

Lecture 2: Kinematics and Control of Medical Robots

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ICRA 2016 Tutorial on Medical Robotics

lecture objectives

- Understand the kinematic structures of medical robots
- Identify common types of sensors and actuation technologies used in medical robots
- Identify control strategies used for human-in-the loop medical robots

Kinematics

suggested references

- Introduction to Robotics : Mechanics and Control
John J. Craig
- Robot modeling and control
Mark W. Spong, Seth Hutchinson, M.Vidyasagar
- A mathematical introduction to robotic manipulation
Richard M. Murray, Zexiang Li, S. Shankar Sastry
- Springer handbook of robotics
B. Siciliano, Oussama Khatib (eds.)

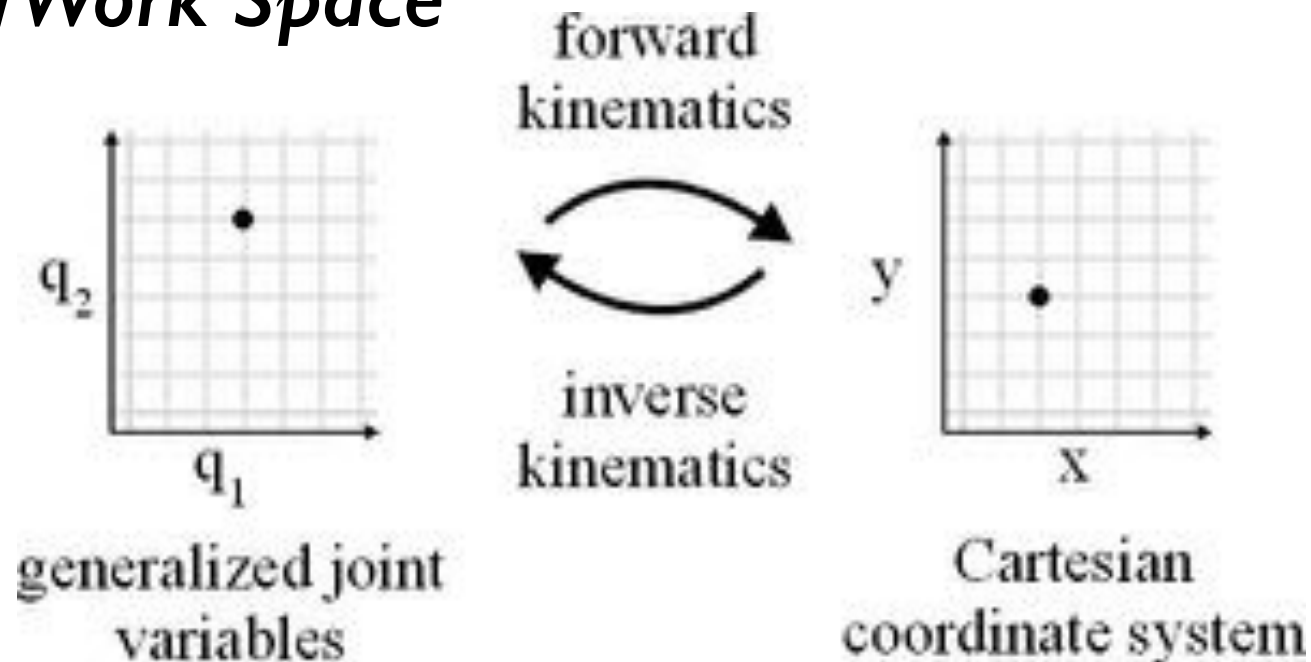
kinematics

The goals of kinematics in medical robots are to:

- Determine endpoint position and/or joint positions and their derivatives for control (forward kinematics and Jacobian)
- Determine the required joint positions for endpoint placement with respect to anatomy (inverse kinematics)
- Calculate force-torque relationships to enable control in workspace coordinates and generate force constraints (Jacobian transpose)

kinematics for robots

- Allows you to move between *Joint Space* and *Cartesian/Work Space*



- Jacobian:

$$\dot{\mathbf{x}} = \mathbf{J}\dot{\boldsymbol{\theta}}$$

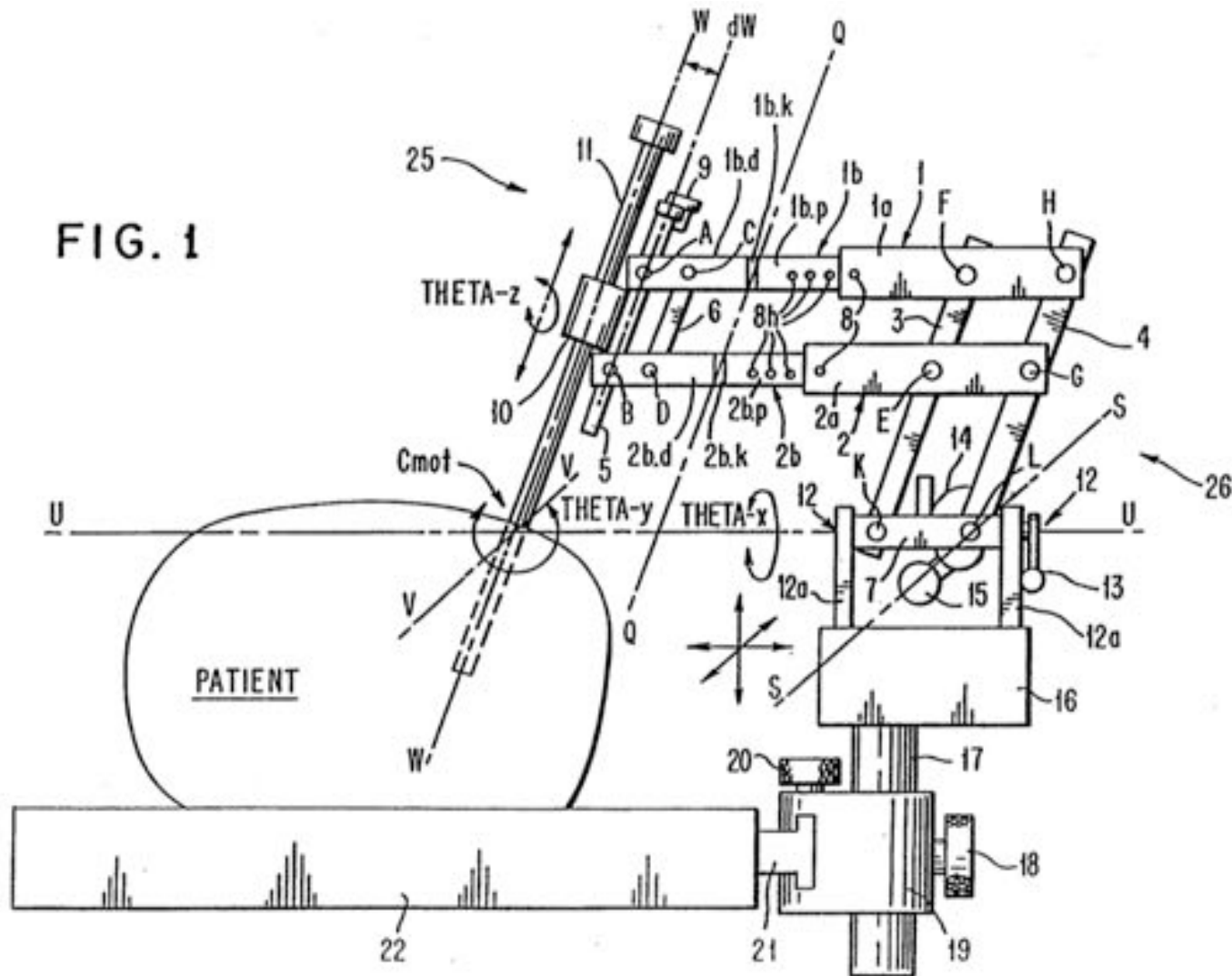
$$\dot{\boldsymbol{\theta}} = \mathbf{J}^{-1}\dot{\mathbf{x}}$$

$$\boldsymbol{\tau} = \mathbf{J}^T \mathbf{F}$$

a note about degrees of freedom

- Number of independent position variables needed to in order to locate all parts of a mechanism
- DOF of motion
- DOF of sensing
- DOF of actuation
- The DOF of a mechanism does not always correspond to number of joints

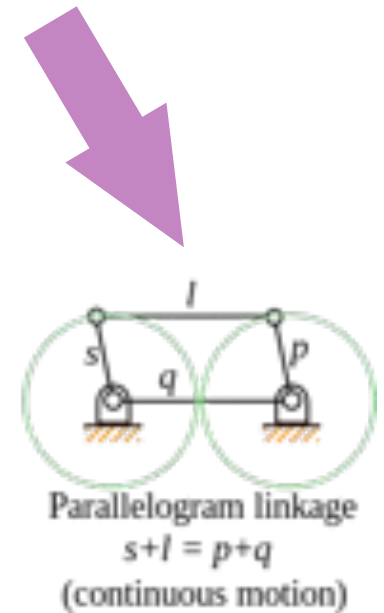
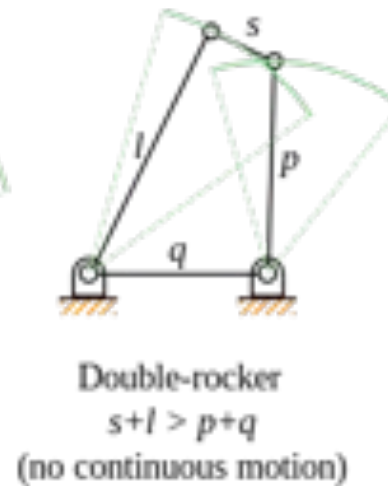
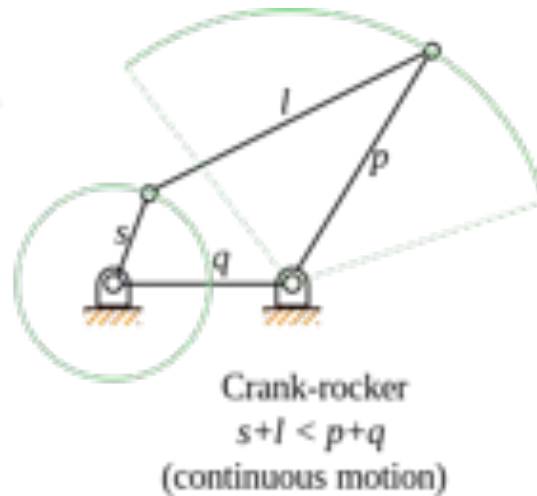
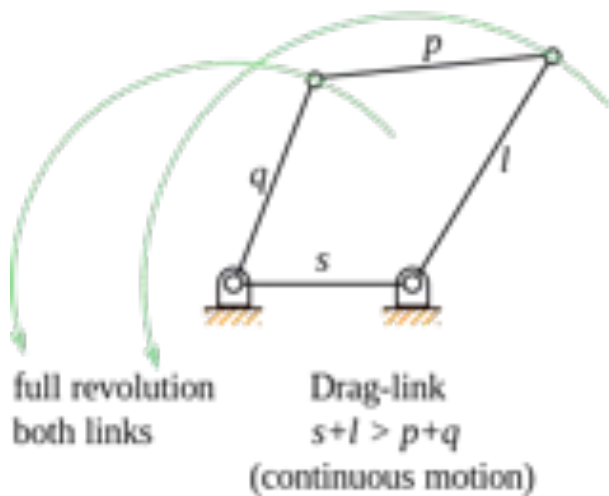
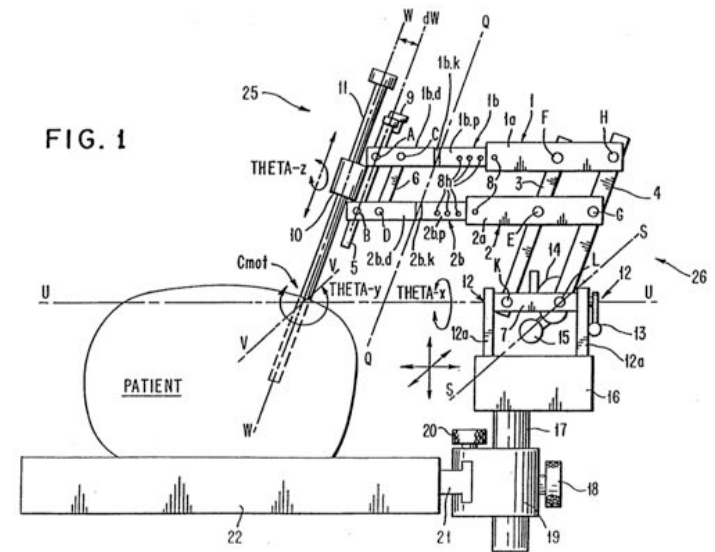
a remote center of motion (RCM) robot



