



# Smart sensing, state estimation and control for enhanced smart grid reliability

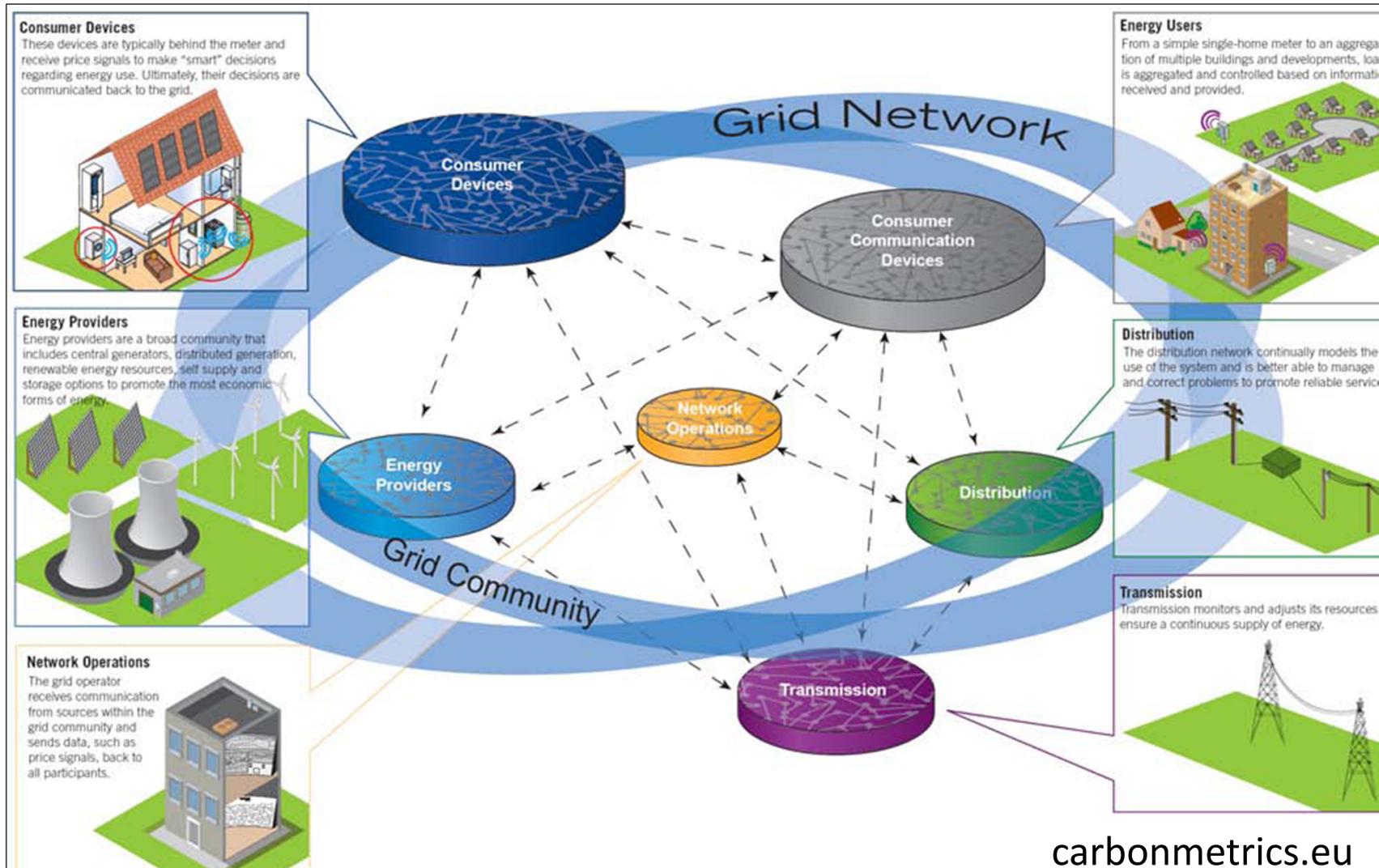
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# The Smart Grid ... *in pictures*



# The Smart Grid ... *in words*

- A unified communications and control system overlay
- On top of the existing/emerging power infrastructure
  - To provide the right information
  - To the right entity (e.g. end-use devices, transmission and distribution systems, energy providers, customers, etc.)
  - At the right time
  - To take the right action

