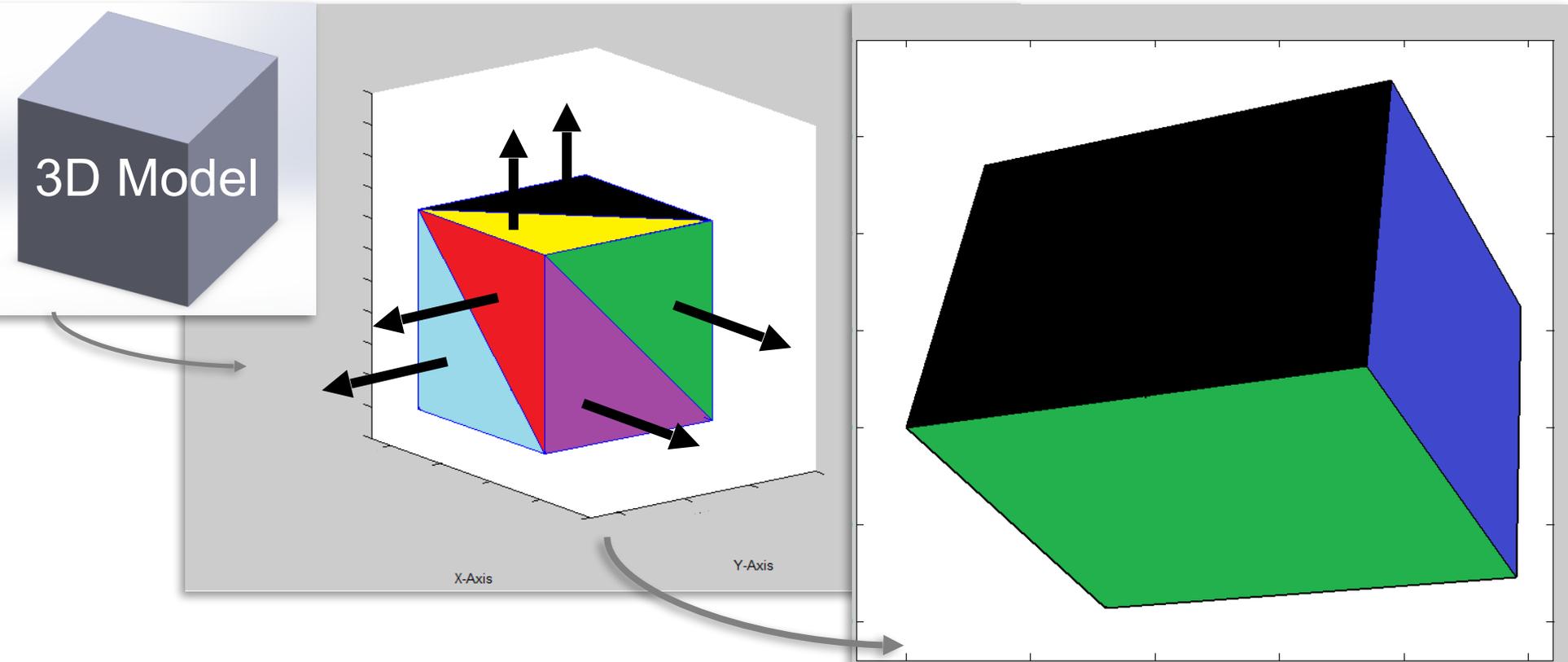
# Focus of Present Work



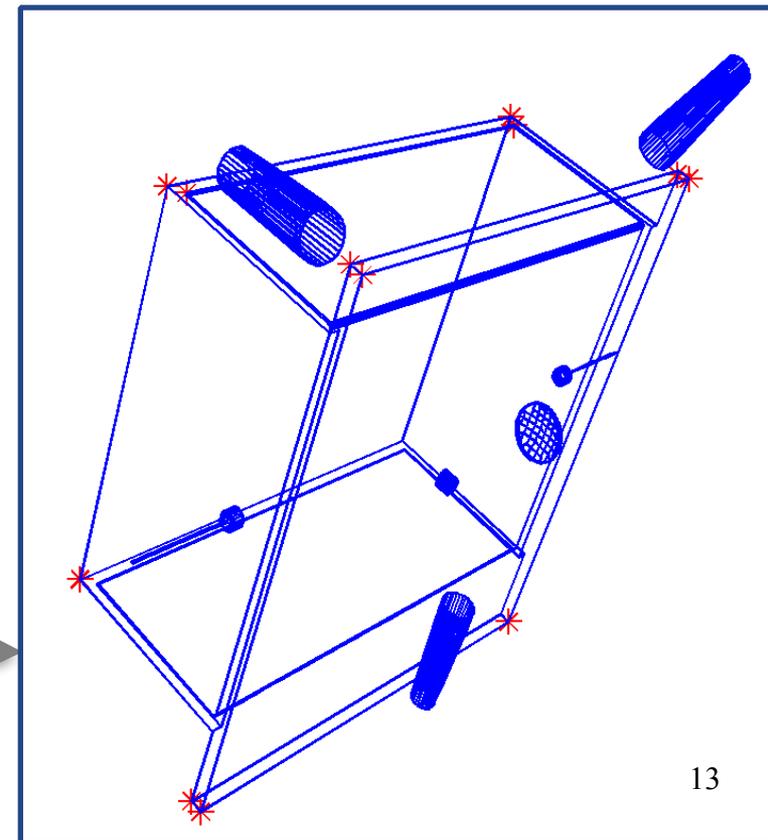
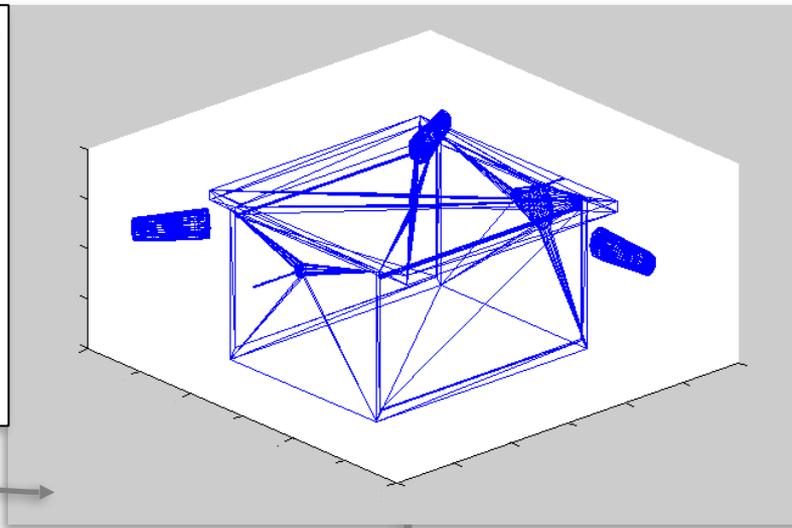
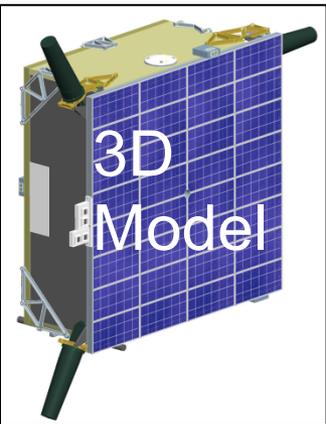
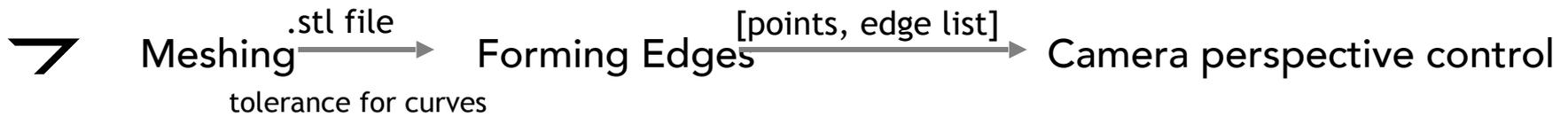
## What do initial pose estimators do?

