Estimating and Simulating a SIRD Model of COVID-19 for Many Countries, States, and Cities

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Extended results for Hubei, China
Based on data through October 9, 2020
Outline of Slides

• Basic data from Johns Hopkins CSSE (raw and smoothed)
• Brief summary of the model
• Baseline results ($\delta = 1.0\%, \gamma = 0.2, \theta = 0.1$)
• Simulation of re-opening – possibilities for raising $R_0$
• Results with alternative parameter values:
  ○ Lower mortality rate, $\delta = 0.8\%$
  ○ Higher mortality rate, $\delta = 1.2\%$
  ○ Infections last longer, $\gamma = 0.15$
  ○ Cases resolve more quickly, $\theta = 0.2$
  ○ Cases resolve more slowly, $\theta = 0.07$
• Data underlying estimates of $R_0(t)$
Underlying data from Johns Hopkins CSSE

- Raw data
- Smoothed = 7 day centered moving average
- No “excess deaths” correction (change as of Aug 6 run)
Hubei, China: Daily Deaths per Million People

Hubei, China

Daily deaths per million people

Feb Mar Apr May Jun Jul Aug Sep Oct

2020
Brief Summary of Model

• See the paper for a full exposition

• A 5-state SIRDC model with a time-varying $R_0$

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Baseline</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\delta$</td>
<td>1.0%</td>
<td>Mortality rate from infections (IFR)</td>
</tr>
<tr>
<td>$\gamma$</td>
<td>0.2</td>
<td>Rate at which people stop being infectious</td>
</tr>
<tr>
<td>$\theta$</td>
<td>0.1</td>
<td>Rate at which cases (post-infection) resolve</td>
</tr>
<tr>
<td>$\alpha$</td>
<td>0.05</td>
<td>Rate at which $R_0(t)$ decays with daily deaths</td>
</tr>
<tr>
<td>$R_0$</td>
<td>...</td>
<td>Initial base reproduction rate</td>
</tr>
<tr>
<td>$R_0(t)$</td>
<td>...</td>
<td>Base reproduction rate at date $t$ ($\beta_t/\gamma$)</td>
</tr>
</tbody>
</table>
Estimates of Time-Varying $R_0$

– Inferred from daily deaths, and
– the change in daily deaths, and
– the change in (the change in daily deaths)
(see end of slide deck for this data)
Hubei, China: Estimates of $R_0(t)$

Hubei, China
$\delta = 0.010 \quad \theta = 0.10 \quad \gamma = 0.20$
Hubei, China: Percent Currently Infectious

Peak I/N = 0.15% Final I/N = 0.03% δ = 0.010 θ = 0.10 γ = 0.20
Hubei, China: Growth Rate of Daily Deaths over Past Week (percent)

Hubei, China

$\delta = 0.010 \quad \theta = 0.10 \quad \gamma = 0.20$
Notes on Interpreting Results
Guide to Graphs

- **Warning**: Results are often very uncertain; this can be seen by comparing across multiple graphs. See the original paper.

- 7 days of forecasts: Rainbow color order!
  ROY-G-BIV (old to new, low to high)
  - Black = current
  - Red = oldest, Orange = second oldest, Yellow = third oldest...
  - Violet (purple) = one day earlier

- For robustness graphs, same idea
  - Black = baseline (e.g. $\delta = 1.0\%$)
  - Red = lowest parameter value (e.g. $\delta = 0.8\%$)
  - Green = highest parameter value (e.g. $\delta = 1.2\%$)
How does $R_0$ change over time?

- Inferred from death data when we have it
- For future, two approaches:
  - Alternatively, we fit this equation:
    \[
    \log R_0(t) = a_0 - \alpha (\text{Daily Deaths})
    \]
    \[\Rightarrow \alpha \approx .05\]
    
    $R_0$ declines by 5 percent for each new daily death, or rises by 5 percent when daily deaths decline
  
- Robustness: Assume $R_0(t) =$ final empirical value. Constant in future, so no $\alpha$ adjustment $\rightarrow \alpha = 0$
Repeated “Forecasts” from the past 7 days of data

- After peak, forecasts settle down.
- Before that, very noisy!
- If the region has not peaked, do not trust
- With $\alpha = .05$ (see robustness section for $\alpha = 0$)
Hubei, China (7 days): Daily Deaths per Million People ($\alpha = .05$)

Hubei, China
$R_0 = 1.3/0.2/0.2$  $\delta = 0.010$  $\alpha = 0.05$  $\theta = 0.1$  $\%$Infect = 1/1/1

DATA THROUGH 09-OCT-2020
Hubei, China (7 days): Cumulative Deaths per Million (Future, $\alpha = .05$)

Hubei, China

$R_0 = 1.3/0.2/0.2 \quad \delta = 0.010 \quad \alpha = 0.05 \quad \theta = 0.1 \quad \%\text{Infect} = 1/1/1$

DATA THROUGH 09-OCT-2020
Hubei, China (7 days): Cumulative Deaths per Million, Log Scale ($\alpha = 0.05$)

$R_0 = 1.3/0.2/0.2$  $\delta = 0.010$  $\alpha = 0.05$  $\theta = 0.1$  $\% \text{Infect} = 1/1/1$

New York City

Italy
Robustness to Mortality Rate, $\delta$
Hubei, China: Cumulative Deaths per Million ($\delta = .01/.008/.012$)

Hubei, China

$R_0 = 1.3/0.2/0.2 \quad \delta = 0.010 \quad \alpha = 0.05 \quad \theta = 0.1 \quad \%\text{Infect} = 1/1/1$

DATA THROUGH 09-OCT-2020
Hubei, China: Daily Deaths per Million People ($\delta = 0.01/0.008/0.012$)