**Control** **Communications**  
**Fundamentally change how energy is**  
**stored, delivered, and consumed**  
**Sensing**



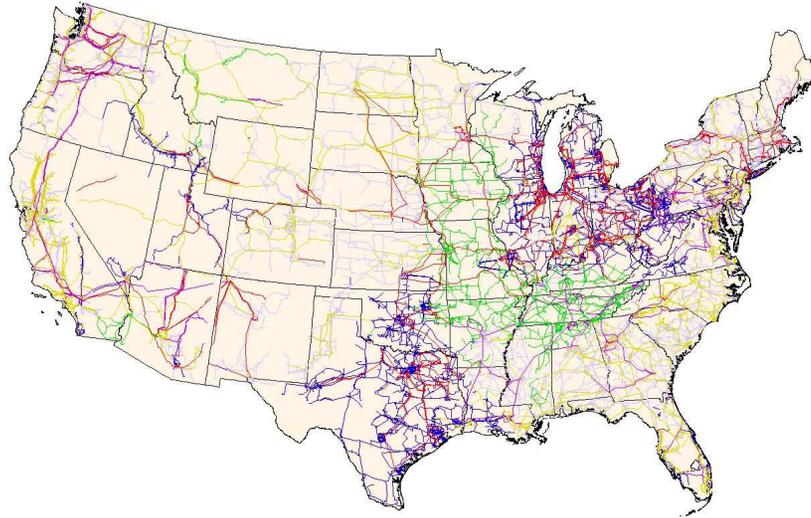
# Much progress in some areas

- Smart metering
- Green buildings and structures
- Optimization
- Demand response
- Modeling and simulation
- Incentives and economics
- ...

*But many of the hard research questions have not yet been asked*

***We focus on grid reliability***

# Motivation and Background



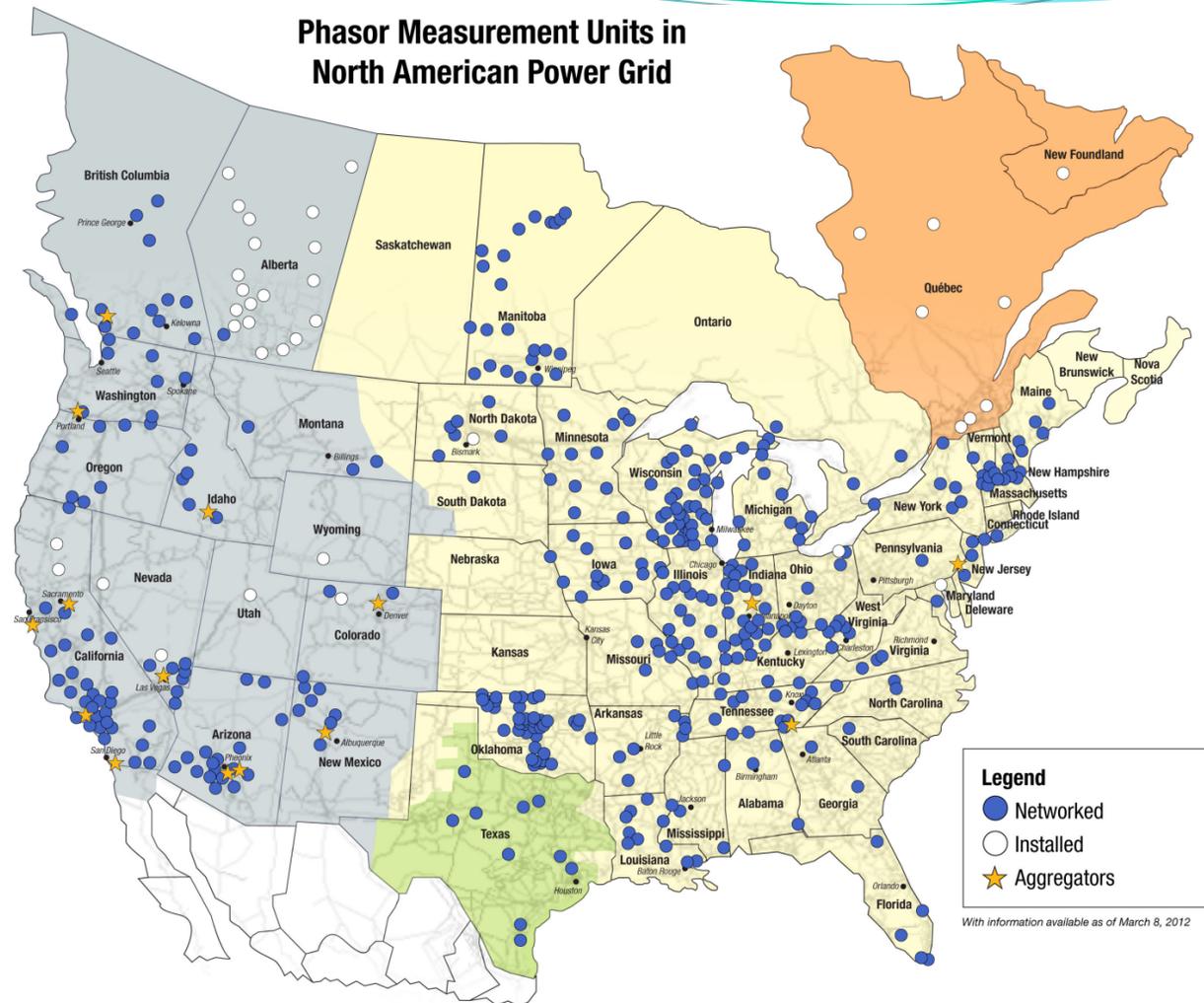
- Cascading failures in wide area transmission networks can cause large-scale blackouts.
- Near-sighted control actions can further deteriorate the grid stability.
- Wide area real-time situational awareness is needed for making the right control action to prevent cascading failures.
- Early detection of **outages** and **attacks** is needed.