- Solve the perspective-n-point (PnP) problem
- Require "n" 3D model points and their 2D projections
- Require fully calibrated perspective camera

# Model Processing

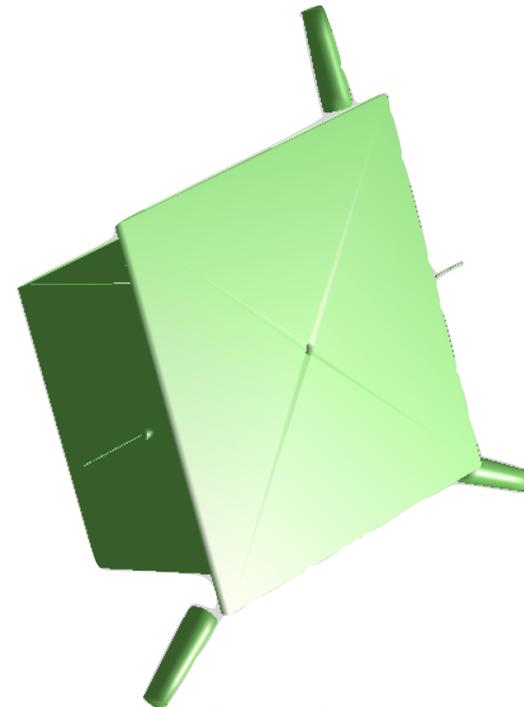
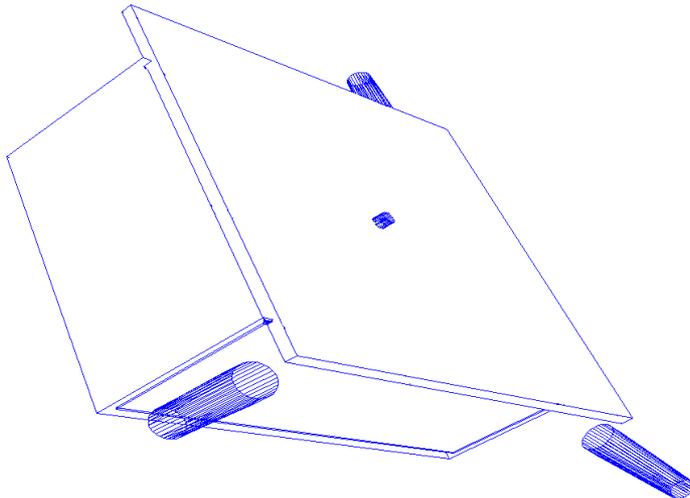


# Model Processing & Reduction

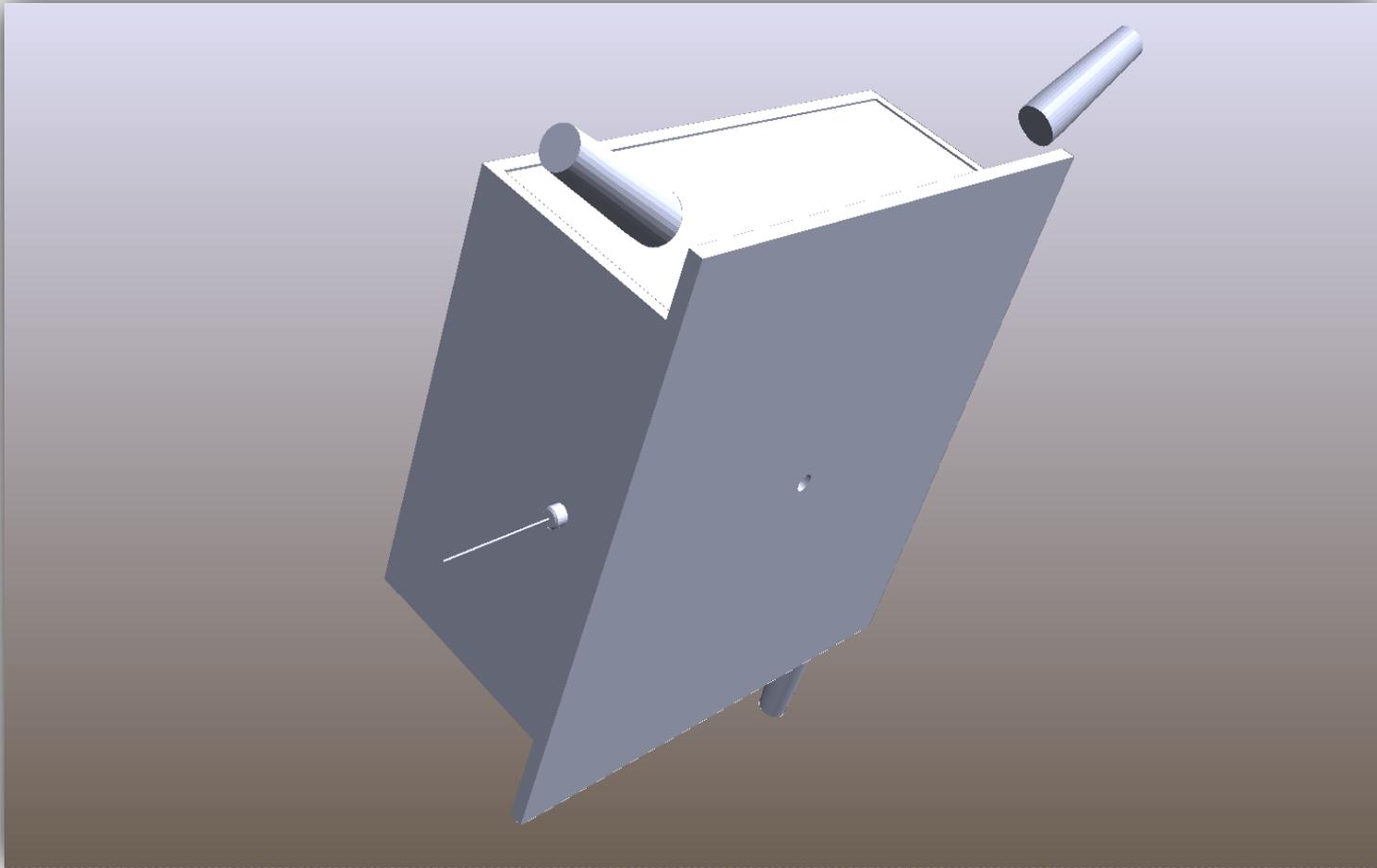


# Image Rendering

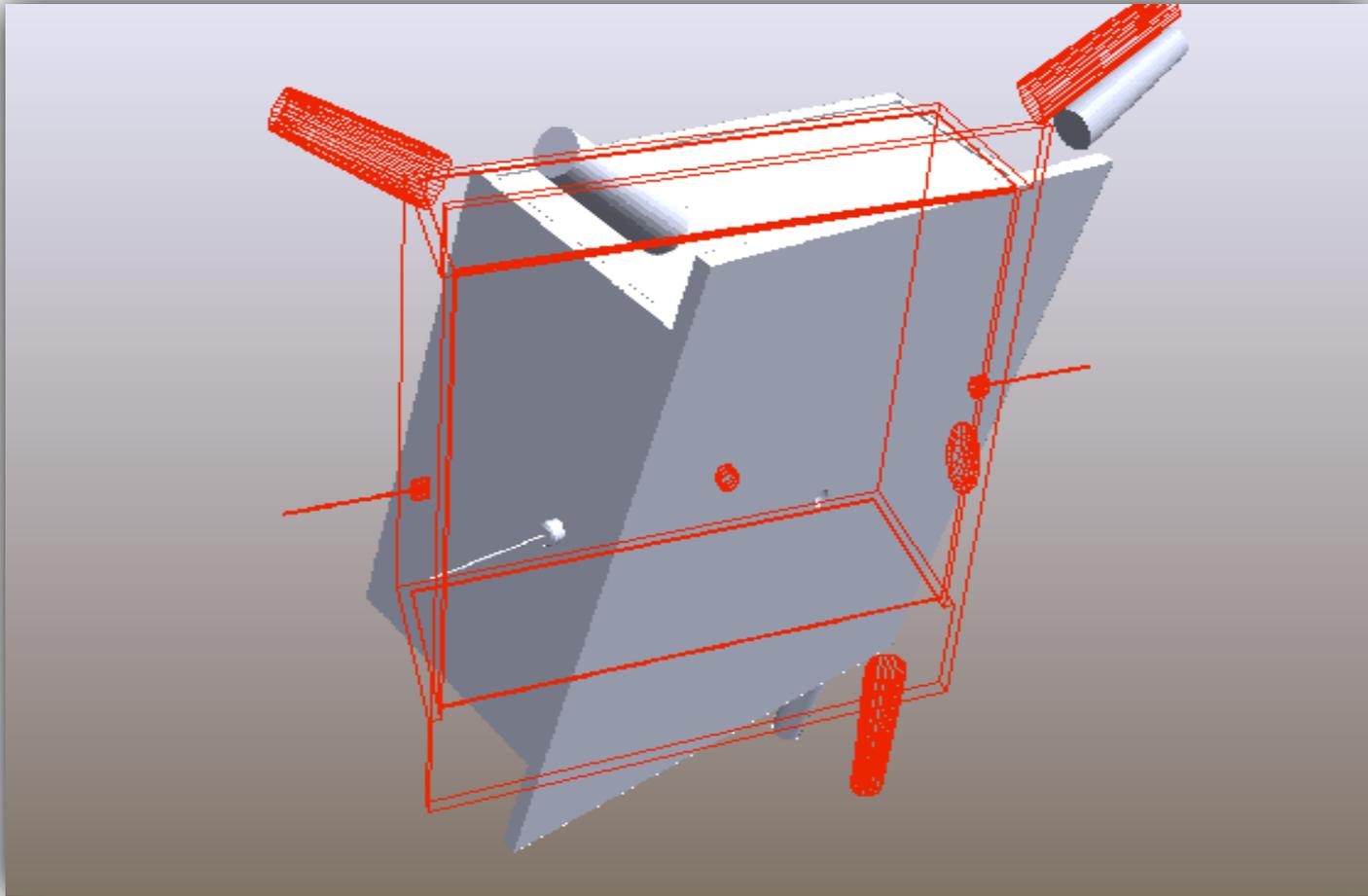
- Complimentary (not a replacement) to images captured by servicer
- Test bed of synthetic images to validate/train pose estimation techniques
- Light control and Camera perspective control



