Estimating and Simulating a SIRD Model of COVID-19 for Many Countries, States, and Cities

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Extended results for Moldova
Based on data through September 11, 2020
Outline of Slides

• Basic data from Johns Hopkins CSSE (raw and smoothed)
• Brief summary of the model
• Baseline results ($\delta = 1.0\%$, $\gamma = 0.2$, $\theta = 0.1$)
• Simulation of re-opening – possibilities for raising $R_0$
• Results with alternative parameter values:
  o Lower mortality rate, $\bar{\delta} = 0.8\%$
  o Higher mortality rate, $\bar{\delta} = 1.2\%$
  o Infections last longer, $\gamma = 0.15$
  o Cases resolve more quickly, $\theta = 0.2$
  o Cases resolve more slowly, $\theta = 0.07$
• Data underlying estimates of $R_0(t)$
Underlying data from Johns Hopkins CSSE

- Raw data
- Smoothed = 7 day centered moving average
- No “excess deaths” correction (change as of Aug 6 run)
Moldova: Daily Deaths per Million People
Moldova: Daily Deaths per Million People (Smoothed)
Brief Summary of Model

• See the paper for a full exposition

• A 5-state SIRDC model with a time-varying $R_0$

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Baseline</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\delta$</td>
<td>1.0%</td>
<td>Mortality rate from infections (IFR)</td>
</tr>
<tr>
<td>$\gamma$</td>
<td>0.2</td>
<td>Rate at which people stop being infectious</td>
</tr>
<tr>
<td>$\theta$</td>
<td>0.1</td>
<td>Rate at which cases (post-infection) resolve</td>
</tr>
<tr>
<td>$\alpha$</td>
<td>0.05</td>
<td>Rate at which $R_0(t)$ decays with daily deaths</td>
</tr>
<tr>
<td>$R_0$</td>
<td>...</td>
<td>Initial base reproduction rate</td>
</tr>
<tr>
<td>$R_0(t)$</td>
<td>...</td>
<td>Base reproduction rate at date $t$ ($\beta_t/\gamma$)</td>
</tr>
</tbody>
</table>
Estimates of Time-Varying $R_0$

– Inferred from daily deaths, and
– the change in daily deaths, and
– the change in (the change in daily deaths)
(see end of slide deck for this data)
Moldova: Estimates of $R_0(t)$

Moldova

$\delta = 0.010 \quad \theta = 0.10 \quad \gamma = 0.20$
Moldova: Percent Currently Infectious

Peak I/N = 0.14%  Final I/N = 0.14%  δ = 0.010  θ = 0.10  γ = 0.20
Moldova: Growth Rate of Daily Deaths over Past Week (percent)

Moldova

$\delta = 0.010 \quad \theta = 0.10 \quad \gamma = 0.20$
Notes on Interpreting Results
Guide to Graphs

- **Warning**: Results are often very uncertain; this can be seen by comparing across multiple graphs. See the original paper.

- 7 days of forecasts: Rainbow color order!
  - ROY-G-BIV (old to new, low to high)
    - Black = current
    - Red = oldest, Orange = second oldest, Yellow = third oldest...
    - Violet (purple) = one day earlier

- For robustness graphs, same idea
  - Black = baseline (e.g. $\delta = 1.0\%$)
  - Red = lowest parameter value (e.g. $\delta = 0.8\%$)
  - Green = highest parameter value (e.g. $\delta = 1.2\%$)
How does $R_0$ change over time?

- Inferred from death data when we have it

- For future, two approaches:
  1. Alternatively, we fit this equation:

$$\log R_0(t) = a_0 - \alpha(Daily\ Deaths)$$

$$\Rightarrow \alpha \approx .05$$

$R_0$ declines by 5 percent for each new daily death, or rises by 5 percent when daily deaths decline

- Robustness: Assume $R_0(t) = $ final empirical value. Constant in future, so no $\alpha$ adjustment $\rightarrow \alpha = 0$
Repeated “Forecasts” from the past 7 days of data

– After peak, forecasts settle down.
– Before that, very noisy!
– If the region has not peaked, do not trust
– With $\alpha = .05$ (see robustness section for $\alpha = 0$)
Moldova (7 days): Daily Deaths per Million People ($\alpha = .05$)

Moldova

$R_0 = 1.1/1.1/1.1$  $\delta = 0.010$  $\alpha = 0.05$  $\theta = 0.1$  %Infect = 3/4/8

DATA THROUGH 11-SEP-2020
Moldova (7 days): Cumulative Deaths per Million (Future, $\alpha = .05$)

Moldova

$R_0=1.1/1.1/1.1$  $\delta = 0.010$  $\alpha=0.05$  $\theta=0.1$  $\%$Infect= 3/ 4/ 8

DATA THROUGH 11-SEP-2020
Moldova (7 days): Cumulative Deaths per Million, Log Scale ($\alpha = .05$)

$R_0 = 1.1/1.1/1.1$, $\delta = 0.010$, $\alpha = 0.05$, $\theta = 0.1$, $\%$ Infect = 3/4/8
Robustness to Mortality Rate, $\delta$
Moldova: Cumulative Deaths per Million ($\delta = .01/ .008/ .012$)

Moldova

$R_0 = 1.1/1.1/1.1$  $\delta = 0.010$  $\alpha = 0.05$  $\theta = 0.1$  %Infect = 3/4/8

DATA THROUGH 11-SEP-2020
Moldova: Daily Deaths per Million People ($\delta = .01/.008/.012$)

Moldova

$R_0=1.1/1.1/1.1 \quad \delta = 0.010 \quad \alpha=0.05 \quad \theta=0.1 \quad \%\text{Infect}=3/4/8$