# Current Sensing in the Grid

- Conventional sensors and SCADA systems:
  - Neither temporally nor spatially dense.
  - Not synchronized, diverse and not easy to integrate.
- Next generation sensors - Phasor Measurement Units (PMU):
  - GPS-synchronized temporally-dense measurements
  - Measure voltage and current phasors.
- Key question: how many sensors is enough?
  - Installing sensors is costly
  - Communication harder with more sensors
  - What price is paid for fewer sensors?

## Phasor Measurement Units in North American Power Grid



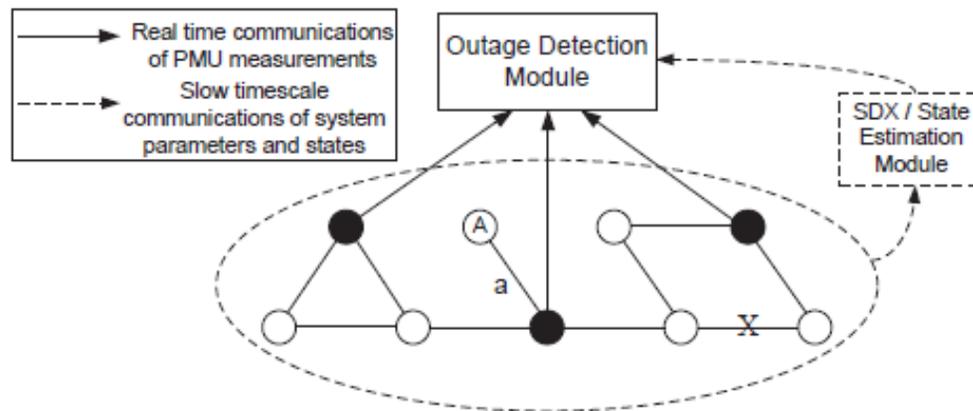
*“New technology can improve electric power system efficiency and reliability”  
US Energy Information Administration, March 30, 2012 (figure from NASPI)*



# Doing more with less

- Can we detect transmission line outages using voltage phase angles measured by a “small” number of PMUs?
- What is the optimal trade-off between the number of PMUs and the outage detection performance?
- Where should the PMUs be located?
- Related work:
  - Possibility of line outage detection using a relatively small number of PMUs [Tate, Overbye 08 09].
  - PMU location selection for other purposes: facilitating state estimation, dynamic security assessment [Li et al. 11] [Sun et al. 07].