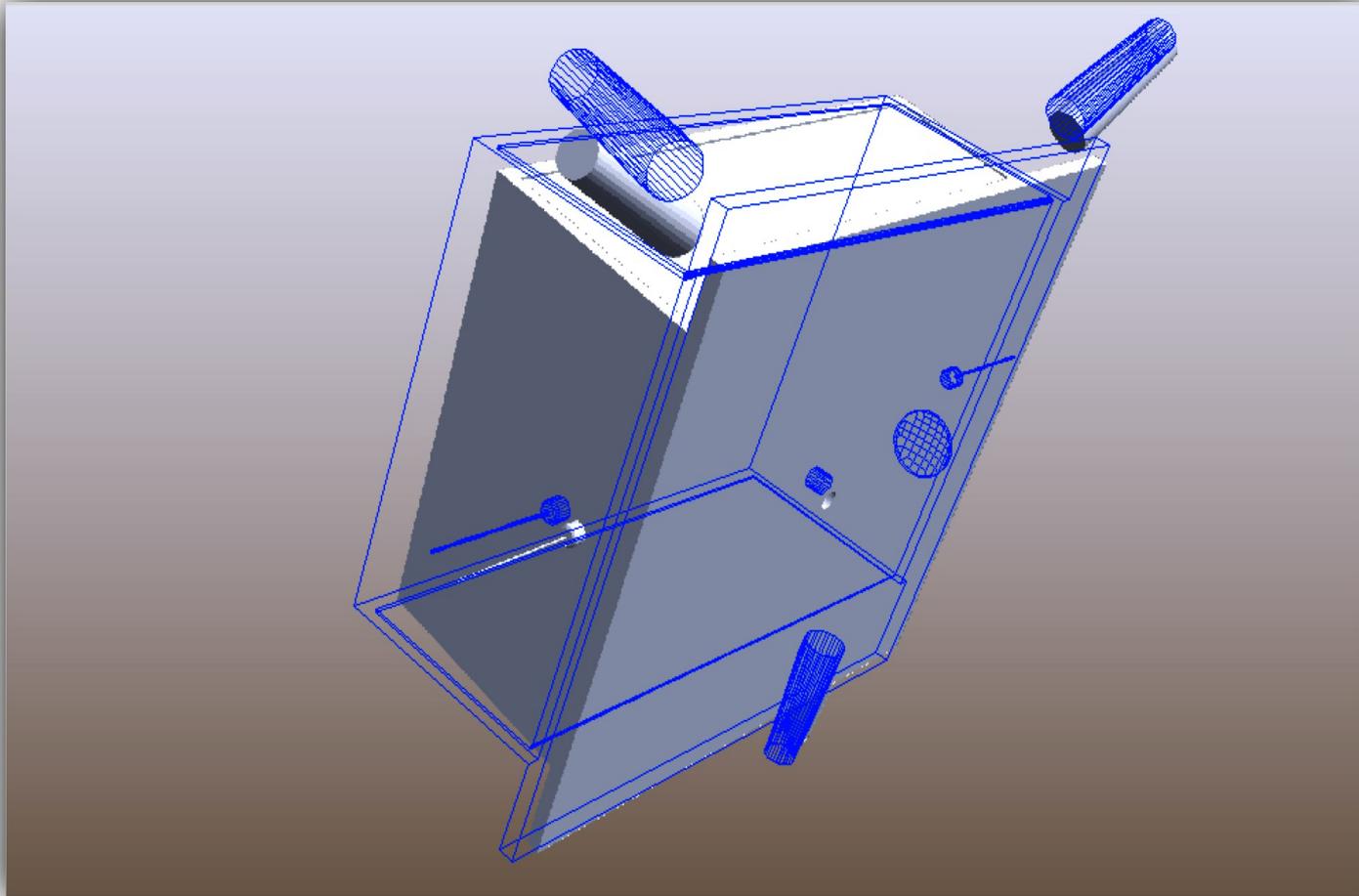
# Initial Pose Estimate



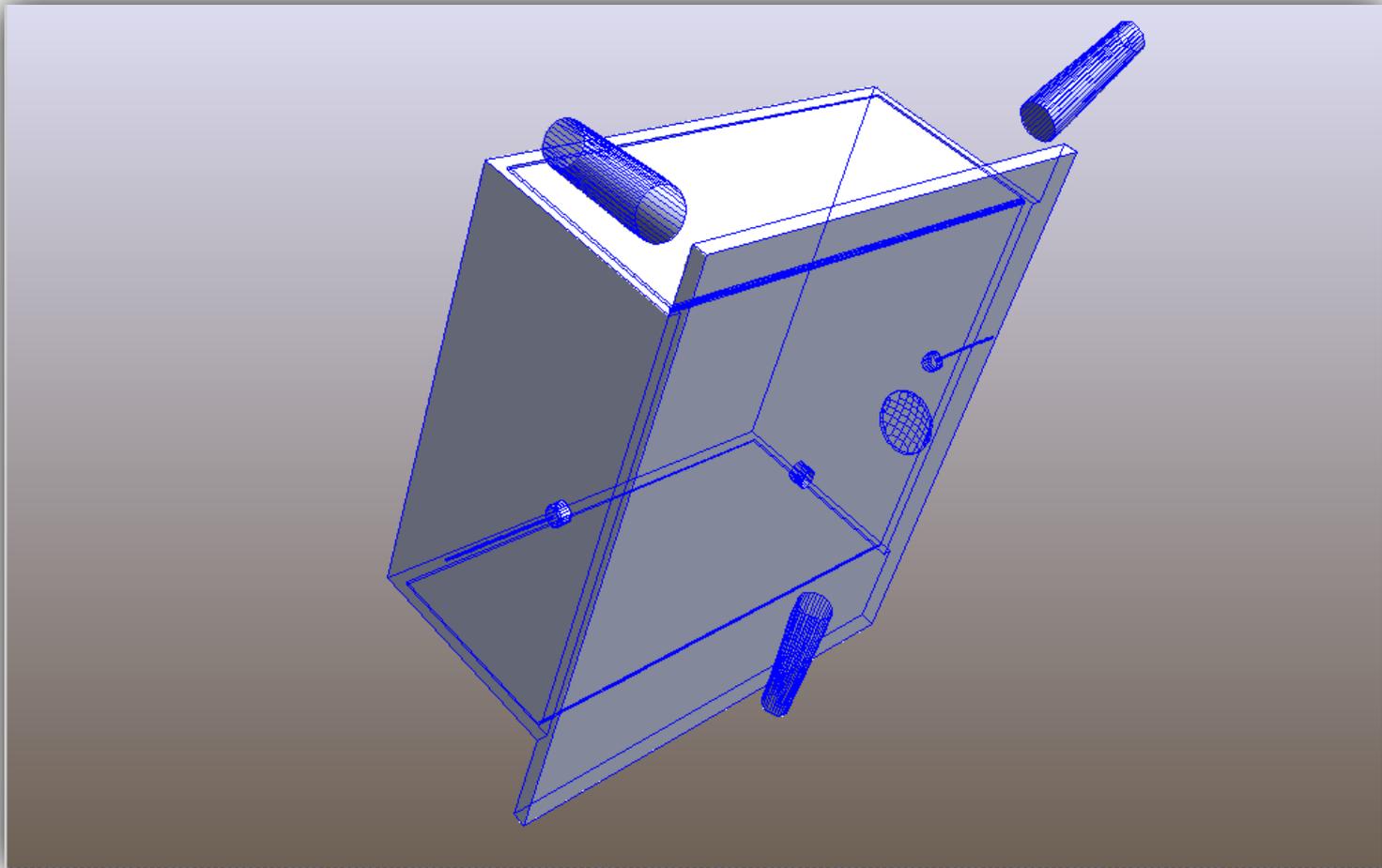
# Initial Pose Estimate



# Initial Pose Estimate

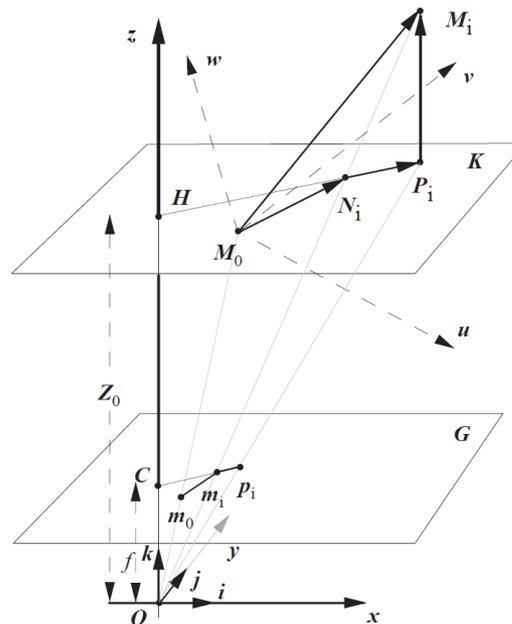


# Final Pose Estimate



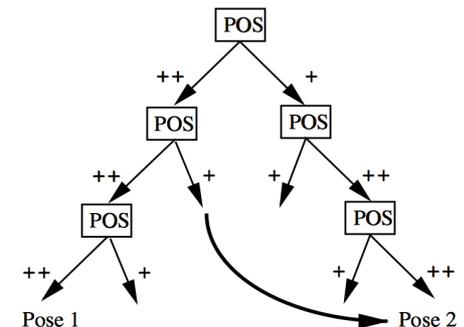
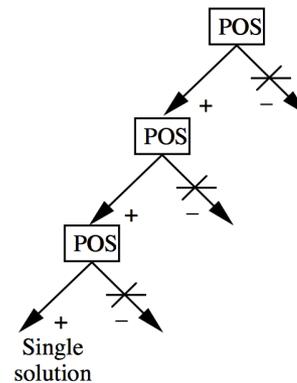
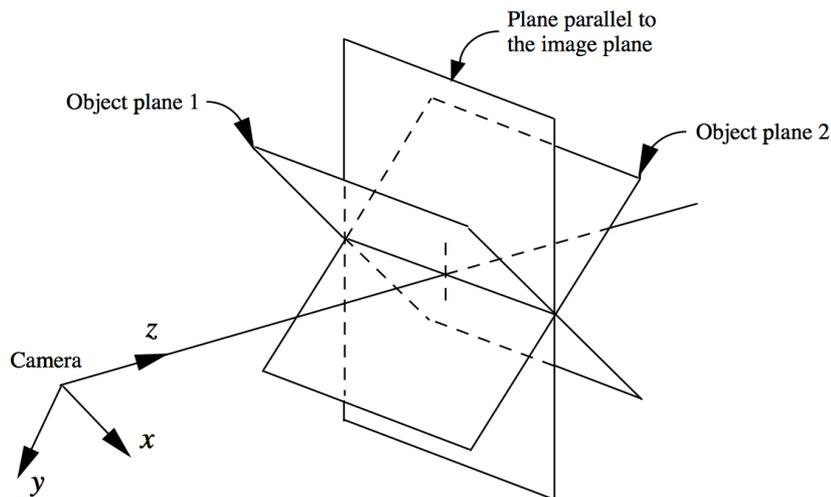
# Initial Pose Estimate - POSIT

- Developed by Dementhon and Davis solves PnP problem
- Does not require initial pose estimate, iteratively solves to satisfy tolerance
- Does not handles coplanar points
- Input of minimum 4 correspondences



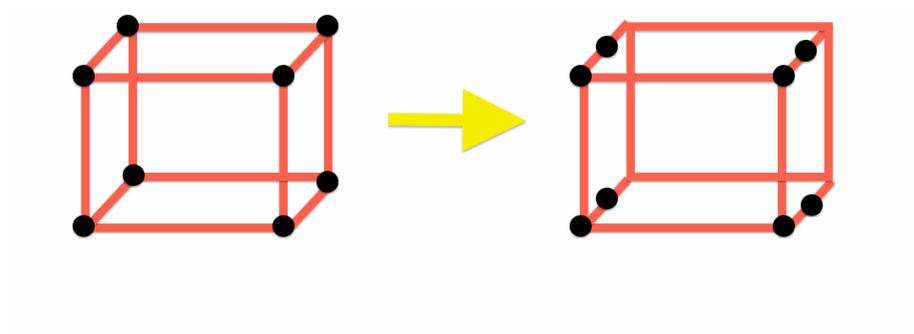
# POSIT for Coplanar points

- Developed by Dementhon and Davis solves PnP problem