US patent 5397323 (Taylor, et al.)

four-bar linkage

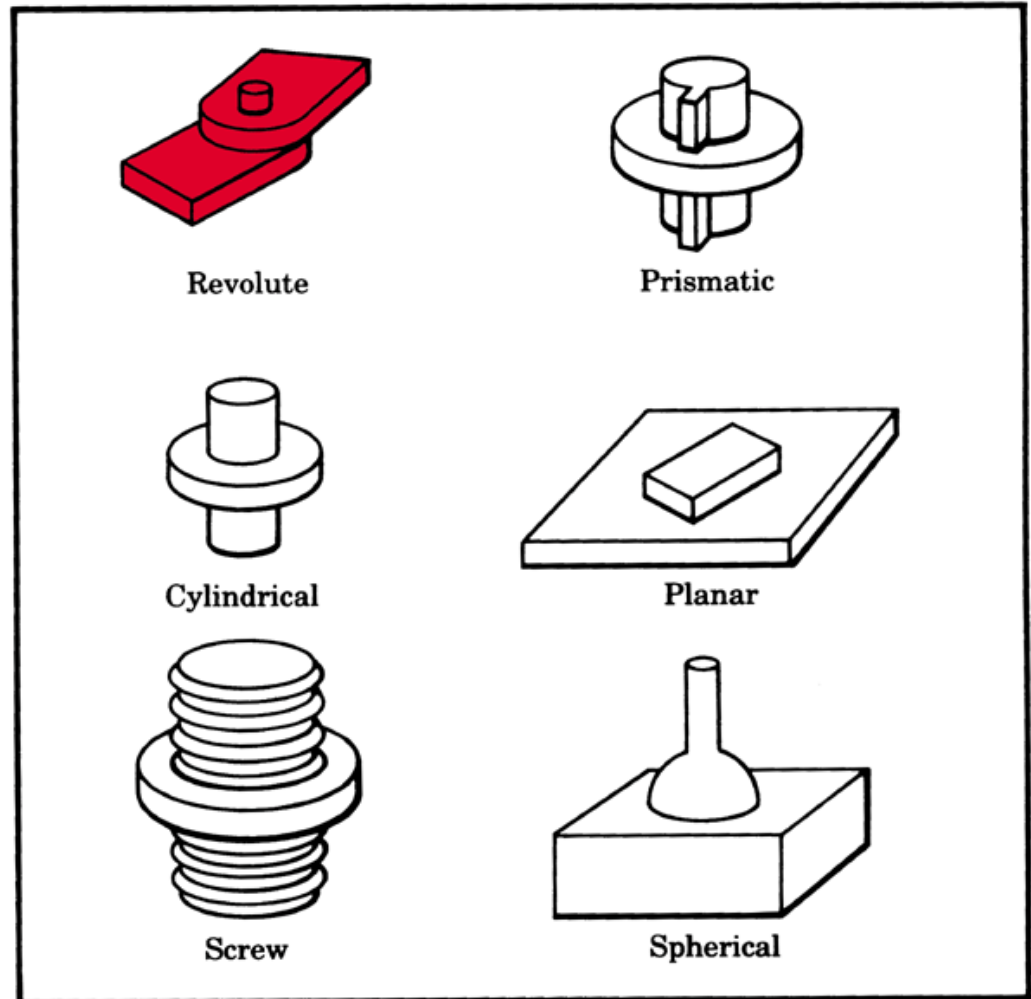
- commonly used 1-DOF mechanism
- relationship between input link angle and output link angle can be computed from geometry



Types of four-bar linkages, s = shortest link, l = longest link

joints

- A robot manipulator a set of bodies connected by a chain of joints
- **Revolute** is the most common - why?



continuum robots

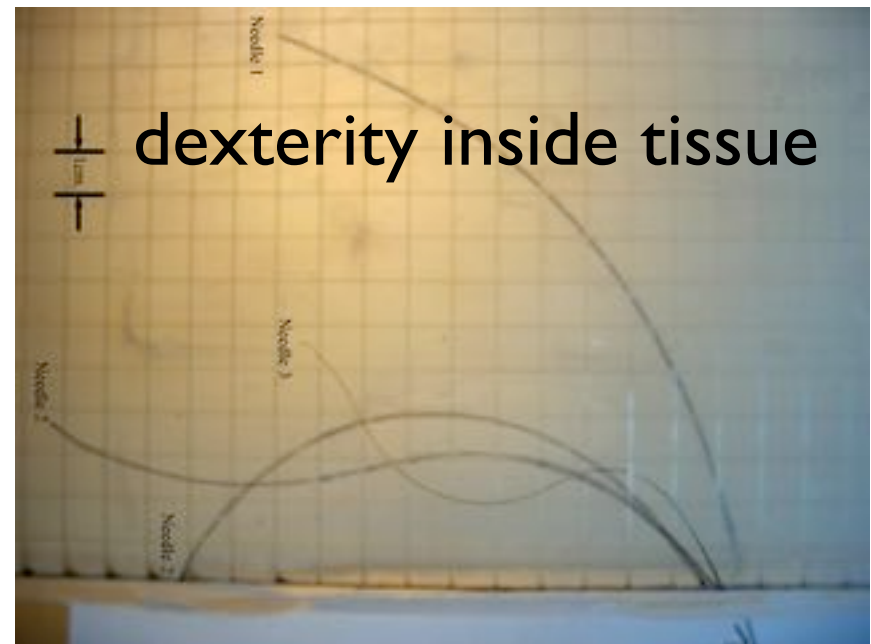
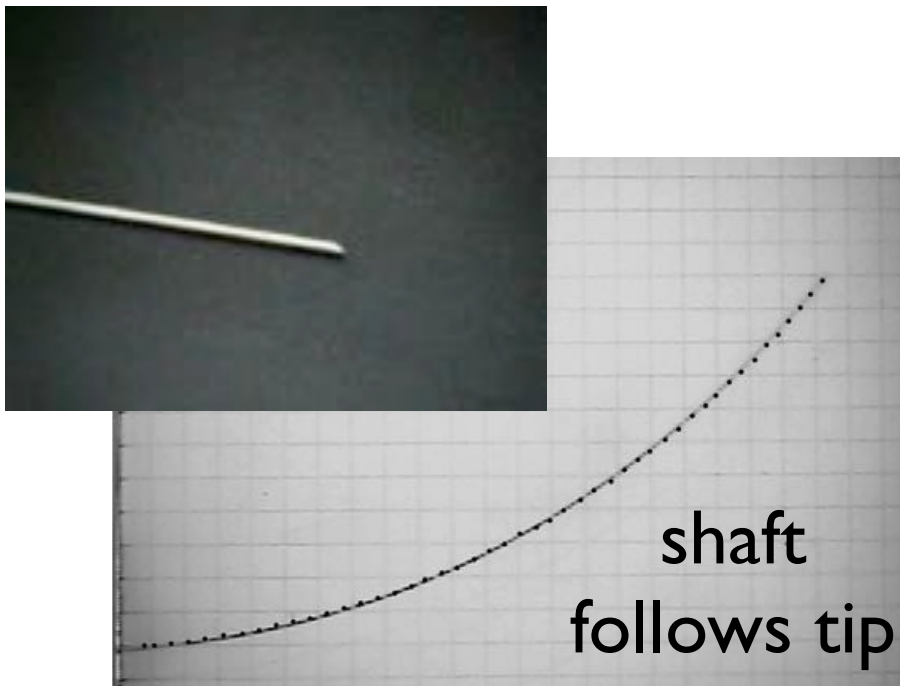
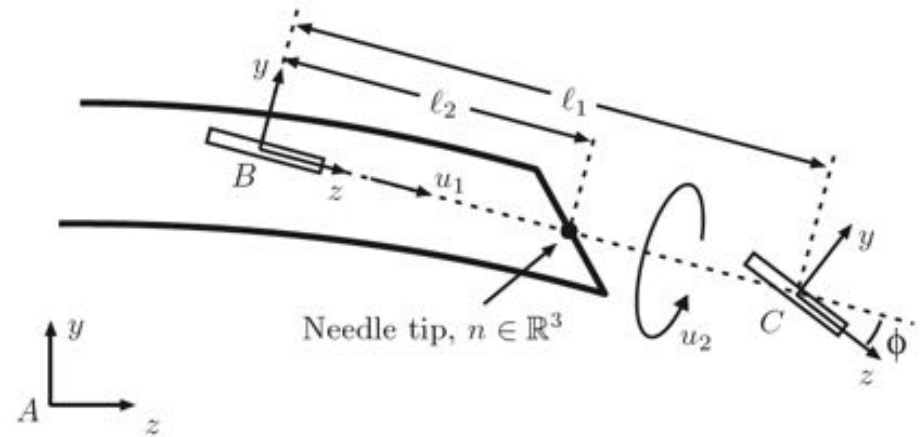
R. J. Webster III and B. A. Jones, “Design and Kinematic Modeling of Constant Curvature Continuum Robots: A Review,” *International Journal of Robotics Research*, 29(13):1661-1683, 2010.
doi: 10.1177/0278364910368147