# Problem Formulation



- $\mathcal{L} = \{1, 2, \dots, L\}$ : the set of all transmission lines.
- $\mathcal{E} = \{E_1, E_2, \dots, E_K\}$ : the set of outage events of interest.  
 $\bar{\mathcal{E}} = \mathcal{E} \cup E_0$ .
- Outage signatures  $\{\theta^{(k)}\}$ ,

$$P = B^{(k)} \theta^{(k)}, k = 0, 1, \dots, K, \quad (1)$$

$$\theta = \theta^{(0)} + z^0, \tilde{\theta} = \theta^{(\kappa)} + z^1, \quad (2)$$



# Detection Methods

- Optimal detection: exhaustive search
  - Observe pre-outage and post-outage phase angle vectors
  - Identify which event has occurred by comparing observations with every outage signature
  - Highly reliable detection, with high complexity
- Can also exploit sparsity to reduce detection complexity (compresses sensing techniques, e.g. Zhu/Giannakis'11)

# Given optimal detection, where to place the sensors?

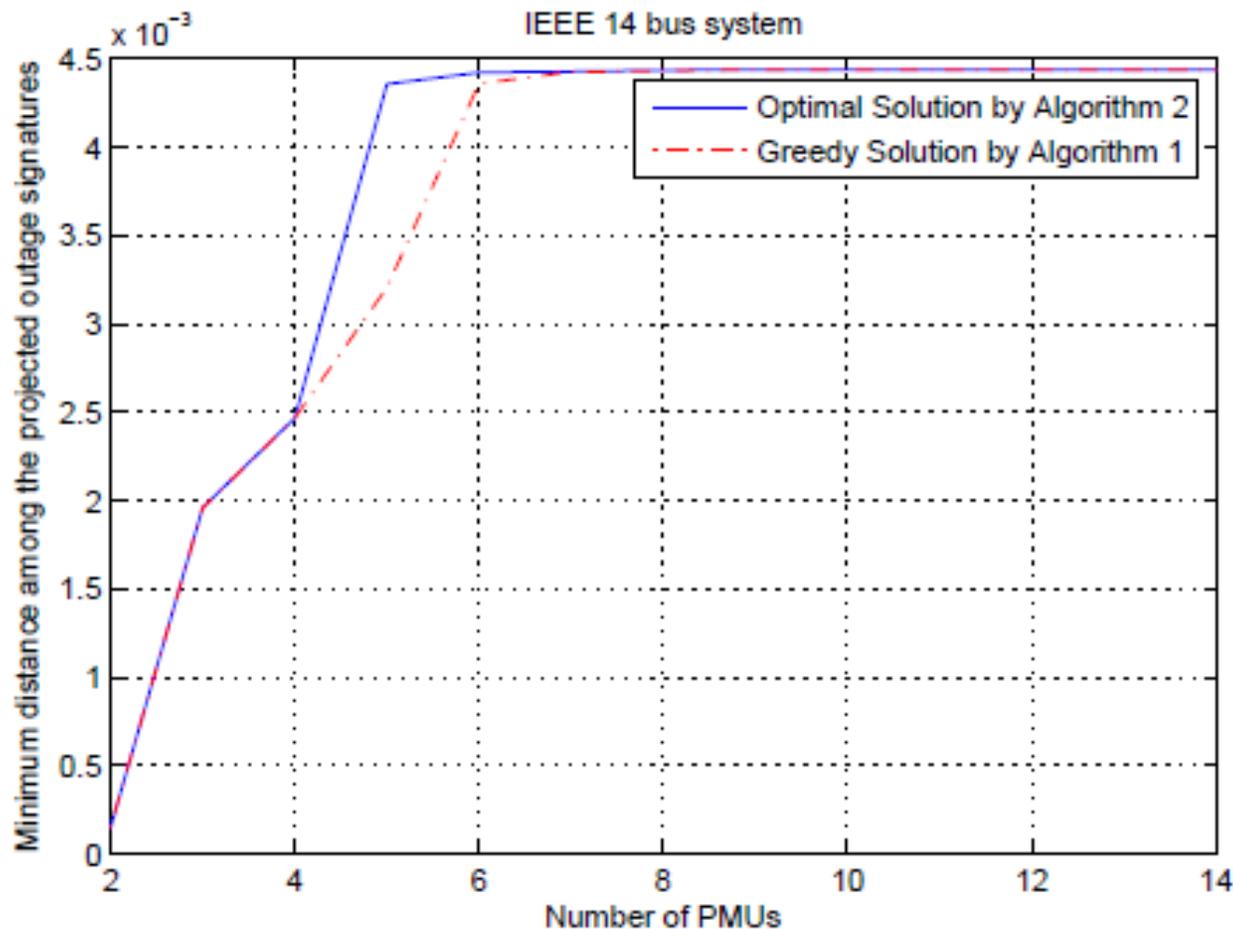
- Use coding ideas: maximize the “separation” of the outage signatures.
- Find the set of buses  $\mathcal{M}$  to collect PMU measurements, given that  $|\mathcal{M}| = M \ll N$ .
- Goal is to maximally separate the projected signatures
- Different criteria can be used to capture separation:
  - Criterion I: Min. Distance Among the Outage Signatures (Integer Programming Problem)
  - Criterion II: Percentage of Indistinguishable Outage Pairs