- Does not require initial pose estimate, iteratively solves to satisfy tolerance
- Handles coplanar points
- Input of minimum 4 correspondences



# Coplanarity

- Tolerance of POSIT and Coplanar POSIT
- Coplanar POSIT worked  $<1.5e-14$ mm
- POSIT worked  $>2.5e-14$ mm
- Use of POSIT+



## Initial Pose Estimate - EPnP

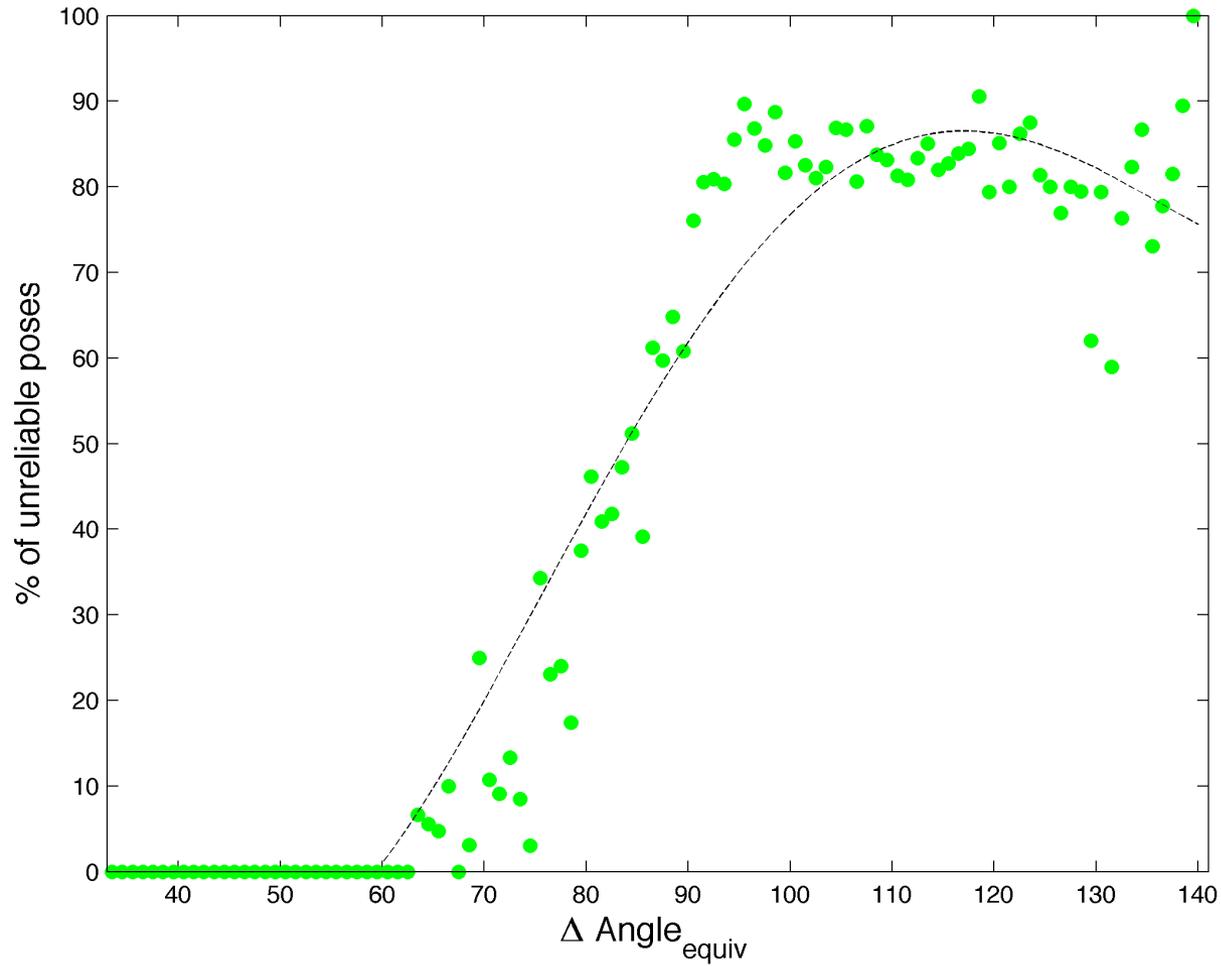
- Lepetit et al. (École polytechnique fédérale de Lausanne)
- Non-iterative  $O(n)$  solution to PnP problem
- Expresses  $n$  3D points as a weighted sum of four virtual control points
- Use of Gauss Newton Optimization to select weights on control points
- Input of minimum 4 correspondences