J. Burgner-Kahrs, D. C. Rucker, H. Choset, “Continuum Robots for Medical Applications: A Survey”, *IEEE Transactions on Robotics*, 31(6):1261-1280, 2015.
dos: 10.1109/TRO.2015.2489500

steerable needles

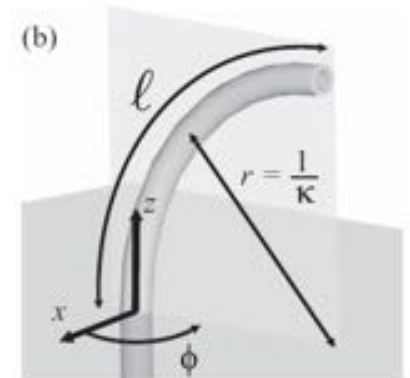
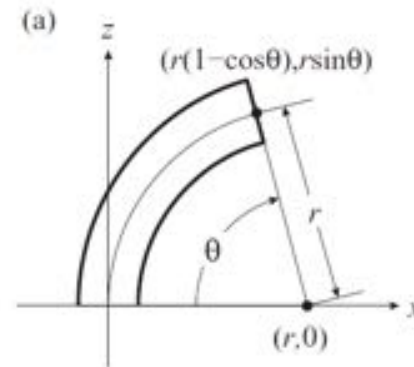
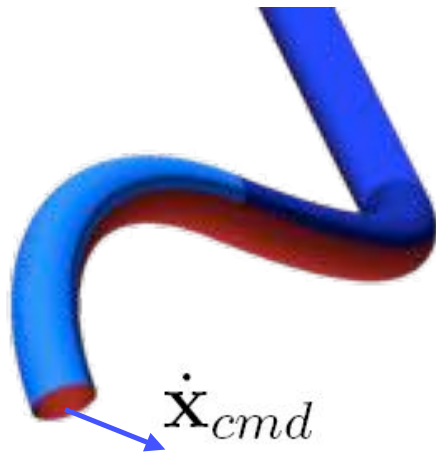
classic nonholonomic
“bicycle” model

the system is controllable
(nonholonomy degree 4)



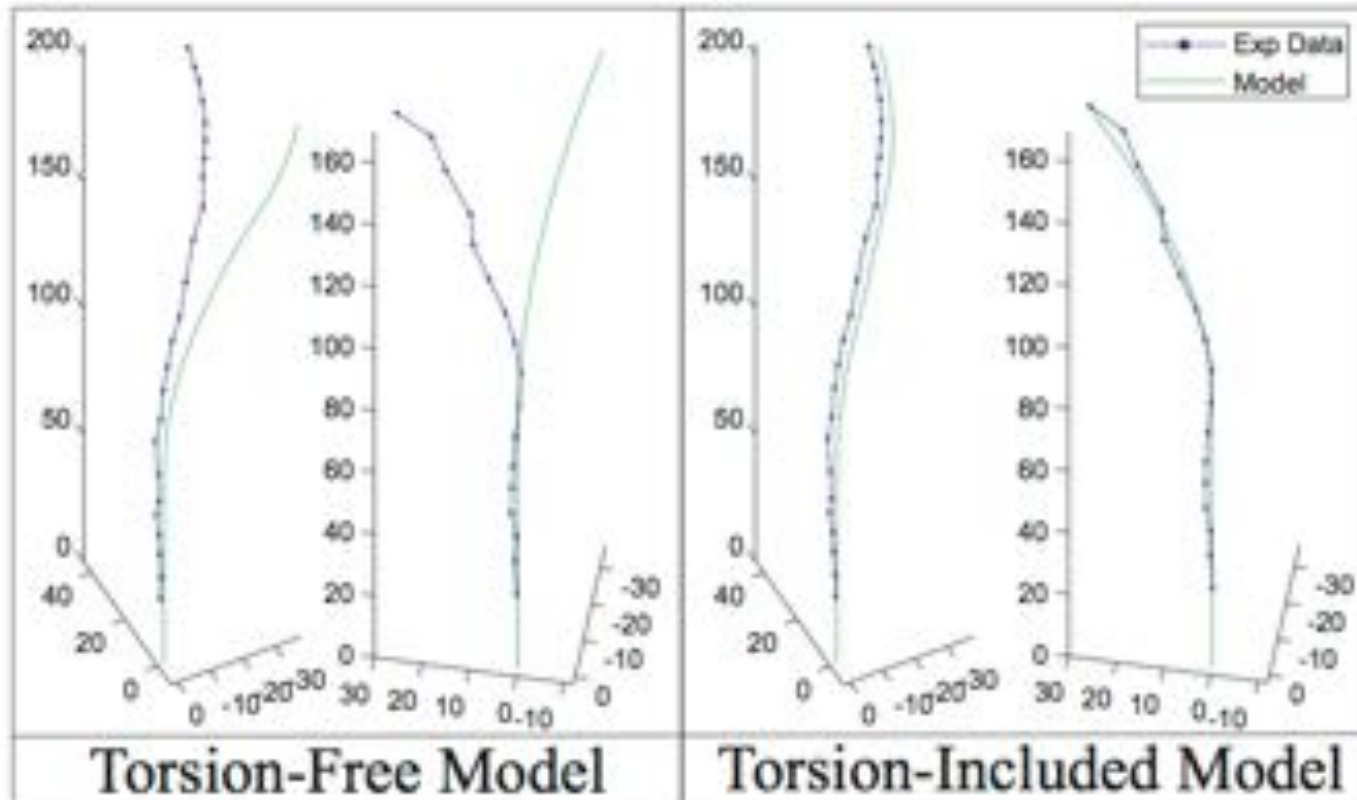
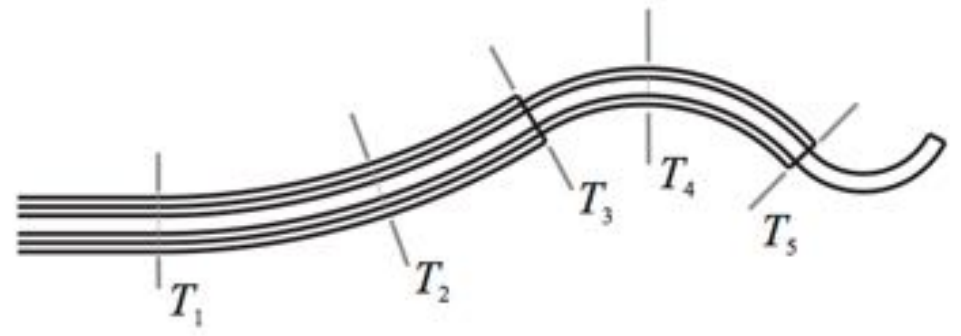
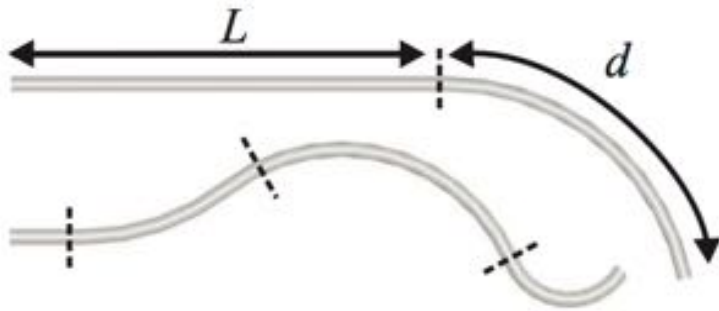
tendon-driven

- $\mathbf{x} = f(\mathbf{y})$ non-linear task-space kinematics
- $\boldsymbol{\tau} \geq \mathbf{0}$ actuation limitation
- Tendon driven systems often redundant

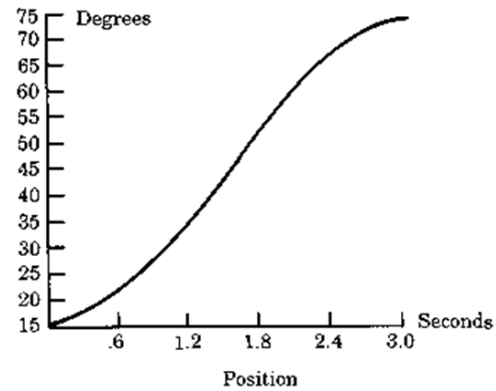


$$\begin{aligned}
 & \underset{\mathbf{y}(t + \Delta t)}{\text{minimize}} && \|\mathbf{C}_m^{-1} \mathbf{y}(t + \Delta t)\| \\
 & \text{subject to} && \dot{\mathbf{x}}_{cmd} \Delta t - (f(\mathbf{y}(t + \Delta t)) - f(\mathbf{y}(t))) = \mathbf{0}, \\
 & && \mathbf{C}_m^{-1} \mathbf{y}(t + \Delta t) \geq \mathbf{0}
 \end{aligned}$$

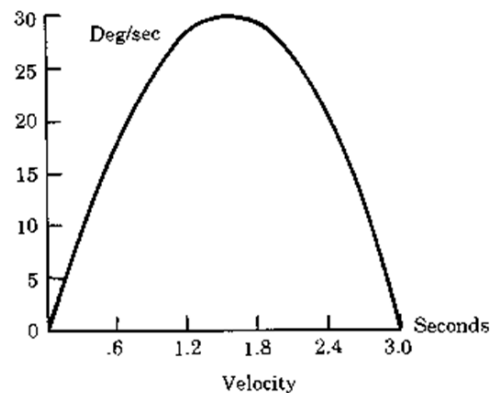
active cannulas



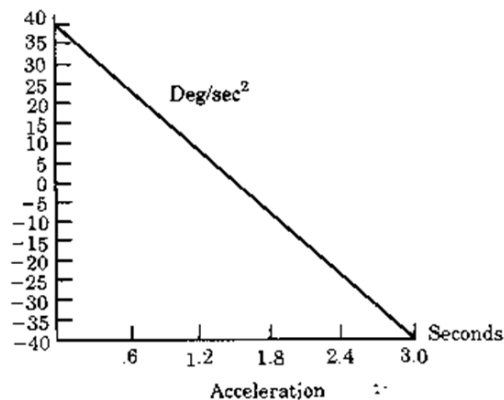
trajectory generation



position
cubic polynomial
C1 continuous



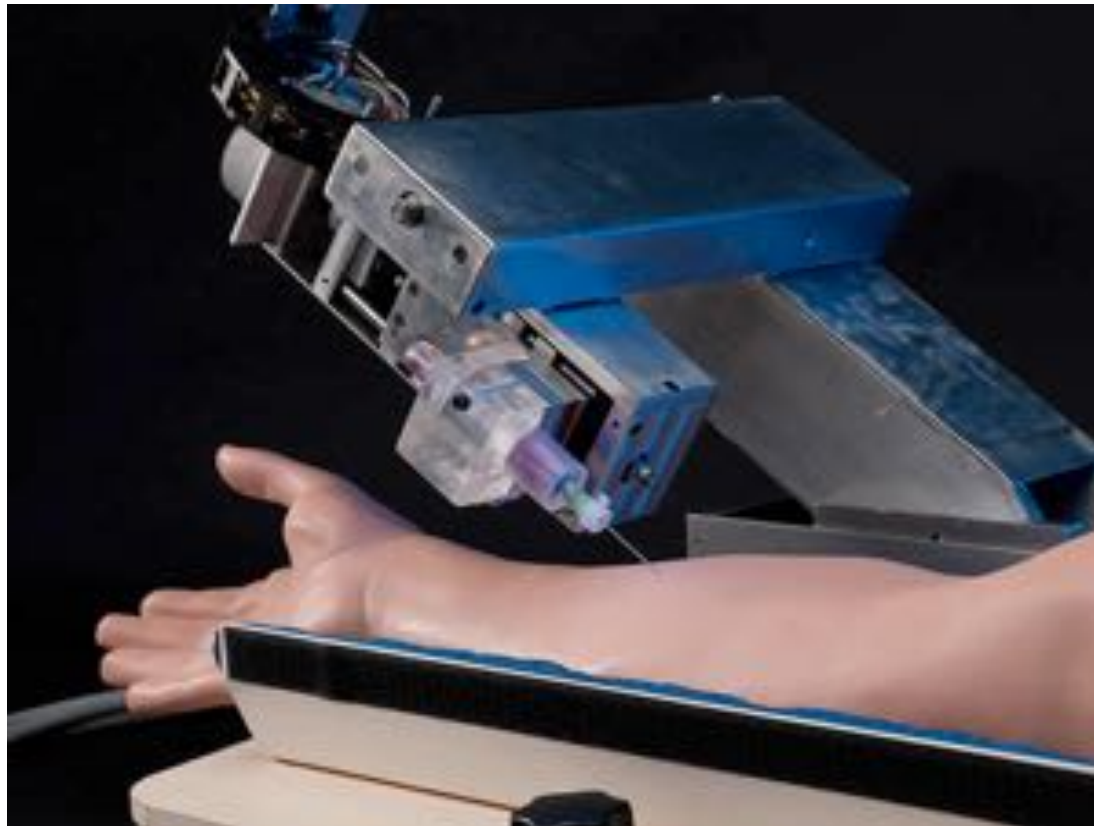
velocity
quadratic polynomial
C0 continuous