# Min Distance Algorithms

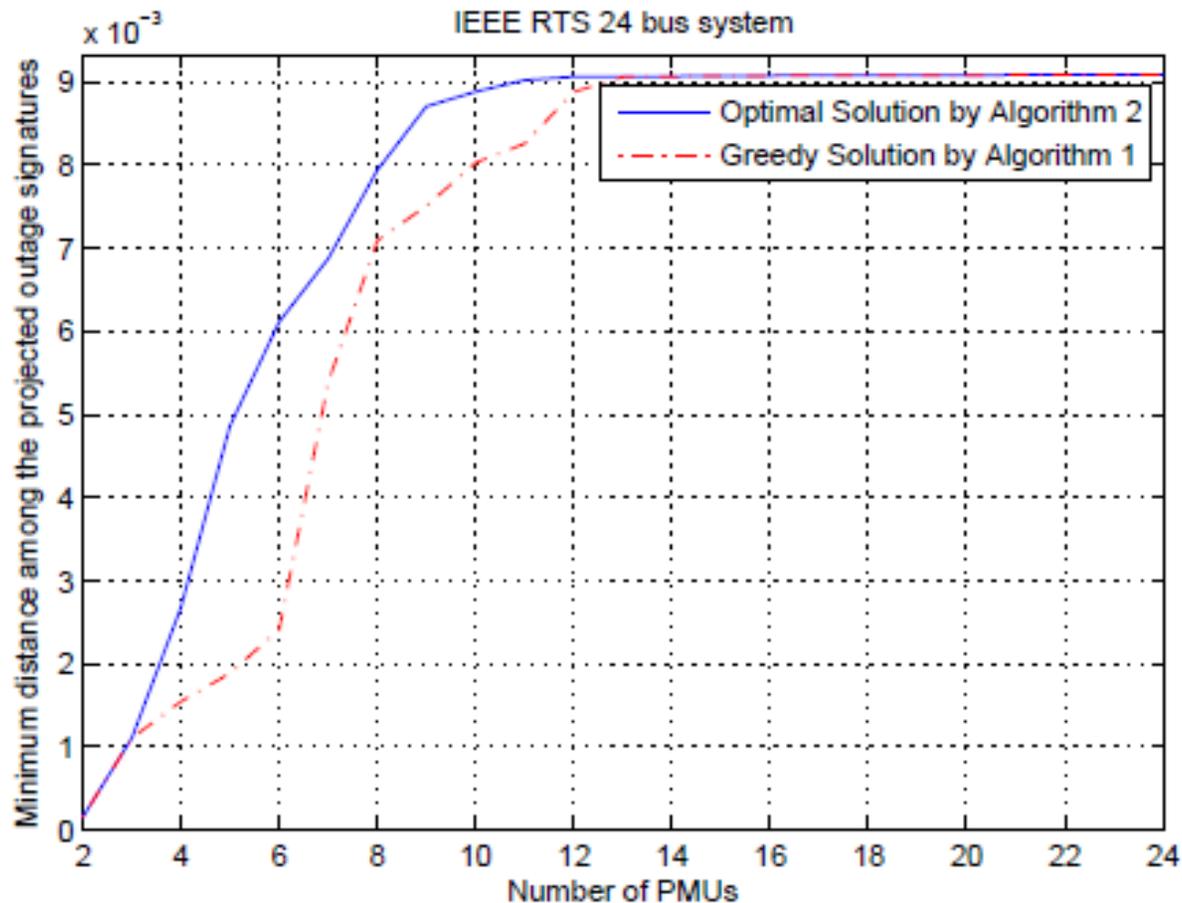
- Global Optimal Exhaustive Search:
  - We propose a branch and bound algorithm for exhaustive search to find the global optimal
- Lower bound
  - We propose a greedy heuristic algorithm that approximates the locations that achieve the minimum distance