# Initial Pose Estimate - Newton Raphson

- Iterative solution to non-linear perspective equations
- Requires a-priori information about pose
- Inverts a 6x6 Jacobian at each iteration

$$\mathbf{E} = \frac{\partial \boldsymbol{\rho}_D}{\partial \mathbf{r}_C} \frac{\partial \mathbf{r}_C}{\partial \mathbf{t}_B} \Delta \mathbf{t}_B + \frac{\partial \boldsymbol{\rho}_D}{\partial \mathbf{r}_C} \frac{\partial \mathbf{r}_C}{\partial \boldsymbol{\phi}_B} \Delta \boldsymbol{\phi}_{BC}$$

# Newton-Raphson Reliability



## Comparison of Initial Pose Estimators: Test Cases

# of Matched  
Pairs

Std Dev of  
Gaussian  
Noise

Coplanarity

# of Outliers,  
Distance of  
Outlier

Distance to  
Camera

Distribution  
(Perceptual/  
Geometric)

## Comparison of Initial Pose Estimators: Performance

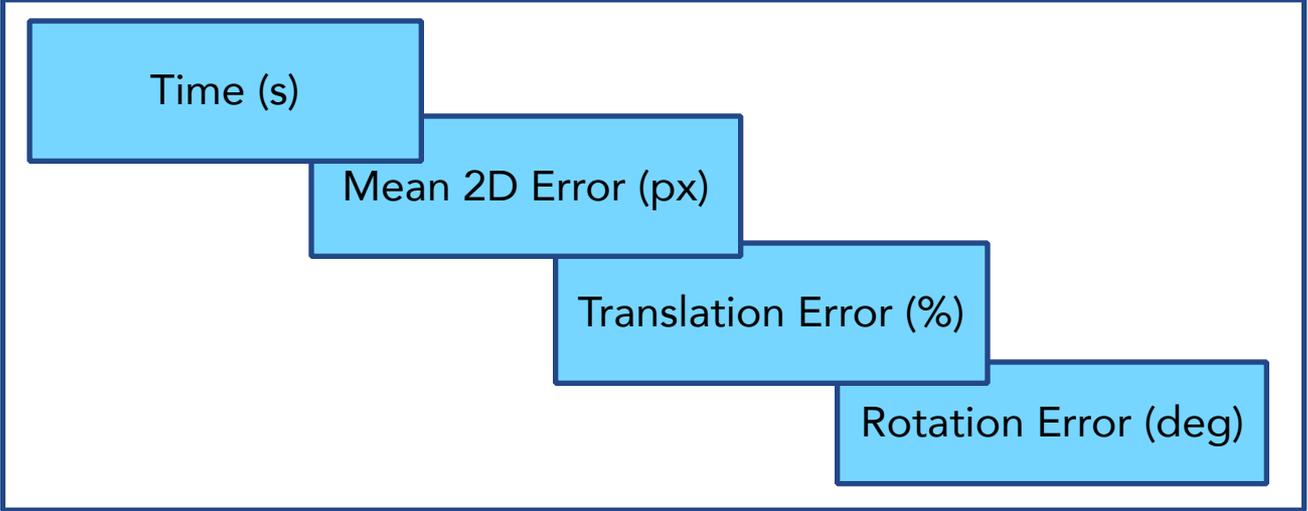
Time (s)

Mean 2D Error (px)

Rotation Error (deg)

Translation Error (%)

# Decision Matrix

	Number of Points	Noise	Outliers	Distance to Camera
Posit				
Epn				
Posit+				
Newton Raphson				

# Comparison of Pose Estimators : Monte Carlo

- MATLAB Environment
- Computation time checked with multiple simulations
- Image generated with camera model used in PRISMA
- Reliability Check