Hubei, China

$R_0 = 1.3/0.2/0.2$  $\delta = 0.010$  $\alpha = 0.05$  $\theta = 0.1$  \%Infect = 1/1/1

DATA THROUGH 09-OCT-2020
Hubei, China: Cumulative Deaths per Million ($\delta = .01/.008/.012$)

Hubei, China

\[ R_0 = 1.3/0.2/0.2 \quad \delta = 0.010 \quad \alpha = 0.05 \quad \theta = 0.1 \quad \%\text{Infect} = 1/1/1 \]

DATA THROUGH 09-OCT-2020

\[ \delta = 0.008 \]
Reopening and Herd Immunity

– Black: assumes $R_0(today)$ remains in place forever
– Red: assumes $R_0(suppress) = 1/s(today)$
– Green: we move 25% of the way from $R_0(today)$ back to initial $R_0$ = “normal”
– Purple: we move 50% of the way from $R_0(today)$ back to initial $R_0$ = “normal”

NOTE: Lines often cover each other up
Hubei, China: Re-Opening ($\alpha = .05$)

Hubei, China

$R_0(t)=0.2$, $R_0\text{(suppress)}=1.0$, $R_0(25/50)=0.7/1.1$, $\delta = 0.010$, $\alpha=0.05$

(Light bars = New York City, for comparison)
Hubei, China: Re-Opening ($\alpha = 0$)

Hubei, China

$R_0(t)=0.2$, $R_0(\text{suppress})=1.0$, $R_0(25/50)=0.7/1.1$, $\delta = 0.010$, $\alpha=0.00$

(Light bars = New York City, for comparison)
Results for alternative parameter values
Hubei, China (7 days): Daily Deaths per Million People ($\alpha = 0$)

Hubei, China

$R_0 = 1.3/0.2/0.2$  $\delta = 0.010$  $\alpha = 0.00$  $\theta = 0.1$  %Infect = 1/1/1

DATA THROUGH 09-OCT-2020
Hubei, China (7 days): Cumulative Deaths per Million (Future, $\alpha = 0$)

Hubei, China

$R_0 = 1.3/0.2/0.2 \quad \delta = 0.010 \quad \alpha = 0.00 \quad \theta = 0.1 \quad \%\text{Infect} = 1/1/1$

DATA THROUGH 09-OCT-2020

Cumulative deaths per million people
Hubei, China (7 days): Cumulative Deaths per Million, Log Scale ($\alpha = 0$)

Hubei, China

$R_0=1.3/0.2/0.2 \quad \delta = 0.010 \quad \alpha=0.00 \quad \theta=0.1 \quad \%\text{Infect}=1/1/1$
Hubei, China: Daily Deaths per Million People ($\delta = 0.8\%$)

Hubei, China

$R_0 = 1.3/0.2/0.2$  $\delta = 0.008$  $\theta = 0.1$  $\gamma = 0.2$  $\%\text{Infect} = 1/1/1$

SOME ERRORS IN ESTIMATION...
Hubei, China: Cumulative Deaths per Million ($\delta = 0.8\%$)

Hubei, China

$R_0 = 1.3/0.2/0.2$  $\delta = 0.008$  $\theta = 0.1$  $\gamma = 0.2$  %Infect = 1/1/1

SOME ERRORS IN ESTIMATION...
Hubei, China: Daily Deaths per Million People ($\delta = 1.2\%$)

Hubei, China

$R_0=1.3/0.2/0.2$  $\delta = 0.012$  $\theta=0.1$  $\gamma=0.2$  $\%$Infect= 1/ 1/ 1

SOME ERRORS IN ESTIMATION...
Hubei, China: Cumulative Deaths per Million ($\delta = 1.2\%$)

Hubei, China
$R_0=1.3/0.2/0.2$  $\delta = 0.012$  $\theta=0.1$  $\gamma=0.2$  %Infect= 1/1/1

SOME ERRORS IN ESTIMATION...
Hubei, China: Daily Deaths per Million People ($\gamma = .2/.15$)

Hubei, China

$R_0 = 1.3/0.2/0.2 \quad \delta = 0.010 \quad \theta = 0.1 \quad \gamma = 0.2 \quad \%\text{Infect} = 1/1/1$

SOME ERRORS IN ESTIMATION...
Hubei, China: Cumulative Deaths per Million $\gamma = .2 / .15$
Hubei, China: Daily Deaths per Million People ($\theta = 0.1/0.07/0.2$)

Hubei, China

$R_0 = 1.5/0.2/0.2$, $\delta = 0.010$, $\theta = 0.2$, $\gamma = 0.2$, $\%\text{Infected} = 1/1/1$

SOME ERRORS IN ESTIMATION...
Hubei, China: Cumulative Deaths per Million People ($\theta = .1/.07/.2$)

Hubei, China

$R_0=1.5/0.2/0.2$  $\delta = 0.010$  $\theta=0.2$  $\gamma=0.2$  %Infect= 1/1/1

SOME ERRORS IN ESTIMATION...
Data Underlying Estimates of Time-Varying $R_0$

– Inferred from daily deaths, and
– the change in daily deaths, and
– the change in (the change in daily deaths)
Hubei, China: Daily Deaths, Actual and Smoothed

Hubei, China: Daily deaths, d

$\delta = 0.010 \quad \theta=0.10 \quad \gamma=0.20$
Hubei, China: Change in Smoothed Daily Deaths

\[ \delta = 0.010 \quad \theta = 0.10 \quad \gamma = 0.20 \]
Hubei, China: Change in (Change in Smoothed Daily Deaths)

\[ \delta = 0.010 \quad \theta = 0.10 \quad \gamma = 0.20 \]