acceleration
quadratic polynomial
not continuous

discussion

what kind of kinematics/trajectory would you want for a robot that inserts a needle into solid tissue?

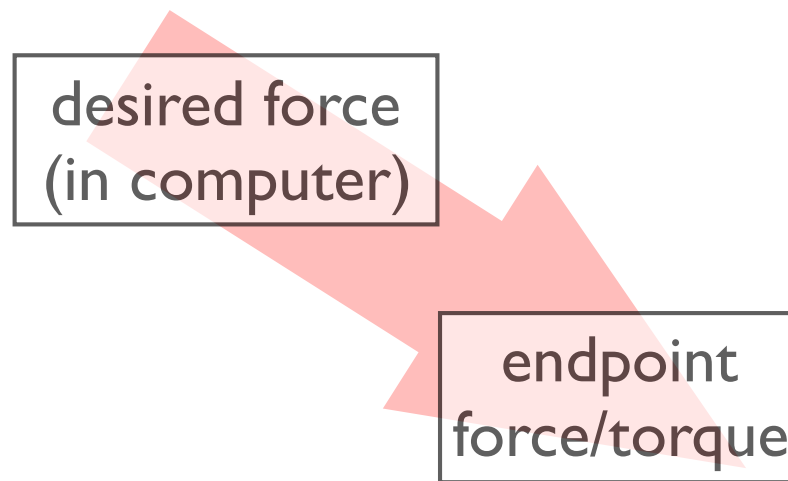


bloodbot (Imperial College of London)

controller on one end, system dynamics on the other

a controller computes
the desired force

e.g. $f = k_p * (x - x_d)$



this force and externally applied
loads result in robot motion

e.g., solve for x in $f = m\ddot{x} + b\dot{x}$

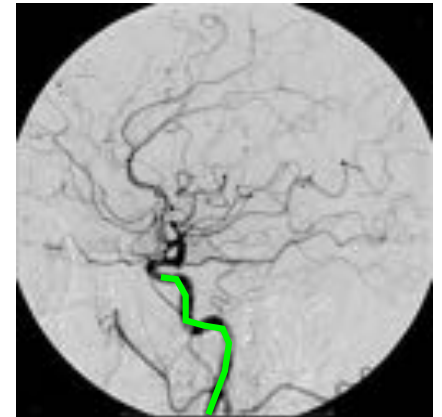
Sensors, Tracking, and Surgical Navigation

tracking

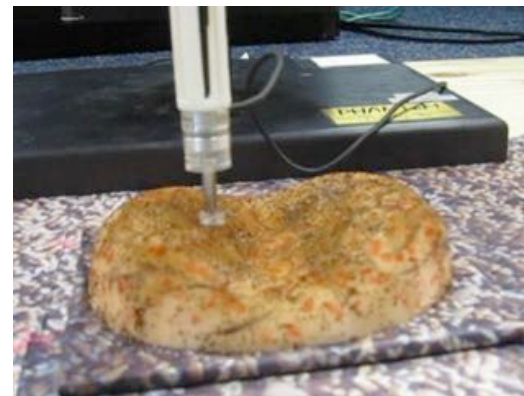
goal: to determine the position and orientation of tools and anatomical structures in image-guided procedures

typical purposes:

1. display a dynamic virtual representation on screen relative to real images (e.g., augmented reality)

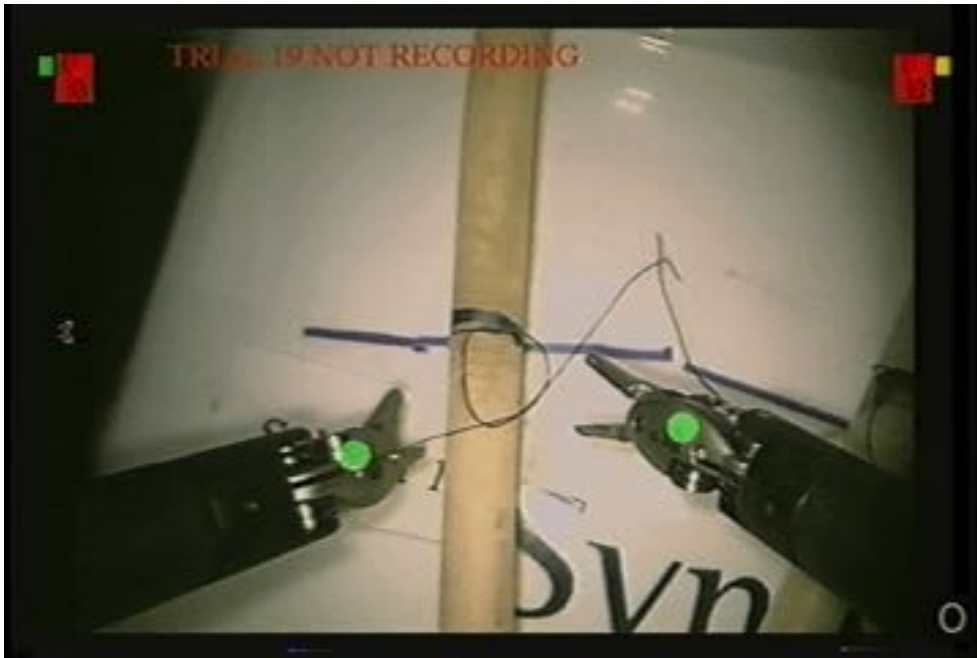


2. control a robot based on pose changes of tools and anatomical structures

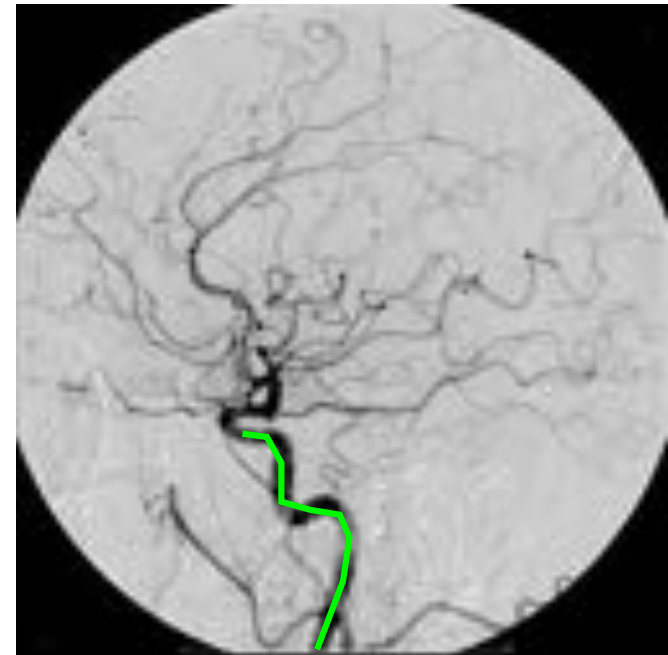


goal I : information display

display a dynamic virtual representation on screen relative to real images (e.g., augmented reality)



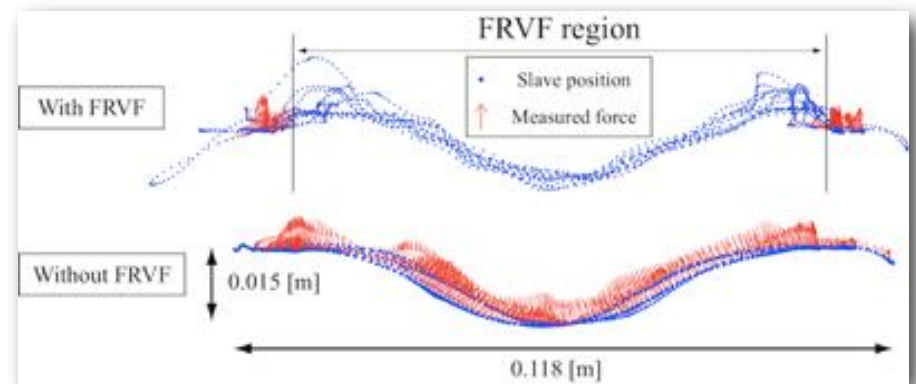
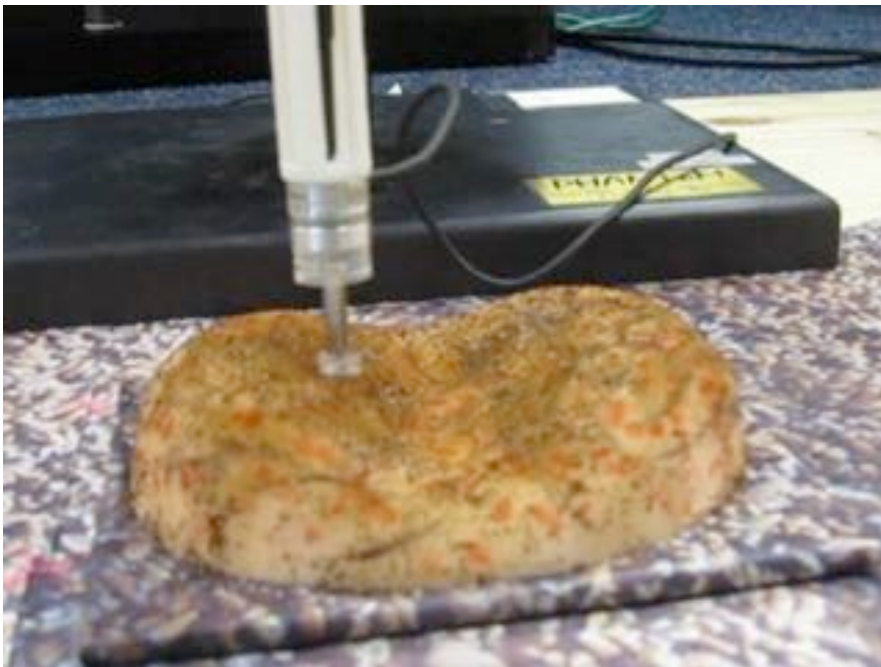
here, instruments are tracked so that “force dots” can be placed on them to prevent occlusion of the workspace



here, a dynamic graphical image of a catheter is overlaid on a static DSA image

goal 2: robot control

control a robot based on pose changes of tools and anatomical structures



in this example, virtual fixtures are created to keep the instrument away from the tissue surface

tracking requirements

1. Refresh rate: refresh rate of $\sim 100\text{Hz}$ with a latency of less than 1ms, regardless of the number of tracked objects.
2. Concurrency: tracks up to n sensors concurrently.
3. Working volume: meets the needs of the procedure
4. Obtrusiveness: sensors are wireless and can function for several hours, all hardware components can be positioned so that they do not restrict the physical access to the patient, and the system does not have any effect on other devices used during the procedure
5. Completeness: sensors are small enough to embed in any tool and provide all 6DOF
6. Accuracy: resolution less than 0.1mm and 0.1°
7. Robustness: not affected by the environment (light, sound, ferromagnetic materials, etc.)
8. Cheap: costs less than $\sim \$5000$