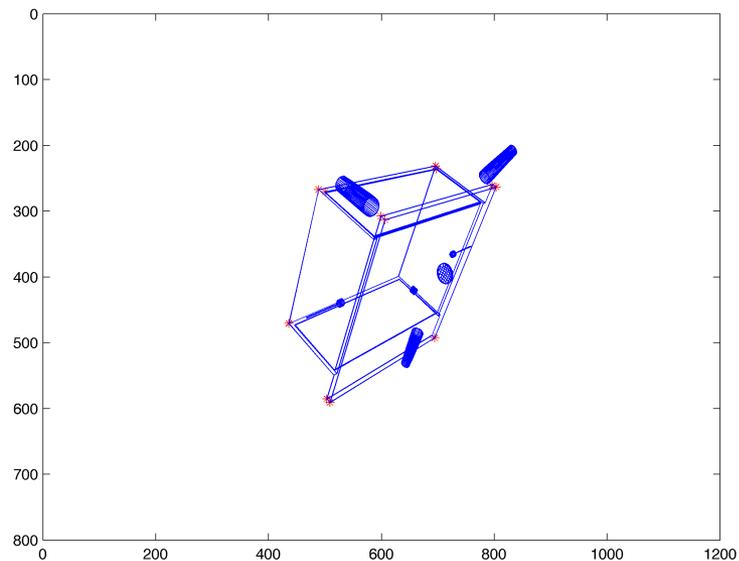
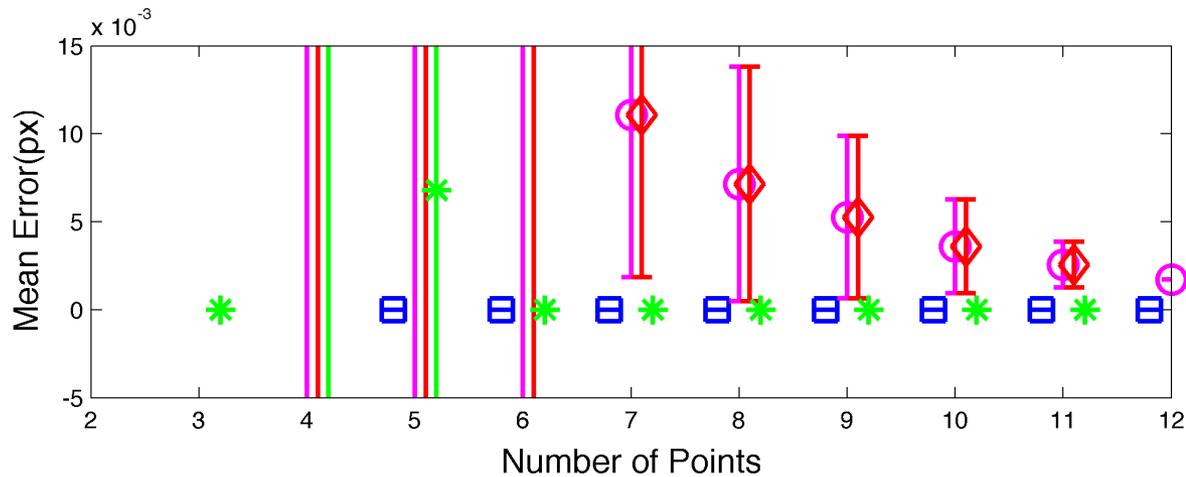
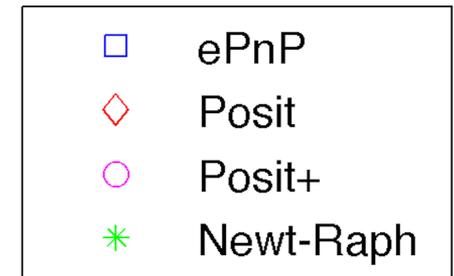
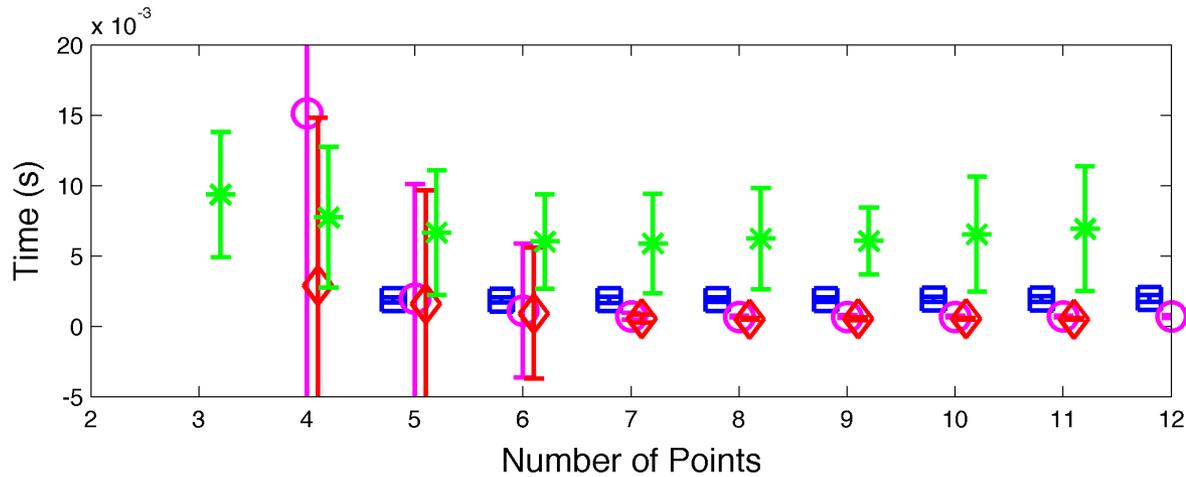
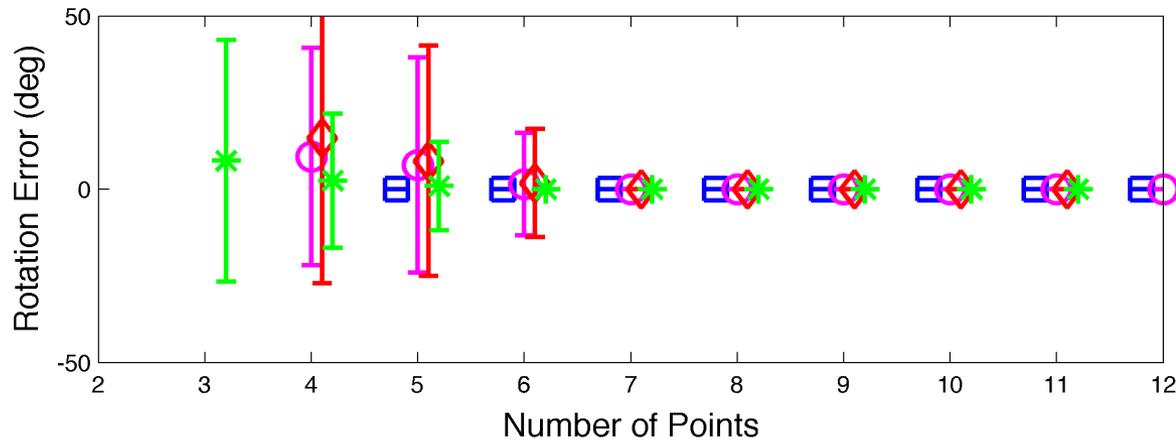
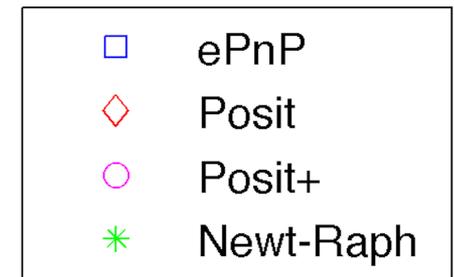
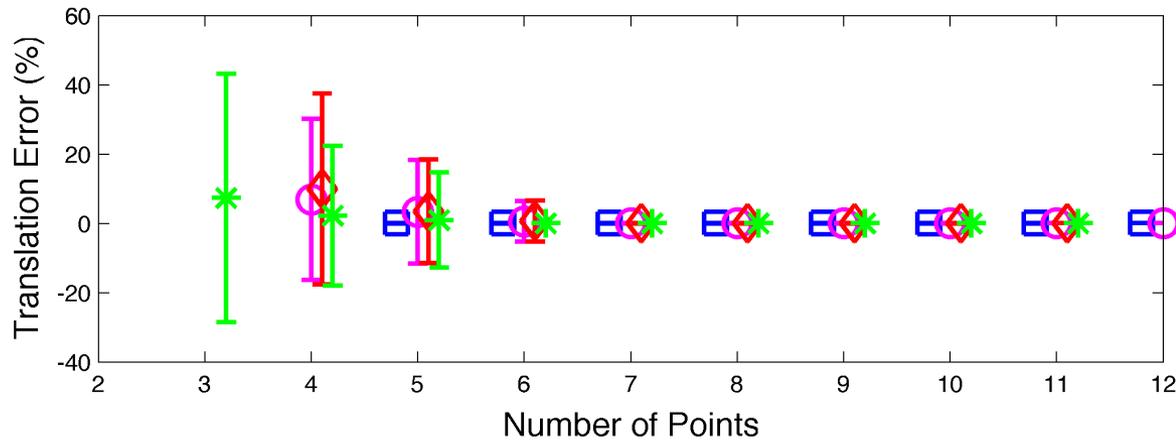