DATA THROUGH 11-SEP-2020
Moldova: Cumulative Deaths per Million ($\delta = .01/.008/.012$)

Moldova

$R_0=1.1/1.1/1.1 \quad \delta = 0.010 \quad \alpha=0.05 \quad \theta=0.1 \quad \%\text{Infect}=3/4/8$

DATA THROUGH 11-SEP-2020
Reopening and Herd Immunity

– **Black**: assumes $R_0(\text{today})$ remains in place forever
– **Red**: assumes $R_0(\text{suppress}) = 1/s(\text{today})$
– **Green**: we move 25% of the way from $R_0(\text{today})$ back to initial $R_0 = \text{“normal”}$
– **Purple**: we move 50% of the way from $R_0(\text{today})$ back to initial $R_0 = \text{“normal”}$

**NOTE**: Lines often cover each other up
Moldova: Re-Opening ($\alpha = .05$)

Moldova

$R_0(t)=1.1$, $R_0(\text{suppress})=1.0$, $R_0(25/50)=1.3/1.6$, $\delta = 0.010$, $\alpha=0.05$

(Light bars = New York City, for comparison)
Moldova: Re-Opening ($\alpha = 0$)

Moldova

$R_0(t) = 1.1$, $R_0(\text{suppress}) = 1.0$, $R_0(25/50) = 1.4/1.6$, $\delta = 0.010$, $\alpha = 0.00$

(Light bars = New York City, for comparison)
Results for alternative parameter values
Moldova (7 days): Daily Deaths per Million People ($\alpha = 0$)

\[ R_0 = 1.1/1.1/1.1 \quad \delta = 0.010 \quad \alpha = 0.00 \quad \theta = 0.1 \quad \%\text{Infect} = 3/5/14 \]

DATA THROUGH 11-SEP-2020
Moldova (7 days): Cumulative Deaths per Million (Future, $\alpha = 0$)

Moldova

$R_0 = 1.1/1.1/1.1$  $\delta = 0.010$  $\alpha = 0.00$  $\theta = 0.1$  $\%\text{Infect} = 3/5/14$

DATA THROUGH 11-SEP-2020
Moldova (7 days): Cumulative Deaths per Million, Log Scale ($\alpha = 0$)

Moldova

$R_0 = 1.1/1.1/1.1$  \( \delta = 0.010 \)  \( \alpha = 0.00 \)  \( \theta = 0.1 \)  \%Infect = 3/5/14

Cumulative deaths per million people

Moldova: Daily Deaths per Million People ($\delta = 0.8\%$)

Moldova

$R_0 = 1.1 / 1.1 / 1.1 \quad \delta = 0.008 \quad \theta = 0.1 \quad \gamma = 0.2 \quad \% \text{Infect} = 4 / 5 / 9$
Moldova: Cumulative Deaths per Million ($\delta = 0.8\%$)

Moldova

$R_0=1.1/1.1/1.1$  $\delta = 0.008$  $\theta=0.1$  $\gamma=0.2$  $\%\text{Infect}= 4/5/9$
Moldova: Daily Deaths per Million People ($\delta = 1.2\%$)

Moldova

$R_0 = 1.1/1.1/1.1$  $\delta = 0.012$  $\theta = 0.1$  $\gamma = 0.2$  $\%$Infect $= 3/4/6$
Moldova: Cumulative Deaths per Million ($\delta = 1.2\%$)

Moldova

$R_0 = 1.1/1.1/1.1$  $\delta = 0.012$  $\theta = 0.1$  $\gamma = 0.2$  $\%$ Infect = 3/4/6
Moldova: Daily Deaths per Million People ($\gamma = .2/.15$)

\[ R_0 = 1.1/1.1/1.1 \quad \delta = 0.010 \quad \alpha = 0.05 \quad \theta = 0.1 \quad \%\text{Infect} = 3/4/8 \]

DATA THROUGH 11-SEP-2020
Moldova: Cumulative Deaths per Million $\gamma = .2/.15$)

Moldova

$R_0=1.1/1.1/1.1$  $\delta = 0.010$  $\alpha=0.05$  $\theta=0.1$  %Infect= 3/ 4/ 8

$\gamma = 0.15$

$\gamma = 0.2$

DATA THROUGH 11-SEP-2020
Moldova: Daily Deaths per Million People ($\theta = 0.1/0.07/0.2$)

Moldova

$R_0 = 1.1/1.1/1.1$  $\delta = 0.010$  $\alpha = 0.05$  $\theta = 0.1$  \%Infect = 3/4/8

DATA THROUGH 11-SEP-2020
Moldova: Cumulative Deaths per Million People \( (\theta = .1/.07/.2) \)

Moldova

\[ R_0 = 1.1/1.1/1.1 \]
\[ \delta = 0.010 \]
\[ \alpha = 0.05 \]
\[ \theta = 0.1 \]

\% Infect: 3/4/8

DATA THROUGH 11-SEP-2020
Data Underlying Estimates of Time-Varying $R_0$

– Inferred from daily deaths, and
– the change in daily deaths, and
– the change in (the change in daily deaths)
Moldova: Daily Deaths, Actual and Smoothed

Moldova: Daily deaths, d
\[ \delta = 0.010 \quad \theta=0.10 \quad \gamma=0.20 \]
Moldova: Change in Smoothed Daily Deaths

Moldova: Delta d
\( \delta = 0.010 \quad \theta = 0.10 \quad \gamma = 0.20 \)
Moldova: Change in (Change in Smoothed Daily Deaths)

Moldova: Delta (Delta d)
\[ \delta = 0.010 \quad \theta = 0.10 \quad \gamma = 0.20 \]