# Outage Signature Distance vs. Number of PMUs (14 buses)



At most 17 iterations to reach convergence of optimal algorithm

# Outage Signature Distance vs. Number of PMUs (24 buses)



At most 400 iterations to reach convergence of optimal algorithm



# Observations

- Using PMUs on roughly one third of the buses is sufficient for near-optimal performance.
- The branch and bound algorithm finds the optimal PMU locations in a small number of iterations.
- The greedy heuristic achieves the global optimum when the number of PMUs is sufficiently large.

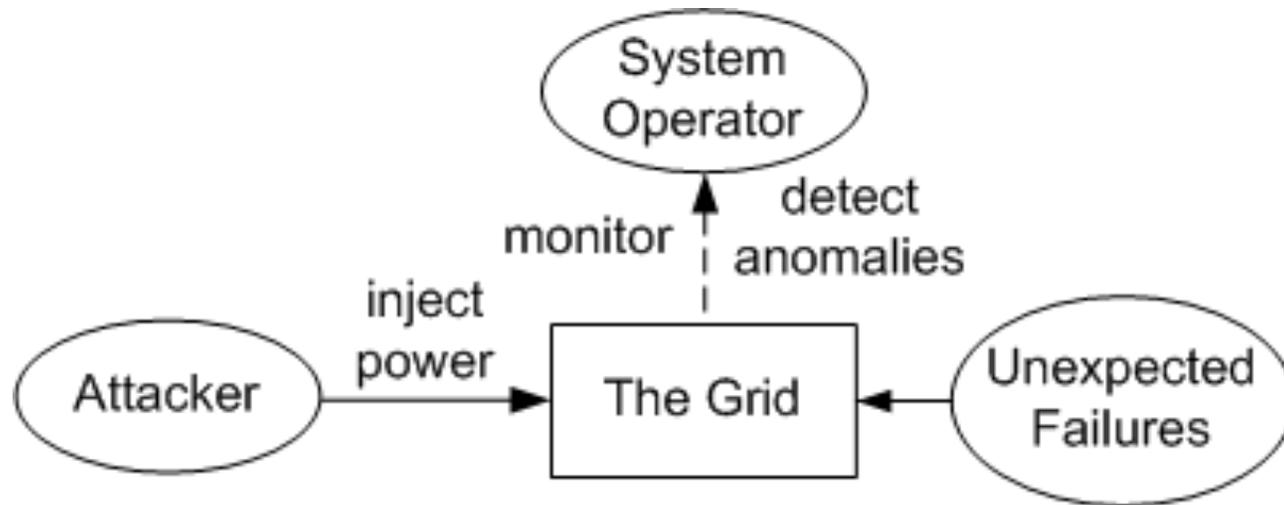


# Extensions and next steps

- Can the model be generalized to
  - An AC power flow model?
  - More sophisticated sensing?
  - A more heterogenous and dynamic network model?
  - A more general communication network structure?
- Can a control model be superimposed on this framework?
- Can the ideas be extended to physical attacks?

# Outage vs. Physical Attack

- Outages – unintended component failures.
- Physical attacks – intended and optimized power injections.





# Model Differences

- Outage model
  - Prior probabilities of outages
    - can be estimated by power engineering analysis.
  - Design the monitoring system based on the priors of the outages.
- Physical attack model
  - Attacker: minimize its effort and maximize its impact without being observed by the monitoring system.
  - System operator: design the monitoring system to maximize the difficulty of forming an attack.

# Physical Attack Model

- Attacker: a sparse vector design problem.