G.Welch and E. Foxlin. Motion Tracking: No Silver Bullet, but a Respectable Arsenal. IEEE Computer Graphics and Applications, 22(6):24-38, 2002.

slide from Ziv Yaniv, Sheikh Zayed Institute for Pediatric Surgical Innovation Children's National Medical Center

mechanical tracking

method: robot kinematics combined with joint sensing is used to compute an end-effector position
(this comes for free with a robot!)

caution:

- accuracy depends on correct kinematics
- limited workspace, obtrusive



stereotactic frame



coordinate measuring
machine (e.g. Faro Arm)



robot (e.g., Mako)

optical tracking

method: use camera rigs to track fiducial markers that are attached to the instrument or anatomical structure of interest



passive markers: spherical markers reflect infrared light, emitted by illuminators on the position sensor

active markers: infrared-emitting markers are activated by an electrical signal (example: Polaris, NDI)

what are the advantages and disadvantages over mechanical trackers?
what about “traditional” computer vision?

electromagnetic tracking

method: a transmitter (magnetic field generator) is used to induce a current in sensor coils that can be embedded into the tracked objects



Aurora, NDI

transmitter



sensor coils



TrakStar, Ascension

what are the advantages and disadvantages over optical trackers?



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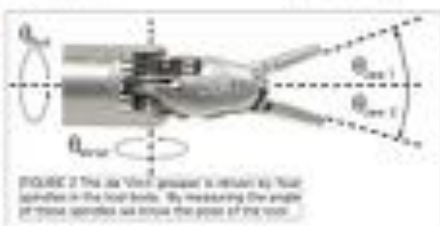
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OBJECTIVE

Robotic surgery provides high resolution video and instrument movement data useful in assessing surgical skill. This data could enable the development of training algorithms to accelerate learning curves. However, only a few research centers have access to the instrument data housed within the da Vinci robot's Application Programming Interface (API). Here we present a hardware and software solution that obviates the need for da Vinci API access during dry, cadaver, and animal lab training: SurgTrak. Our method achieves comparable data (all degrees of freedom of the tool and wrist and camera) to the da Vinci API at a far lower cost and without the intellectual property agreements needed to license API access from Intuitive Surgical. Our hardware and software is highly configurable and does not put the robot at risk of damage or malfunction. Further, it is deployable to any unmodified da Vinci robot.



DESCRIPTION

Our system consists of synchronized video and surgical tool motion recording unified by custom software. Video is recorded at up to 30Hz from the da Vinci master console using an Epiphan DV2USB device, Epiphan Systems Incorporated, Ottawa, Ontario, Canada. Tool position and orientation are captured with a 3D Guidance trakSTAR magnetic tracking system, Ascension Technology Corporation, Burlington, VT, USA. Grasper and wrist position is recorded by measuring the angular position of the four spindles driving the four tool degrees of freedom (See figures 2 and 3). Custom USB-enabled hardware based on PhidgetsInterfaceKit 8/8/8 (Phidgets Incorporated, Alberta, Calgary, Canada) was developed, including a set of inexpensive potentiometers that extract absolute spindle angle and additional environmental signals. Data streams from the video recording, position recording and wrist signal recording are united by purpose-built Visual C++ software running on a Windows 7 based laptop computer utilizing the windows multimedia timer.

RESULTS

SurgTrak requires no modification of the da Vinci surgical robot and no access to its inner workings. It can be adapted to da Vinci standard, da Vinci S and da Vinci Si surgical robots. The addition of SurgTrak recording equipment is transparent to the surgeon. It requires only one wired connection to each tool and camera. Data is recorded to compact, manageable files for later analysis. Video data can be analyzed manually via an Objective Structured Assessment of Technical Skills protocol or via automated methods. SurgTrak is currently in use in a multicenter study to validate robotic surgical education curricula. Two complete systems have been constructed and deployed: one to the University of Washington Institute for Simulation and Interprofessional Studies (ISIS) and the second to Madigan Army Medical Center. To date, over 750 iterations of surgery-like tasks have been logged. These include tasks such as FLS Block Transfer and a new, more challenging rocking peg-board task. Figure 4 depicts the system and typical results.



Surgical Data Capture Using SurgTrak



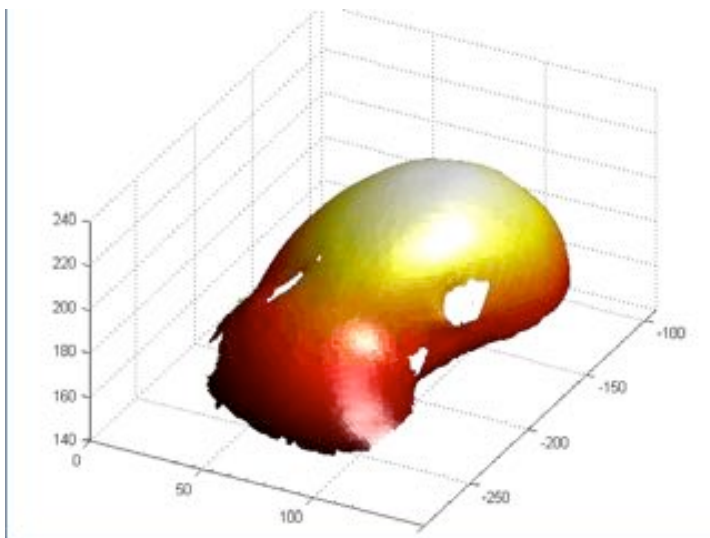
surface imaging (computer vision, depth sensing)



Bumblebee Firewire Stereo Vision Camera



Microsoft Kinect



Optimet
Conoprobe
surface
scanning
(Vanderbilt)

Sick Laser Measurement Sensor

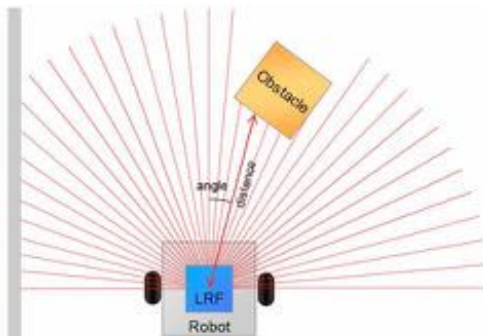
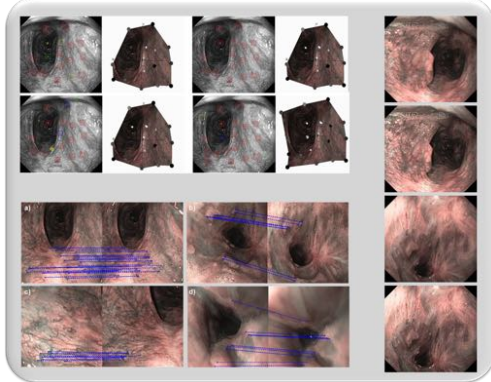


image: Microsoft

other trackers



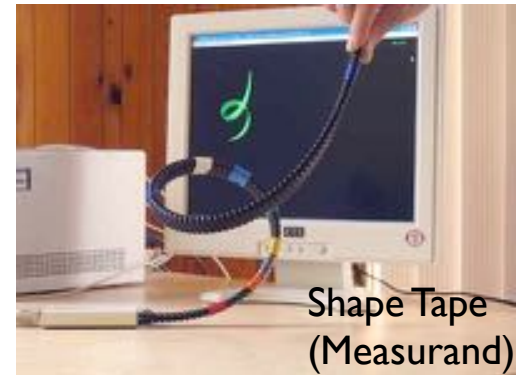
optical ego-motion
(self-motion) computes
camera motion;
appropriate for
endoscopes

Technische Universität München

ultrasonic systems: sound
point sources are attached
to the objects; time of flight
between the source and a
number of detectors is used
to estimate the location of
the source

inertial measurement units
use accelerometers and
gyroscopes to detect
acceleration and orientation

Shape Tape uses fiber
optics to estimate the
location and orientation
along its length



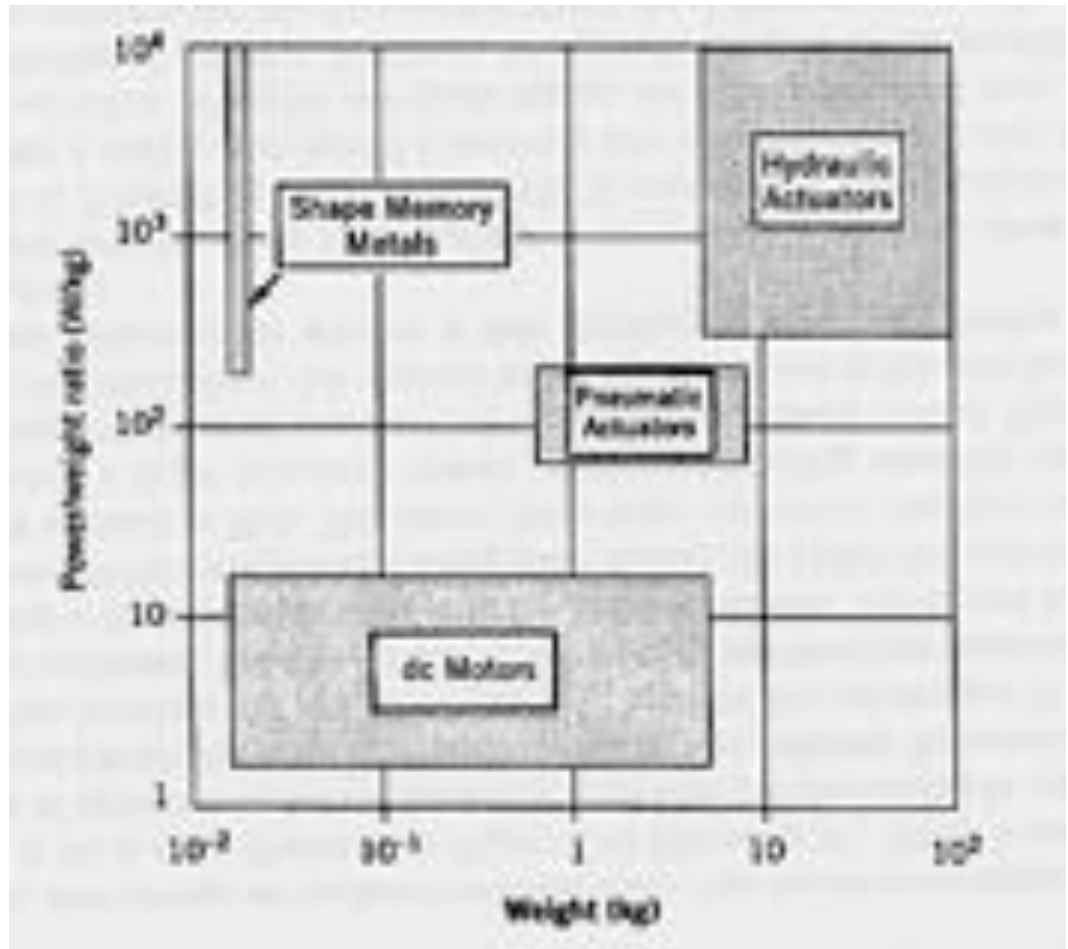
Shape Tape
(Measurand)