Image (ground truth)  
used for comparison

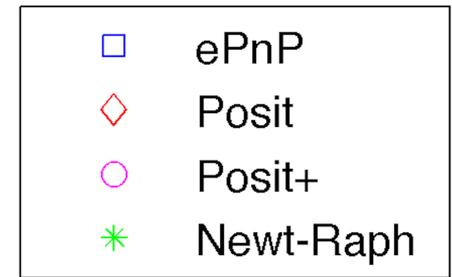
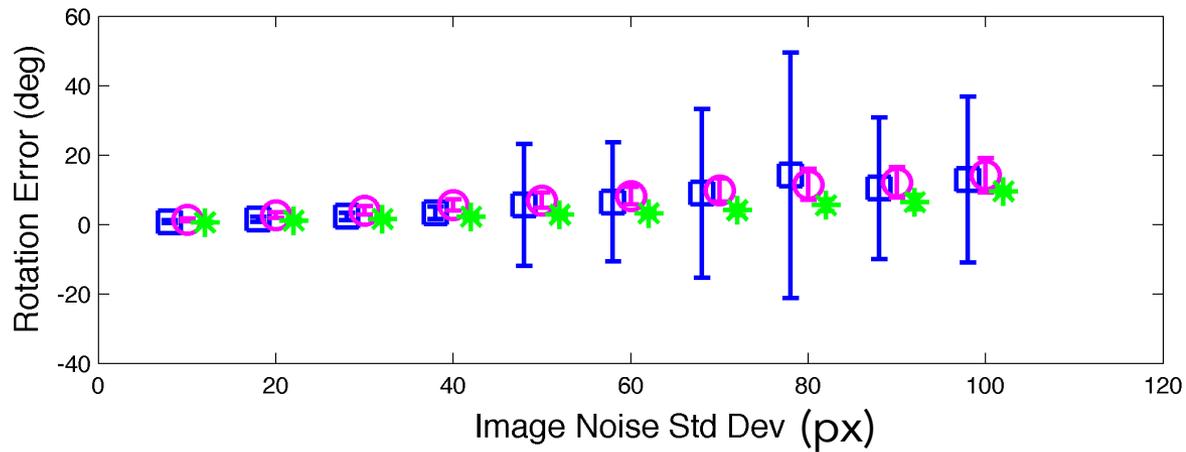
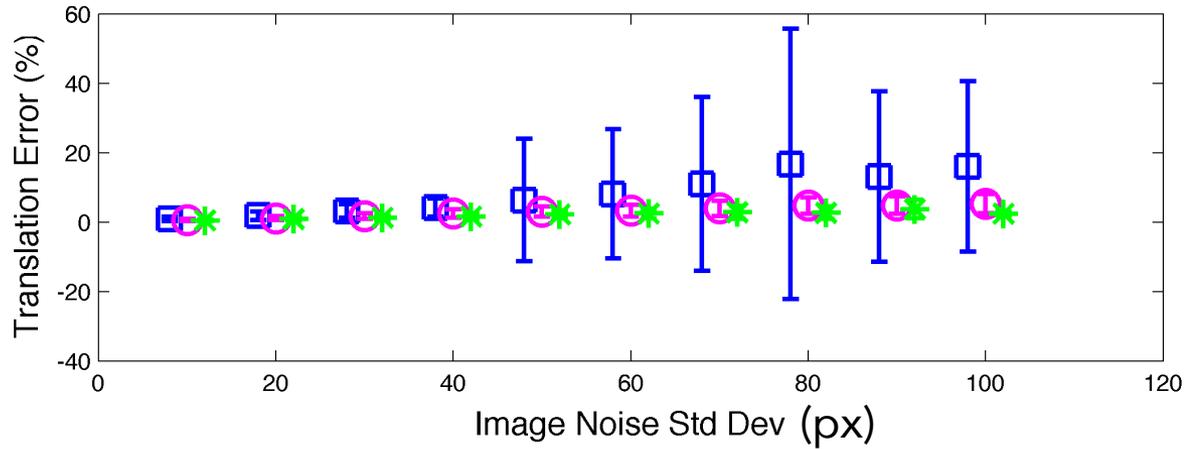
# Criteria: Number of Matched Pairs



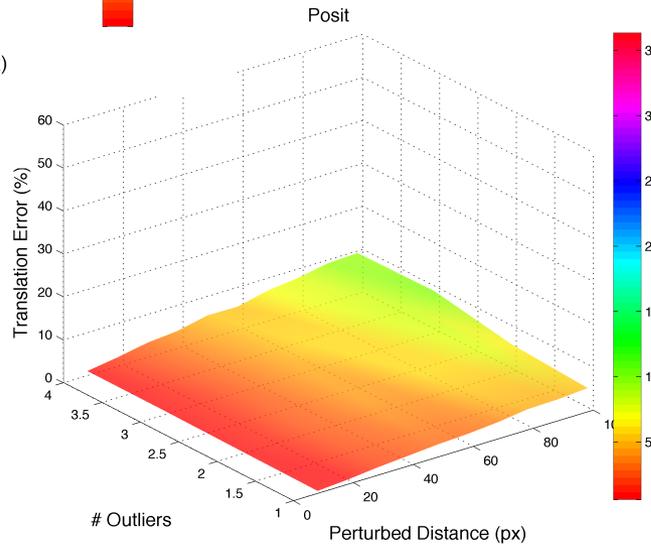
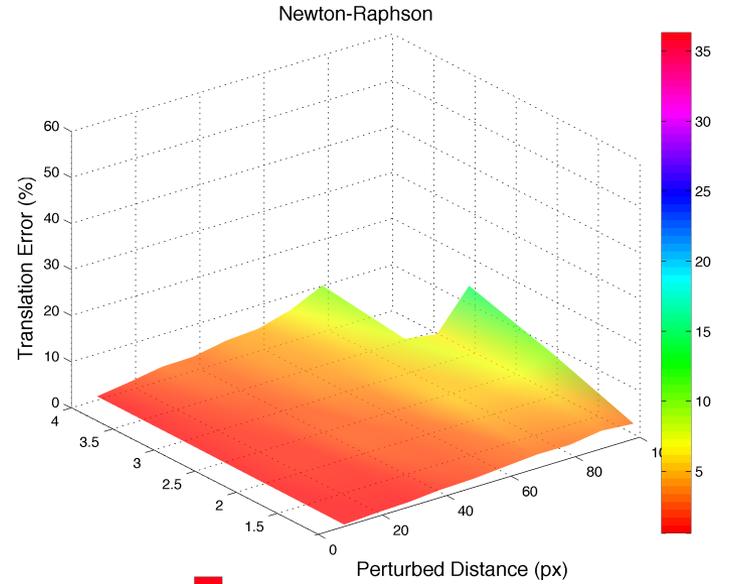
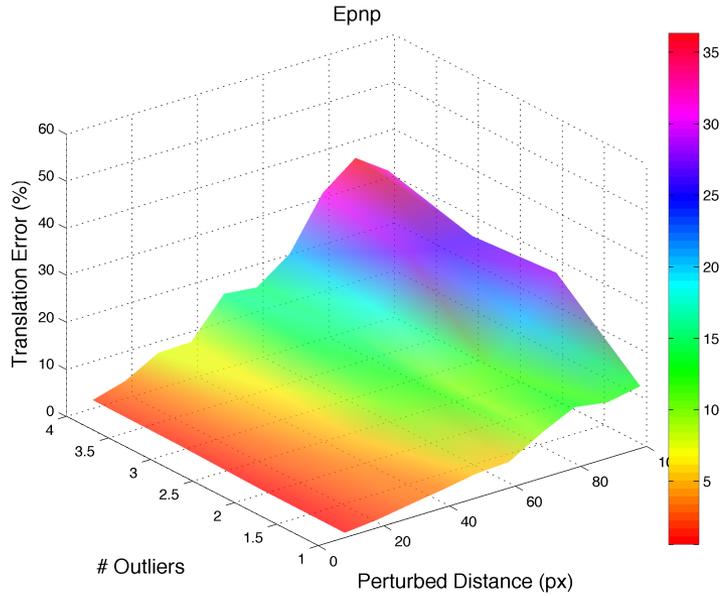
# Criteria: Number of Matched Pairs