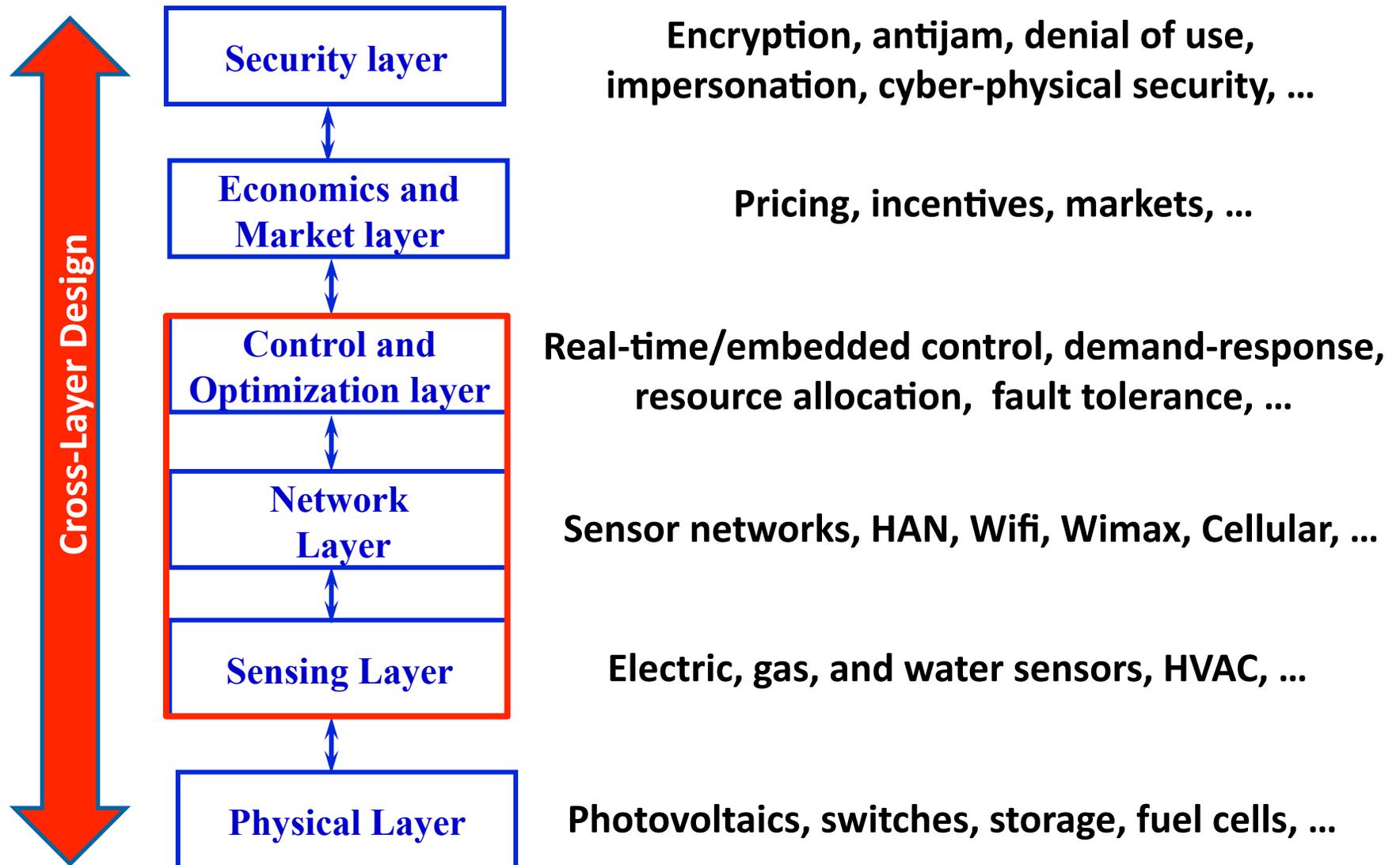
$$\begin{aligned} \min_{\mathbf{a}} \quad & \|\mathbf{a}\|_0 \\ \text{s.t.} \quad & \left\| \left( \mathbf{B}^+ \mathbf{a} \right)_M \right\|_\infty \leq \varepsilon, \\ & \text{Impact}(\mathbf{a}) \geq C. \end{aligned}$$

- System operator: a max-min subset selection problem.

$$\begin{aligned} \max_M \quad & \|\mathbf{a}^*\|_0 \\ \text{s.t.} \quad & |\mathbf{M}| \leq M. \end{aligned}$$

***Currently extending the PMU location problem to maximize detection probability of attacks***

# Possible Dichotomy for Smart Grid Design





# Summary

- Smart grids provide a tremendous opportunity for changing the way power is delivered and consumed
- The design of smart grids is a challenging interdisciplinary problem with many questions and few answers to date
- Capitalizing on new sensor technology and sophisticated optimization tools can significantly improve robustness in the grid.