Virginia Tech Shape Tape example: <http://www.youtube.com/watch?v=ZMZrIjNDVGY>

Actuators

actuator types

- Electric motors
 - DC (direct current)
 - Brushed
 - PM (permanent magnet)
- Pneumatic Actuators



Pneumatic Actuators

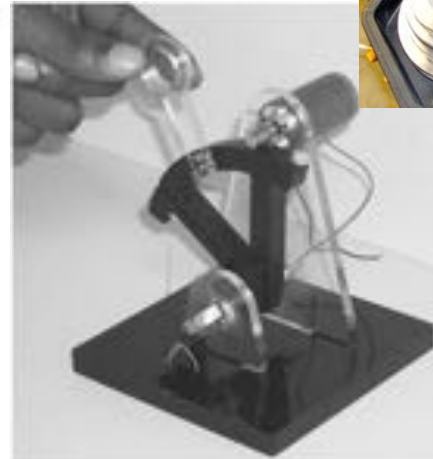
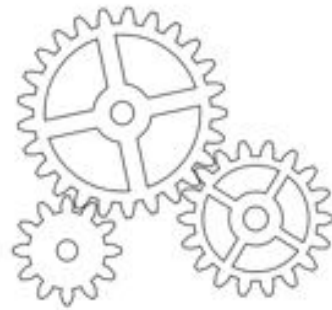
- How do they work?
 - Compressed air pressure is used to transfer energy from the power source to haptic interface.
- Many different types
- Concerns are friction and bandwidth

transmission

- Transfers/amplifies force/torque from motor
- You don't want to feel or see the effects of the transmission!

- Types:

- Gears
- Belts/pulleys
- Capstan Drive
- None (direct drive)

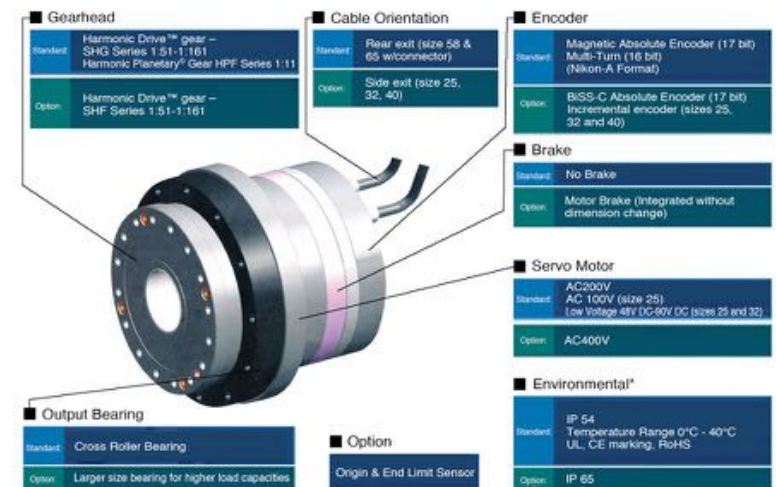


harmonic drive

- mechanical gear system
- advantages:
 - no backlash
 - compactness and light weight
 - high gear ratios
 - high torque capability
 - coaxial input and output shafts



wikipedia.org



*Environmental: Standard product housing design structurally meets IP-54 requirements.
Note: The output shaft and encoder cable seals, in the top contact areas, are not IP-54 compliant both in static and dynamic conditions.
Connectors: SHH-35A, 32A and 45A are not IP-54 compliant. SHH-58A and 65A connectors are IP-54 compliant provided they are connected to equivalent mating connector.

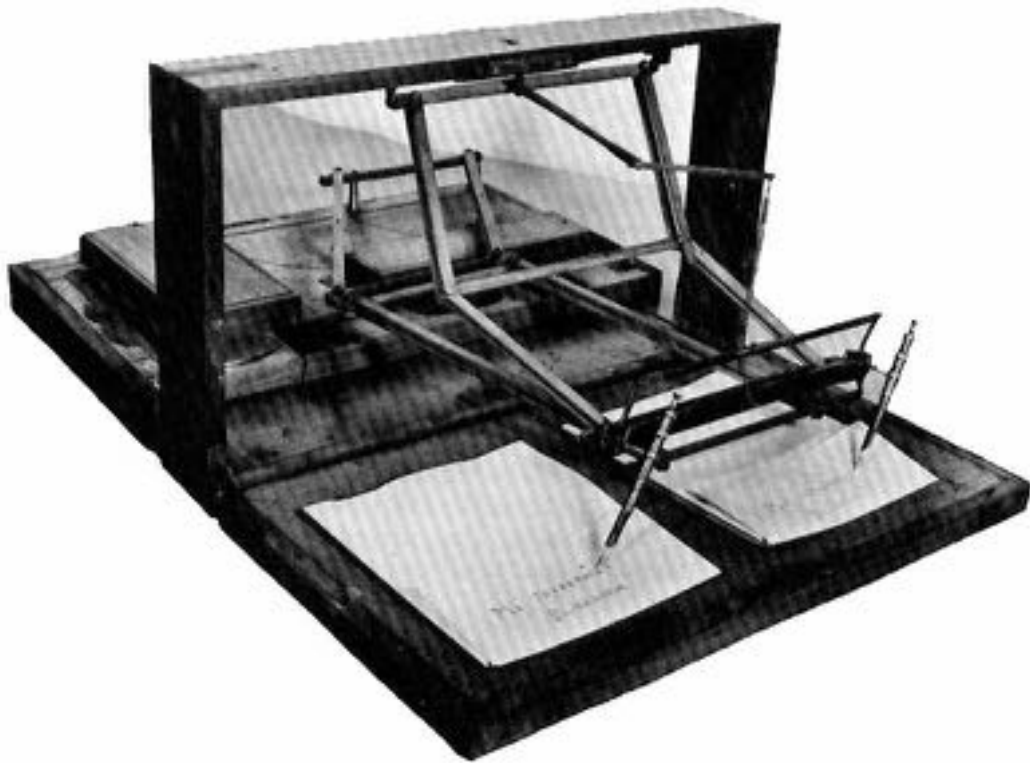
capstan drive

- High force
- Low friction
- Make sure it doesn't slip!



Teleoperation

the genesis of teleoperation?



A Polygraph is a device that produces a copy of a piece of writing simultaneously with the creation of the original, using pens and ink.

Famously used by Thomas Jefferson ~1805.

Typically uses a pantograph mechanism: a four-bar linkage with parallel bars such that motion at one point is reproduced at another point

teleoperation history

History:

- First Master-Slave Manipulator: 1948, Ray Goertz, U.S. Atomic Energy Commission
- Goal: protection of workers from radiation, while enabling precise manipulation of materials
- a device which is responsive to another device is termed a "slave" and the controlling device is termed a "master"

At first, mechanical linkages and cables

- 1954: electrical and hydraulic servomechanisms
- 1960s: Closed circuit television and HMDs



these people probably
never envisioned
robot-assisted surgery



in surgery,
slave robot =
patient-side robot

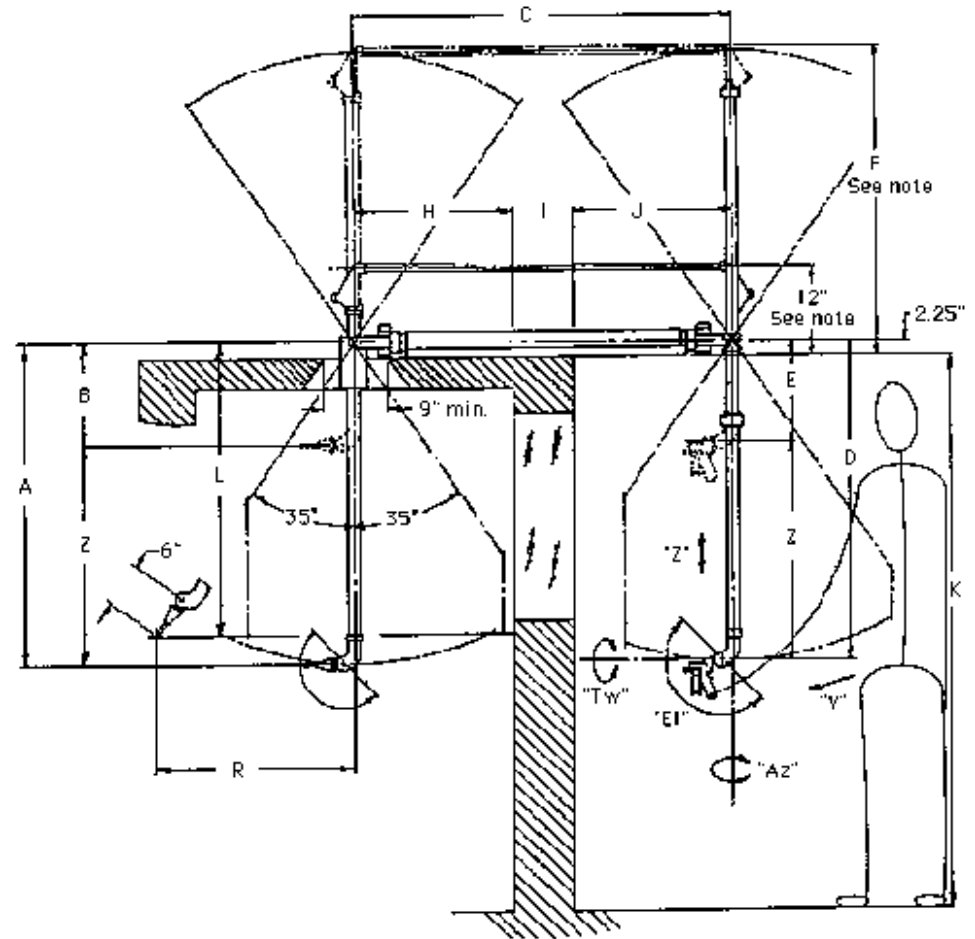


bilateral control: force/haptic feedback

inherent in “mechanical”
teleoperators

forces at the slave end-
effector are reflected to the
master end-effector

displacements produced at the
slave end-effector produce a
displacement at the master
end-effector



modern telemanipulators

Undersea: exploration and oil acquisition

Space

- 1967: Surveyor III landed on the surface of the Moon (a few seconds delay in the two-way transmission to earth of commands and information)
- 1976: Viking spacecraft, landed on Mars was programmed to carry out strictly automated operations
- Shuttle Remote Manipulator System (SRMS): retrieves satellites and place them in the cargo bay; mobile work platform for astronauts during space walks