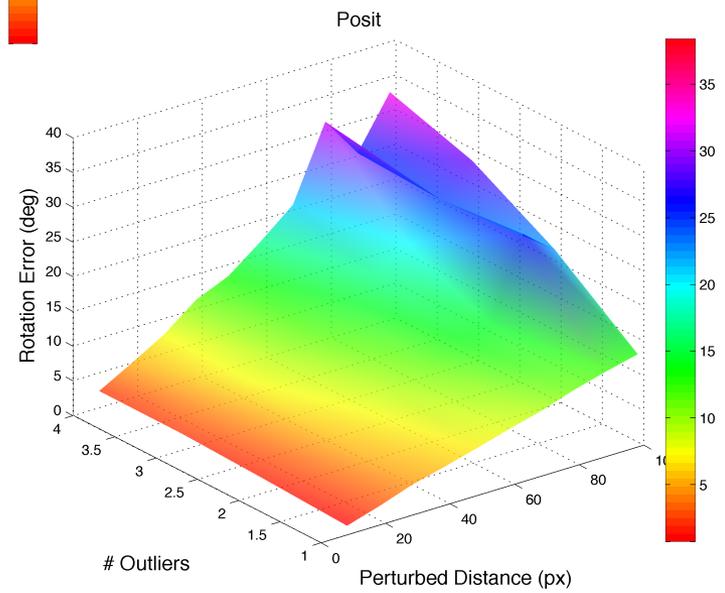
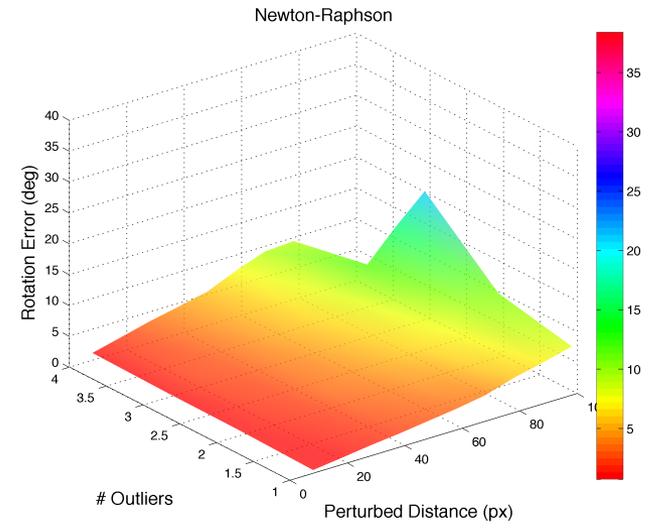
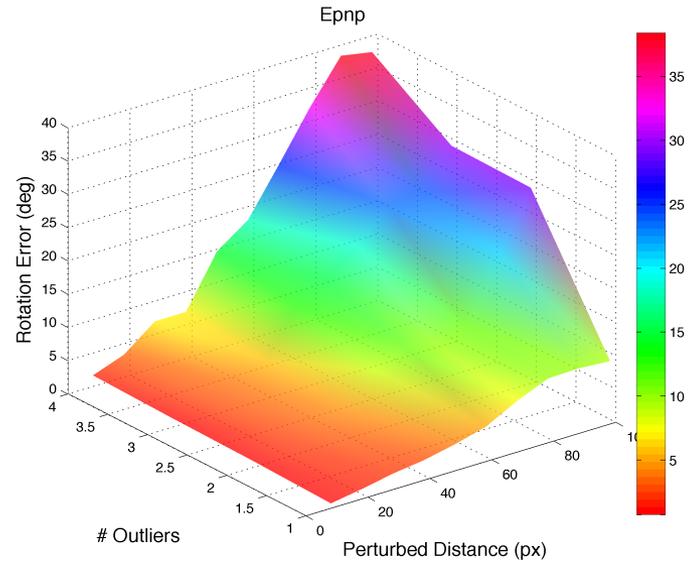
# Gaussian Noise



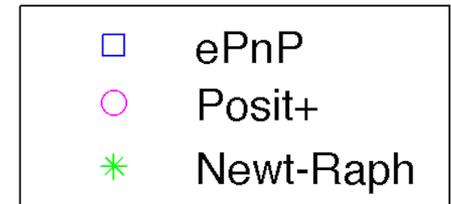
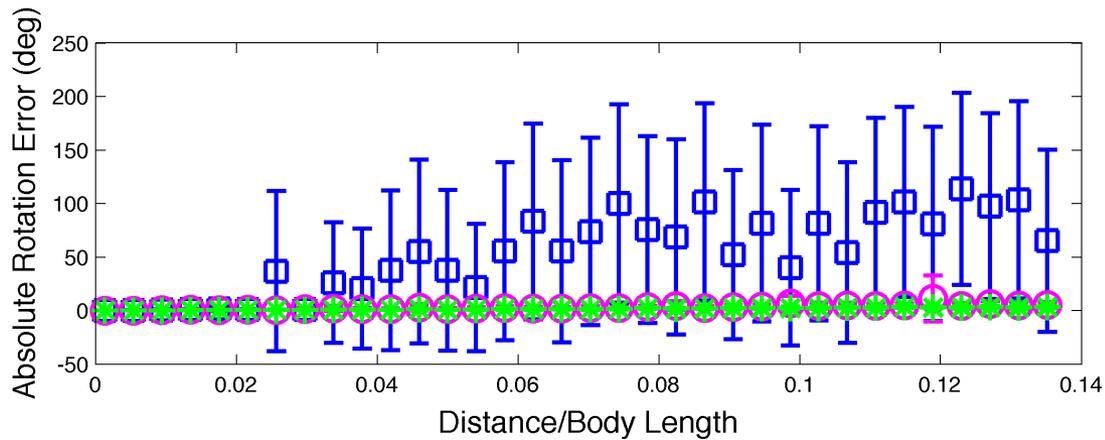
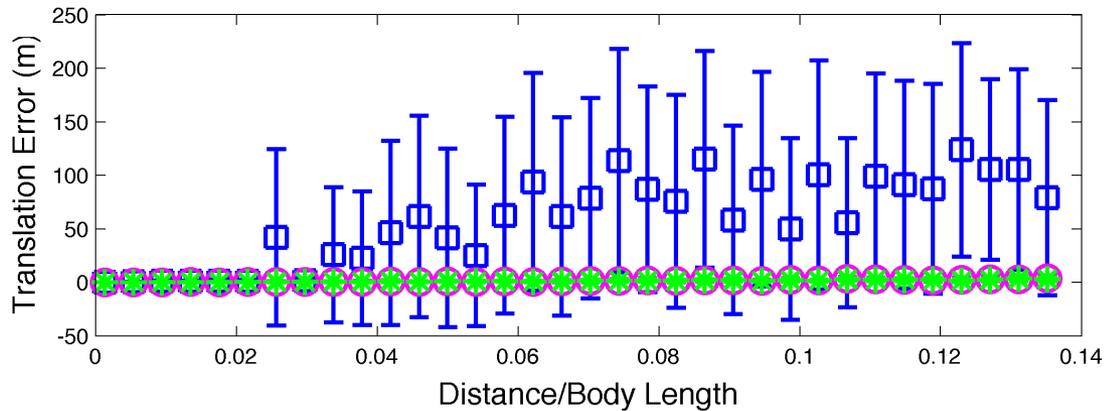
# Outliers



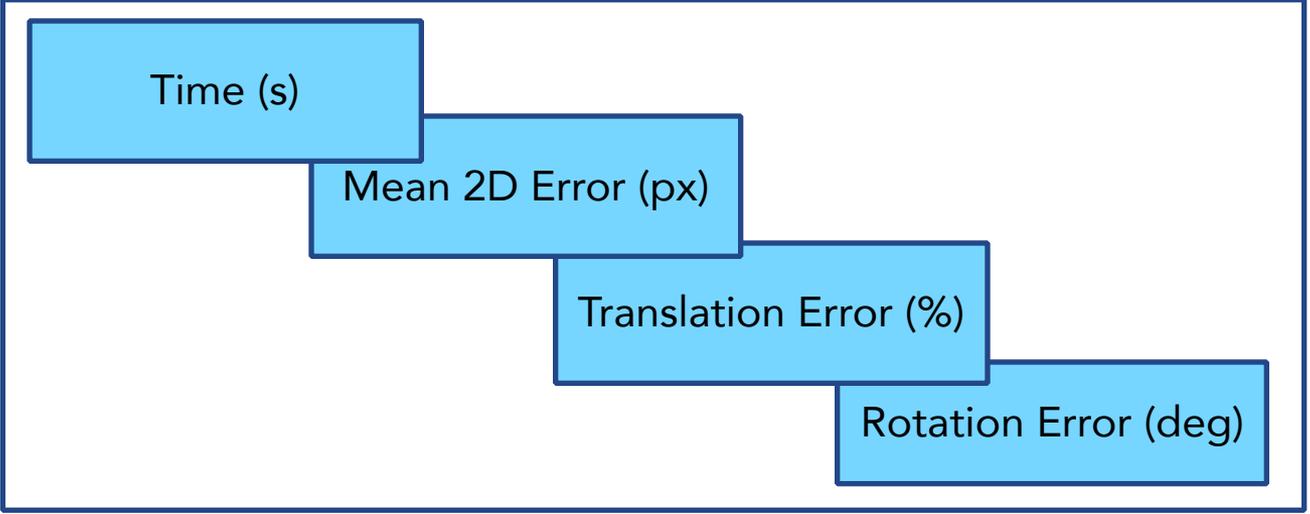
# Outliers



# Distance along Optical Axis



# Conclusions: Decision Matrix

	Number of Points	Noise	Outliers	Distance to Camera
Posit				
Epn				
Posit+				
Newton Raphson				

# Conclusions: Decision Matrix

	Number of Points	Noise	Outliers	Distance to Camera
Posit	Yellow	Green	Orange	Yellow
Epn	Green	Yellow	Orange	Orange
Posit+	Yellow	Green	Orange	Yellow
Newton Raphson	Green	Green	Yellow	Yellow

# Future Challenges

- Link with Model Matching (carrying multiple poses)
- Closed loop with image processing
- Explore synergy between different methods