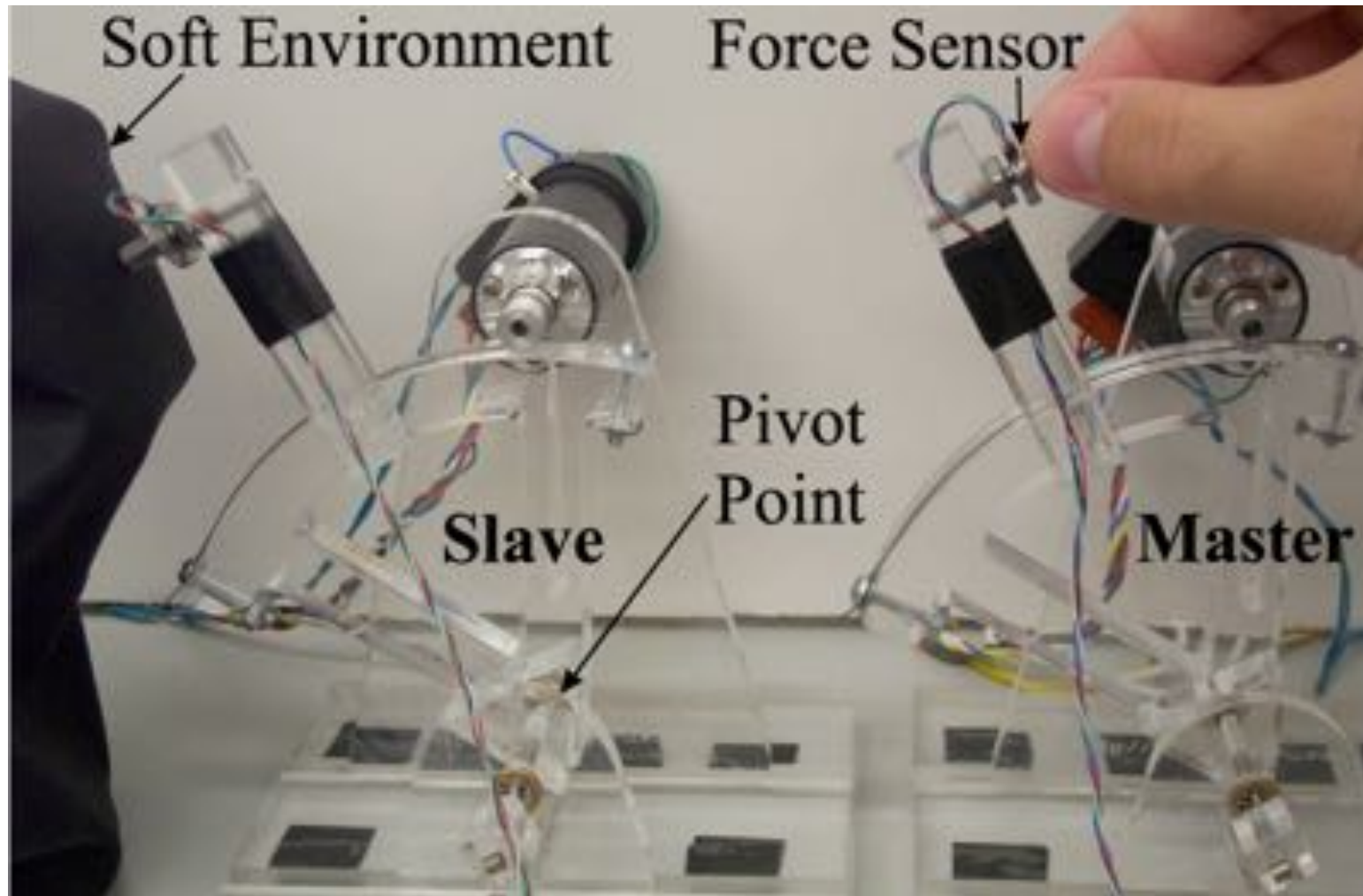
even more dexterous teleoperation

Robonaut

- Robot Systems Technology Branch at NASA's Johnson Space Center
- Purpose: Replace astronauts in dangerous missions, such as space walk, on the space shuttle and/or the space station
- Both autonomous operation and teleoperation are being developed



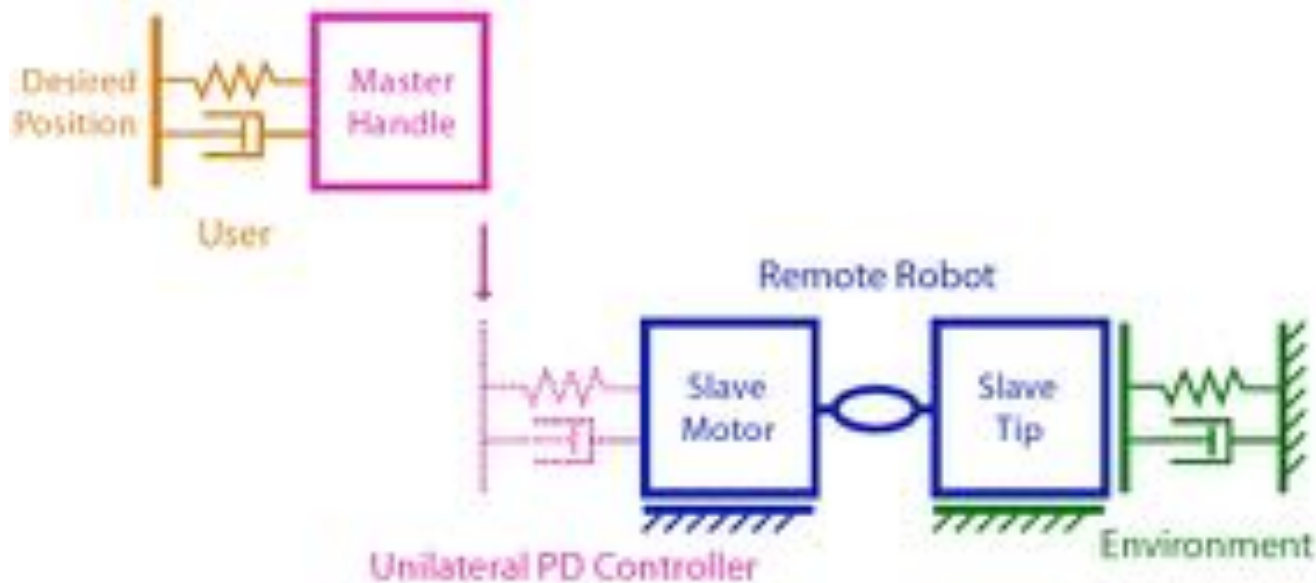
simple system example



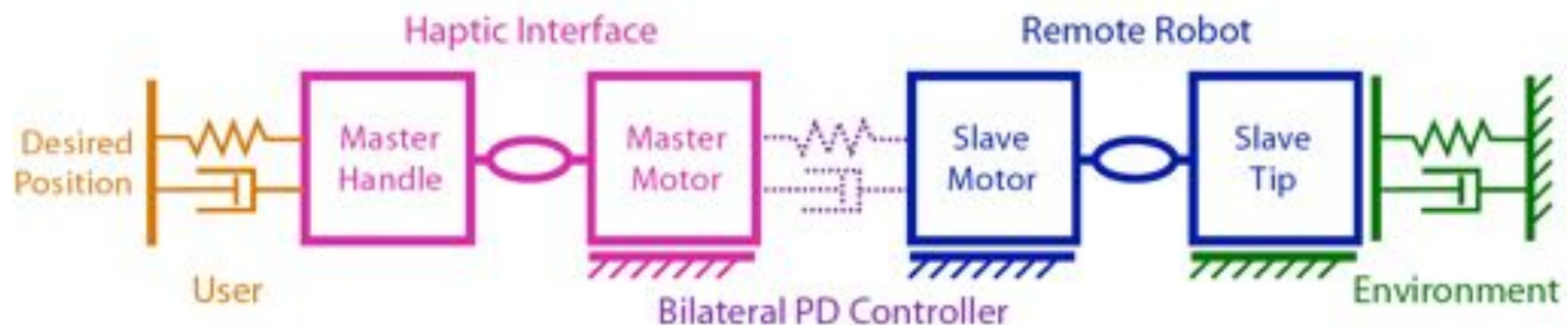
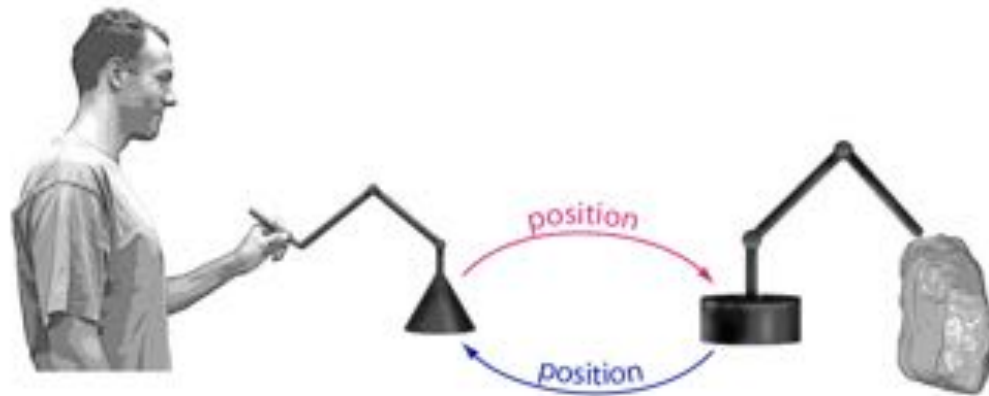
simple system example



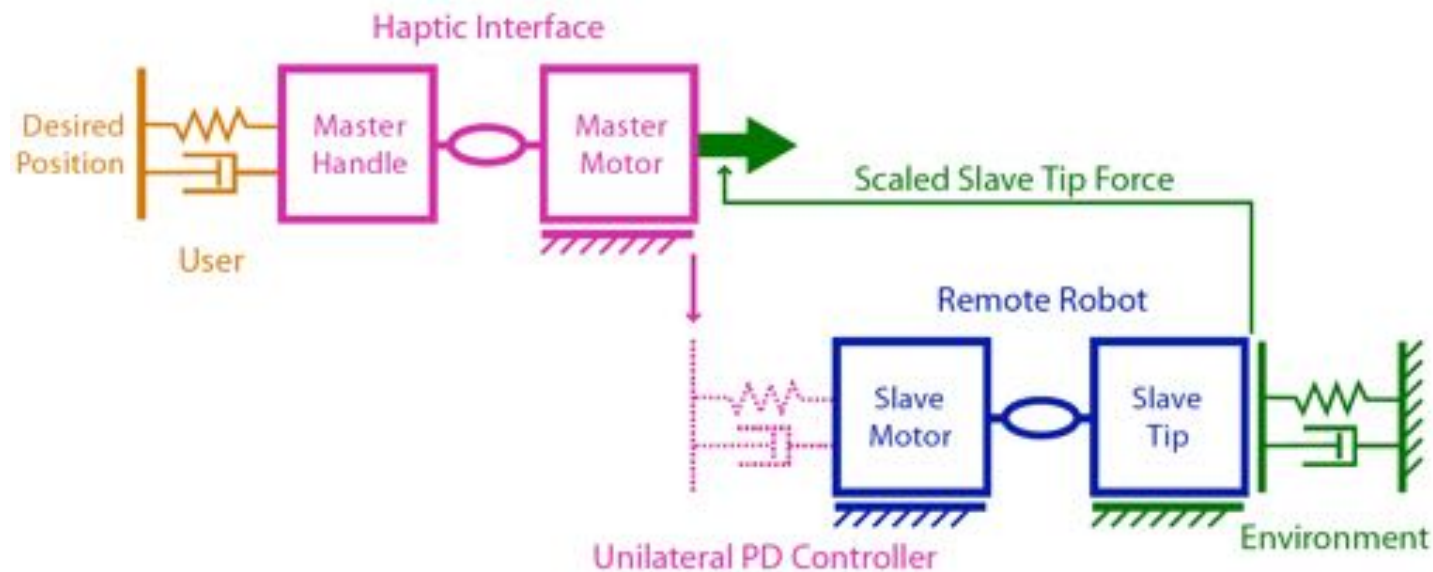
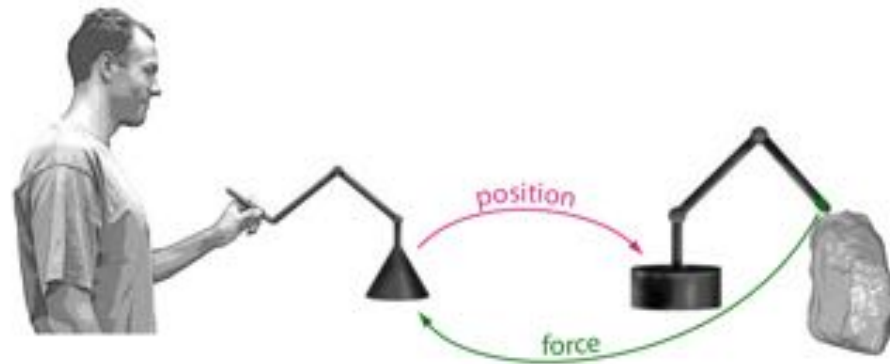
unilateral teleoperator model



bilateral teleoperator model (using position)



bilateral teleoperator model (using force)



typical slave robot controller

this is a proportional-derivative controller,
which attempts to make the slave follow the
master's position *and* velocity

$$f_{as}(t) = k_{ps}(x_m - x_s) + k_{ds}(\dot{x}_m - \dot{x}_s)$$

$f_{as}(t)$ slave actuator force

x_m position of master

x_s position of slave

k_{ps} slave proportional gain

k_{ds} slave derivative gain

every time the master's position is recorded, the slave robot attempts to follow the master using this control law

master robot controller for unilateral teleoperation

$$f_{am} = 0$$

$f_{am}(t)$ master actuator force

the force applied by the master actuator
(if it even exists) is zero

master robot controller for bilateral teleoperation (using position)

$$f_{am}(t) = k_{pm}(x_s - x_m) + k_{dm}(\dot{x}_s - \dot{x}_m)$$

$f_{am}(t)$ master actuator force

x_s position of slave

x_m position of master

k_{pm} master proportional gain

k_{dm} master derivative gain

every time the slave's position is recorded, the master robot attempts to follow the slave using this control law

master robot controller for bilateral teleoperation (using force)

$$f_{am}(t) = f_e$$

$f_{am}(t)$ master actuator force

f_e measured environment force

every time the force between the slave and the environment is recorded, the master robot outputs this amount of force

impedance control

attempts to make the user feel a particular impedance

an assumption often made in analysis/prediction of performance
both the master and slave are ideal impedance-type devices:

- linear $f(t) = m\ddot{x} + b\dot{x}$
- no multi-dof coupling
- no nonlinear friction
- no backlash
- infinite mechanical stiffness

questions

motion scaling: why would you want this, and how would you change the control laws to accomplish this?

force amplification: why would you want this, and how would you change the control laws to accomplish this?

questions

what might limit the values of the controller gains that you can choose?

what are the comparative advantages and disadvantages of position- and force-based bilateral teleoperation?

teleoperation performance metrics

tracking

the ability of the slave to follow the master

transparency

(for bilateral teleoperation only)

many definitions, but a popular one is whether the mechanical impedance felt by the user is the same as the impedance of the environment

questions

what factors might affect tracking?

what factors might affect transparency?

Cooperative Manipulation

so-called “steady-hand” robots



Mako's RIO Robotic Arm
Interactive Orthopedic System



JHU Eye Surgery Robot

steady-hand robot behavior



Warning!

If you are sensitive to graphic images/videos of surgical procedures, please step out for about 5 minutes.

MAKO Surgical Robot (makoplasty)



**Please bring back
any of our
sensitive friends
who left the room.**

Barrett WAM Arm



The WAM and associated technologies are the basis for the MAKO surgical robot

**Robodoc is a
similar system
(with much
more history)**

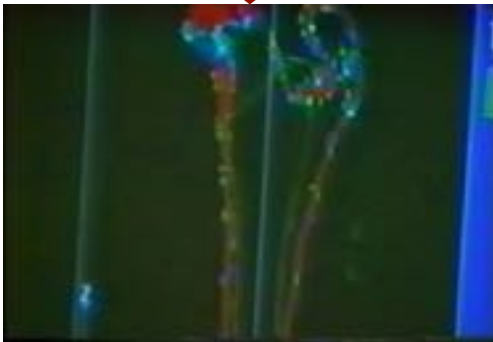


http://robodoc.com/patient_about_history.html

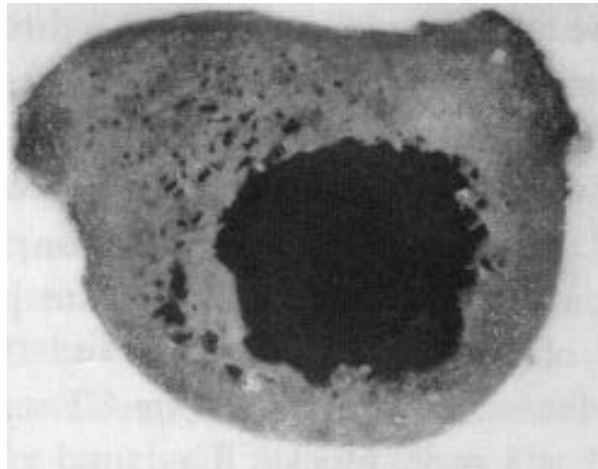
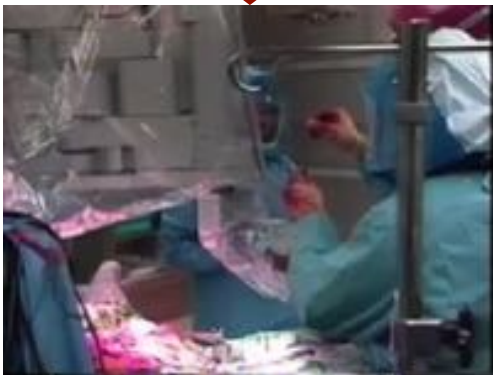
a more “intelligent” surgical system than the da Vinci?



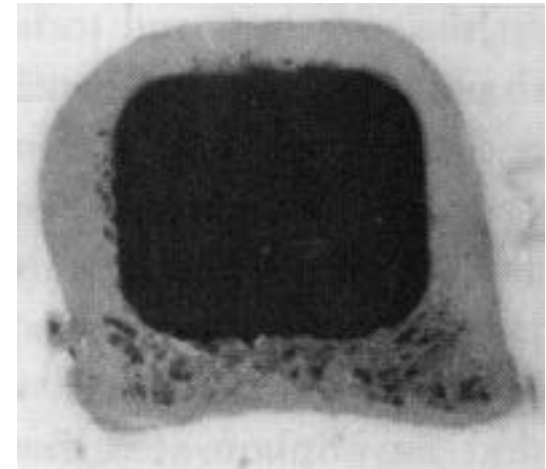
close integration with
information systems



more active user assistance



Manual Surgery



Robotic Surgery

admittance control

the user's applied force is measured, and the robot is controlled to move proportionally to that force

a typical implementation is:

$$\dot{x}_d = k_a f$$

$$f_a = k_p(x_d - x) + k_d(\dot{x}_d - \dot{x})$$

x_d, \dot{x}_d desired robot position, velocity

f_a actuator force

k_a admittance gain

x, \dot{x} robot position, velocity

f force applied by the user (measured)

k_p, k_d proportional and derivative gains

note: not all cooperative manipulators use admittance control, but many do...

questions

- what happens when k_a is zero?
- how would you create a virtual surface/wall using admittance control?

admittance control

enables very slow, steady motions

is an excellent underlying control structure for applying “virtual fixtures” to guide motions

can be applied to teleoperators as well as cooperative manipulators

for cooperative manipulation,
it is best used on a very accurate,
nonbackdrivable robot

impedance

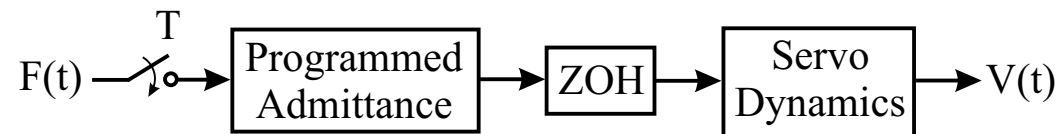
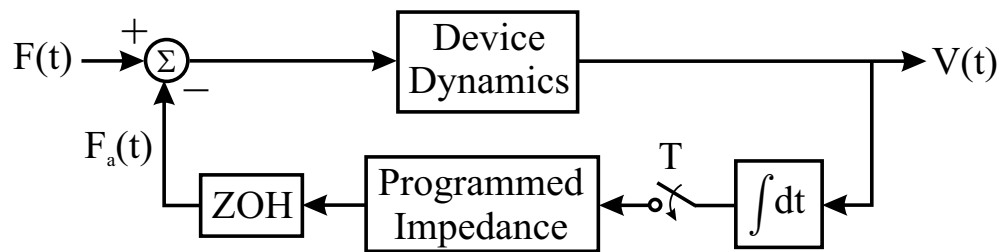
$$F(s) = Z(s)X(s)$$

admittance

$$X(s) = Y(s)F(s)$$

dual concepts, just different causality

with implications for practical implementation on robots



questions

- what are some advantages and disadvantages of cooperative manipulation as compared to teleoperation?
- what are some advantages and disadvantages of admittance control as compared to impedance control?